

Simulation Exercise

Tejus

Title :

Overview :

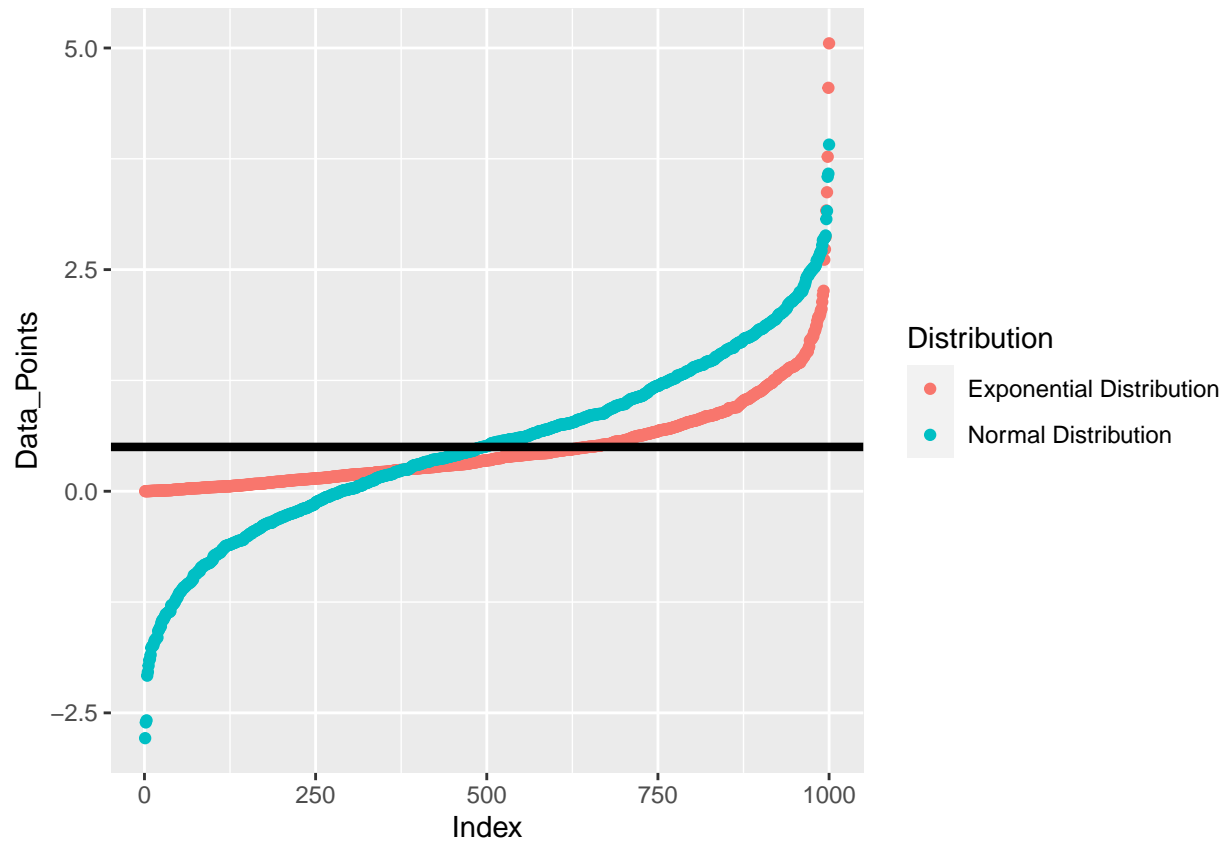
- Investigating the exponential distribution & comparing it with the Central Limit Theorem.
- In R we can use the distribution using `rexp(n, lambda)`, where `lambda` is the rate parameter.
- Assuming that the population & the randomness governing our sample can be given by densities and mass functions. We work with characteristics of these densities & mass functions instead of the whole function.

Key characteristics about the distribution :

- Mean of the exponential distribution $1 / \lambda$ [Characterization of it's center]
- Standard deviation is also $1 / \lambda$ [Characterization of spread of data.]

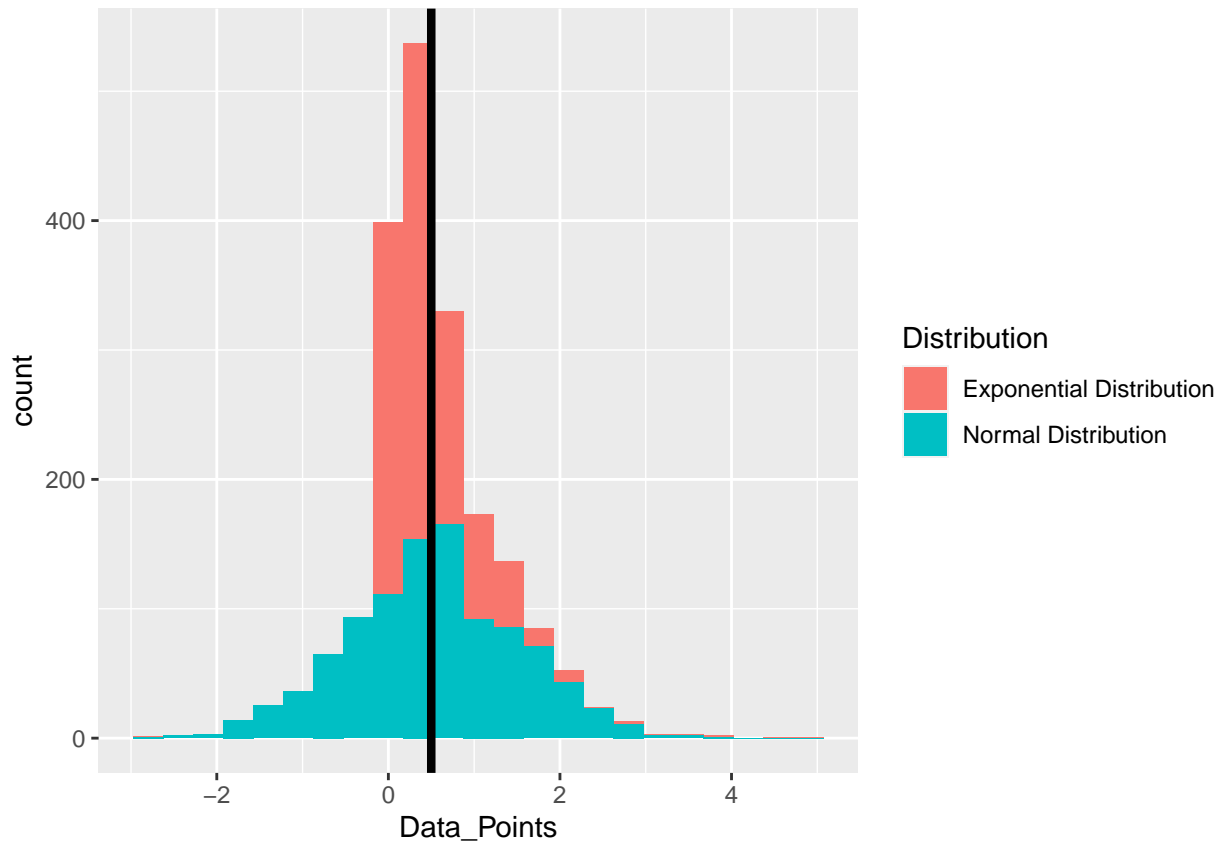
Note : Setting $\lambda = 2$ for all the simulations & averages of 40 exponentials will be investigated by simulating 1000 times

The following plot shows the Normally distributed points along with our Exponentially distributed points both with the same mean 0.5. Black horizontal line is for the mean of those distributions.



- From the plot you can see that unlike Normal Distribution, data points are not symmetrical around mean. As per the name **Exponential Distribution** the data does look like it's growing exponentially.

Histogram of an typical exponential curve would look something like this



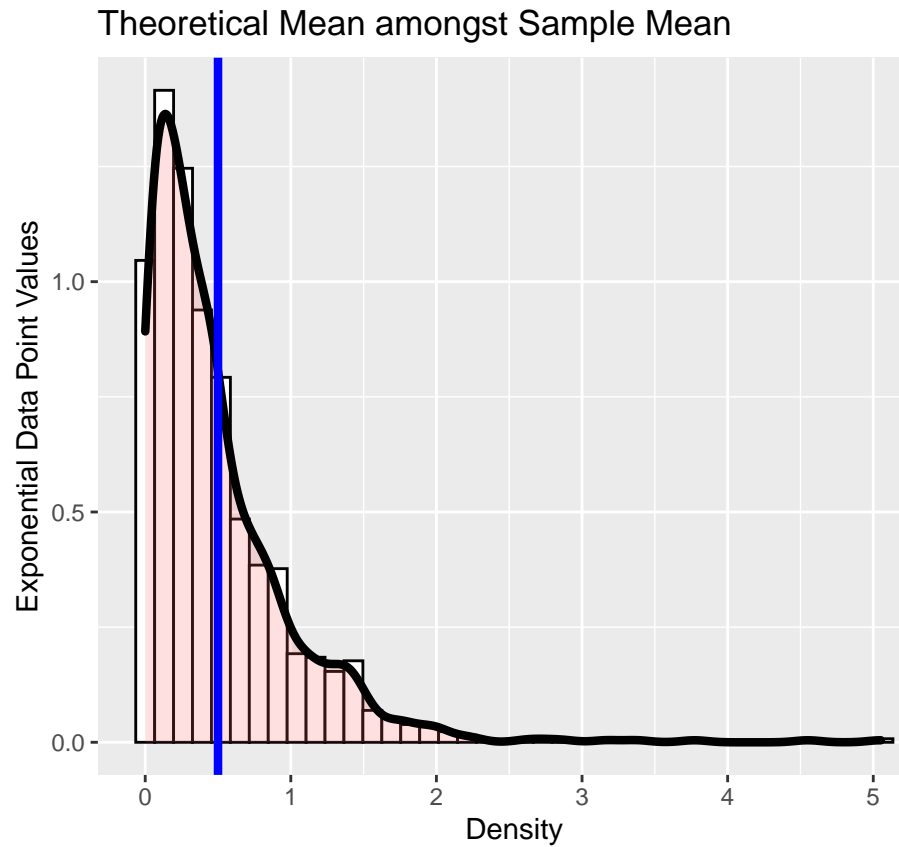
Again you can see in this histogram that the **Exponential** distribution compared to **Normal** distribution is centered around the same mean (black vertical line) but not symmetric around that.

The sample mean and the theoretical mean of the distribution.

- The black line above is the population mean. Since we have simulated these points from the mean 0.5 we know the absolute value of it. However in real life experiments we want to know what that value is.
- Why ? Because as I said above that mean (true mean) of a distribution is a very good characteristic to estimate so that we get an idea about the distribution; to make inferences about the population.

Sample Mean

- Sample Mean is an estimate of **Population Mean** (Theoretical Mean).
- After doing some experiments & collecting data the mean of that data is our **Sample Mean** which is the estimate for our population mean.



Sample Mean versus Theoretical Mean:

Clearly the peak (sample mean) is close to the *Population mean* but not exactly the same. It will approach the population mean as we increase the sample size.

Simulations

Sample Variance versus Theoretical Variance:

Distribution: