

## Data sampling for surrogate modeling and optimization

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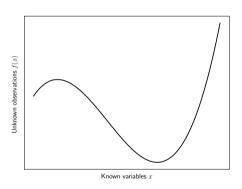
ICIAM 2023, Tokyo, Japan Aug 23, 2023

#### Outlines

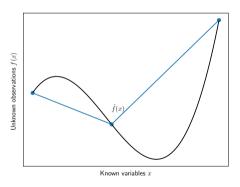
Inference problems, the curse of dimensionality, and measure collapse

Modeling for high-dimensional optimization

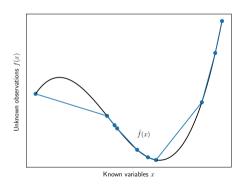
Some Applications



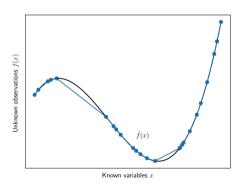
Want to predict unknown f(x) for observation x



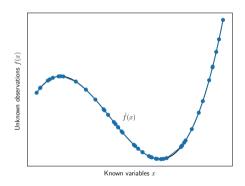
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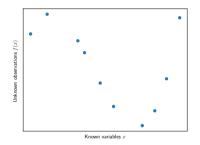


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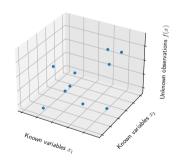


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- ► If we have enough data, it doesn't matter

## The curse of dimensionality

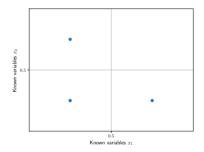


10 training points in 1D



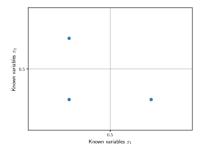
10 training points in 2D

## The curse of dimensionality no data



Need data in all quadrants?

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Need data in all quadrants?

- ▶ Inference in 2D :  $2^2 = 4$
- ▶ Inference in 10D :  $2^{10} \approx 1000$
- ▶ Inference in  $100\text{D}:2^{100}\approx10^{30}$  (orders of magnitude bigger than exascale)
- ► Many ML problems : inference in 1000+ dimensions

### Measure collapse

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If  $\mathcal X$  are sampled from any distribution,  $\mu(\mathit{CH}(\mathcal X)) o 0$  exponentially as d grows

This is called a concentration of measure

Gorban and Tyukin, Stochastic separation theorems. Neural Networks 94, pp. 255-259 (2017).



### Example

Suppose that we uniformly sample  $x = (x_1, x_2, ..., x_d)$  from  $[0,1]^d$ 

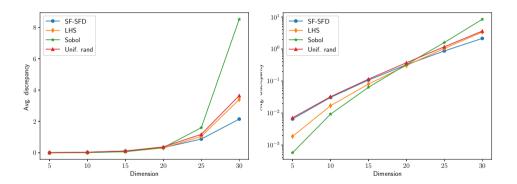
$$\|x - \frac{1}{2}\|_2^2 = \sum_{i=1}^d (x_i - \frac{1}{2})^2.$$

$$\mathbb{E}\left[\left(x_i - \frac{1}{2}\right)^2\right] = \int_0^1 \left(u - \frac{1}{2}\right)^2 du = \frac{1}{12}$$

with finite variance v

By CLT for all  $x \in \mathcal{X}$ :  $\mathbb{E}[\|x - \frac{1}{2}\|_2^2] = \frac{d}{12}$  with variance  $\frac{v}{d} \to 0$  as  $d \to \infty$ .

### Collapse of some common distributions



Garg, Chang, and Raghavan, Stochastic optimization of Fourier coefficiencts to generate space-filling designs. To appear in Winter Sim 2023.

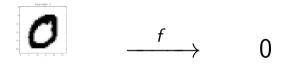
### Representation learning solution

"There's more to machine learning than function approximation"

## Representation learning solution

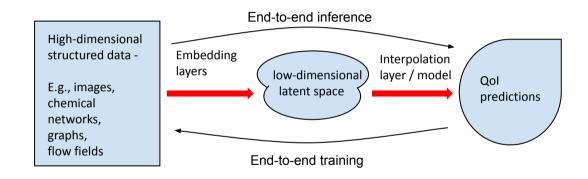
#### "There's more to machine learning than function approximation"

▶ *f* is often highly *structured* − MLPs with nothing else are from the 60s

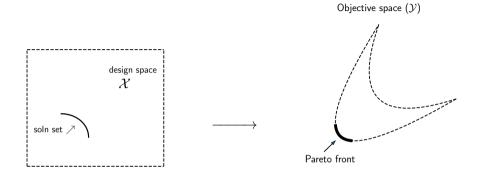


 $28 \times 28$  pixels  $\neq 784$  dimensions...

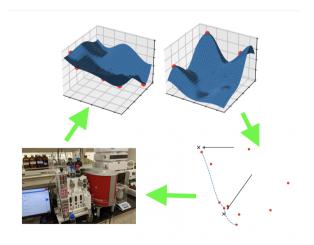
## Modern deep learning pipeline



# Multiobjective Black-Box Optimization



# General Workflow and Data Acquisition

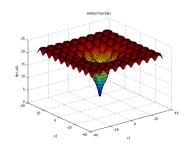


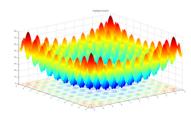
### Global optimization

In global optimization literature...

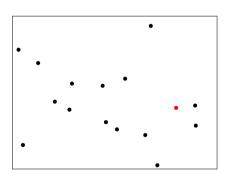
- ▶ Balance exploration vs. exploitation
- ▶ Drive *global model error* to zero
- ▶ Need exponentially many samples to guarantee global convergence

Guarantees convergence for problems with thousands of local minima

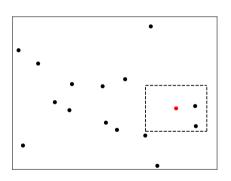




- Only exploit maybe multi-start or large initial search
- Fit a model that is *locally accurate* 
  - ► Sample requirement grows only linearly with dimension
- Modification is as simple as putting a trust-region around interesting points

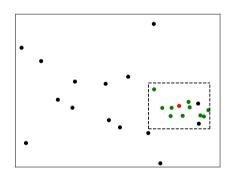


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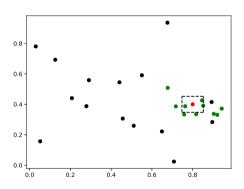




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#### **ParMOO**



#### Written in Python

Version 0.3.0 is now available on available on pip, conda-forge, and GitHub







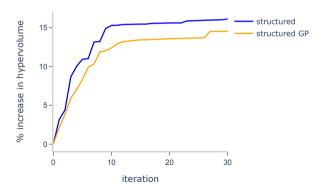
https://github.com/parmoo/parmoo

https://parmoo.readthedocs.io

Chang and Wild. ParMOO: A Python library for parallel multiobjective simulation optimization. JOSS 8(82):4468 (2023).

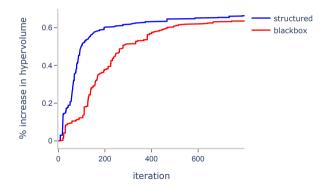
## Chemical Design on a Limited Budget

- ▶ 6-dimensional latent space embedding of a mixed-variable problem
- ▶ 3-objectives electrolyte manufacturing
  - high yield, minimal byproduct, low reaction times
- Running real-world experiments with very limited budget



# Fayans Model Calibration (Inverse Problem)

- ▶ 13-variable, 3-objective problem
- ► Higher dimensional, requires trust-region methods

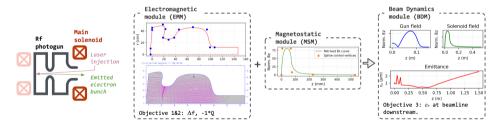


Chang and Wild. Designing a framework for solving multiobjective simulation optimization problems. *Under review, preprint https://arxiv.org/abs/2304.06881*.



### Particle Accelerator Beam Design

- ▶ 22-variable, 2-objective problem
- ▶ 3 physics constraints, nearly impossible to satisfy
- ► Matched well-known reference gun geometry with just **1300** true simulation evaluations



Chen, Chang, et al. An Integrated Multi-Physics Optimization Framework for Particle Accelerator Design. Under review.



#### Some Conclusions

- ▶ Doing anything global (modeling, optimization, etc.) in high-dimensions is very hard (maybe impossible)
- Easier to identify low-dimensional structures and model these locally
  - In my experience, giving up global accuracy is the only thing that scales to big problems
- ► Some problems (optimization) don't necessarilly require global accuracy
  - Don't demand it if you don't need it!
- Optimization rarely truly requires global accuracy

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  - In my experience, giving up global accuracy is the only thing that scales to big problems
- ► Some problems (optimization) don't necessarilly require global accuracy
  - Don't demand it if you don't need it!
- Optimization rarely truly requires global accuracy
- ▶ But there are other problems that do require global accuracy...



#### References

Garg, Chang, and Raghavan. Stochastic optimization of Fourier coefficiencts to generate space-filling designs. To appear in Winter Sim 2023.

Chang and Wild. ParMOO: A Python library for parallel multiobjective simulation optimization. JOSS 8(82):4468 (2023).

Chang and Wild. Designing a framework for solving multiobjective simulation optimization problems. Under Review, ArXiv preprint 2304.06881 (2023).

Chang et al. A framework for fully autonomous design of materials via multiobjective optimization and active learning: challenges and next steps. In ICLR 2023, Workshop on ML4Materials.

Chen, Chang, et al. An Integrated Multi-Physics Optimization Framework for Particle Accelerator Design. Under review.



#### Resources

GitHub: github.com/parmoo/parmoo

Pip: pip install parmoo

Conda: conda install --channel=conda-forge parmoo

Test problems: github.com/parmoo/parmoo-solver-farm

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