# Homework 1

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# Part I

## Problem Ia

### Cars

VIN	make	model	year	color
0	"Toyota"	"Tacoma"	2008	"Red"
1	"Toyota"	"Tacoma"	1999	"Green"
2	"Tesla"	"Model 3"	2018	"White"
3	"Subaru"	"WRX"	2016	"Blue"
4	"Ford"	"F150"	2004	"Red"

## Salespeople

SSN	name
0	"Arnold"
1	"Jessica"
2	"Steve"

## Selling

SSN	VIN
0	0
0	1
1	0
1	4
2	2

## Problem 1b

Each salesperson can only sell up to one car.

## Problem Ic

Each car can only be dealt by at most one salesperson.

Part 2

## Problem 2

Attribute sets	Superkey	Proper subsets	Key
{A1}	no	{}	no
{A2}	no	{}	no
{A3}	no	{}	no
{A1, A2}	yes	{A1}, {A2}, {}	yes
{A1, A3}	no	{A1}, {A3}, {}	no
{A2, A3}	no	{A2}, {A3}, {}	no
{A1, A2, A3}	yes	{A1, A2}, {A1, A3}, {A2, A3}, {A1}, {A2}, {A3}, {}	no

## Part 3

## Problem 3a

- PK{CardNum}
- UQ{Serial}

### **Problem 3b**

- PK{ISBN}
- UQ{Title, Author}

## **Problem 3c**

- PK{ISBN}
- UQ{Title}

### **Problem 3d**

• PK{Phone}

## Part 4

### **Problem 4**

- CheckedOut.CardNum references Patrons.CardNum
- CheckedOut.Serial references Inventory.Serial
- Phones.CardNum references Patrons.CardNum
- Titles.ISBN references Inventory.ISBN

#### Part 5

#### Problem 5a

True. If  $\{x\}$  is a superkey, all cells in column x are unique, so all rows containing column x are forced to be unique too.

#### **Problem 5b**

False. If  $\{x\}$  is a key, any set containing x will have  $\{x\}$  as a proper subset, but that's already a superkey.

#### Problem 5c

True. Being a superkey is one condition of being a key.

#### Problem 5d

True. This is included in case 5a, where if  $\{x\}$  is a superkey, then  $\{x, \text{ anything}\}$  is a superkey.

#### Problem 5e

False. As shown in 5d, If  $\{x\}$  is a superkey, then  $\{x, y\}$  is a superkey regardless of what is in column y (where y may contain duplicate cells).

#### **Problem 5f**

False. For example, if  $\{x, y, z\}$  was a key, none of its proper subsets could be a superkey.

### Problem 5g

True. A valid relation must have unique rows, so in this case it is only possible that  $\{x, y, z\}$  is a key, since no other combination of attributes make a key to enforce that uniqueness.

#### **Problem 5h**

False. The following relation has one unique  $\langle x, z \rangle$  pair ( $\langle 0, 0 \rangle$ ) but two unique y values, 0 and 1:

$$\begin{array}{c|cccc}
x & y & z \\
0 & 0 & 0 \\
0 & 1 & 0
\end{array}$$