

Verifying V(s)

Saturday, May 21, 2022 9:14 PM

①

$$S = \{s_1, s_2, s_3, s_4\} \quad A = \{a_1, a_2\}$$

Deterministic $\gamma = 0.9$

$$s_f = f(s, a) = \begin{matrix} s_1 & \begin{bmatrix} a_1 & a_2 \\ s_2 & s_3 \\ s_3 & s_1 \\ s_4 & s_4 \end{bmatrix} \end{matrix}$$

Solution:

$$f_R = \begin{matrix} s_1 & \begin{bmatrix} 2 \\ 1 \\ -1 \\ 10 \end{bmatrix} \\ s_2 \\ s_3 \\ s_4 \end{matrix} \quad f_{\pi} = \begin{matrix} s_1 & \begin{bmatrix} a_1 \\ a_1 \\ a_2 \\ a_2 \end{bmatrix} \\ s_2 \\ s_3 \\ s_4 \end{matrix}$$

$$V(s) = \begin{matrix} s_1 & s_2 & s_3 & s_4 \\ 14.74 & 15.26 & 15.26 & 99.13 \end{matrix}$$

$$V(s_1) = f_R(s_f) + 0.9(V(s_f))$$

$$= 1 + 0.9(V(s_2))$$

$$= 1 + 0.9(15.26)$$

$$14.74 = 14.734 \rightarrow \text{coincides}$$

$$V(s_2) = f_R(s_f) + 0.9(V(s_f))$$

$$= 2 + 0.9(V(s_1))$$

$$= 2 + 0.9(14.74)$$

$$= 15.266 \rightarrow \text{coincides}$$

$$V(s_3) = f_R(s_f) + 0.9(V(s_f))$$

$$= 2 + 0.9(V(s_1))$$

$$= 2 + 0.9(14.74)$$

$$= 15.266 \rightarrow \text{coincides}$$

$$V(s_4) = f_R(s_f) + 0.9(V(s_f))$$

$$= f_R(s_4) + 0.9(V(s_4))$$

$$= 10 + 0.9(99.13)$$

$$= 99.217 \rightarrow \text{coincides}$$

$$s_f = s_2$$

$$s_1 \rightarrow a_1$$

$$s_f = s_1$$

$$s_2 \rightarrow a_1$$

$$s_f = s_1$$

$$s_3 \rightarrow a_2$$

$$s_f = s_4$$

$$s_4 \rightarrow a_2$$