



# Formalização de Teoremas em Assistentes de Prova

## Section 3: Provas em papel e lápis versus provas formais

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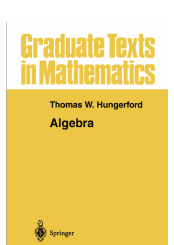
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# Talk's Plan

## 1 Section 3

- Formalizing a simple remark in Hungerford's abstract algebra textbook

# Hungerford's remark



**Definition 3.5.** *An integral domain  $R$  is a unique factorization domain provided that:*

- (i) *every nonzero nonunit element  $a$  of  $R$  can be written  $a = c_1 c_2 \cdots c_n$ , with  $c_1, \dots, c_n$  irreducible.*
- (ii) *If  $a = c_1 c_2 \cdots c_n$  and  $a = d_1 d_2 \cdots d_m$  ( $c_i, d_i$  irreducible), then  $n = m$  and for some permutation  $\sigma$  of  $\{1, 2, \dots, n\}$ ,  $c_i$  and  $d_{\sigma(i)}$  are associates for every  $i$ .*

**REMARK.** Every irreducible element in a unique factorization domain is necessarily prime by (ii). Consequently, irreducible and prime elements coincide by Theorem 3.4 (iii).