## 1. Plain TEXnology

**Theorem T.** All things are not necessarily the same

## 2. Permutations

TAoCP\* 1.2.5 gives two methods to generate all permutations of a given ordered set. Quantites of permutations are considered with relevance to computing efficiencies.

## 3. The Wide-Awake example Group

We re-think, re-word, and re-start with a set of attributes, elements or objects,  $W = \{woozy, vacuous, sleepy, wide - awake\}$ . These elements are used to generate all possible arrangements  $\eta$  which are orderd n-tuples with  $1 \le n \le 4$ . For example,  $\eta = (woozy, wide - awake)$  is a 2-tuple. Now the set Woozy is the set of all permutations that jumble such elements like  $\eta$ 

Let  $(Woozy, \circ, 0, -)$  be the group with the set Woozy, a binary operation  $\circ$ , a neutral elment 0, and for each element  $\pi \in Woozy$  there is an inverse element  $-\pi \in Woozy$  such that  $\pi \circ -\pi = 0$ .

For now, here, we call this group's binary operation *composition*. Given two elements  $\pi, \eta \in Woozy$ , then  $\pi \circ \eta \in Woozy$  and  $\eta \circ \pi \in Woozy$ .

Permutations 1

<sup>\*</sup> https://www-cs-faculty.stanford.edu/%7Eknuth/taocp.html