

Word Break:-

Word Break

Difficulty: Medium Accuracy: 48.88% Submissions: 152K+ Points: 4

You are given a string `s` and a list `dictionary[]` of words. Your task is to determine whether the string `s` can be formed by concatenating one or more words from the `dictionary[]`.

Note: From `dictionary[]`, any word can be taken any number of times and in any order.

Examples:

Input: `s = "like", dictionary[] = ["l", "like", "gfg"]`
Output: true
Explanation: `s` can be breakdown as "l like".

Input: `s = "likegfg", dictionary[] = ["l", "like", "man", "india", "gfg"]`
Output: true
Explanation: `s` can be breakdown as "l like gfg".

Input: `s = "likemangoes", dictionary[] = ["l", "like", "man", "india", "gfg"]`
Output: false
Explanation: `s` cannot be formed using `dictionary[]` words.

Constraints:
 $1 \leq s.size() \leq 3000$
 $1 \leq dictionary.size() \leq 1000$
 $1 \leq dictionary[i].size() \leq 100$

[Try more examples](#)

```
bool solve(int i, unordered_set<int> s) {
    if(i == n) return true;
    if(dp[i] != -1) return dp[i];
    bool ans = false;
    for(int j = i; j < n; j++) {
        if(s.count(st.substr(i, j+1))) {
            ans = ans || solve(j+1, s);
        }
    }
    dp[i] = ans;
    return ans;
}
```

[Naive Approach] Using Recursion - $O(2^n)$ Time & $O(n)$ Space:-

The idea is to consider each prefix & search for it in dictionary. If the prefix is present in dictionary, we recur for rest of the string (or suffix). If the recursive call for suffix returns true, otherwise we try next prefix. If we have tried all prefixes, & none of them resulted in a soln, we return false.

```
bool wordBreakRec(int i, string &s, vector<string> dic) {
    if(i == s.length()) return true;
    int n = s.length();
    string prefix = "";
    for(int j = i; j < n; j++) {
        prefix += s[j];
        if(find(dic.begin(), dic.end(), prefix) != dic.end()) {
            if(wordBreakRec(j+1, s, dic)) return true;
        }
    }
    return false;
}

bool wordBreak(string &s, vector<string> dic) {
    return wordBreakRec(0, s, dic);
}
```

Using Top-Down DP - $O(n^2)$ Time & $O(n+m)$ Space:-

1. Optimal Substructure
2. Overlapping Subproblems

```
vector<string> & dic, vector<int> & dp)
```

1. Optimal subproblems

2. Overlapping Subproblems

```
bool wordBreakRec(int ind, string &s, vector<string> & dic, vector<int> &dp)
```

```
{ if(ind >= s.size()) return true;
```

```
if(dp[ind] != -1) return dp[ind];
```

```
bool possible = false;
```

```
for(int i = 0; i < dic.size(); i++)
```

```
    string temp = dic[i];
```

```
    if(temp.size() > s.size() - ind) continue;
```

```
    bool ok = true;
```

```
    for(int j = 0; j < temp.size(); j++) {
```

```
        if(temp[j] != s[ind+j]) {
```

```
            ok = false;
```

```
            break;
```

```
        }
```

```
    } else
```

```
        k++;
```

```
}
```

```
if(ok) {
```

```
    possible |= wordBreak(ind + temp.size(), s, dic, dp);
```

```
}
```

```
}
```

```
return dp[ind] = possible; }
```

manual string matching

```
bool wordBreak(string s, vector<string> & dic) {
```

```
    int n = s.size();
```

```
    vector<int> dp(n+1, -1);
```

```
    return wordBreakRec(0, s, dic, dp);
```

```
}
```

[Expected Approach-2] Using Bottom Up DP - $O(n \times m \times k)$ time & $O(n)$ space: -

The idea is to use bottom-up dynamic programming to determine if a string can be segmented into dictionary words. Create a boolean array $dp[]$ where each position $dp[i]$ represents whether the substring from 0 to that position can be broken into dictionary words.

Step by step approach: -

1. Start from the beginning of the string & mark it as valid (base case)

i.e. $dp[0] = true$;

2. For each position, check if any dictionary word ends at that position & leads to

i.e. $dp[0] = \text{true}$;

2. For each position, check if any dictionary word ends at that position & leads to an already valid position.
3. If such a word exists, mark the current position as valid, i.e. $dp[i] = \text{true}$.
4. At the end return the last entry of $dp[]$.

```
bool wordBreak(string &s, vector<string> &dictionary){
```

```
    int n = s.size();  
    vector<bool> dp(n+1, 0);
```

```
    dp[0] = 1;
```

// Traverse through the given string

```
    for(int i=1; i<=n; i++){
```

// Traverse through the dictionary words

```
        for(string &w: dictionary){
```

// check if current word is present

// the prefix before the word is also

// breakable

```
            int start = i - w.size();  
            if(start >= 0 && dp[start] && s.substr(start, w.size()) == w){
```

```
                dp[i] = 1;
```

```
                break;
```

```
            } } }
```

```
    return dp[n];
```

```
}
```

Important :-

```
class Solution {  
public:  
    bool wordBreak(string &s, vector<string> &dictionary) {  
        // code here  
        unordered_set<string> st;  
        for(auto &d: dictionary) st.insert(d);  
        int n = s.size();  
        vector<int> dp(n, -1);  
        return solve(s, 0, st, dp);  
    }  
  
    bool solve(string &s, int i, unordered_set<string> st, vector<int> dp){  
        int n = s.size();  
        if(i==n) return 1;  
        if(dp[i] != -1) return dp[i];  
        bool ans = 0;  
        string ss;  
        for(int j=i; j<n; j++){  
            ss = ss + s[j];  
            ans = ans || (st.count(ss) > 0 && (solve(s, j+1, st, dp)));  
        }  
        return dp[i] = ans;  
    }  
};
```

The Time Complexity of this approach is $O(n^3)$ due to this part (each time new string is created). That's why

we use manual string matching.