

1. Plain TeXnology

Theorem T. *All things are not necessarily the same*

2. Permutations

TAoCP* 1.2.5 gives two methods to generate all permutations of a given ordered set. Quantities of permutations are considered with relevance to computing efficiencies.

3. The Wide-Awake example Group

We re-think, re-word, and re-start with a set of attributes, elements or objects, $W = \{ \text{woozy, vacuous, sleepy, wide-awake} \}$. These elements are used to generate all possible arrangements η which are ordered n -tuples with $1 \leq n \leq 4$. For example, $\eta = (\text{woozy, wide-awake})$ is a 2-tuple. Now the set *Woozy* is the set of all permutations that jumble such elements like η .

Let $(\text{Woozy}, \circ, 0, -)$ be the group with the set *Woozy*, a binary operation \circ , a neutral element 0, and for each element $\pi \in \text{Woozy}$ there is an inverse element $-\pi \in \text{Woozy}$ such that $\pi \circ -\pi = 0$.

For now, here, we call this group's binary operation *composition*. Given two elements $\pi, \eta \in \text{Woozy}$, then $\pi \circ \eta \in \text{Woozy}$ and $\eta \circ \pi \in \text{Woozy}$.

* <https://www-cs-faculty.stanford.edu/%7Eknuth/taocp.html>