

(* Comandos usan [], listas o estructuras de almacenamiento usan {}, metodos usan → *)
 (* Si pones xy wolfram piensa que es el nombre de una variable,
 si pones x y, como tiene espacio, wolfram piensa que es el producto x * y *)
 (* Ctrl + 6: exponentes

Con tab mueves entre espacios de escritura, el actual espacio se pinta en azul.

Alt + arriba o abajo con mouse: zoom a un plot (debe hacerse sobre el plot) *)

(* Tienes un metodo, por ejemplo PlotTheme,

y quiero que el tema sea tanto Detailed como clasico,

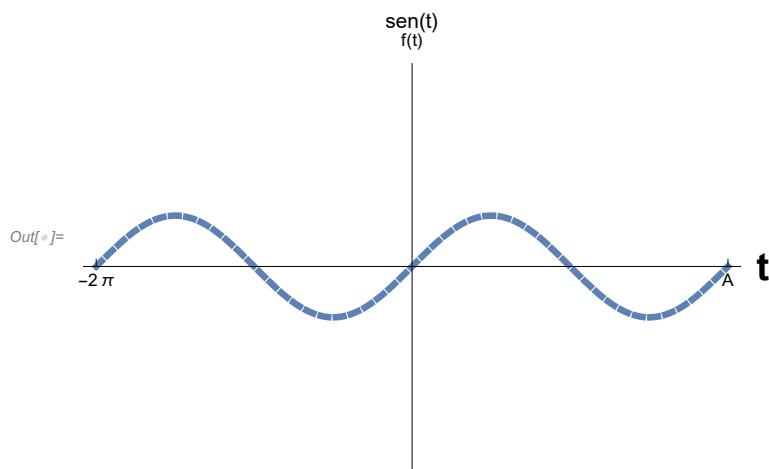
entonces cambias el input del metodo por una lista de parámetros dentro de {}

A cualquier constante de texto ("") se le puede hacer un StyleForm *)

```
Plot[Sin[x], {x, -2 Pi, 2 Pi}, PlotRange → { $-\frac{8}{2}$ ,  $\frac{8}{2}$ },
```

```
PlotStyle → {Dashed, Thickness[0.01]}, AxesLabel → {StyleForm["t", Bold, 20], "f(t)"},  

Ticks → {{-2 Pi, {2 Pi, "A"}}, None }, PlotLabel → "sen(t)"]
```



In[]:=

```
Plot3D[ $\sqrt{x^2 + y^2}$ , {x, -4, 4}, {y, -4, 4},
```

```
PlotLabel → "Cono (coordenadas cartesianas)", PlotTheme → "Automatic"]
```

(* Cono con Plot3D, y este comando necesita funciones*)

```
ParametricPlot3D[{{r Cos[t], r Sin[t], r}}, {r, 0, 2},  

{t, 0, 2 Pi}, Mesh → None, PlotStyle → {Opacity[0.5]},
```

```
PlotLabel → "Cono (coordenadas polares)", PlotTheme → "Detailed"]
```

(* Si no tienes o quieres comandos, mejor parametrizas con coordenadas polares *)

(* Si definimos parametrización en coordenadas cartesianas, tendríamos x = u,

y = v, donde z (dependiente) resultaría igual. Como no sirve,

usamos parametrizaciones llamadas coordenadas polares, esféricas, etc. *)

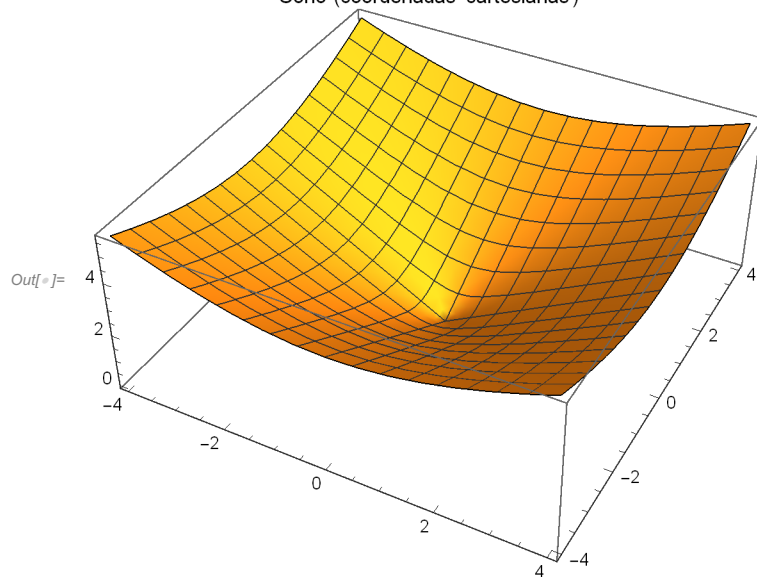
```
ParametricPlot3D[{{r Cos[t], r Sin[t], r^2}}, {r, 0, 2},
```

```
{t, 0, 2 Pi}, Mesh → None, PlotStyle → {Opacity[0.8]}, PlotLabel →
```

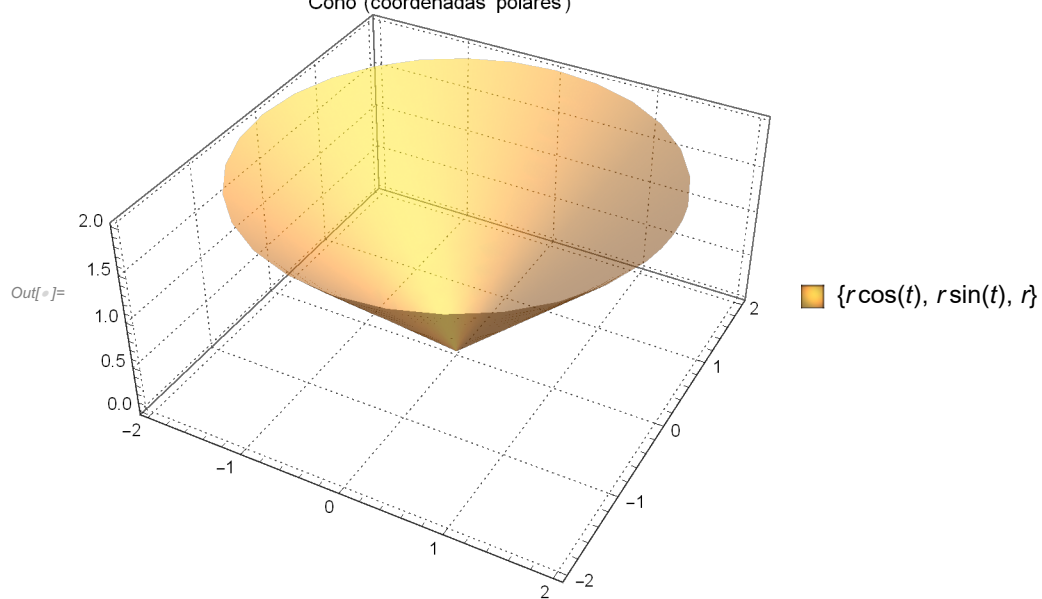
```
StyleForm["Paraboloid (coordenadas polares)", Bold, 15, FontFamily → "Helvetica"],
```

```
PlotTheme → {"Detailed", "Classic"}]
```

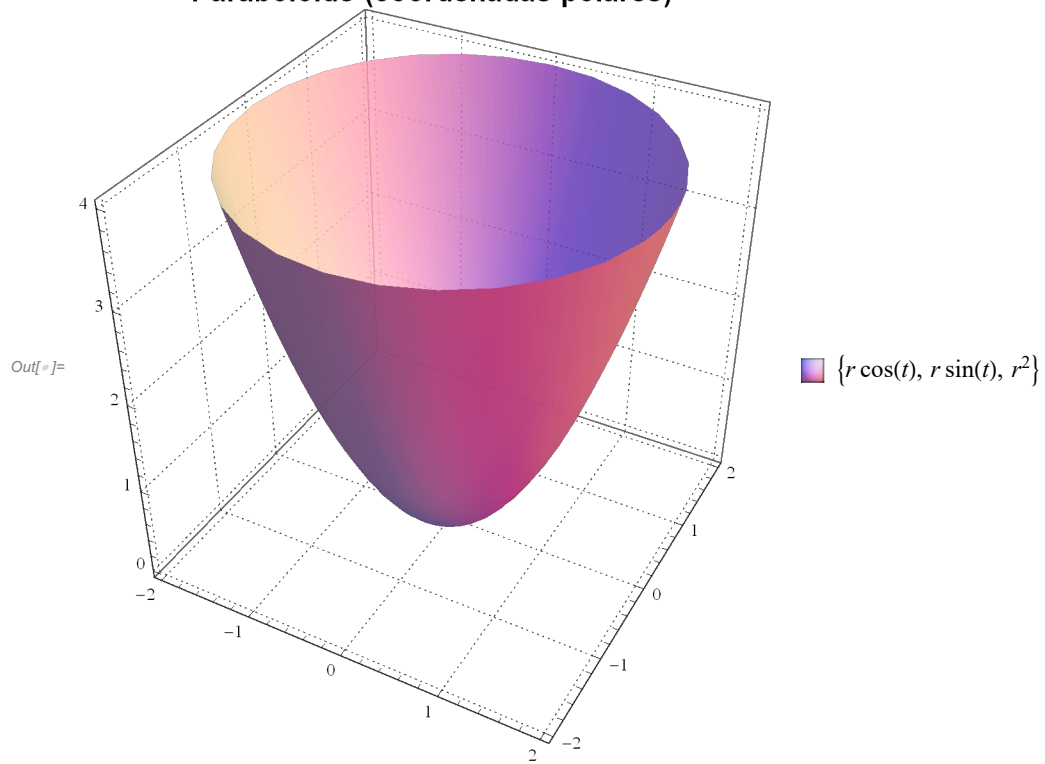
Cono (coordenadas cartesianas)



Cono (coordenadas polares)

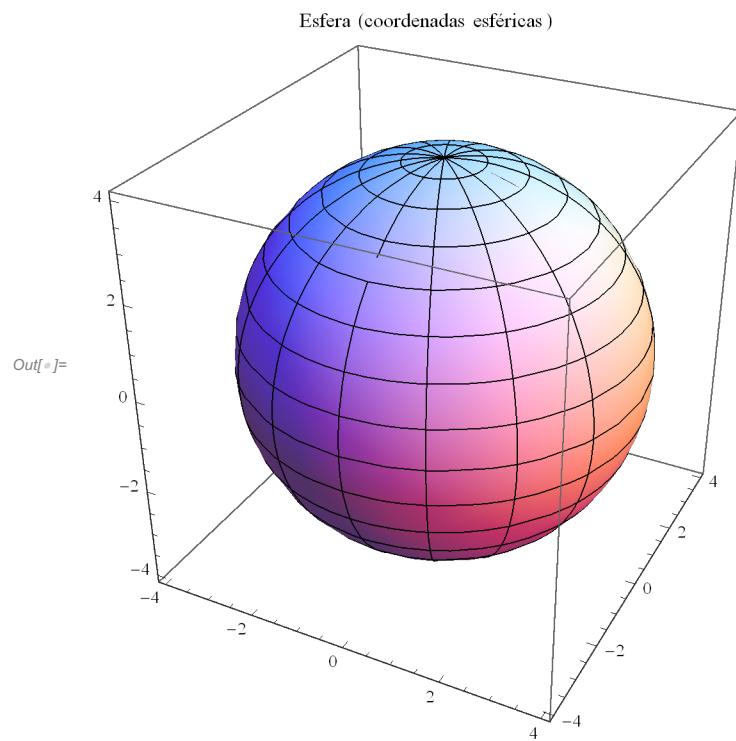


Paraboloide (coordenadas polares)



(* Hacer esfera con parametrización de coordenadas esféricas *)

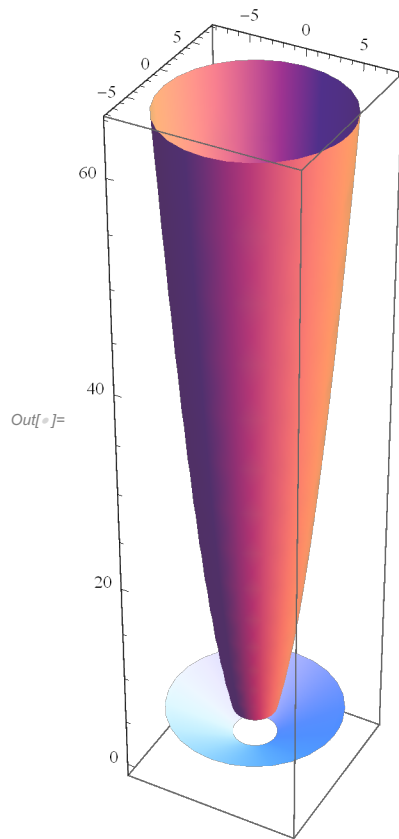
```
In[ ]:= ParametricPlot3D[{{4 Sin[x] Cos[t], 4 Sin[x] Sin[t], 4 Cos[x]}}, {x, 0, Pi},  
  {t, 0, 2 Pi}, PlotLabel -> "Esfera (coordenadas esféricas)", PlotTheme -> "Classic"]
```



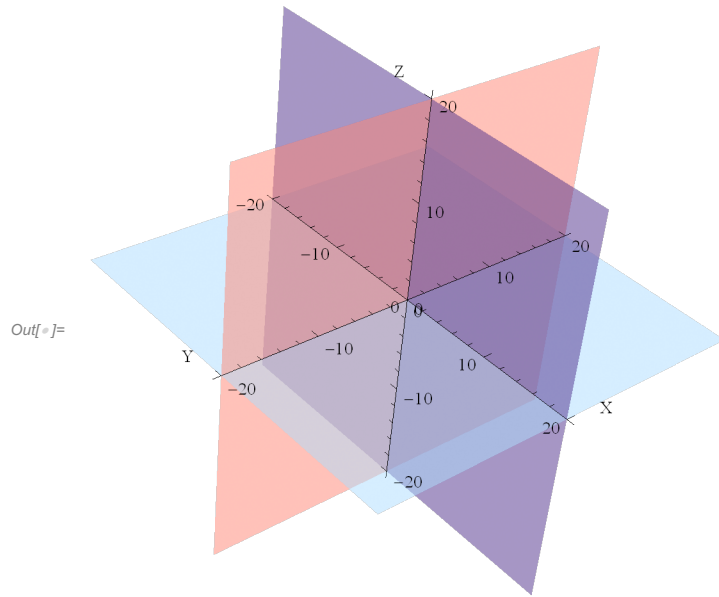
```

In[ ]:= fig1 = ParametricPlot3D[{{r Cos[t], r Sin[t],  $\frac{1}{2} r$ }, {r Cos[t], r Sin[t],  $r^2$ }},
  {r, 2, 8}, {t, 0, 2 Pi}, Mesh -> None, PlotTheme -> "Classic"]

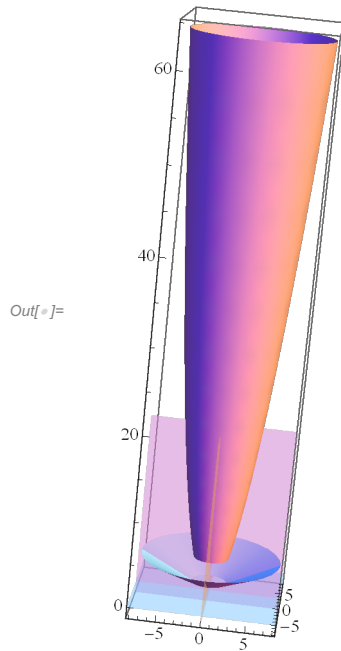
```



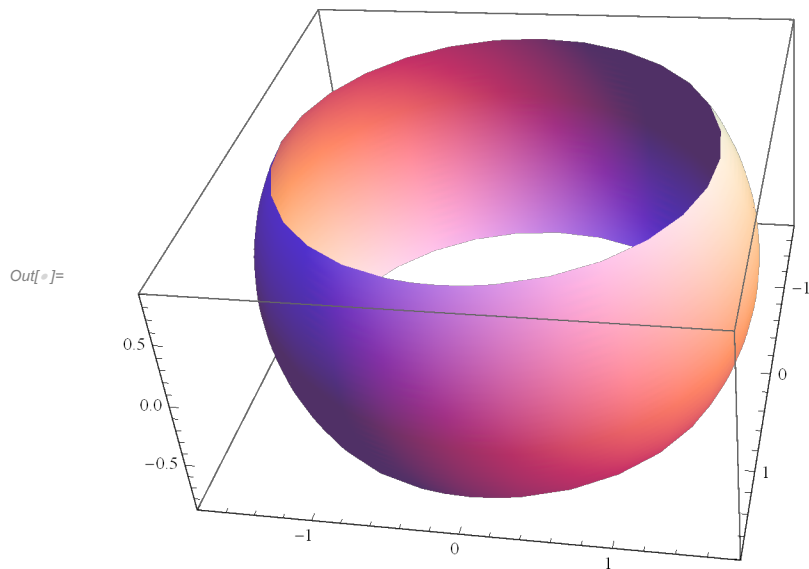
```
In[8]:= planos = ParametricPlot3D[{{a, b, 0}, {a, 0, b}, {0, a, b}}, {a, -20, 20},  
  {b, -20, 20}, Mesh → None, PlotStyle → {Opacity[0.5]}, PlotTheme → "Classic",  
  Boxed → False, AxesOrigin → {0, 0, 0}, AxesLabel → {"X", "Y", "Z"}]
```



In[]:= Show[fig1, planos]



In[]:= ParametricPlot3D[{{ $\sqrt{3} \sin[x] \cos[t]$, $\sqrt{3} \sin[x] \sin[t]$, $\sqrt{3} \cos[x]$ }},
 $\{x, \pi / 3, (2 * \pi) / 3\}, \{t, 0, 2 \pi\}, \text{Mesh} \rightarrow \text{None}, \text{PlotTheme} \rightarrow \text{"Classic"}$]

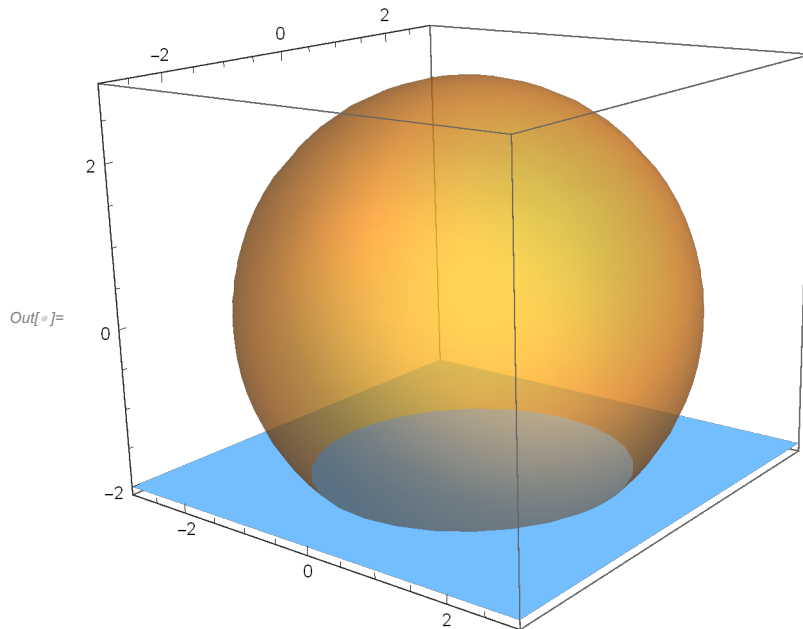


(* porción superior de esfera $x^2 + y^2 + z^2 = 8$ cortada por plano $z = -2$ *)

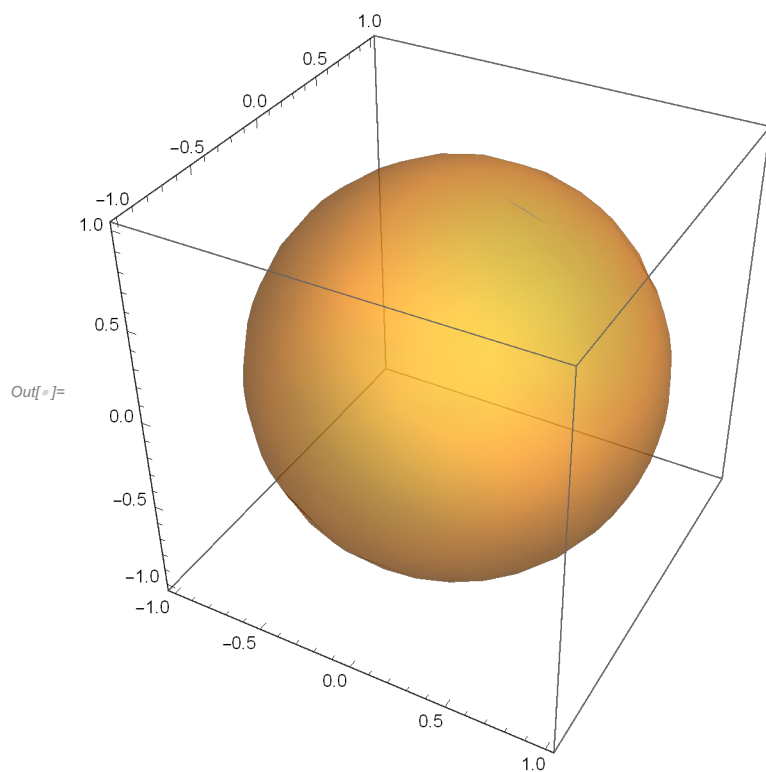
```

In[ ]:= esfera1 =
  ParametricPlot3D[{2 Sqrt[2] Sin[x] Cos[t], 2 Sqrt[2] Sin[x] Sin[t], 2 Sqrt[2] Cos[x]}, {x, 0,  $\frac{3\pi}{4}$ },
    {t, 0, 2 Pi}, Mesh -> None, PlotTheme -> "Automatic", PlotStyle -> {Opacity[0.5]}]
planoZ = ParametricPlot3D[{x, y, -2}, {x, -4, 4},
  {y, -4, 4}, Mesh -> None, PlotTheme -> "Classic"]
In[ ]:= Show[esfera1, planoZ]

```



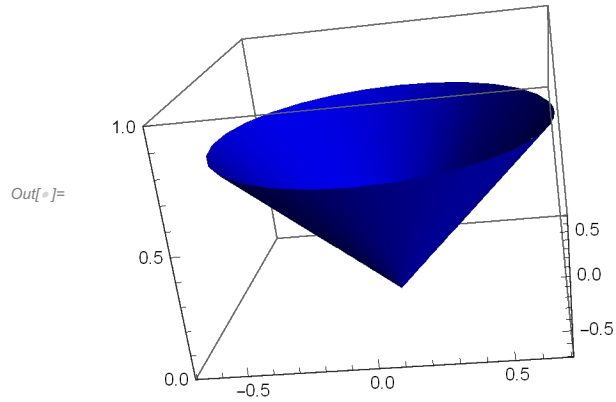

```
In[ ]:= esfera2 = ParametricPlot3D[{Sin[x] Cos[t], Sin[x] Sin[t], Cos[x]}, {x, 0, Pi},  
  {t, 0, 2  $\pi$ }, Mesh  $\rightarrow$  None, PlotTheme  $\rightarrow$  "Automatic", PlotStyle  $\rightarrow$  {Opacity[0.5]}]
```



```

In[ ]:= cono2 = ParametricPlot3D[{r Cos[t], r Sin[t], r}, {r, 0,  $\frac{1}{\sqrt{2}}$ }, {t, 0, 2 Pi},
    Mesh -> None, PlotStyle -> {Blue}, PlotRange -> {{ $\frac{-1}{\sqrt{2}}$ ,  $\frac{1}{\sqrt{2}}$ }, { $\frac{-1}{\sqrt{2}}$ ,  $\frac{1}{\sqrt{2}}$ }, {0, 1}}]

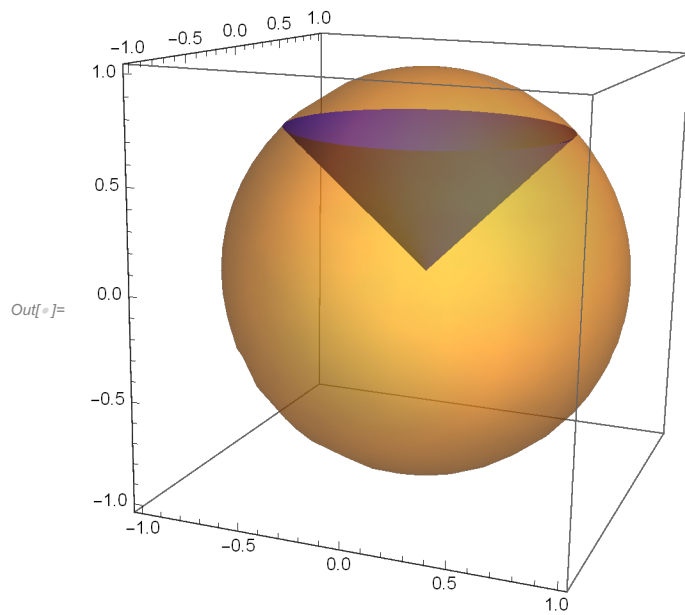
```



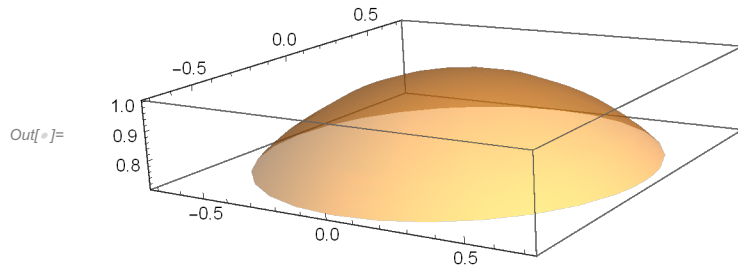
```

In[ ]:= Show[esfera2, cono2]

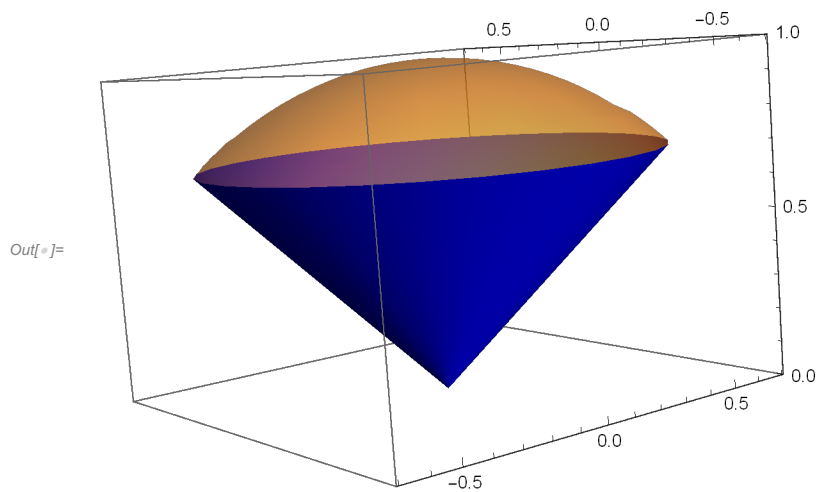
```



```
esfera3 = ParametricPlot3D[{Sin[x] Cos[t], Sin[x] Sin[t], Cos[x]}, {x, 0, Pi / 4},
  {t, 0, 2 Pi}, Mesh → None, PlotTheme → "Automatic", PlotStyle → {Opacity[0.5]}]
```



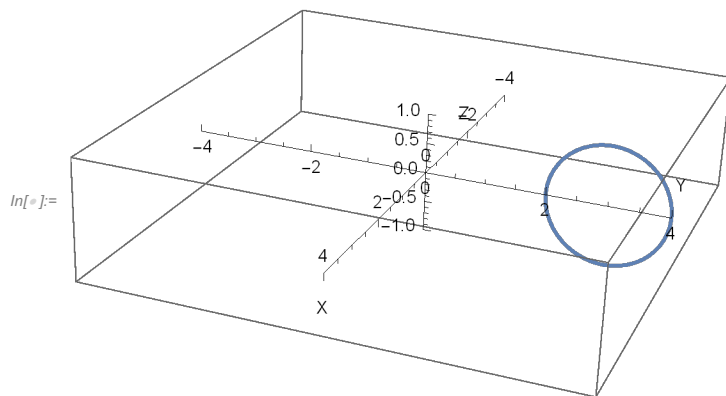
```
In[ ]:= Show[cono2, esfera3]
```



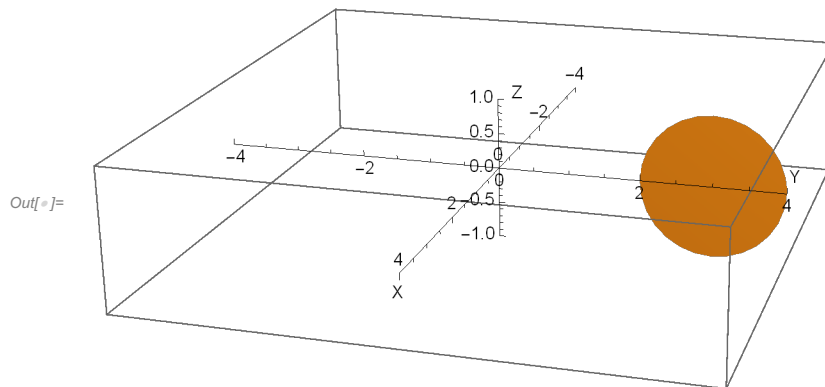
(* 1*)

```
(*ParametricPlot3D[{0, r Cos[x], r Sin[x]}, {r, 0, 2 Cos[x]},
  {x, -Pi / 2, Pi / 2}, AxesOrigin→{0, 0, 0}, AxesLabel→ {"X", "Y", "Z"}]*)
(* cambias centro en x, y la dejas en sinX porque ya está centrada *)
```

```
In[ ]:= ParametricPlot3D[{0, (3 + Cos[x]), Sin[x]}, {x, 0, 2 Pi}, AxesOrigin → {0, 0, 0},
  AxesLabel → {"X", "Y", "Z"}, PlotRange → {{-4, 4}, {-4, 4}, {-1, 1}}]
```



```
ParametricPlot3D[{0, (3 + r Cos[x]), r Sin[x]}, {x, 0, 2 Pi},
  {r, 0, 1}, AxesOrigin -> {0, 0, 0}, AxesLabel -> {"X", "Y", "Z"},
  PlotRange -> {{-4, 4}, {-4, 4}, {-1, 1}}, Mesh -> None]
```

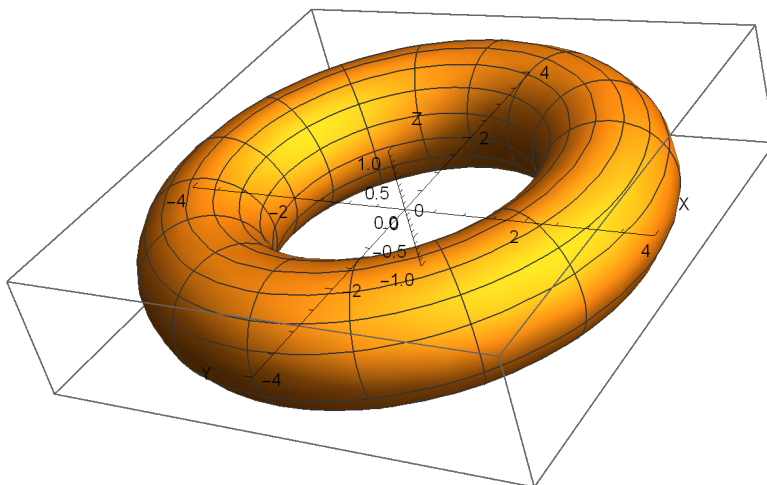


(* Ahora la distancia al origen es $3 + \cos X$ *)

distance = $(3 + \cos[x])$

```
In[ ]:= ParametricPlot3D[{distance * Cos[t], distance * Sin[t], Sin[x]},  
  {x, 0, 2 Pi}, {t, 0, 2 Pi}, AxesOrigin -> {0, 0, 0},  
  AxesLabel -> {"X", "Y", "Z"}, PlotRange -> {{-4, 4}, {-4, 4}, {-1, 1}}]
```

Out[]:=

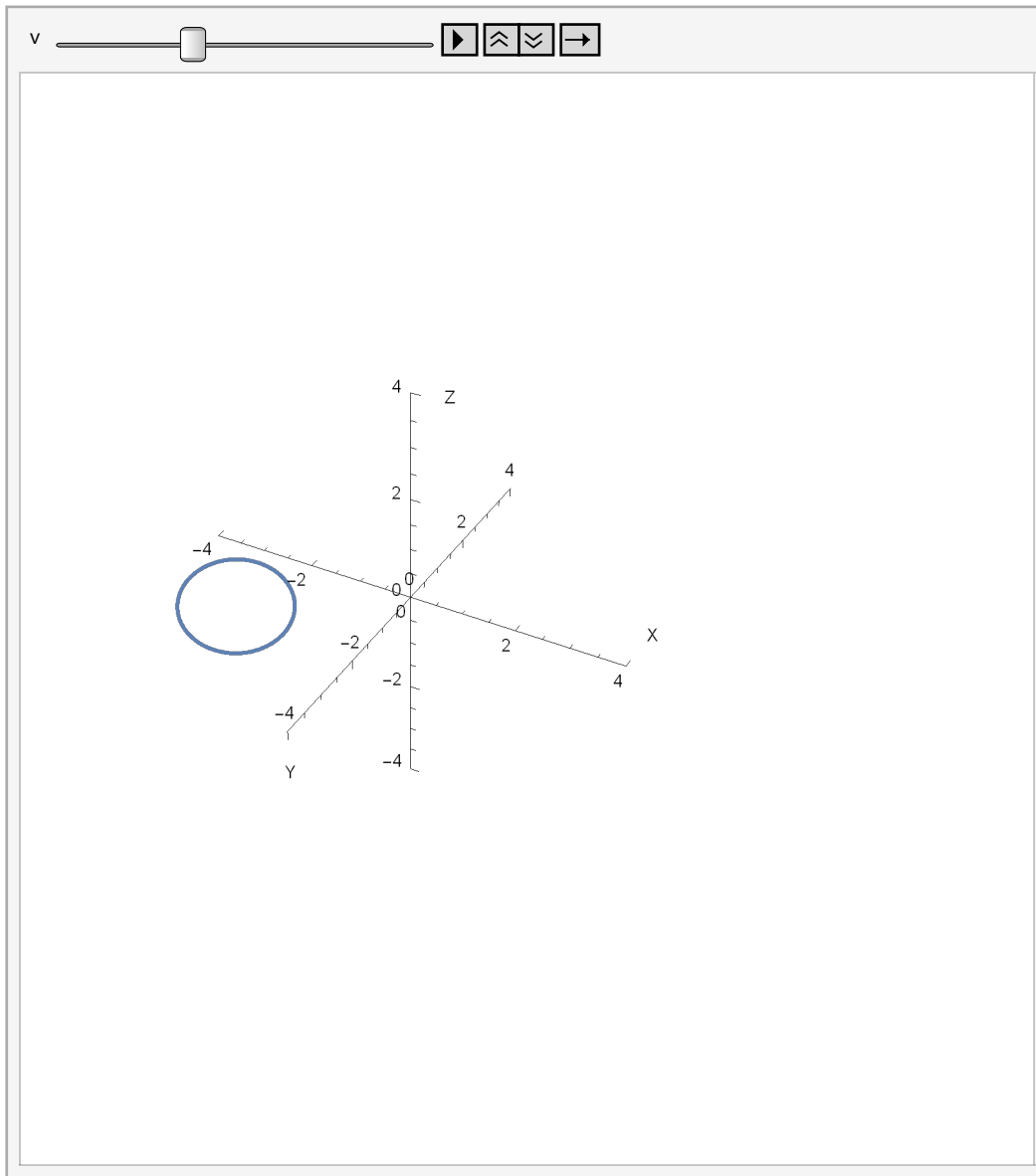


```

Animate[ParametricPlot3D[RotationMatrix[v, {0, 0, 1}].{0, (3 + Cos[x]), Sin[x]},
  {x, 0, 2 Pi}, AxesOrigin -> {0, 0, 0}, AxesLabel -> {"X", "Y", "Z"}, Boxed -> False,
  PlotRange -> {{-4, 4}, {-4, 4}, {-4, 4}}, {v, 0, 2 Pi}, AnimationRunning -> False]
RotationMatrix[v, {0, 0, 2}] // MatrixForm
(*RotationMatrix[v, {0, 0, 1}].{0, (3 + Cos[x]), Sin[x]} esto funciona
generando cada punto y rotándolo, porque una parametrización ya es una matriz *)

```

Out[]=



Out[]//MatrixForm=

$$\begin{pmatrix} \cos[v] & -\sin[v] & 0 \\ \sin[v] & \cos[v] & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

```
(* Esto es el eje de rotacion, si dejan de ser ejes coordenados {1, 0, 0},
{0, 1, 0}, {0, 0, 1}, la matriz se complica mas. *)
RotationMatrix[v, {0, 1, 0}] // MatrixForm
```

Out[]//MatrixForm=

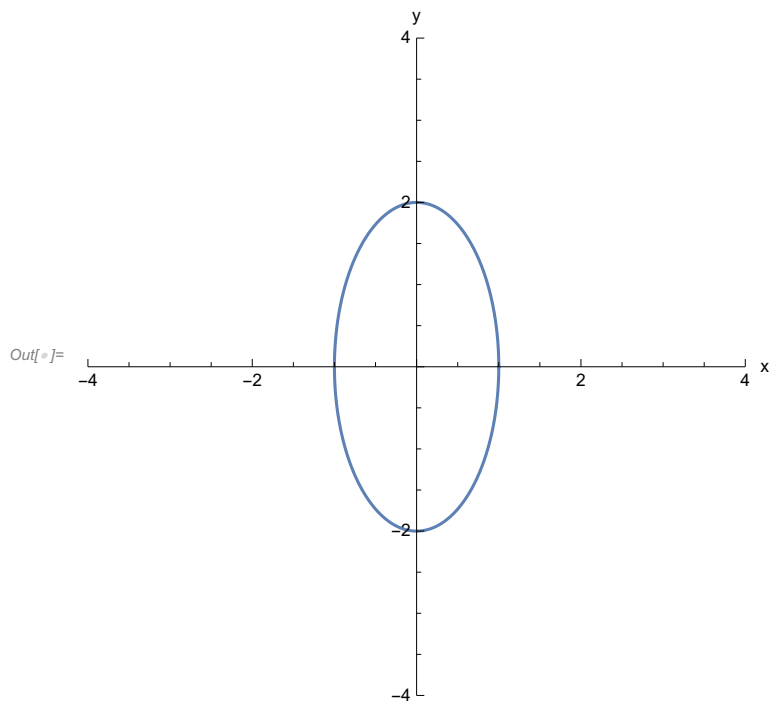
$$\begin{pmatrix} \cos[v] & 0 & \sin[v] \\ 0 & 1 & 0 \\ -\sin[v] & 0 & \cos[v] \end{pmatrix}$$

```
In[ ]:= RotationMatrix[v, {1, 0, 0}] // MatrixForm
```

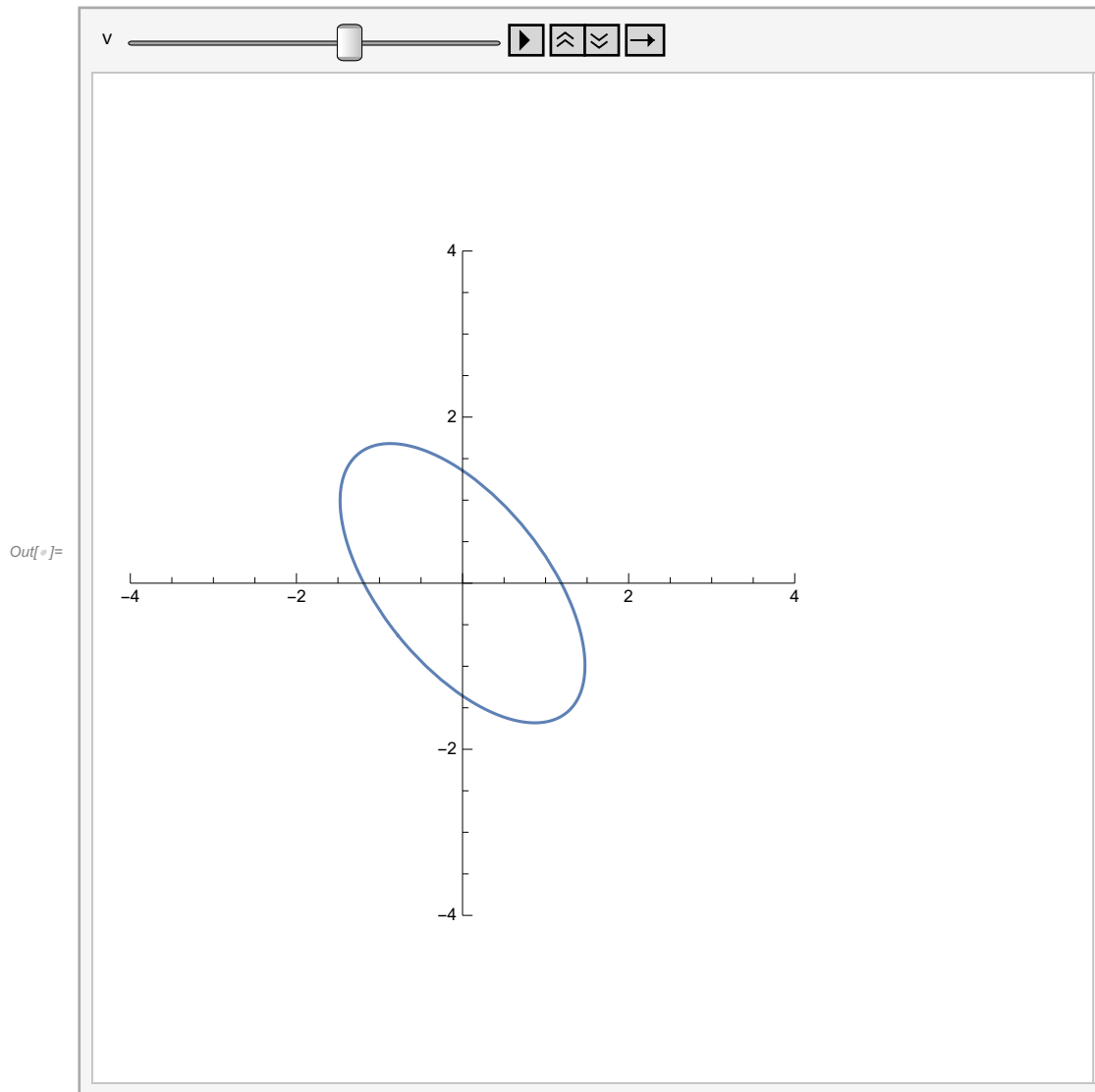
Out[]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos[v] & -\sin[v] \\ 0 & \sin[v] & \cos[v] \end{pmatrix}$$

```
In[ ]:= ParametricPlot[{Cos[t], 2 Sin[t]}, {t, 0, 2 \pi},
PlotRange -> {{-4, 4}, {-4, 4}}, AxesLabel -> {"x", "y"}]
```



```
In[ ]:= Animate[ParametricPlot[RotationMatrix[v].{Cos[t], 2 Sin[t]}, {t, 0, 2 Pi},
  PlotRange -> {{-4, 4}, {-4, 4}}, {v, 0, 2 Pi}, AnimationRunning -> False]
```



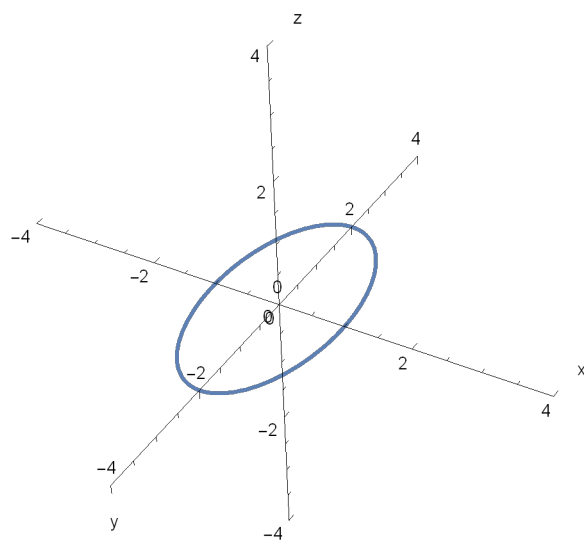
RotationMatrix[v] // MatrixForm (*Matriz de rotación 2D, con eje y {0, 1}*)

Out[]//MatrixForm=

$$\begin{pmatrix} \cos[v] & -\sin[v] \\ \sin[v] & \cos[v] \end{pmatrix}$$


```
In[ ]:= ParametricPlot3D[{Cos[t], 2 Sin[t], 0}, {t, 0, 2  $\pi$ }, AxesOrigin -> {0, 0, 0},  
  AxesLabel -> {"x", "y", "z"}, PlotRange -> {{-4, 4}, {-4, 4}, {-4, 4}}, Boxed -> False]
```

Out[]:=

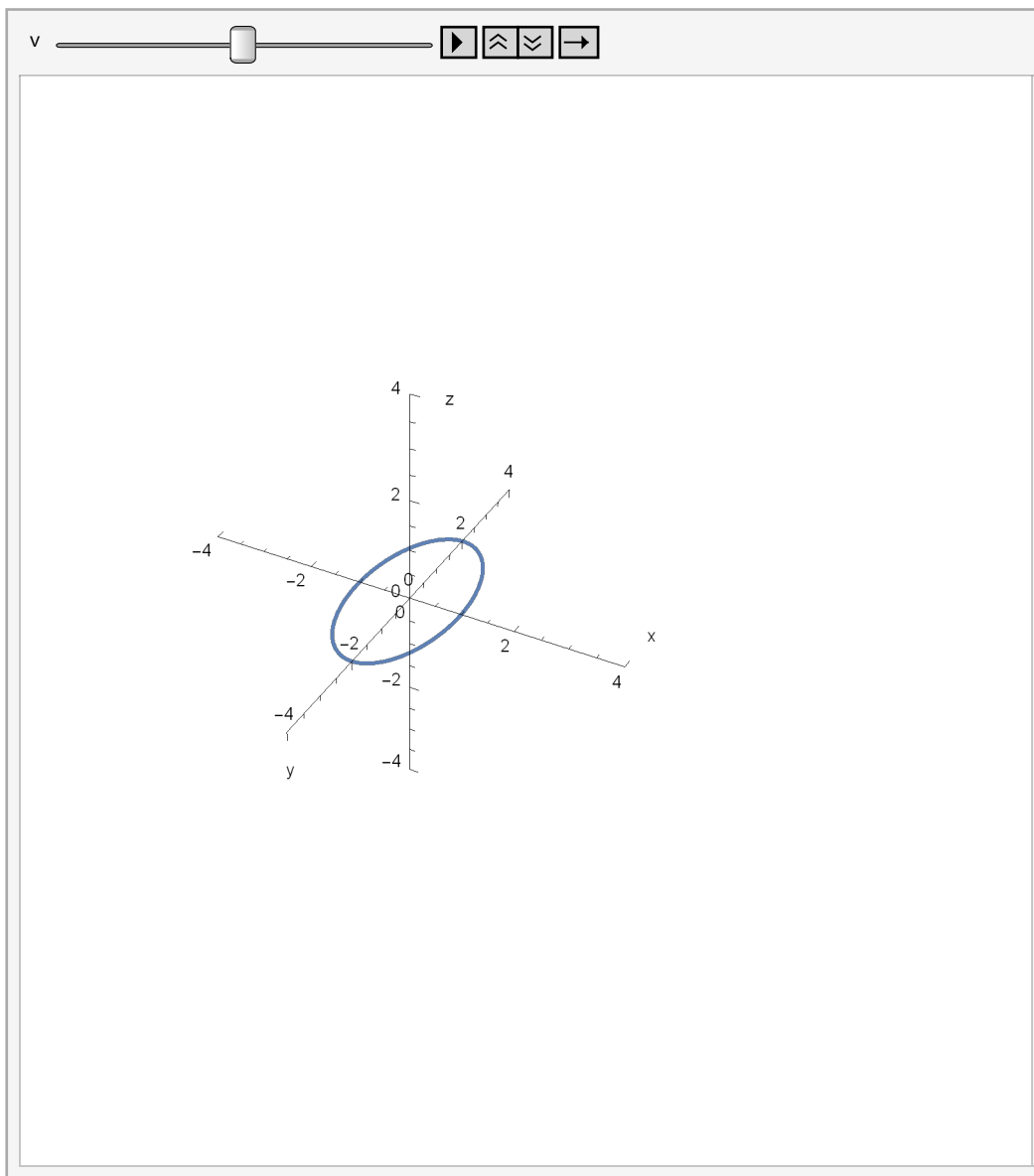


```

In[ ]:= Animate[ParametricPlot3D[RotationMatrix[v, {0, 0, 1}].{Cos[t], 2 Sin[t], 0},
  {t, 0, 2  $\pi$ }, AxesOrigin -> {0, 0, 0}, AxesLabel -> {"x", "y", "z"},
  PlotRange -> {{-4, 4}, {-4, 4}, {-4, 4}}, Boxed -> False],
  {v, 0, 2  $\pi$ }, AnimationRunning -> False]

```

Out[]:=

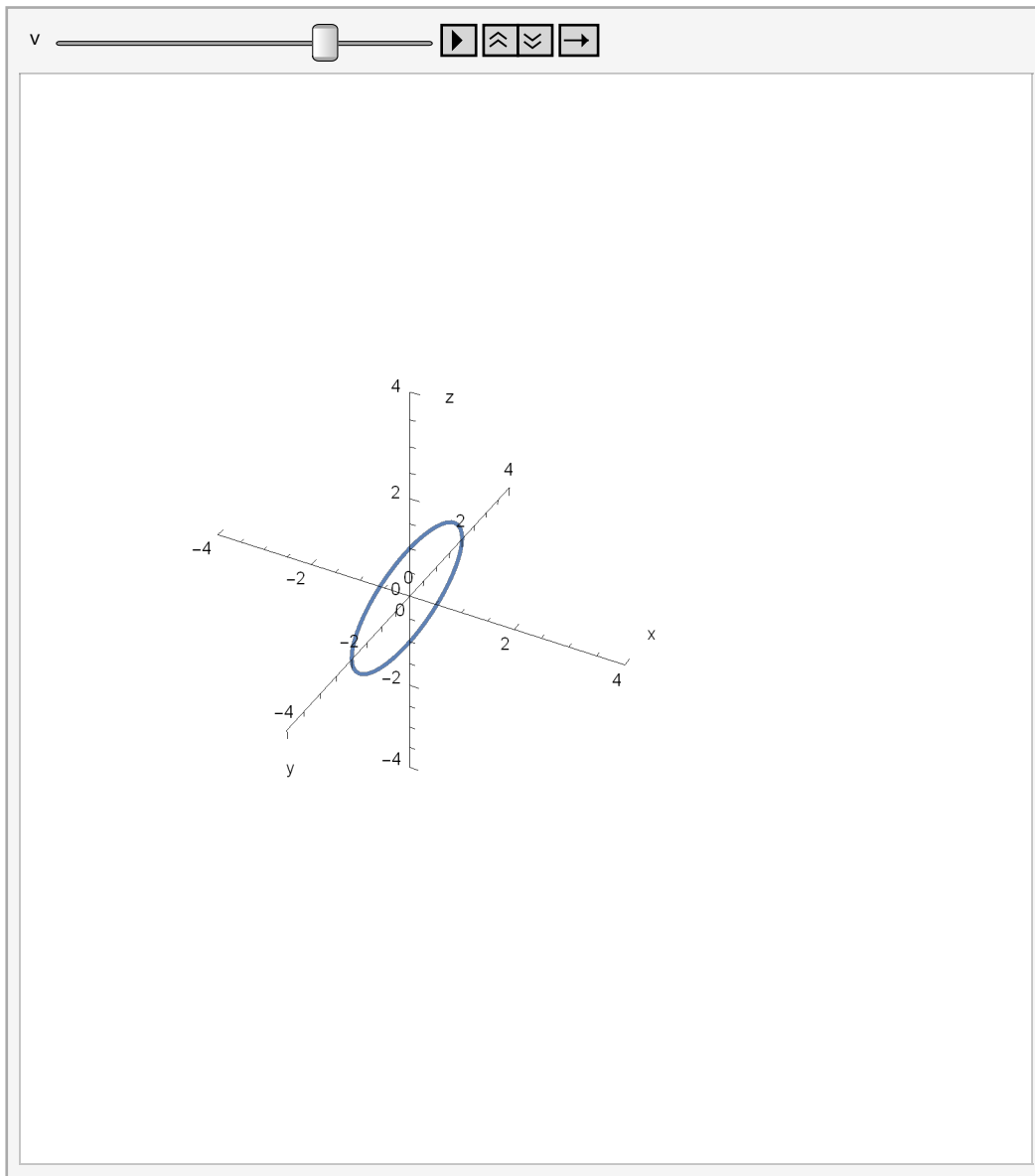


```

In[ ]:= Animate[ParametricPlot3D[RotationMatrix[v, {0, 1, 0}].{Cos[t], 2 Sin[t], 0},
  {t, 0, 2  $\pi$ }, AxesOrigin -> {0, 0, 0}, AxesLabel -> {"x", "y", "z"},
  PlotRange -> {{-4, 4}, {-4, 4}, {-4, 4}}, Boxed -> False],
{v, 0, 2  $\pi$ }, AnimationRunning -> False]

```

Out[]:=

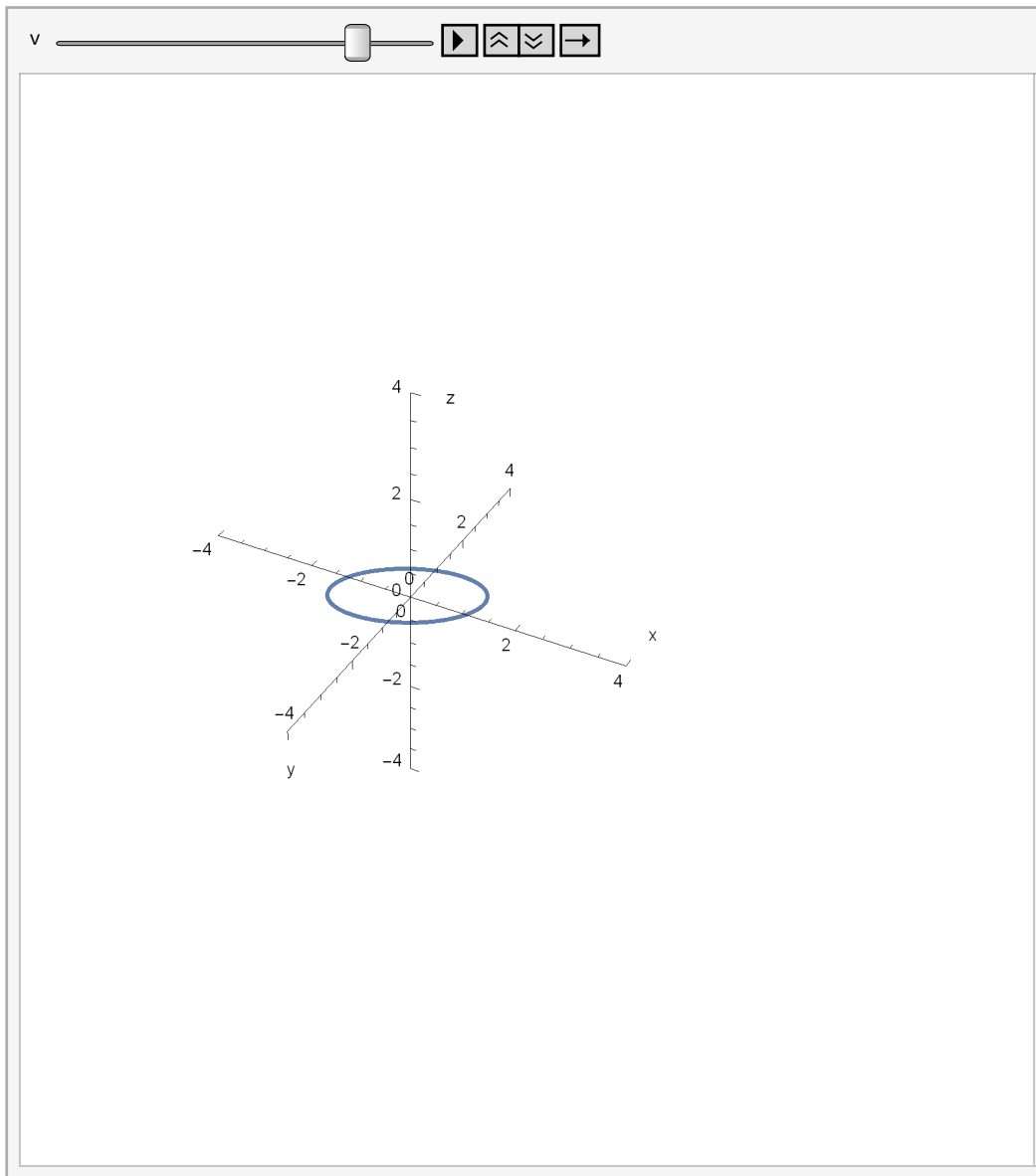


```

In[ ]:= Animate[ParametricPlot3D[RotationMatrix[v, {1, 1, 0}].{Cos[t], 2 Sin[t], 0},
  {t, 0, 2 π}, AxesOrigin → {0, 0, 0}, AxesLabel → {"x", "y", "z"},
  PlotRange → {{-4, 4}, {-4, 4}, {-4, 4}}, Boxed → False],
{v, 0, 2 π}, AnimationRunning → False]

```

Out[]:=



(* Si el eje de rotación deja de ser un eje coordenado {0, 0, 1}, {0, 1, 0}, {0, 0, 1}, la matriz de rotación se complica *)

RotationMatrix[v, {1, 1, 0}] // MatrixForm

(*Matriz de rotación para el eje de rotación i + j *)

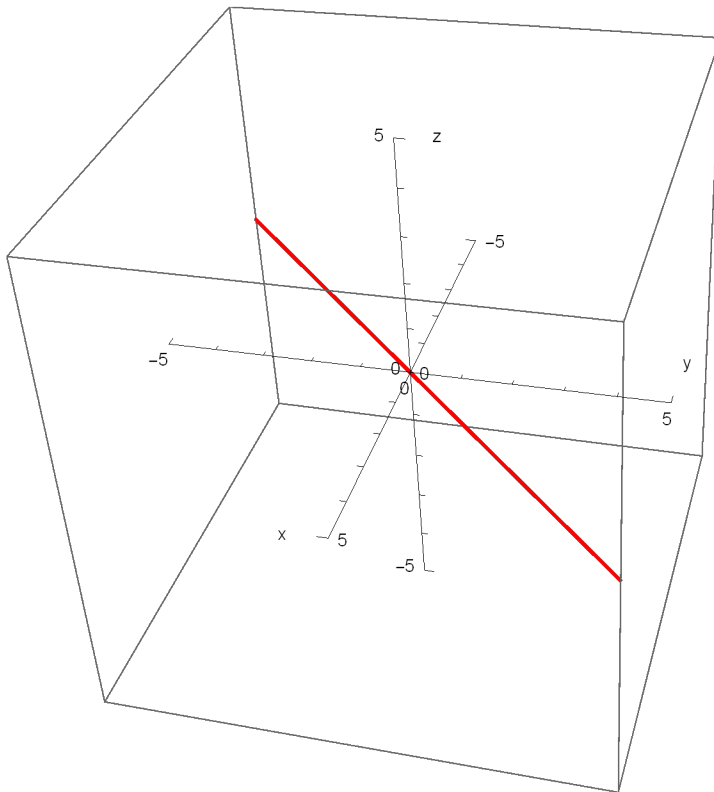
Out[]//MatrixForm=

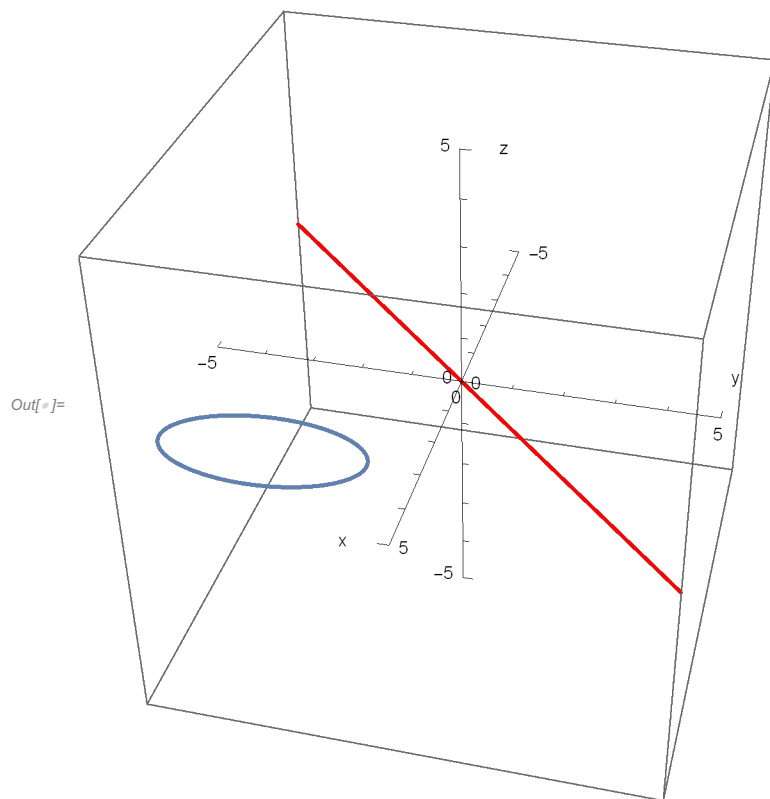
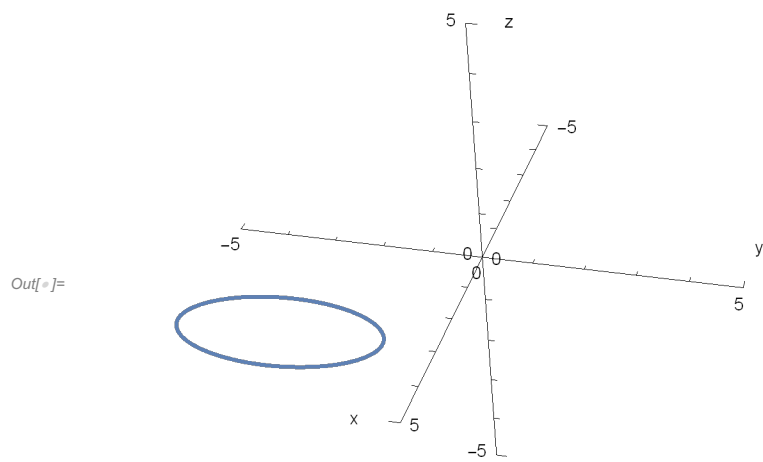
$$\begin{pmatrix} \frac{1}{2} (1 + \cos[v]) & \frac{1}{2} (1 - \cos[v]) & \frac{\sin[v]}{\sqrt{2}} \\ \frac{1}{2} (1 - \cos[v]) & \frac{1}{2} (1 + \cos[v]) & -\frac{\sin[v]}{\sqrt{2}} \\ -\frac{\sin[v]}{\sqrt{2}} & \frac{\sin[v]}{\sqrt{2}} & \cos[v] \end{pmatrix}$$

(*Parametrización de la recta $z = y$ en coordenadas polares,
extensión del vector $i + j$ *)

```
In[ ]:= recta = ParametricPlot3D[{r Cos[ $\frac{\pi}{4}$ ], r Cos[ $\frac{\pi}{4}$ ], 0}, {r, - $\sqrt{50}$ ,  $\sqrt{50}$ },
  AxesOrigin -> {0, 0, 0}, PlotRange -> {{-5, 5}, {-5, 5}, {-5, 5}},
  AxesLabel -> {"x", "y", "z"}, Boxed -> True, PlotStyle -> {Red}]
ellipse = ParametricPlot3D[{3 + Cos[t], -3 + 2 Sin[t], 0},
  {t, 0, 2  $\pi$ }, AxesOrigin -> {0, 0, 0}, AxesLabel -> {"x", "y", "z"},
  PlotRange -> {{-5, 5}, {-5, 5}, {-5, 5}}, Boxed -> False]
Show[recta, ellipse]
```

Out[]:=





In[]:= (* Si giramos esa elipse y mostramos la recta $i + j$ *)

```

Animate[
  Show[ParametricPlot3D[RotationMatrix[v, {1, 1, 0}].{3 + Cos[t], -3 + 2 Sin[t], 0},
    {t, 0, 2  $\pi$ }, AxesOrigin -> {0, 0, 0}, AxesLabel -> {"x", "y", "z"},
    PlotRange -> {{-5, 5}, {-5, 5}, {-5, 5}}, Boxed -> False],
  ParametricPlot3D[{r Cos[ $\frac{\pi}{4}$ ], r Cos[ $\frac{\pi}{4}$ ], 0}, {r, - $\sqrt{50}$ ,  $\sqrt{50}$ }, AxesOrigin -> {0, 0, 0},
    PlotRange -> {{-5, 5}, {-5, 5}, {-5, 5}}, AxesLabel -> {"x", "y", "z"},
    Boxed -> True, PlotStyle -> {Red}]], {v, 0, 2  $\pi$ }, AnimationRunning -> False]

```

