

Q2 Boundary Condⁿ: $T=0$ for all boundaries

$$\tau=1, \phi=1, \quad L \times L = 1 \times 1$$

$$\left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) + 1 = 0$$

No. of grid points = n

$$\Delta x = \Delta y = \frac{L}{n-1}$$

Discretization of Domain

Discretization Scheme for governing eqns:

$$\frac{\partial^2 T}{\partial x^2} = \frac{T_{i+1,j} + T_{i-1,j} - 2T_{i,j}}{(\Delta x)^2}$$

$$\frac{\partial^2 T}{\partial y^2} = \frac{T_{i,j+1} + T_{i,j-1} - 2T_{i,j}}{(\Delta y)^2}$$

Central difference Method

$$\Rightarrow \frac{T_{i+1,j} + T_{i-1,j} - 2T_{i,j}}{(\Delta x)^2} + \frac{T_{i,j+1} + T_{i,j-1} - 2T_{i,j}}{(\Delta y)^2} + 1 = 0$$

$$\Rightarrow (\Delta y)^2 (T_{i+1,j} + T_{i-1,j}) + (\Delta x)^2 (T_{i,j+1} + T_{i,j-1}) - 2T_{i,j} (\Delta x^2 + \Delta y^2) + \Delta x^2 \Delta y^2 = 0$$

$$\Rightarrow T_{i,j} = \frac{(\Delta y)^2 (T_{i+1,j} + T_{i-1,j}) + (\Delta x)^2 (T_{i,j+1} + T_{i,j-1}) + \Delta x^2 \Delta y^2}{2(\Delta x^2 + \Delta y^2)}$$