

$$\begin{cases} \frac{dx_1}{dt} = -x_2 + x_1(x_1^2 + x_2^2)^{-\frac{1}{2}}(1 - x_1^2 - x_2^2) \\ \frac{dx_2}{dt} = x_1 + x_2(x_1^2 + x_2^2)^{-\frac{1}{2}}(1 - x_1^2 - x_2^2) \end{cases}$$

$$x_1 = \rho \cos(\theta) \text{ e } x_2 = \rho \sin(\theta)$$

$$-\rho \sin \theta + \rho \cos \theta (\rho^2)^{-1/2} (1 - \rho^2) \quad , \quad \rho \cos \theta + \rho \sin \theta (\rho^2)^{-1/2} (1 - \rho^2)$$

$$\begin{cases} (1 - \rho^2) \cos \theta - \rho \sin \theta = \frac{d(\rho \cos \theta)}{dt} = \rho \sin \theta \frac{d\theta}{dt} + \cos \theta \frac{d\rho}{dt} & \times \cos \theta \\ (1 - \rho^2) \sin \theta + \rho \cos \theta = \frac{d(\rho \sin \theta)}{dt} = \rho \cos \theta \frac{d\theta}{dt} + \sin \theta \frac{d\rho}{dt} & \times \sin \theta \end{cases} +$$

$$(1 - \rho^2)(\cos^2 \theta + \sin^2 \theta) - \cancel{\rho \sin \theta \cos \theta} + \cancel{\rho \cos \theta \sin \theta} = -\cancel{\rho \sin \theta \cos \theta} \frac{d\theta}{dt} + \cancel{\rho \sin \theta \cos \theta} \frac{d\theta}{dt} + \frac{d\rho}{dt}(\cos^2 \theta + \sin^2 \theta)$$

$$\begin{cases} 1 - \rho^2 = \frac{d\rho}{dt} \\ 1 = \frac{d\theta}{dt} \end{cases}$$

$$\begin{cases} \frac{dx_1}{dt} = -x_2 + x_1(x_1^2 + x_2^2 - 1) \\ \frac{dx_2}{dt} = x_1 + x_2(x_1^2 + x_2^2 - 1) \end{cases}$$

$$x_1 = \rho \cos \theta$$

$$x_2 = \rho \sin \theta$$

$$\frac{d\rho}{dt} \cos \theta - \rho \sin \theta \frac{d\theta}{dt} = -\rho \sin \theta + \rho \cos \theta (\rho^2 - 1) \times \cos \theta +$$

$$\frac{d\rho}{dt} \sin \theta + \rho \cos \theta \frac{d\theta}{dt} = \rho \cos \theta + \rho \sin \theta (\rho^2 - 1) \times \sin \theta$$

$$\begin{cases} \frac{d\rho}{dt} = \rho(\rho^2 - 1) \\ \frac{d\theta}{dt} = 1 \end{cases}$$