## Performance

martes, 15 de marzo de 2022 06:56 a.m.

1)eally:

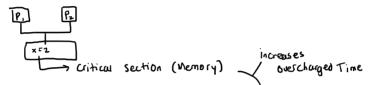
$$t_p^{ideal} = \begin{bmatrix} t_s \\ n_p \end{bmatrix}$$
 -> sequential time

-> number of processors

When working in parallel. from this, we can calculate Overcharged Time:

## · In Shared Memory

-> Means we have problems in communication. There are many synchronization techniques that involve Blockers to Critical Sections. Example



-> Blocking sertalizes our program, which also involves dependency on Distributed Memory

-> Each processor has its memory, and thus only with Messaging the Overcharge Time (acreases.

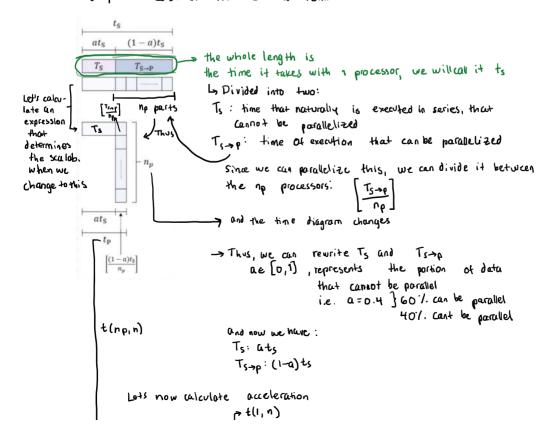
Overcharge Time increases.

The more Data we need to message through the network, the more Overcharge Time we will have

1 Data = 1 tsc

## -> Ambdahl's Law

Is a specific case of the General Form



Let's now calculate acceleration
$$S = \frac{t_s}{t_p} = \frac{T_s + T_s \rightarrow \rho}{T_s + \left[\frac{T_s \rightarrow \rho}{n_p}\right]}$$

Ts = ats and Ts +p = (1-a) ts, we now have with

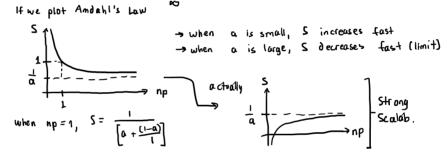
$$S = \frac{ats + (1-a)ts}{at_s + \left[\frac{(1-a)ts}{np}\right]}$$
we have  $\frac{ts (num)}{ts (denom)}$  Thus we can cancel out to term.

$$= \frac{\alpha + (1-\alpha)}{\alpha + \frac{(1-\alpha)}{n_{B}}}$$

$$S = \frac{1}{\left[Q + \frac{(1-a)}{np}\right]}$$

S= 1
Amdahl's Law: a relationship of
how time changes from 1 to np processors

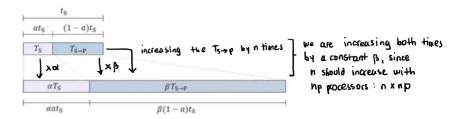
 $\lim_{np\to\infty} \frac{1}{\left[\alpha + \frac{(1-\alpha)}{np}\right]} = \frac{1}{\alpha} \quad \text{the acceleration}$   $\lim_{n\to\infty} \frac{1}{np} = \lim_{n\to\infty} \frac{1}{np}$ If we say np > 00, then



Let's say 0=0.1 (10%)

Let's say 
$$a=0.01$$
 (1%) The problem itself has almost no dependencies (a small), thus 100 of S.

However, Ambahl's Law does not take on account n (problem's size), and since n is fixed in the law, Scalability (Weak) is not considered. So if we want to scale in naturally, we need to scale it (3 (Ts→p):



Thus,

ats - a ats - represents that the problem increases

Let's calculate scalability (acceleration),

$$S = \frac{t_{s}}{t_{p}} = \frac{T_{s} + T_{s \to p}}{T_{s} + \left[\frac{T_{s \to p}}{n_{p}}\right]}$$
 with  $T_{s} = \alpha \alpha t_{s}$  and  $T_{s \to p} = \beta (1 - \alpha) t_{s}$ 

$$= \frac{\alpha \alpha t_{s} + \beta (1 - \alpha) t_{s}}{\alpha \alpha t_{s} + \left[\frac{\beta (1 - \alpha) t_{s}}{n_{p}}\right]}$$

One again to is a common factor on both numerator and denominator, and therefore we can cancel is out,

$$= \frac{\alpha\alpha + \beta(1-\alpha)}{\alpha\alpha + \left[\frac{\beta(1-\alpha)}{\alpha}\right]}$$

If we divide numerator and denominator by '/d,

$$= \frac{\frac{\alpha \alpha}{\alpha} + \frac{\beta(1-\alpha)}{\alpha}}{\frac{\alpha \alpha}{\alpha} + \left[\frac{\beta(1-\alpha)}{\alpha n \rho}\right]}$$

And we can again cancel out do

$$= \frac{\alpha + \left[\frac{r_2}{\alpha}\right](1-\alpha)}{\alpha + \left[\frac{r_2}{\alpha}\right]\frac{(1-\alpha)}{np}}, \text{ with } Y = \left[\frac{r_2}{\alpha}\right], \text{ we have}$$

$$S = \frac{a + 4(1-a)}{a + 4\left[\frac{1-a}{np}\right]}$$
 General Law

-> If we have 4=1 ( M= x), we get Ambahl's Law:

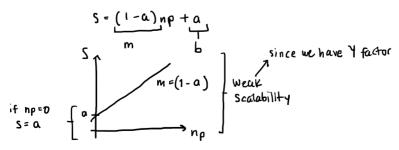
$$S = \frac{\alpha + (1-\alpha)}{\alpha + \left[\frac{1-\alpha}{np}\right]} = \frac{1}{\alpha + \left[\frac{1-\alpha}{np}\right]} A m \partial ah is Law$$

multiplying n x np. Here, that would mean Y = np,

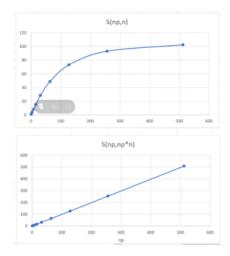
$$S = \frac{\alpha + np(1-\alpha)}{\alpha + np\left[\frac{1-\alpha}{np}\right]} = \frac{\alpha + np(1-\alpha)}{\alpha + (1-\alpha)} = \alpha + np(1-\alpha)$$

$$S = \frac{\alpha + np(1-\alpha)}{\alpha + (1-\alpha)} = \frac{\alpha + np(1-\alpha)}{\alpha + (1-\alpha$$

And we also can derive from General's Law, the bustatson's Law. It has a linear form:



And these Scalability plots resemble what we have been doing:



Confirming that indeed 5-trong and wear scalab have a log an Unear form

these two plots are just the computation time, if you have communication, just add it at the end.