

Exploiting structures in multiobjective simulation optimization problems

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SIAM OP 23



Outlines

Intro, ParMOO, and Problem Types

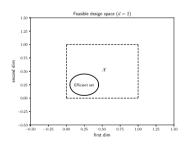
Initial Results + Optimizer Stalling

Deep-dive into RBFs and Connection to Bayesian optimization

Comparison with Bayesian optimization



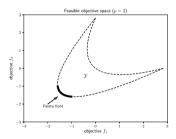
Multiobjective Optimization Problems





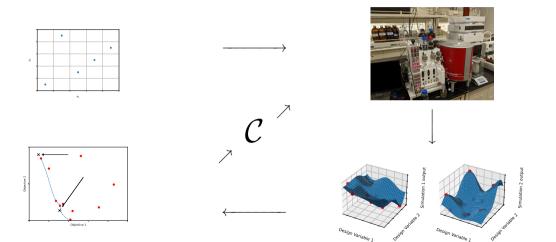


expensive blackbox process



Multiobjective Response Surface Methodology

or Model-Based Optimization or Active Learning



Industry applications



"Using Bayesian optimization for balancing metrics in recommendation systems" by Yunbao Ouyang et al. on LinkedIn Engineering Blog.



"The makings of a smart cookie" by Daniel Golovin on Google Research Blog.



"Accelerating molecular optimization with Al" by Payel Das et al. on IBM Research Blog.



"Optimizing model accuracy and latency using Bayesian multi-objective NAS" by David Eriksson et al. on Meta Al Research Blog.



"Archai can design your neural network with state-of-the-art NAS" by Shital Shah et al. on Microsoft Research Blog.

ParMOO Design Criteria

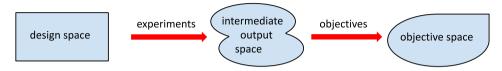
Design goals:

- 1. Highly customizable framework for multiobjective RSM
- 2. Flexible problem types (mixed-variables, constraints, etc.)
- 3. Easy to use, deploy, and extend (unforeseen use-cases and environments)
- 4. Solve large-scale problems + exploit structure and domain knowledge

Chang and Wild. ParMOO: A Python library for parallel multiobjective simulation optimization. JOSS 8(82):4468 (2023).



Problem structures



Least-squares structure:

$$h_i(x, S(x)) = \sum_{j \in N_i} (S_j(x))^2$$

where each N_1, \ldots, N_o is an index set.

Increases order of approximation \Rightarrow increases order of convergence

Heterogeneous MOOPs:

$$h_1(x, S(x)) = S_1(x)$$

 $h_2(x, S(x)) = ||x||^2$

Use expensive surrogate models for h_1 (i.e., S_1) but not for h_2



Example 1: Material Manufacturing with ParMOO

Choose optimal settings for material manufacturing in a continuous flow reactor (CFR)

We know how to make a desired material, need to produce at scale:

- 1. Maximize the product (battery electrolyte: TFML)
- 2. Can increase temperature to reduce reaction time
- 3. Too much heat activates a side reaction; need to minimize unwanted byproduct

Challenges:

- Mixed variable types
- Heterogeneous objectives
- Must send experiments to run on CFR
- ► Limited budget

Design vars and bound constraints

	Parameter	LB	UB	
	Temp (deg C)	40	150	
	Reaction time (secs)	60	300	
	Equivalence ratio (N/A)	0.9	2	
	Solvent (categorical)	2	lvls	
	Base (categorical)	2	lvls	



CFR Optimization with ParMOO

Extend MOOP class to send/receive experiment data using MDML library (Apache Kafka)

Used embeddings to represent categorical variables

Modeled Product/Byprod as sims and reaction time using ID mapping from input



Ran to convergence and used data to create a surrogate problem for future study

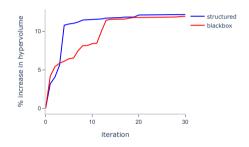


Chang et al. A framework for fully autonomous design of materials via multiobjective optimization and active learning: challenges and next steps. In ICLR 2023, Workshop on ML4Materials.

CFR Optimization Results

- 5 mixed-type design variables (including reaction time), 3 heterogeneous objs
- ➤ 50-pt Latin hypercube design-of-experiments
- ► Fit **global** Gaussian RBF surrogate on 2 simulation outputs
- ► 3rd obj is identity mapping of reaction time
- ▶ 3 ε -constraint scalarization functions
- Multi-start L-BFGS-B global optimization of scalarized objectives
- Compared against blackbox implementation: all 3 objectives modeled with Gaussian RBFs

Ran 30 iterations (batch size 3) after 50-pt DOE (avg over 5 seeds)



Notice: structure-exploiting is better early on, then **stalls out** at the end...



Example 2: Fayans EDF Model Calibration

Find params $x \in [0,1]^{13}$ to fit the Fayans model to data d_i :

$$M(\xi_i;x)\approx d_i \qquad i=1,\ldots,198$$

ParMOO simulation:

$$S_i(x) = M(\xi_i; x) - d_i, \qquad i = 1, ..., 198;$$

Min SOS across 3 observable classes

$$F_t = \sum_{i=1}^{m_t} \left(S_{t,i}(x) \right)^2$$

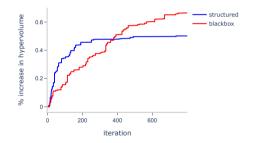
Bollapragada et al. Optimization and supervised machine learning methods for fitting numerical physics models without derivatives. Journal of Physics G 48(2):024001 (2020).



Fayans Solution with ParMOO

- Approximated Fayans residuals with MLP trained on existing dataset
- ► Implemented batch-parallel structure-exploiting solver in ParMOO
 - ▶ 13 continuous design variables
 - 2000-pt LH design-of-experiments
 - Use local Gaussian RBF surrogates to model sim outs
 - ► SOS structure applied on top of Gauss RBF surrogate outputs
 - Solve 10 randomized ε -constraint scalarizations per batch
 - ► Solve each with a trust-region multi-start L-BFGS-B
- Compared against same solver w/o exploiting least-squares structure (Gaussian RBFs fit directly to three objective values)

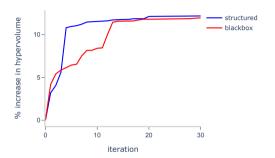
Ran for 800 iterations (10K sim evals) Avg over 5 random seeds



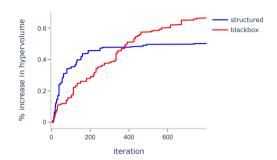
Structure-exploiting is better at small budgets, but **again stalls** out...



Two different problems, same issue...



- Mixed-variable problem
- Extremely limited budget
- Heterogeneous objectives
- ► Global Gaussian RBF modeling



- Continuous optimization problem
- ▶ 13 vars, 3 objs, healthy budget
- ► Nonlinear least-squares
- ► Local RBF (trust-region method)

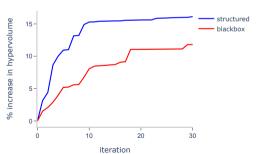


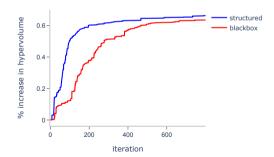
What happened?

Many months of debugging and testing...

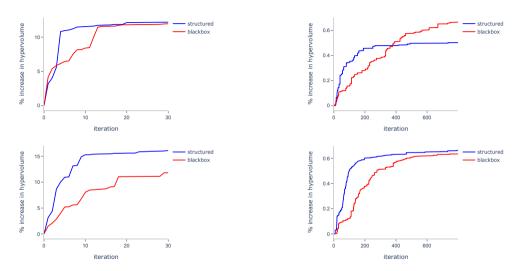
Finally tried centering response values at 0 before fitting surrogate...

Fixed!





Comparison



Chang and Wild. Designing a framework for solving multiobjective simulation optimization problems. ArXiv preprint 2304.06881 (2023).

Equivalence between Gaussian RBFs and GPs

For both Gaussian RBFs and (traditional) Gaussian process mean-function:

$$\hat{F}_{RBF}(x) = \omega^{ op} \left[egin{array}{c} e^{-\parallel x_1 - x \parallel^2/\sigma} \ e^{-\parallel x_2 - x \parallel^2/\sigma} \ dots \ e^{-\parallel x_n - x \parallel^2/\sigma} \end{array}
ight]$$

where $A\omega = y$ and

$$A = \begin{bmatrix} 1 & e^{-\|x_1 - x_2\|^2/\sigma} & \dots & e^{-\|x_1 - x_n\|^2/\sigma} \\ e^{-\|x_2 - x_1\|^2/\sigma} & 1 & \dots & e^{-\|x_2 - x_n\|^2/\sigma} \\ \vdots & \vdots & & \vdots & & \vdots \\ e^{-\|x_n - x_1\|^2/\sigma} & e^{-\|x_n - x_2\|^2/\sigma} & \dots & 1 \end{bmatrix} \qquad y = \begin{bmatrix} F(x_1) \\ F(x_2) \\ \vdots \\ F(x_n) \end{bmatrix}$$

RBF/GP Conditioning and Accuracy

$$A = \begin{bmatrix} 1 & e^{-\|x_1 - x_2\|^2/\sigma} & \dots & e^{-\|x_1 - x_n\|^2/\sigma} \\ e^{-\|x_2 - x_1\|^2/\sigma} & 1 & \dots & e^{-\|x_2 - x_n\|^2/\sigma} \\ \vdots & \vdots & & \vdots \\ e^{-\|x_n - x_1\|^2/\sigma} & e^{-\|x_n - x_2\|^2/\sigma} & \dots & 1 \end{bmatrix}$$

- As we optimize, data points cluster
- ▶ As $||x_i x_j|| \rightarrow 0$, $A \rightarrow \text{singularity}$
- lacktriangle Decrease the shape parameter σ to keep A nonsingular
- Descreasing σ restricts the support of \hat{F}_{RBF}
 - ▶ With 0-prior, optimizer will be driven to low-support regions
 - ▶ With GP, uncertainty will be maximal in low-support regions (will drive Bayesian optimization to behave similarly?)
- "Uncertainty principle" for imbalanced datasets, cannot have accuracy and solvability when working with RBF-like models



Big Question

Does Bayesian optimization stall out for structure-exploiting solvers?

How to even check something like this?

Implemented Bayesian Optimization in ParMOO

To check, we implemented Bayesian optimization in ParMOO

Showing 18 changed files with 3,394 additions and 852 deletions.

- When composing GPs (from simulation outputs) into nonlinear objectives, the posterior depends on the function
 - May or may not be iid
- ▶ Monte carlo integrated to evaluate expected-improvement in the ε -constraint scalarization
 - It's very expensive

Bayesian optimization of CFR problem

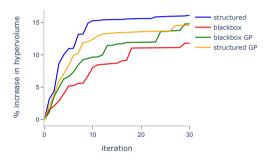
- ▶ 5 mixed-type design variables (including reaction time)
- ▶ 50-pt Latin hypercube design-of-experiments
- ▶ Fit **global** Gaussian RBF surrogate on 2 simulation outputs
- ► 3rd obj is identity mapping of reaction time
- Compared against blackbox implementation: all 3 objectives modeled with Gaussian RBFs
- ▶ 3 El of ε -constraint acquisition functions
- ► Monte carlo integration of 2 Gaussian sim outs
- ► Multi-start GPS for global optimization of scalarized objectives



^{*}Green highlight = changes made from before

CFR Bayesian optimization results

Deja vu?



Bayesian optimization of Fayans problem

- ▶ 13 continuous design variables
- ► 2000-pt LH design-of-experiments
- ▶ Use **local** Gaussian proc. surrogates to model sims[†]
- SOS structure applied on top of Gauss RBF surrogate outputs
- Implemented batch-parallel structure-exploiting solver in ParMOO
- Compared against same solver w/o exploiting least-squares structure (Gaussian RBFs fit directly to three objective values)
- ▶ 10 El of ε -constraint acquisition functions
- ▶ Monte carlo integration of 198-dim Gaussian sim outs
- ► Multi-start GPS in TR to solve optimization of scalarized objectives

*Green highlight = changes made from before

† Eriksson et al. Scalable global optimization via local Bayesian optimization. In NeurIPS 2019.

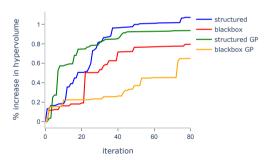


Fayans Bayesian optimization results

Had to drastically reduce budget (200 pt LH, 80 iterations)

MC integration with only 300 samples (enough?)

Only 2 random seeds



Conclusion & Next steps

- Solving Bayesian optimization too fast seems to stall out
 - ► This is actually mentioned in literature
 - ▶ Related to poor conditioning of RBF kernels?
 - ▶ Is it just the Gaussian processes? What about other models?
 - What if I optimized the shape parameter instead of setting it algebraically?
 - ► How do the "default" BoTorch methods do?
- Do this at a larger scale to get more thorough results
 - Parallelize surrogate problem solvers
 - Gradient-based solvers & faster MC integrators

Garnett. Bayesian optimization [Ch. 9.2] (2023).



References

Related work

Eriksson et al. Scalable global optimization via local Bayesian optimization. In NeurIPS 2019.

Garnett. Bayesian optimization [Ch. 9.2] (2023).

ParMOO software & test problems

Chang and Wild. ParMOO: A Python library for parallel multiobjective simulation optimization. JOSS 8(82):4468 (2023).

Chang and Wild. Designing a framework for solving multiobjective simulation optimization problems. ArXiv preprint 2304.06881 (2023).

Datasets

Bollapragada et al. Optimization and supervised machine learning methods for fitting numerical physics models without derivatives. Journal of Physics G 48(2):024001 (2020).

Chang et al. A framework for fully autonomous design of materials via multiobjective optimization and active learning: challenges and next steps. In ICLR 2023 Workshop on ML4Materials.

Resources

GitHub: github.com/parmoo/parmoo

Pip: pip install parmoo

Conda: conda install --channel=conda-forge parmoo

Test problems: github.com/parmoo/parmoo-solver-farm

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This material is based upon work supported by the U.S. Department of Energy, Office of Science, Office of Advanced Scientific Computing Research, SciDAC program under contract number DE-AC02-06CH11357.

