

Assignment Deep Learning

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Feed Forward Network

$inputs = [1, X_1, X_2, \dots, X_n]$

$weights = [W_0, W_1, W_2, \dots, W_n]$

$Z = X_0W_0 + X_1W_1 + X_2W_2 + \dots + X_nW_n$

Z is summation of product of Input and their Associated weights

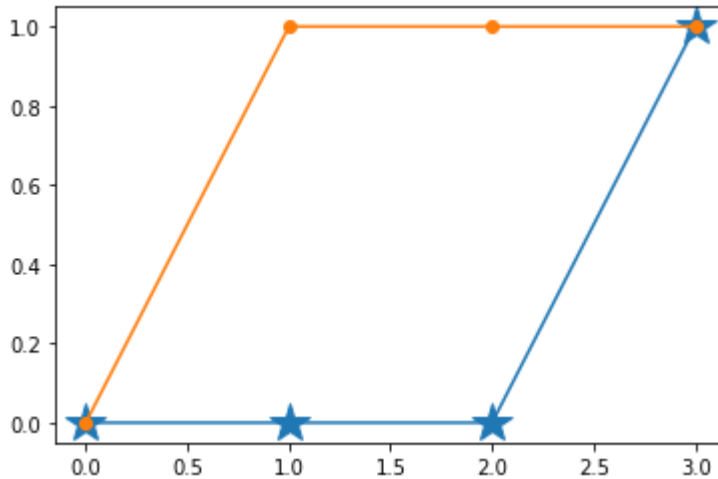
Step Function is used to decide output based on value of Z

```
In [10]: import numpy as np
import matplotlib.pyplot as plt
i_input=np.array([[0,0],[0,1],[1,0],[1,1]]) #input values of AND gate
labels=np.array([0,0,0,1]) #initially labels for each input of i_input set
weights=[0.784,0.897] #associated weights
threshold=0.54 #threshold value
# Defining step function
def step_fun(sum):
    if sum>threshold:
        return 1
    else:
        return 0
#iterating through i_input array to calculate Z
updated_labels=[]
for i in range(0, i_input.shape[0]):
    actual_value=labels[i]
    instances=i_input[i]
    x0=instances[0]
    x1=instances[1]
    z=x0*weights[0]+x1*weights[1] # Z is sum of Product of Inputs and their ass
    fire= step_fun(z)
    updated_labels.append(fire)
    delta=actual_value-fire #delta is Error (When Error is 0 it means predict
    print("Predicted value ", fire, " Whereas Actual Value", labels[i], " Error
```

```
Predicted value 0 Whereas Actual Value 0 Error is 0
Predicted value 1 Whereas Actual Value 0 Error is -1
Predicted value 1 Whereas Actual Value 0 Error is -1
Predicted value 1 Whereas Actual Value 1 Error is 0
```

```
In [2]: plt.plot(labels, marker='*', ms=20)
plt.plot(updated_labels, marker='o')
```

```
Out[2]: [<matplotlib.lines.Line2D at 0x7f72c46b7e48>]
```



SUMMARY

We have a set of input along with actual output. Now this model associates some weights randomly in order to predict the output. We have can track whether our outcome is Correctly predicted or not with the help of Error (delta).

In above graph Orange Circles indicate Actual Value and Blue Stars indicate Predicted Value . We can see that for 3rd input [1,0] Predicted and Actual outcomes vary

This Variation can be solved using Gradient Descent approach by using Learning rate for Weight Updation

Perceptron Training Rule

Learning Problem is to determine Weights that causes perceptron to produce correct output

delta- delta is the difference between Predicted and Actual outputs ¶

We keep on modifying weights whenever it misclassifies an example. Weights are modified at each step iteratively according to perceptron learning rate until it classifies all training examples correctly

$$W_i = W_i + \Delta W$$

$$\Delta W = \eta(t-o)X_i$$

η is positive learning rate. Role of η to moderate degree at which weights are changing

```

In [5]: import numpy as np
import matplotlib.pyplot as plt
i_input=np.array([[0,0],[0,1],[1,0],[1,1]]) #input values of AND gate
y=np.array([0,0,0,1]) #y is target output for each input of i_input set
w=[0.78,0.91] #associated weights
threshold=0.54 #threshold value
iteration=5
eta=0.1 #eta is learning rate

# Defining step function
def step_fun(sum):
    if sum>threshold:
        return 1
    else:
        return 0
print("Initial Weights ", w)

#iterating through i_input array to calculate Z
updated_labels=[]
for j in range(0,iteration):
    print("Iteration ",j)
    print("Actual(y)", " ", "Predicted(y')", " ", "Error")
    for i in range (0, i_input.shape[0]):
        actual_value=y[i]
        instances=i_input[i]
        x0=instances[0]
        x1=instances[1]
        z=x0*w[0]+x1*w[1] # Z is sum of Product of Inputs and their associated
        fire= step_fun(z)
        updated_labels.append(fire)
        delta=actual_value-fire #delta is Error (When Error is 0 it means pre
        print( y[i], " "*12,fire," "*12,delta)
        w[0]=w[0]+delta*eta #Updating Weights
        w[1]=w[1]+delta*eta
    print("_"*35)
print("Updated Weights after Iteration",w) #Updated Weights after learning

```

```

Initial Weights [0.78, 0.91]
Iteration 0
Actual(y)    Predicted(y')    Error
0            0              0
0            1              -1
0            1              -1
1            1              0

```

```

Iteration 1
Actual(y)    Predicted(y')    Error
0            0              0
0            1              -1
0            0              0
1            1              0

```

```

Iteration 2
Actual(y)    Predicted(y')    Error
0            0              0
0            1              -1
0            0              0
1            1              0

```

```

Iteration 3
Actual(y)    Predicted(y')    Error
0            0              0
0            0              0
0            0              0
1            1              0

```

Iteration	4		
Actual(y)	Predicted(y')	Error	
0	0	0	
0	0	0	
0	0	0	
1	1	0	

Updated Weights after Iteration [0.38000000000000001, 0.51000000000000001]

Summary

Initially a random weight was chosen and the Two predicted outputs were misclassified.

After applying Perceptron Training Rule , Weights were Modified till it classified Examples correctly till some iteration

Initially weights was [0.78,0.91] after Updation [0.38, 0.51] and this updated weights predicted output Correctly after few iterations

Gradient Descent

Activation fun $1/(1+e^{-\text{weighted_sum}})$

$\text{weighted_sum} = W_1X_1 + W_2X_2 + \dots W_iX_i + \text{Bias}$

$\text{Loss} = -(\text{target} \log(\text{pred}) + (1 - \text{target}) \log(1 - \text{pred}))$

$W_i = W_i + \Delta W$

$\Delta W = \eta(t - o)X_i$

$\text{New Bias}(b') = \text{Old Bias}(b) + \eta(\text{target} - \text{predicted})$

η is Learning rate which ensures gradual weight update

Bias helps to tune our model .

```
In [ ]: import numpy as np
import matplotlib.pyplot as plt
def Activation_fun(z): #z is weighted sum of input and associated weights
    return 1/(1+np.e**(-z))
def get_prediction(Input,Weights,bias):
    return Activation_fun(np.dot((Input,Weights)+bias))
def Gradient_Descent(Input, Weights, Target, Prediction, eta,bias):
    new_weight=[]
    bias=bias+eta*(Target-Prediction)
    for x,w in zip(Input,Weights):
        new_w=w+eta*(Target-Prediction)*x
        new_weight.append(new_w)
    return new_weight,bias

#DATA
Input=np.array([[0,1,0],[0,1,1],[1,1,0],[1,1,1],[1,0,0]])
Target=np.array([0,1,1,0,1])
Weights=np.array([0.3,0.1,0.5,-0.1,0.45])
bias=0.5
eta=0.01
for i in range(10):
    for x,y in zip(Input, Target):
        pred=get_prediction(x,Weights, bias)
        weights,bias=Gradient_Descent(x,Weights,y,pred,eta,bias)
```