

Homework 0: The Foster Method

Sunday, January 30, 2022 2:29 PM

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Data: abcdefghbc dsb

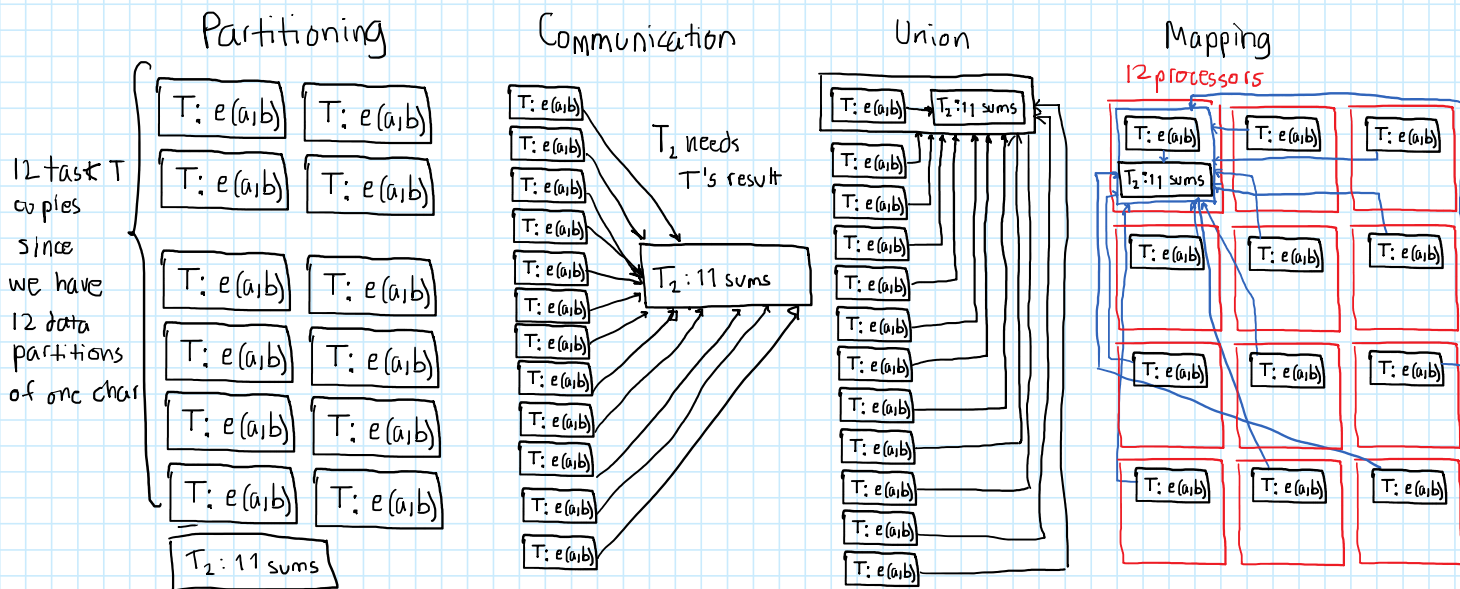
Task: count the number of "b" in the data.

↳ basic operation: $\text{equals}(a, b) \begin{cases} T & \text{if } a=b \\ F & \text{if } a \neq b \end{cases} \Rightarrow T: e(a, b)$

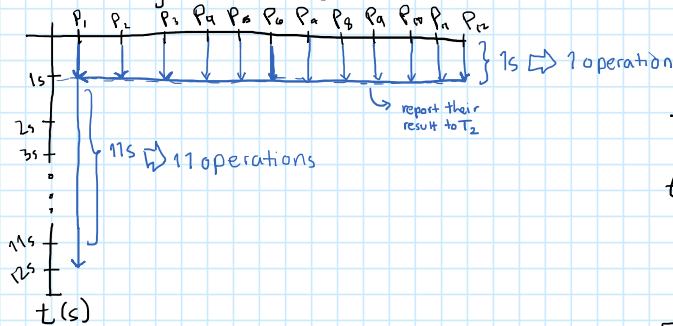
↳ counter: $c = \text{int}(r_1) + \text{int}(r_2) + \dots + \text{int}(r_{12}) \Rightarrow T_2: 11 \text{ sums}$
Assuming $\text{int}(\text{equals}(a, b))$ outputs 0 or 1.

① 12 processors, 1 data partition

Solution



Time diagram: Assuming that 1 operation ($=, +, -, *, /$) takes 1s:



$$t_{\text{TOTAL}} = \max\{P_1, P_2, P_3, \dots, P_{12}\}$$

$$t_{\text{TOTAL}} = \max\{12s, 1s, 1s, 1s, 1s, 1s, 1s, 1s, 1s, 1s, 1s, 1s\}$$

$$t_{\text{TOTAL}} = 12s$$

Ex 2

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② 6 processors, data partition

Solution

Data: abc fgv hbc dsb

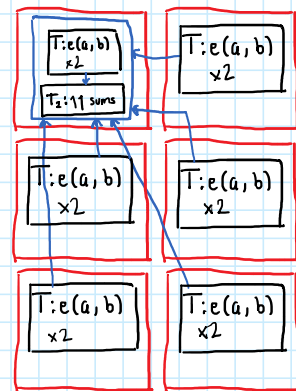
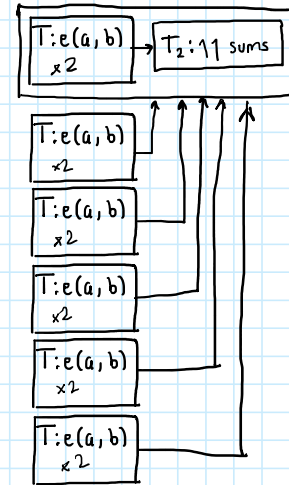
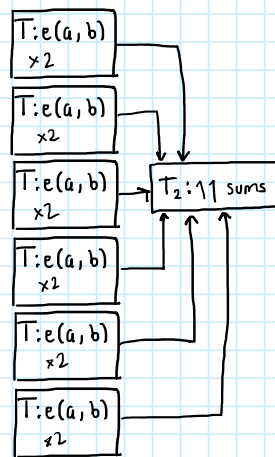
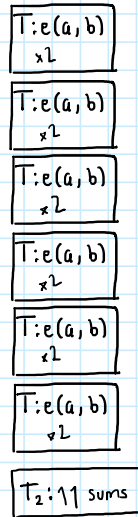
1 2 3 4 5 6 Parts → 6 processors

Partitioning

Communication

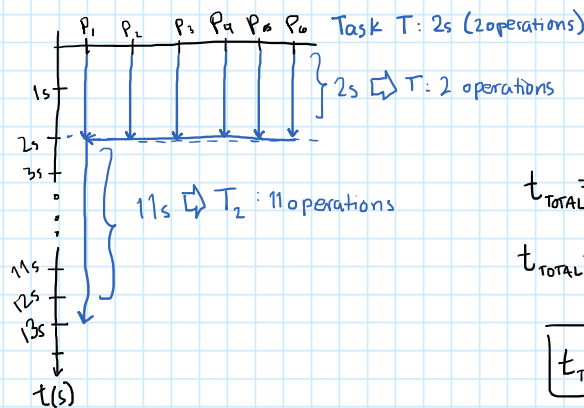
Union

Mapping



Task T has 1 basic instruction that is executed on 1 data piece (2 letters) = 2 operations

Time diagram: Assuming that 1 operation (=, +, -, *, /) takes 1s:



$$t_{\text{TOTAL}} = \max\{P_1, P_2, \dots, P_6\}$$

$$t_{\text{TOTAL}} = \max\{13s, 2s, 2s, 2s, 2s, 2s\}$$

$$t_{\text{TOTAL}} = 13s$$

Ex 3

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③ 3 processors, data partition

Data: abc fgv hbc dsb

Solution

3 processors \rightarrow 3 data partitions

abcf gvhb cdsb

$T: e(a,b)$
 $\times 4$

Task T receives 4 letters

that's why I put " $\times 4$ "

Task T has 1 basic instruction that is executed on 1 data piece (4 letters) = 4 operations

Partitioning

Communication

Union

Mapping

$T: e(a,b)$
 $\times 4$

$T: e(a,b)$
 $\times 4$

$T: e(a,b)$
 $\times 4$

$T_2: 11 \text{ sums}$

$T: e(a,b)$
 $\times 4$

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$T_2: 11 \text{ sums}$

$T: e(a,b)$
 $\times 4$

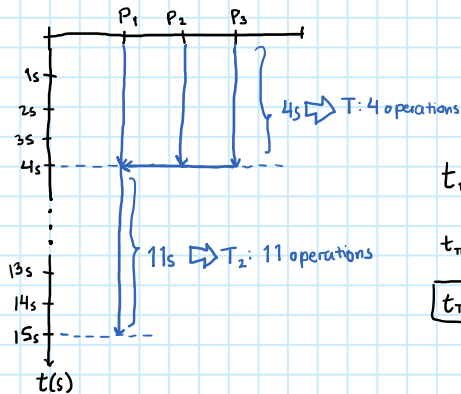
$T: e(a,b)$
 $\times 4$

$T: e(a,b)$
 $\times 4$

$T: e(a,b)$
 $\times 4$

$T: e(a,b)$
 $\times 4$

Time diagram: Assuming that 1 operation ($=, +, -, *, /$) takes 1s:



$$t_{\text{TOTAL}} = \max\{P_1, P_2, P_3\}$$

$$t_{\text{TOTAL}} = \max\{15s, 4s, 4s\}$$

$$t_{\text{TOTAL}} = 15s$$

Ex 4

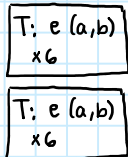
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④ 2 processors, data partition

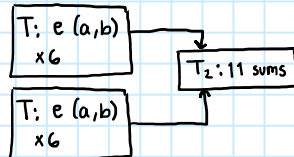
Data: a b c f g v h b c d s b
 1 2
 2 processors → 2 data partitions

T: e(a,b)
x6
 Task T receives 6 letters (1 partition)
 that's why 1 pt "x6" → Task T has 1 basic instruction that is executed in 1 data piece (6 letters) = 6 operations

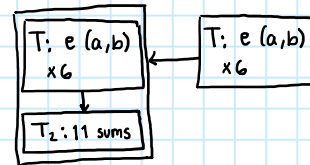
Partitioning



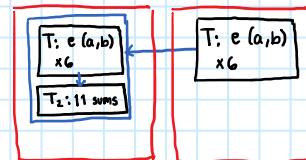
Communication



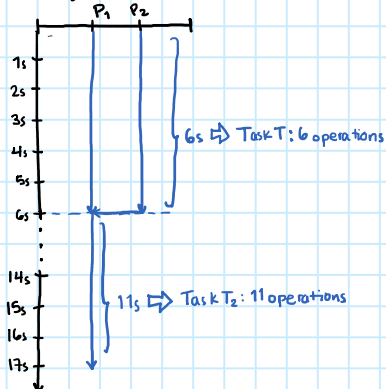
Union



Mapping



Time diagram: Assuming that 1 operation (=, +, -, *, \) takes 1s:



$$t_{TOTAL} = \max\{P_1, P_2\}$$

$$t_{TOTAL} = \max\{17s, 6s\}$$

$$t_{TOTAL} = 17s$$