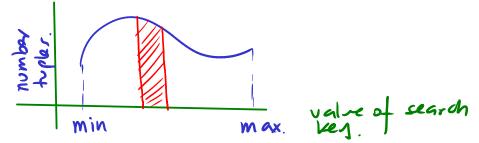
Selectivity of matching a primary Key: 1

Selectuits of matching a nonprimary vey:
We need a distribution.



We need to compute proportion of the tuples that match the predicate.

Example:

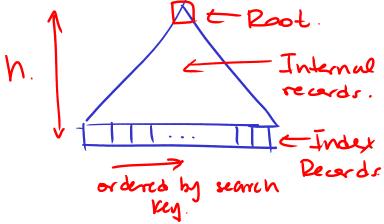
- · Relation R(9,6)
- · Assume a mifern distribution et valer of b, min 1, max 100.

Selection (b>20 and b<30) = 
$$\frac{9}{100}$$
  
Selection (b>200) =  $\emptyset$ 

Indexer.

B+-tree

- · Atomakcally Balanud
- · Finder records are at the leaves

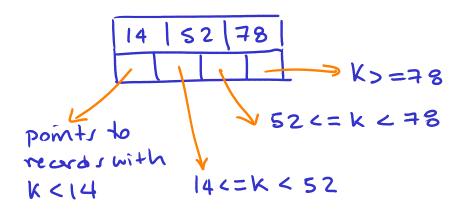


- · Every record is a block.
- · Index records form a list
  - . They can be traversed in the order of the search key

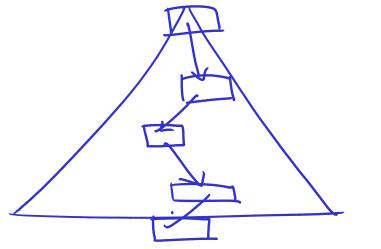
Internal records

 Example.

Assume n = 3



Index is traversed from root to leaf



We assume noot is always in memory hence, to reach the leaf we read h blocks.

#bbck: in index = 
$$\left[\frac{\text{# matching types}}{\text{n. fill}}\right]$$
  
=  $\frac{.5 \cdot 10^6}{10^2} = .5 \cdot 10^4$ 

$$Cost = h - 1 + 0.5 \cdot 10^4 + 10^6$$
  
  $\approx 10^6!!$ 

Approximately 10 times more than Sparse index!!

How do we know how many typer match a given grang?

selectify (p) = probability that a type in R matcher predicate P.

Example.

R(a,b) |R| = 106 typles.
heap: 10 typles per block
Dense index on R(a)
Effective index records per block: 100
h = 4

a)  $O_{a=s} R$ if type exists: cost = h+1.

if type does not exist: cost = h.

Same as sparse!!.

b) Ta>10 R Assume 50% of types match.



We need to scan 50% of them. Cost of index:

· Cost of reaching the leafs · Cost of reading the matching records.

Example:

1) Asame Pla, b)

Ta = 5 R

Only one or zero matching tyle:

⇒ We must traverse the index h The leaf either

· contains a = 5 or not

Cost of index = h of index.

2) Ja70 R

What if all types match?

· We traverse index (cast h) Reads front leaf.

· We must read all leaves of index

Cost of index = h + # leaver -1

To be able to compute the cost of an index we need:

Calalate # of leaf blocks of index proportional to # index records per block.

# of index records depends you a) type of index Sparse ss. Dense

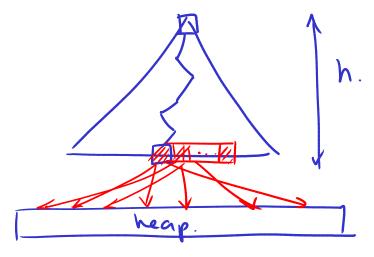
b) Number of types in Rel.

#index reards per block depends upon:

- a) size of search lay
- h) occupancy rate =) How much waste spece is there in the index (to Keep it balanced).

We assume that occupancy rate of inner nodes and leaves is the same as internal nodes.

Dense Index.



Cost:

h-1+# leaves in Index + 1 bbck per matching typle.

- · Traverse tree to first leaf: h · Might need to read Ø or more leafs.
- · For every type in result, read one

Example.

a) 
$$O_{a=s} R$$

if type exists: cost = h+1.

if type does not exist: cost = h.

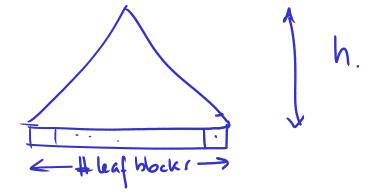
b) Ja>10 R

Assume 50% of tiples match gueny:

⇒ We must scan 50% of sorted heap. Cost = h +  $\frac{B(R)}{Z}$ 

$$B(R) = \frac{10^6}{10} = 10^5$$

Hence, height of tree depends upon # of leaf records.



n = max number of leys per record.

fill = occupancy rate (between 0-1,
but usually around 1/2 to 3/4)

For h, we simplify calculations:

## Example:

Assume 
$$n = 150$$
,  $fill = \frac{2}{3}$ 

How many index records can we store in an index of height 1,2,3,4,5,6.

Let is wany about max # index leards

h # index Pecard ()

1 100 = 
$$10^2$$

2 100<sup>2</sup> =  $10^4$ 

3 100<sup>3</sup> =  $10^6$ 

4 100<sup>5</sup> =  $10^9$ 

With 5 block reads we can find a leaf with a given search key in an index of 10 giga-records!!

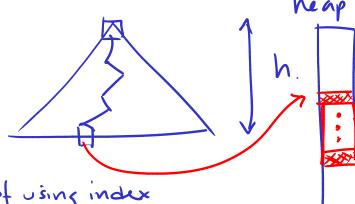
How many search lays do we need to store?

- · Sparse index: B(R)
- · Dense index: [R]

Sparse index is marginally shorter than dense index.

Cost of Using an Index

Sparce Index.



Cost of using index h + #blocks read in heap.

- · We only read one record in index
- · We read 1 or more blocks from heap