USING QUEUEING THEORY TO FIND THE OPTIMAL CHARACTER-VEHICLE COMBINATION FOR 150CC MARIO KART WORLD RACES



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SUMMARY

This investigation entailed using Queueing Theory to determine the probabilities of possessing any given number of coins during a race and evaluating the expected overall speed of every possible character-vehicle combination according to its speed increase from its speed attribute for each terrain, its weight-dependent coin effects, the coin possession probabilities, and the effects of its acceleration attribute on the drift and trick boost durations to find the optimal character-vehicle combinations for 150cc races in Mario Kart World.

The optimal character-vehicle combinations were found to be a solid-focused heavyweight character (i.e. Wario or Wriggler) with the Reel Racer, which maximises the speed attribute for maximum progress while the racer is uninterrupted, and a flyweight character (i.e. Swoop, Para-Biddybud, Baby Peach, or Baby Daisy) with the W-Twin Chopper, which relies on faster recovery when necessary and higher speed increases at the middling numbers of coins in possession to enhance the racer's overall expected speed, with viable alternatives being a flyweight character with the Reel Racer, a solid-focused heavyweight character with the Junkyard Hog, and Bowser with the Reel Racer. The solid-focused middleweight character (i.e. Mario or Rocky Wrench) with the Baby blooper, being 30th best, is no longer a contender for the best character-vehicle combination.

The results of this investigation reveal two distinct dominant strategies for Mario Kart World that players may choose according to their preferred approach to the game.

All spreadsheets and Python scripts used in this investigation are available in the folder where this report resides.

ACKNOWLEDGEMENTS

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LIST OF SYMBOLS

```
\varepsilon = relative speed increase
s = speed attribute
c = number of coins in possession
w = weight attribute
t = terrain\ identifier
a = acceleration attribute
\tau = race\ duration\ (s)
\zeta = zero-to-top-speed duration (s)
\tau_1, \tau_2 = different race duration (s)
a_1, a_2 = different acceleration attributes
v = racer top speed (px s^{-1})
\Delta x = racetrack\ distance\ (px)
\lambda = coin\ collection\ rate\ (min^{-1})
\mu = coin\ dispossession\ rate\ (min^{-1})
r = coin \ reset \ rate \ (i.e. \ frequency \ of \ races) \ (min^{-1})
P = coin possession probabilities
d_1, d_2, d_3, b_1, b_2 = intermediate calculation variables
E = expected overall speed increase relative to the baseline
\overrightarrow{B} = non-item boost rate column matrix (min<sup>-1</sup>)
\overrightarrow{T} = non-item boost duration column matrix (s)
nib = non-item\ boost
\tau_{mean} = mean \ race \ duration \ (s)
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NOMENCLATURE

RAW

rails, air, and walls; a terrain in Mario Kart World

1. INTRODUCTION

Selecting an optimal character-vehicle combination is essential for maximising one's chances of winning races in Mario Kart World. Members of the Mario Kart World community have found the performance attributes (i.e. speed, acceleration, weight, and handling) of each character and vehicle and how they interact with the in-game mechanics (e.g. MK World Builder [1], Mario Kart World Stats [2], and The Mario Kart World Stratpedia [3]), including how each coin's effect on the racer's speed depends on the number of coins in possession and the racer's weight attribute, but the probability distribution of the number of coins in possession from 0 to 20 for a racer at any given moment, the effects of the acceleration attribute on the racer's average speed through drift and trick (non-item) boost durations, and, by extension, the expected overall speed for each character-vehicle combination, have yet to be derived until this investigation.

Therefore, this investigation aimed to find the optimal character-vehicle combinations in 150cc Mario Kart World races by maximising the expected overall speed while maintaining a reasonable acceleration. This investigation was conducted via the following objectives:

- a. Apply Queueing Theory to determine the probabilities of possessing any given number of coins during a race from 0 to 20.
- b. Evaluate the expected overall speed of each possible character-vehicle combination, according to its speed increase from its speed attribute for each terrain, its weight-dependent coin effects, the coin possession probabilities obtained from objective {a}, and the effects of its acceleration attribute on the non-item boost durations.
- c. Find the character-vehicle combination with the highest expected overall speed and runners-up within a tolerance window.

2. RELEVANT GAME MECHANICS

The background information relevant to this investigation is as follows.

2.1. Speed attribute, coins, and weight attribute

For each terrain, the speed attribute increases the racer's 0-coin speed linearly from a baseline, and coins increase the racer's speed by up to 5% of the racer's 0-coin speed at 20 coins, where the weight attribute determines the rate at which each coin, from the 1st to the 20th, increases the racer's speed (Figure 1) [3].

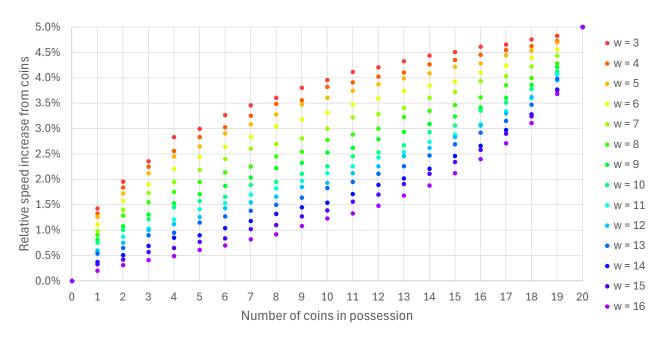


Figure 1. A simultaneous plot of $\varepsilon_{c,w}$ vs the number of coins in possession for $w=0,1,2,\ldots,13$.

 $\varepsilon = relative speed increase$

$$s = speed \ attribute$$
 $c = number \ of \ coins \ in \ possession$
 $w = weight \ attribute$
 $t = terrain \ identifier$
(lowercase means specific and uppercase means averaged)
 $\varepsilon_{s,t} \approx 0.312\% \cdot s_t$
(1)
$$\varepsilon_{s,t,c,w} = (1 + \varepsilon_{s,t})(1 + \varepsilon_{c,w}) - 1$$
(2)

There are four terrains in Mario Kart World. They are solid (e.g. asphalt, brick, metal, carpet, wood, ice), grainy (e.g. sand, soil, snow), water, and rails, air, and walls (abbreviated RAW). The solid, grainy, water, and RAW terrains constitute 51.88%, 21.31%, 7.47%, and 19.34% of all roads in Mario Kart World [3]. While the solid, grainy, and water terrains have distinct speed attributes, that for RAW terrain is 13 points across all character-vehicle combinations. These proportions inform the weighted mean speed increase.

$$\varepsilon_{s.T.c.w} = 0.5188\varepsilon_{s.solid.c.w} + 0.2131\varepsilon_{s.arainv.c.w} + 0.0747\varepsilon_{s.water.c.w} + 0.1934\varepsilon_{13.RAW.c.w}$$
(3)

2.2. The effects of the acceleration attribute

Meanwhile, the acceleration attribute determines the duration required to get to top speed from zero and the duration of boosts from drifting and tricking [3]. The boost types are mini-turbo, super mini-turbo, ultra mini-turbo, ramp tricks, mid-air or in-water tricks, rail tricks, and charge jumps. Only the boosts from ramp tricks and mid-air or in-water tricks were found to be independent of the acceleration attribute. The acceleration attribute for each character-vehicle combination is constant across all terrains.

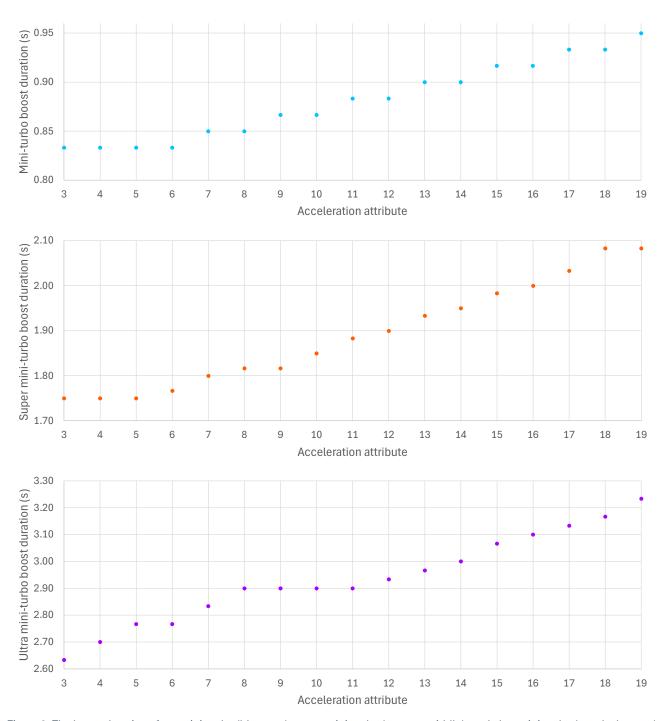


Figure 2. The boost durations for a mini-turbo (blue; top), super mini-turbo (orange; middle), and ultra mini-turbo (purple, bottom) as the acceleration attribute increases from 3 to 19 points.

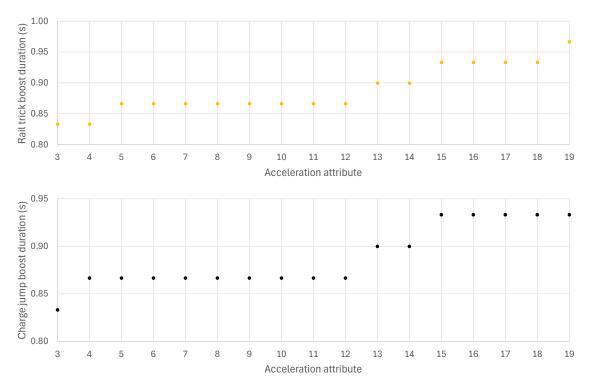


Figure 3. The boost durations for a rail trick (yellow; top), and charge jump (black; bottom) as the acceleration attribute increases from 3 to 19 points.

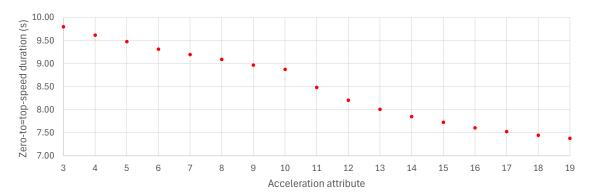


Figure 4. The zero-to-top-speed duration as the acceleration attribute increases from 3 to 19 points.

Given that the frequency of zero-to-top-speed occurrences is once per race [3], the reduction in the acceleration attribute's contribution to the reduction in the duration of a race was evaluated as half the reduction in the zero-to-top-speed duration from picking a higher acceleration attribute, assuming the speed increase from zero to top speed is linear.

 $a = acceleration \ attribute$ $\tau = race \ duration \ (s)$ $\zeta = zero\text{-}to\text{-}top\text{-}speed \ duration \ (s)$ $\tau_1, \tau_2 = different \ race \ duration \ (s)$ $a_1, a_2 = different \ acceleration \ attributes$ $v = racer \ top \ speed \ (px \ s^{-1})$ $\Delta x = racetrack \ distance \ (px)$

$$\Delta x = v \cdot (\tau_1 - \zeta|_{a_1}) + \frac{1}{2} (0 + v \cdot \zeta|_{a_1}) = v \cdot (\tau_2 - \zeta|_{a_2}) + \frac{1}{2} (0 + v \cdot \zeta|_{a_2})$$

$$\therefore \tau_1 - \tau_2 = \frac{1}{2} (\zeta|_{a = a_1} - \zeta|_{a = a_2})$$
(4)

The method used in this investigation is as follows.

3.1. The Markov chain of coin possession

In Queueing Theory, each possible number of coins in possession, from 0 to 20, is treated as a state. In this model, collecting coins means moving to a higher state and dispossessing coins, either by being hit by an item, running into an obstacle, falling off track and requiring Lakitu to intervene, or finishing a race and starting a new one, means moving to a lower state. Given that coins are collected one at a time, each mid-race dispossession is 3 coins or the entire possession, whichever is less, and coin possessions reset at the start of each race to between 0 and 5 coins depending on the racer's position, the model of the coin possession probabilities can be illustrated as follows.

 $\lambda = coin\ collection\ rate\ (min^{-1})$

 $\mu = coin\ dispossession\ rate\ (min^{-1})$

 $r = coin \ reset \ rate \ (i.e. \ frequency \ of \ races) \ (min^{-1})$

P = coin possession probabilities

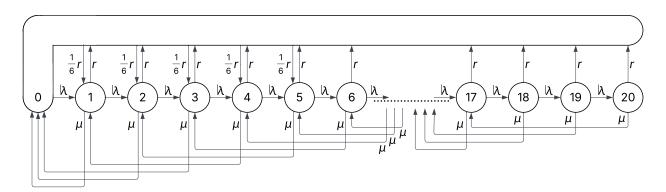


Figure 5. The Markov chain for coin possession in a 150cc Mario Kart World race.

Since the inflows and outflows at each state are balanced for any system at equilibrium, the following equations were derived.

$$-\lambda P_0 + \left(\mu + \frac{5}{6}r\right)(P_1 + P_2 + P_3) + \frac{5}{6}r(P_4 + P_5) + r(P_6 + P_7 + \dots + P_{20}) = 0$$
 (5)

for
$$1 \le c \le 5$$
, $\lambda P_{c-1} - \left(\lambda + \mu + \frac{5}{6}r\right)P_c + \mu P_{c+3} = 0$ (6)

for
$$6 \le c \le 17$$
, $\lambda P_{c-1} - (\lambda + \mu + r)P_c + \mu P_{c+3} = 0$ (7)

for
$$18 \le c \le 19$$
, $\lambda P_{c-1} - (\lambda + \mu + r)P_c = 0$ (8)

$$\lambda P_{19} - (\mu + r)P_{20} = 0 \tag{9}$$

and by definition
$$P_0 + P_1 + P_2 + \dots + P_{20} = 1$$
 (10)

Substituting Equation 8 into Equation 7 when c = 19 yields the following matrix-vector equation.

3.2. Finding the rates

An hour-long YouTube video of Mario Kart World online gameplay uploaded by Shortcat [4] was watched. The numbers of occurrences of coin collections, coin dispossessions, and drift boosts, trick boosts, and charge jumps of each kind were counted, and the race times were recorded. The coin collection, dispossession, and reset (i.e. the number of races) occurrences were divided by the total racing time to find λ , μ , and r. Similarly, the non-item boost rates were found by the number of occurrences divided by the total racing time.

3.3. Evaluating the expected overall speed

For each of the 480 unique character vehicle combinations (from 20 unique character classes and 24 unique vehicle attribute profiles), after evaluating $\varepsilon_{s,T,c,w}$ for all $1 \le c \le 20$ using Equations 1 to 3, finding the proportion of time spent in non-item boosts by the dot product of the boost rates and boost durations for the separated types, and finding the proportion of time saved from the zero-to-top-speed performance, the expected overall speed increase relative to the baseline during 150cc races E was evaluated using Equations 12 and 13. Finding the optimal character-vehicle combinations then required identifying the combination with the highest E and all runners-up within 0.100% from the highest E. (ε_{nib} was found through manual testing.)

E = expected overall speed increase relative to the baseline

 $\overrightarrow{B} = non\text{-}item boost rate column matrix (min}^{-1})$

 \overrightarrow{T} = non-item boost duration column matrix (s)

 $nib = non-item\ boost$

 $\tau_{mean} = mean \ race \ duration \ (s)$

$$\varepsilon_{s,T,c,w,a} \approx \left(1 + \varepsilon_{s,T,c,w}\right) \left(1 + \frac{1\min}{60 \text{ s}} \overrightarrow{B}_{(7\times 1)} \cdot \overrightarrow{T}_{(7\times 1)} \varepsilon_{nib}\right) \frac{\tau_{mean}}{\tau_{mean} - \frac{1}{2} (\zeta|_{a=3} - \zeta)} - 1 \qquad (12)$$

$$E = \sum_{c=0}^{20} P_c \cdot \varepsilon_{s,T,c,w,a} \tag{13}$$

3.4. Assumptions and simplifications

This investigation has relied on the following assumptions and simplifications:

- The terrain on which the racer is driving and the number of coins in possession were treated as independent events.
- The terrain on which the racer is driving and whether the racer is in a non-item boost were treated as independent events.

4. RESULTS

First, the following coin collection, dispossession, and reset rates were found (Table 1).

Table 1. The data collected on coin collection, dispossession, and resets [4].

Tota	al number of		Total racing time (min)	λ	μ	r
Coins collected	Dispossessions	Races	Total racing time (min)	(min^{-1})	(min^{-1})	(min^{-1})
411	61	20	46.40	8.858	1.315	0.4310

The coin possession probabilities were found to be higher towards 0 coins and at 19 coins or 20 coins (Figure 6). This trend is supported by anecdotal evidence from gameplay, as frontrunning and sandbagging both enable the racer to collect coins easily, chaos in the racer pack in median positions tends to minimise coin possession, and there are no known phenomena to keep coin possession counts away from the extremes.

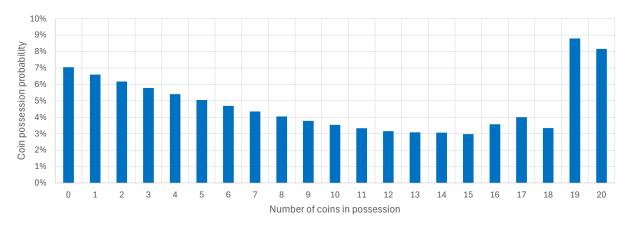


Figure 6. A bar chart of P_c versus c.

Then, the following non-item boost rates were found (Table 2). ε_{nib} was found to be 9%.

Table 2. The data collected on the non-item boost occurrences and rates.

Non-item	Mini-t	urbo drift l	boosts		Charge jumps			
boost type	(Basic)	Super	Ultra	Ramp	Mid-air or in-water	Rail or wall	Charge Jumps	
Occurrences	134	71	23	233	24	120	16	
Rates (min ⁻¹)	2.888	1.530	0.496	5.022	0.517	2.586	0.345	

In light of the coin possession probabilities and the effects of the acceleration attributes on the average racing speed, the optimal character-vehicle combinations were found to be a solid-focused heavyweight character (i.e. Wario or Wriggler) with the Reel Racer at $E_{max} \approx 10.086\%$ and a flyweight character (i.e. Swoop, Para-Biddybud, Baby Peach, or Baby Daisy) with the W-Twin Chopper at $E_{max} \approx 10.073\%$, with viable alternatives at $E \geq E_{max} - 0.100\%$ being a flyweight character with the Reel Racer, a solid-focused heavyweight character with the Junkyard Hog, and Bowser with the Reel Racer. Figure 6 shows their $\varepsilon_{s.T.c.w.a}$ versus c profiles.

Table 3. The attribute profile of the optimal combinations and the viable alternatives.

Obavastav alasa	Attributes								
<u>Character class</u> Vehicle	Speed			Acceleration	Weight	Handling			E (%)
venicle	Solid	Grainy	Water	Acceleration	vveigni	Solid	Grainy	Water	
<u>Solid Heavyweight</u> Reel Racer	17	16	16	6	12	9	7	7	10.086
<u>Flyweight</u> W-Twin Chopper	10	10	10	13	5	14	14	14	10.073
<u>Solid Heavyweight</u> Junkyard Hog	17	16	16	7	13	7	5	5	10.043
<u>Flyweight</u> Reel Racer	11	11	11	12	6	13	13	13	10.033
<u>Bowser</u> Reel racer	17	17	17	5	13	7	7	7	10.000

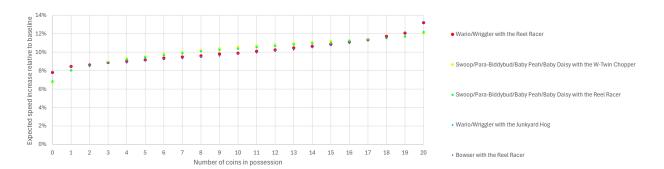


Table 4. A simultaneous plot of the $\varepsilon_{s,T,c,w,a}$ versus c profiles of the optimal combinations and the viable alternatives.

The results reveal two distinct dominant strategies to character and vehicle selection for 150cc races in Mario Kart World, being maximising the speed attribute with no other priorities or only while minimising the weight attribute and maintaining a reasonable acceleration attribute at 12 or 13 points. The maximum speed strategy maximises progress while the racer is uninterrupted, whereas the minimum weight strategy relies on faster recovery when necessary and higher speed increases at the middling numbers of coins in possession between 3 and 17 to compensate for the lower speed attribute. While the maximum speed strategy has a slightly higher \boldsymbol{E} for skilled Mario Kart World players, the higher handling attribute (in all non-RAW terrains) of the minimum weight strategy is more forgiving for most players.

The Reel Racer was featured in both strategies as it offered 8 points of speed attribute for all non-RAW terrains for only 3 points of weight attribute, being one of the most advantageous vehicles in maximising the speed attribute while limiting the weight attribute. The W-Twin Chopper, offering 7 points of speed attribute for all non-RAW terrains for 2 points of weight attribute, was paired only with the flyweight character class, since the benefits of reducing the weight attribute to maximise speed increases from coins are not as pronounced in the maximum speed strategy.

Where the speed attribute is not uniform across all non-RAW terrains, emphasis should be placed on that on solid terrain, as it is the most common out of all non-RAW terrains in Mario Kart World.

The solid-focused middleweight character (i.e. Mario or Rocky Wrench) with the Baby blooper, being 30th best at $E \approx 9.867\%$, is no longer a contender for the best character-vehicle combination.

5. CONCLUSION

To conclude, by using Queueing Theory to determine the probabilities of possessing any given number of coins during a race and evaluating the expected overall speed of every possible character-vehicle combination according to its speed increase from its speed attribute for each terrain, its weight-dependent coin effects, the coin possession probabilities, and the effects of its acceleration attribute on the drift and trick boost durations, this investigation has found the optimal character-vehicle combinations for 150cc races in Mario Kart World.

The results of this investigation reveal two distinct dominant strategies for Mario Kart World, being either maximising the speed attribute for maximum progress while the racer is uninterrupted or relying on faster recovery when necessary and higher speed increases at the middling numbers of coins in possession to enhance the racer's overall expected speed, that players may choose according to their preferred approach to the game.

The aim of this investigation was achieved successfully.

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