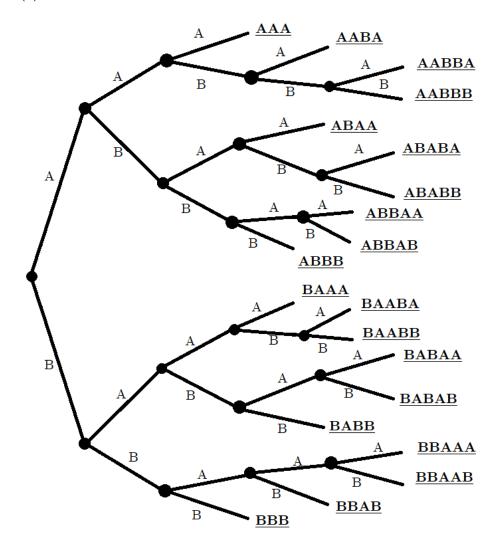
# Homework 5

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# Section 5.1 (p383)

## 1. Exercise 10

## Part (a)



#### Part (b)

20 ways (by counting straight from the tree).

#### Part (c)

3 ways (by counting straight from the tree).

#### Part (d)

First of all, since exactly 4 games are played, A must win the 4th game in order to win the match. Since a player needs to win 3 games to win the match, A must have won 2 out of the 3 games before going into the 4th game. Since each game can only be won by either A or B, the number of ways the above statement can happen is equal to the question from the problem.

#### Part (e)

6 ways (by counting straight from the tree).

### Part (f)

4; 3.

#### 2. Exercise 19

### Part (a)

Given three integers in the range of [1..6], increase the second integer by 1, and increase the third integer by 2. Write down an eight-digit binary sequence as follows: write down a "1" if the position is equal to any of the three integers, or a "0" if it is not.

#### Part (b)

10101000	$\{1, 2, 3\}$
01010100	${2,3,4}$
00100101	${3,5,6}$
00010101	$\{4, 5, 6\}$
10010010	$\{1, 3, 5\}$
10010001	{1,3,6}
00101010	${3,4,5}$
01001001	${2,4,6}$

## Section 5.2 (p395)

### 3. Exercise 7

Part (a)

$$7 \times (10 + 7 - 1) \times (10 + 7 - 2) = \boxed{1,680}$$

Part (b)

$$7 \times 10 \times (10 + 7 - 2) = \boxed{1,050}$$

Part (c)

$$\left(\frac{7\times(7-1)}{2} + \frac{10\times(10-1)}{2}\right) \times (10+7-2) = \boxed{990}$$

Part (d)

$$(10+7) \times (10+7-1) \times (10+7-2)$$

$$- \left(\frac{10 \times (10-1) \times (10-2)}{2} + \frac{7 \times (7-1) \times (7-2)}{2}\right) = \boxed{3,615}$$

#### 4. Exercise 21

Part (a)

Part (b)

$$P(365,30) = \frac{365!}{(365-30)!}$$

$$= \begin{bmatrix} 21,710,301,835,085,570,660,575,334,772,480,813,994,655,203,436,676,745,965,233,\\ 568,177,192,960,000,000 \end{bmatrix}$$

Part (c)

$$1 - \frac{365^{30}}{P(365, 30)} \approx \boxed{70.6\%}$$

This percentage is right around what I would expect as a professional statistics student.

#### 5. Exercise 24.a and Exercise 32

Exercise 24.a

$$2,380 + 2,380 - 560 = 4,200$$

### Exercise 32

The Rules of Sums can only apply to disjoint pieces. However, the committees having Jack and the committees having Jill are not disjoint, meaning that some committees have both Jack and Jill. Therefore, the Rule of Sums cannot apply here.

The Rule of Sums with Overlap should be used here instead:

2,380+2,380-560 [the committees having both Jack and Jill] =4,200

# Section 5.3 (p407)

### 6. Exercise 18

Part (a)

$$C(100,6) = \frac{100!}{(100-6)! \times 6!} = \boxed{1,192,052,400}$$

Part (b)

• Number of samples:

$$C(100 - 4, 6 - 4) = \frac{96!}{(96 - 2)! \times 2!} = \boxed{4,560}$$

• Percentage:

$$\frac{4,560}{1,192,052,400} \approx \boxed{0.000\ 383\%}$$

Part (c)

• Number of samples:

$$C(100,6) - C(100 - 4,6) = 1,192,052,400 - \frac{96!}{(96-6)! \times 6!} = \boxed{265,004,096}$$

• Percentage:

$$\frac{265,004,096}{1,192,052,400} \approx \boxed{22.2\%}$$

7. Exercise 22

$$C(20-2,7) = \frac{18!}{(18-7)! \times 7!} = \boxed{31,824}$$

8. We need to form a 5-person committee from a group of seven Idahoans and five Utahns. How many ways can this committee be formed if it must consist of at least one person from each state?

$$C(7+5,5) - C(7,5) - C(5,5) = \frac{12!}{(12-5)! \times 5!} \times \frac{7!}{(7-5)! \times 5!} \times \frac{5!}{(5-5)! \times 5!}$$
$$= \boxed{770}$$

# Section 5.4 (p417)

## 9. Exercise 4

- Part (a)
- Part (b)
- Part (c)
- 10. Exercise 6
- Part (a)
- Part (b)
- Part (c)
- 11. Exercise 11
- 12. Exercise 22
- 13. Exercise 26