Tuesday, March 22, 2022

10:54 AM

1) Given the world defined by the following transition function  $f_{MT}(s, a)$ , the reward function  $f_{R}(s, a, s_{f}) = f_{R}(s_{f})$  and 4 = 0.9:

$$f_{M_T}(s,a) = \begin{matrix} s_1 & a_2 \\ s_1 & s_2 & s_2 \\ s_2 & s_1 & s_3 \\ s_3 & s_1 \\ s_4 & s_1 & s_4 \end{matrix} \qquad f_R(s_f) = \begin{matrix} s_1 & 2 \\ s_2 & 1 \\ s_3 & -1 \\ s_4 & 10 \end{matrix}$$

© Calculate the accumulated reward function  $f_{AR}(T_1)$  for the trajectory:  $T_1=s_1,s_2,s_3,s_1,s_2,s_1$ 

$$A = \left\{ \begin{array}{l} a_{1} \quad a_{2} \\ \end{array} \right\} \qquad S = \left\{ \begin{array}{l} s_{1} \quad s_{2} \quad s_{3} \quad s_{4} \\ \end{array} \right\}$$

$$T_{1} \rightarrow \begin{array}{l} \begin{array}{l} 1 \\ 0 \\ 0 \\ \end{array} \right\} \xrightarrow{\left\{ \begin{array}{l} 0 \\ 0 \\ \end{array} \right\}} \xrightarrow{\left\{ \begin{array}{l} 0 \\ 0 \end{array} \right\}} \xrightarrow{\left\{ \begin{array}{l} 0 \end{array} \right\}} \xrightarrow{\left\{ \begin{array}{l} 0 \\ 0 \end{array} \right\}} \xrightarrow{\left\{ \begin{array}{l} 0 \\ 0 \end{array} \right\}} \xrightarrow{\left\{ \begin{array}{l} 0$$

(b) Calculate the accumulated remard function far(I1) for the trajectory:

Solution

$$\begin{array}{c}
2 \\
\hline
S_3
\end{array} \longrightarrow \begin{array}{c}
1 \\
\hline
S_3
\end{array} \longrightarrow \begin{array}{c}
1 \\
\hline
S_3
\end{array} \longrightarrow \begin{array}{c}
1 \\
\hline
S_3
\end{array}$$
with  $y = 0.9$ 

T 2= S3 , S1, S1, S3

with 
$$\forall = 0.9$$
  
 $f_{AR}(T_1) = 2 + \forall (1) + \forall^2 (-1)$   
 $\frac{c}{f_{AR}(T_1)} = \frac{1}{2 \cdot 0.9}$ 

@Calculate the accumulated reward function far (T1) for the trayectory:

Solution

$$f_{AR} (T_3) = 2 + V(1)$$

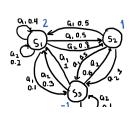
$$= 2 + 0.9(1)$$

$$= 2 + 0.9$$

$$f_{BR} (T_3) = 2.9$$

Given the world defined by the transition function  $P_{MT}(S_f|s,\alpha)$ , the reward function  $f_R(S_f,s,\alpha)=f_R(S_f)$  and  $\gamma=0.6$ :

(a) Calculate the accumulated reward function  $f_{AR}(T_1)$  for the trayectory:  $T_1=S_1,\,S_2,\,S_3,\,S_1,\,S_2,\,S_1$ Solution



$$S = \left\{ \begin{array}{l} S_{1} S_{2} S_{3} \right\} & A = \left\{ \alpha_{1} \alpha_{1} \right\} \\ T_{1} = \begin{array}{l} \left( S_{3} \right) \longrightarrow \left( S_{3} \right)$$

$$f_{AR}(\tau_{i}) = 1 + \gamma(-1) + \gamma^{2}(2) + \gamma^{3}(1) + \gamma^{4}(2)$$

$$= 1 + (0.6)(-1) + (0.6)^{2}(2) + (0.6)^{3}(1) + (0.6)^{4}(2)$$

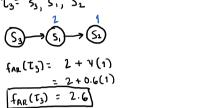
$$f_{AR}(\tau_{i}) = 1.59$$

b Calculate the accumulated reward function  $f_{AB}(T_2)$  for the trajectory:  $T_2=S_3, S_1, S_2, S_3$ 

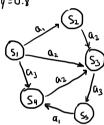
Solution

© Calculate the accumulated reward function  $f_{AR}(T_3)$  for the trayectory:  $T_3=s_3,\,s_1,\,s_2$ 

Solution



(3) Given the world defined by the following graph, the reward function  $f_R(s_f, s, a)$  and  $\gamma = 0.8$ 



© Calculate the accumulated reward function  $f_{AR}(T_i)$  for the trajectory:  $T_1 = S_{11}, S_{21}, S_{32}, S_{53}, S_{41}, S_{33}, S_{5}$ 

Solution

(b) Calculate the accumulated reward function  $f_{AR}(T_2)$  for the trajectory:  $T_2$ = s, , s3, s5, s4

Solution

© Calculate the accumulated reward function  $f_{AR}(T_3)$  for the trajectory:  $T_3 = s_{4_1} s_{5_2}, s_{5_3}$ 

with 
$$V=0.8$$

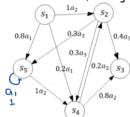
$$f_{AR}(T_3) = -1 + V(6)$$

$$= -1 + (0.8)(6)$$

$$= -1 + V.8$$

$$f_{AR}(T_3) = 3.8$$

4 Given the world defined by the following graph where 0.84, means a, with probability 0.8, and so on, and with the following reward function and 400.7



( Calculate the accumulated reward function far([1) for the trayectory:

Solution

(b) Calculate the accumulated reward function  $f_{AR}(C_2)$  for the trayectory:

Solution

 $f_{AR} = 0 + (0.7)(-1) + (0.7)^2(-1)$   $f_{RR} = -1.19$  with 0.24 of probability

Calculate the accumulated reward function far ([2) for the trajectory: T3= 59,51,53

Solution

$$\begin{cases} 0.2 & -3 & 0.4 \\ 0.2 & -3 & 0.3 \\ 0.3 & 0.3 \end{cases} = \begin{cases} -3 & +(0.7)(-1) = -3.7 \\ 0.7 & 0.08 \end{cases}$$
with 0.08 probability

(5) El mundo tiene el siguiente conjunto de estados S={s1, s2, s3, sF1, sF2} donde s1=estado inicial y, sF1 y sF2 son estados terminales:

El mundo tiene el siguiente conjunto de acciones  $A=\{\rightarrow,\leftarrow\}$  donde:

- →=Agente se mueve a la derecha una sola celda
- ←=Agente se mueve a la izquierda una sola celda

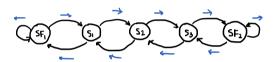
La función de recompensa  $f_R(s, a, s_f) = f_R(s_f)$  solo depende del estado al que el Agente llega y esta definida como:

		-		
-10	0	-0.4	-0.4	10

Es decir, si el agente transiciona de s1 a s2 entonces recibe la recompensa -0.4 que esta definide en el estado s2. El agente tiene la siguiente función de acción  $f_{\pi}(s)$ :

$$f_{\pi}(s) = \begin{cases} s_1 \\ s_2 \\ \rightarrow \\ s_3 \\ \rightarrow \\ s_{F1} \\ \leftarrow \\ s_{F2} \\ \rightarrow \end{cases}$$

a Build the graph of the world



(s,a) Write the transition function fnt (s,a)

$$f_{MT}(S_{10}) = \begin{cases} S_{1} \\ S_{2} \\ S_{3} \\ S_{4} \\ S_{5} \\ S_{7} \\ S$$

© Build all the possible trajectories from the initial state s, given the action function  $f_{\pi}(s)$  that go to a final state, either SF, or SF2

Build all the possible trajectories from the state  $S_2$ , given the action function  $f_\pi(s)$  that go to a final state, either  $sF_1$  or  $sF_2$ 

$$T_1 = S_{2,1} S_{3,1} SF_{2}$$
  
 $T_2 = S_{1,1} S_{3,1} SF_{1,1} S_{3,1} SF_{2}$ 

© Build all the possible trajectories from the state  $s_3$ , given the action function  $f_{\pi}(s)$  that go to a final state, either  $sF_1$  or  $sF_2$ 

$$T_1 = S_{3_1} SF_{1_1}$$
 $T_2 = S_{3_1} SF_{1_1} S_{3_1} SF_{1_1}$ 

For Calculate the accumulated reward of every possible trayectory in c, d, e using Y = 0.7.  $SF_1$   $S_2$   $S_3$   $SF_2$   $S_4$   $S_5$   $S_6$   $S_6$  S

$$T_{2}=S_{2,1}S_{3,2}SF_{2,3}SF_{2} \qquad f_{RA}=-0.4+(0.7)(10)+(0.7)^{2}(0.4)+(0.7)^{3}(10)=9.83$$

$$S(0)=S_{3}$$

$$T_{1}=S_{3,3}SF_{2} \qquad f_{RA}=10$$

$$T_{2}=S_{3,3}SF_{2,3}SF_{2,3}SF_{3,3}SF_{2,4}$$

$$T_{1}=S_{3,5}SF_{2,5}SF_{3,5}S$$

El mundo tiene el siguiente conjunto de estados S={s1, s2, s3, sF1, sF2} donde s1=estado inicial y, sF1 y sF2 son estados terminales:

El mundo tiene el siguiente conjunto de acciones  $A=\{\rightarrow,\leftarrow\}$  donde:

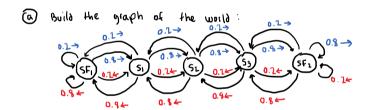
- →=Agente se mueve a la derecha una sola celda con probabilidad 0.8 y se mueve una sola celda a la izquierda con probabilidad 0.2
- ←=Agente se mueve a la izquierda una sola celda con probabilidad 0.8 y se mueve una sola celda a la derecha con probabilidad 0.2

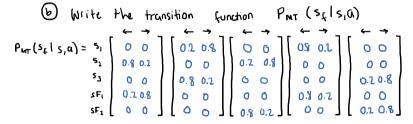
La función de recompensa  $f_R(s, a, s_f) = f_R(s_f)$  solo depende del estado al que el Agente llega y esta definida como:

Es decir, si el agente transiciona de s1 a s2 entonces recibe la recompensa -0.4 que esta definide en el estado s2.

El agente tiene la siguiente función de acción  $f_{\pi}(s)$ :

$$f_{\pi}(s) = \begin{cases} s_1 \\ s_2 \\ \rightarrow \\ S_{F1} \\ \downarrow \\ S_{F2} \end{cases} \xrightarrow{s_1} \leftarrow \xrightarrow{s_1} \leftarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_1} \leftarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_1} \leftarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_1} \rightarrow \xrightarrow{s_2} \rightarrow \xrightarrow{s_$$





c. Construya todas las trayectorias posibles a partir del estado inicial s1 dada la función de acción  $f_{\pi}(s)$  que lleven a un estado final ya sea sF1 o sF2

(NOTA: Dado que es un número infinito de trayectorias solo escriba 10)

$$f_{\pi}(s) = \begin{cases} s_{1} \\ s_{2} \\ \vdots \\ s_{F_{1}} \\ \vdots \\ s_{F_{2}} \\ \vdots \\ s_{F_{2}} \end{cases} \xrightarrow{0.1 \xrightarrow{\circ}} \begin{cases} 0.1 \xrightarrow{\circ} \\ 0.1 \xrightarrow{$$

d. Construya todas las trayectorias posibles a partir del estado s2 dada la función de acción  $f_\pi(s)$  que lleven a un estado final ya sea sF1 o sF2

(NOTA: Dado que es un número infinito de trayectorias solo escriba 10)

e. Construya todas las trayectorias posibles a partir del estado s3 dada la función de acción  $f_{\pi}(s)$  que lleven a un estado final ya sea sF1 o sF2

(NOTA: Dado que es un número infinito de trayectorias solo escriba 10)

d. Calcule la recompensa acumulada de cada posible trayectoria en los incisos c, d, e usando  $\gamma$ =0.7.

```
→ s(o)=s,
                        \Rightarrow s(0) = S_1
t 5 = 1.39
                        tis = -2.29 [20 = -3.7]
          て<sub>の</sub>- - 2
→ s(o)=s3
                         All these numbers
 T 21 = 10
            T16= 9.72
 T21 = -5.3
            <sub>11</sub> - - 5.3
                        were calculated using:
t_{13} = 4.22 t_{18} = 1.39
                             r: r, + y[far(t)]
 Tz4 = 1.67
            T29 = - 2.99
                          Programmed in python
 [15 = -3.28
            T10= 2.10
```

the code

```
r = [-10,0,-0.4,-0.4,10]
g = 0.7

for t in ts:
    acc = 0
    for i in range(1,len(t)):
        s = t[i]
        acc += (g**(i-1))*(r[s])
    print(f"T{ts.index(t)+1}:{acc}")
```