→ A bigger problem can be solved using the optimal sol^n of small subproblem.

→ Overlapping subproblems

(*) Those who forget the past, are condemened to repeat it.

→ Top down (Recursion + Memoization)

→ Bottom up (Tabulation)

↓

Store the value of subproblem.

} Space Optimization

Fibonacci Sequence :-

```cpp
// User function Template for C++
class Solution {
  public:
    int getFib(int n, vector<int> &dp) {
        if(n ≤ 1) return n;
        if(dp[n] ≠ -1) return dp[n];
        return dp[n] = getFib(n - 1, dp) + getFib(n - 2, dp);
    }
    int nthFibonacci(int n){
        vector<int> dp(n + 1, -1);
        return getFib(n, dp);
    }
};
```

→ Top down approach

```
Time Complexity : O(N)

Space Complexity : O(2*N)
```

```cpp
class Solution {
  public:
    int nthFibonacci(int n){
        vector<int> dp(n + 1);
        dp[0] = 0;
        dp[1] = 1;

        for(int i = 2; i ≤ n; i++) {
            dp[i] = (dp[i - 1] + dp[i - 2]);
        }
        return dp[n];
    }
};
```

→ Tabulation

```
Time Complexity : O(N)

Space Complexity : O(N)
```

→ Space Optimization

```cpp
class Solution {
  public:
    int mod = 1e9 + 7;
    int nthFibonacci(int n){
        long long prev2 = 0;
        long long prev1 = 1;

        for(int i = 2; i ≤ n; i++) {
            int curr = (prev1 + prev2) % mod;
            prev2 = prev1;
            prev1 = curr;
        }
        return prev1;
    }
};
```

```
Time Complexity : O(N)

Space Complexity : O(1)
```
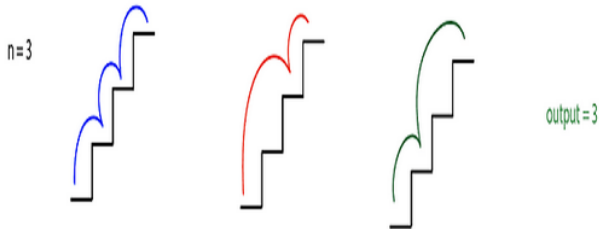
Count ways to reach the nth stairs

You have been given a number of stairs. Initially, you are at the 0th stair, and you need to reach the Nth stair.

Each time, you can climb either one step or two steps.

You are supposed to return the number of distinct ways you can climb from the 0th step to the Nth step.

Example :

N=3

output = 3

We can climb one step at a time i.e. {(0, 1) ,(1, 2),(2,3)} or we can climb the first two-step and then one step i.e. {(0,2),(1, 3)} or we can climb first one step and then two step i.e. {(0,1), (1,3)}.

→ Recursion :-

```cpp
long long countDistinctWays(long long nStairs) {
    if(nStairs < 0)
        return 0;
    else if(nStairs == 0)
        return 1;
    return countDistinctWays(nStairs - 2) + countDistinctWays(nStairs - 1);
}
```

→ Memoization :-

```cpp
#define mod 1000000007;

int getWays(int nStairs, vector<long long> &dp) {
    if(nStairs <= 1) return 1;
    if(nStairs == 2) return 2;

    if(dp[nStairs] != -1) return dp[nStairs];

    return dp[nStairs] = (getWays(nStairs - 1, dp) + getWays(nStairs - 2, dp)) % mod;
}

int countDistinctWays(int nStairs) {
    vector<long long> dp(nStairs + 1, -1);
    return getWays(nStairs, dp);
}
```

→ Tabulation :-

```cpp
#include <bits/stdc++.h>
#define mod 1000000007;

int getWays(int n) {
    vector<long long> dp(n + 1, -1);
    dp[0] = 1;
    dp[1] = 1;
    dp[2] = 2;

    for(int i = 3; i <= n; i++) {
        dp[i] = (dp[i - 1] + dp[i - 2]) % mod;
    }

    return dp[n];
}

int countDistinctWays(int nStairs) {
    return getWays(nStairs);
}
```

→ Space Optimization :-

```cpp
#include <bits/stdc++.h>
#define mod 1000000007;

int getWays(int n) {
    long long prev0 = 1, prev1 = 1, prev2 = 2;

    for(int i = 3; i <= n; i++) {
        int curr = (prev2 + prev1) % mod;
        prev1 = prev2;
        prev2 = curr;
    }
    return prev2;
}

int countDistinctWays(int nStairs) {
    if(nStairs == 0 || nStairs == 1) return 1;
    return getWays(nStairs);
}
```

Minimum cost climbing stairs

You are given an integer array `cost` where `cost[i]` is the cost of ith step on a staircase. Once you pay the cost, you can either climb one or two steps.

You can either start from the step with index `0`, or the step with index `1`.

Return *the minimum cost to reach the top of the floor.*

Example 1:

```
Input: cost = [10,15,20]
Output: 15
Explanation: You will start at index 1.
- Pay 15 and climb two steps to reach the top.
The total cost is 15.
```

Example 2:

```
Input: cost = [1,100,1,1,1,100,1,1,100,1]
Output: 6
Explanation: You will start at index 0.
- Pay 1 and climb two steps to reach index 2.
- Pay 1 and climb two steps to reach index 4.
- Pay 1 and climb two steps to reach index 6.
- Pay 1 and climb one step to reach index 7.
- Pay 1 and climb two steps to reach index 9.
- Pay 1 and climb one step to reach the top.
The total cost is 6.
```

Constraints:

- `2 <= cost.length <= 1000`
- `0 <= cost[i] <= 999`

→ Recursion :-

```cpp
class Solution {
public:
    int solve(vector<int> cost, int n) {
        if(n == 0) return cost[0];
        if(n == 1) return cost[1];
        int ans = cost[n] + min(solve(cost, n - 1), solve(cost, n - 2));

        return ans;
    }

    int minCostClimbingStairs(vector<int>& cost) {
        int n = cost.size();
        int ans = min(solve(cost, n - 1), solve(cost, n - 2));
        return ans;
    }
};
```

→ Memoization :-

```cpp
class Solution {
public:
    int solve(vector<int> cost, int n, vector<int> &dp) {
        if(n == 0) return cost[0];
        if(n == 1) return cost[1];

        if(dp[n] != -1) return dp[n];

        dp[n] = cost[n] + min(solve(cost, n - 1, dp), solve(cost, n - 2, dp));

        return dp[n];
    }
    int minCostClimbingStairs(vector<int>& cost) {
        int n = cost.size();
        vector<int> dp(n + 1, -1);
        int ans = min(solve(cost, n - 1, dp), solve(cost, n - 2, dp));
        return ans;
    }
};
```

→ Tabulation :-

```cpp
class Solution {
public:
    int solve(vector<int> &cost, int n) {
        vector<int> dp(n + 1);
        dp[0] = cost[0];
        dp[1] = cost[1];
        for(int i = 2; i < n; i++) {
            dp[i] = cost[i] + min(dp[i - 1], dp[i - 2]);
        }
        return min(dp[n - 1], dp[n - 2]);
    }
    int minCostClimbingStairs(vector<int>& cost) {
        int n = cost.size();
        return solve(cost, n);
    }
};
```

→ Space Optimization :-

```cpp
class Solution {
public:
    int solve2(vector<int> &cost, int n) {
        int prev1 = cost[1];
        int prev2 = cost[0];
        for(int i = 2; i < n; i++) {
            int curr = cost[i] + min(prev1, prev2);
            prev2 = prev1;
            prev1 = curr;
        }
        return min(prev1, prev2);
    }
    int minCostClimbingStairs(vector<int>& cost) {
        int n = cost.size();
        return solve2(cost, n);
    }
};
```

Minimum Coins

Bob went to his favourite bakery to buy some pastries. After picking up his favourite pastries his total bill was P cents. Bob lives in Berland where all the money is in the form of coins with denominations {1, 2, 5, 10, 20, 50, 100, 500, 1000}.

Bob is not very good at maths and thinks fewer coins mean less money and he will be happy if he gives minimum number of coins to the shopkeeper. Help Bob to find the minimum number of coins that sums to P cents (assume that Bob has an infinite number of coins of all denominations).

Detailed explanation (Input/output format, Notes, Images)

Constraints:

1 <= T <= 10
1 <= P <= 10^9

Time Limit: 1 sec

Sample Input 1:

```
3
60
10
24
```

Sample Output 1:

```
2
1
3
```

Explanation of Sample Input 1:

In the 1st test case, we need one coin of 50 cents and one coin of 10 cents.
In the 2nd test case, we need a coin of 10 cents.
In the 3rd test case, we need one coin of 20 cents and two coins of 2 cents.

→ Recursion :-

```cpp
int solveRec(int denominations[], int x, int n) {
    if (x == 0)
        return 0;
    if (x < 0)
        return INT_MAX;

    int mini = INT_MAX;

    for (int i = 0; i < n; i++) {
        int ans = solveRec(denominations, x - denominations[i], n);
        if (ans != INT_MAX)
            mini = min(mini, 1 + ans);
    }
    return mini;
}

int minimumCoins(int p) {
    int denominations[9] = {1, 2, 5, 10, 20, 50, 100, 500, 1000};
    int ans = solveRec(denominations, p, 9);
    if (ans == INT_MAX)
        return -1;

    return ans;
}
```

→ Memoization:-

```cpp
int solveRec(int denominations[], int x, int n, vector<int> &dp) {
    if (x == 0)
        return 0;
    if (x < 0)
        return INT_MAX;

    if (dp[x] != -1)
        return dp[x];

    int mini = INT_MAX;

    for (int i = 0; i < n; i++) {
        int ans = solveRec(denominations, x - denominations[i], n, dp);
        if (ans != INT_MAX)
            mini = min(mini, 1 + ans);
    }
    dp[x] = mini;
    return dp[x];
}

int minimumCoins(int p){
    int denominations[9] = {1, 2, 5, 10, 20, 50, 100, 500, 1000};
    vector<int> dp(p + 1, -1);
    int ans = solveRec(denominations, p, 9, dp);
    if (ans == INT_MAX)
        return -1;

    return ans;
}
```

→ Tabulation :-

```cpp
int solveRec(int denominations[], int x, int n) {
    vector<int> dp(x + 1, INT_MAX);

    dp[0] = 0;

    for (int i = 1; i <= x; i++) {
        for (int j = 0; j < 9; j++) {
            if( (i - denominations[j]) >= 0 && (dp[i - denominations[j]]) != INT_MAX )
                dp[i] = min(dp[i], 1 + dp[i - denominations[j]]);

        }
    }
    if(dp[x] == INT_MAX) return -1;
    return dp[x];
}

int minimumCoins(int p) {
    int denominations[9] = {1, 2, 5, 10, 20, 50, 100, 500, 1000};
    int ans = solveRec(denominations, p, 9);
    if (ans == INT_MAX)
        return -1;

    return ans;
}
```

Minimum Elements

You are given an array of 'N' distinct integers and an integer 'X' representing the target sum. You have to tell the minimum number of elements you have to take to reach the target sum 'X'.

Note:

You have an infinite number of elements of each type.

For example

If N=3 and X=7 and array elements are [1,2,3].
Way 1 - You can take 4 elements [2, 2, 2, 1] as 2 + 2 + 2 + 1 = 7.
Way 2 - You can take 3 elements [3, 3, 1] as 3 + 3 + 1 = 7.
Here, you can see in Way 2 we have used 3 coins to reach the target sum of 7.
Hence the output is 3.

Detailed explanation (Input/output format, Notes, Images)   ⌄

Constraints:

1 <= T <= 10
1 <= N <= 15
1 <= nums[i] <= (2^31) - 1
1 <= X <= 10000

All the elements of the "nums" array will be unique.
Time limit: 1 sec

→ Recursion :-

```cpp
#include <bits/stdc++.h>

int solveRec(vector<int> &num, int x) {
    if(x == 0) return 0;
    if(x < 0) return INT_MAX;

    int mini = INT_MAX;
    for(int i = 0; i < num.size(); i++) {
        int ans = solveRec(num, x - num[i]);
        if(ans != INT_MAX)
            mini = min(mini, 1 + ans);
    }
    return mini;
}

int minimumElements(vector<int> &num, int x)
{
    int ans = solveRec(num, x);
    if(ans == INT_MAX) {
        return -1;
    }
    return ans;
}
```


→ At every node, we will have N no. of choice where N is the size of array.
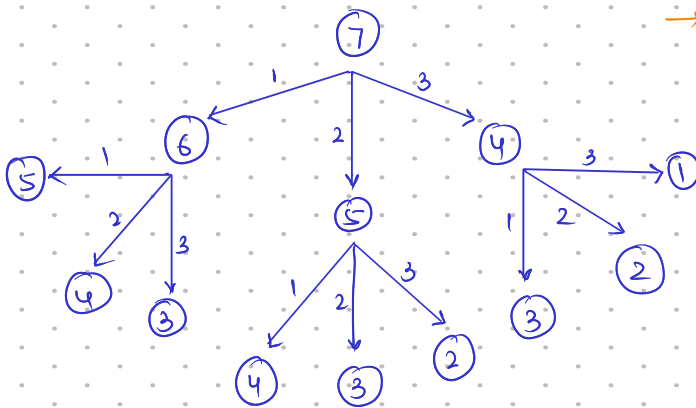
→ Memoization :-

```cpp
int solveMem(vector<int> &num, int x, vector<int> &dp) {
    if(x == 0) return 0;
    if(x < 0) return INT_MAX;

    if(dp[x] != -1) return dp[x];

    int mini = INT_MAX;
    for(int i = 0; i < num.size(); i++) {
        int ans = solveMem(num, x - num[i], dp);
        if(ans != INT_MAX)
            mini = min(mini, 1 + ans);
    }
    dp[x] = mini;
    return dp[x];
}

int minimumElements(vector<int> &num, int x)
{
    vector<int> dp(x + 1, -1);
    int ans = solveMem(num, x, dp);

    if(ans == INT_MAX) return -1;
    return ans;
}
```

→ Tabulation :-

```cpp
int solveTab(vector<int> &num, int x) {
    vector<int> dp(x + 1, INT_MAX);
    dp[0] = 0;

    // dp[i] represents minimum number of coins required to make target 'i'
    for (int i = 1; i <= x; i++) {
        // i am trying to solve for every amount figure from 1 to x
        for (int j = 0; j < num.size(); j++) {
            if ((i - num[j]) >= 0 && (dp[i - num[j]] != INT_MAX))
                dp[i] = min(dp[i], 1 + dp[i - num[j]]);
        }
    }
    if (dp[x] == INT_MAX)
        return -1;
    return dp[x];
}

int minimumElements(vector<int> &num, int x) {
    int ans = solveTab(num, x);
    return ans;
}
```

Maximum sum of non-adjacent elements

You are given an array/list of 'N' integers. You are supposed to return the maximum sum of the subsequence with the constraint that no two elements are adjacent in the given array/list.

Note:

A subsequence of an array/list is obtained by deleting some number of elements (can be zero) from the array/list, leaving the remaining elements in their original order.

Detailed explanation (Input/output format, Notes, Images) ⌄

Constraints:

1 <= T <= 500
1 <= N <= 1000
0 <= ARR[i] <= 10^5

Where 'ARR[i]' denotes the 'i-th' element in the array/list.

Time Limit: 1 sec.

Sample Input 1:

2
3
1 2 4
4
2 1 4 9

Sample Output 1:

5
11

Explanation to Sample Output 1:

In test case 1, the sum of 'ARR[0]' & 'ARR[2]' is 5 which is greater than 'ARR[1]' which is 2 so the answer is 5.

In test case 2, the sum of 'ARR[0]' and 'ARR[2]' is 6, the sum of 'ARR[1]' and 'ARR[3]' is 10, and the sum of 'ARR[0]' and 'ARR[3]' is 11. So if we take the sum of 'ARR[0]' and 'ARR[3]', it will give the maximum sum of sequence in which no elements are adjacent in the given array/list.

→ **Recursion :-**

```cpp
int solve(vector<int> &nums, int n) {
    if(n < 0) {
        return 0;
    }
    if(n == 0) {
        return nums[0];
    }

    int incl = solve(nums, n - 2) + nums[n];
    int excl = solve(nums, n - 1);
    return max(incl, excl);
}

int maximumNonAdjacentSum(vector<int> &nums){
    int n = nums.size();
    int ans = solve(nums, n - 1);
    return ans;
}
```
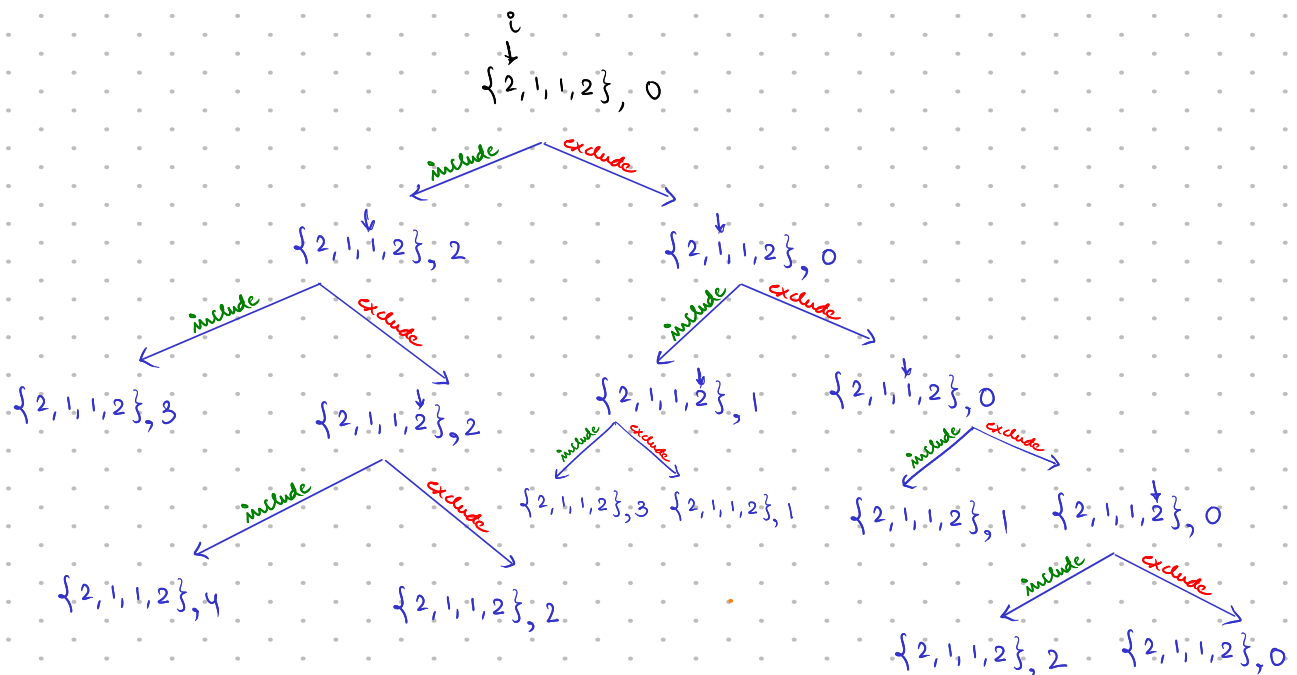
→ **Memoization :-**

```cpp
int solve(vector<int> &nums, int n, vector<int> &dp) {
    if(n < 0) {
        return 0;
    }
    if(n == 0) {
        return nums[0];
    }

    if(dp[n] != -1) return dp[n];

    int incl = solve(nums, n - 2, dp) + nums[n];
    int excl = solve(nums, n - 1, dp);
    return dp[n] = max(incl, excl);
}

int maximumNonAdjacentSum(vector<int> &nums){
    int n = nums.size();
    vector<int> dp(n + 1, -1);
    int ans = solve(nums, n - 1, dp);
    return ans;
}
```

i
↓
{2, 1, 1, 2}, 0

include / exclude

{2, 1, 1, 2}, 2   {2, 1, 1, 2}, 0

include / exclude   include / exclude

{2,1,1,2},3   {2,1,1,2},2   {2,1,1,2},1   {2,1,1,2},0

include / exclude   include / exclude   include / exclude

{2,1,1,2},4   {2,1,1,2},2   {2,1,1,2},3 {2,1,1,2},1   {2,1,1,2},1   {2,1,1,2},0

include / exclude

{2,1,1,2},2   {2,1,1,2},0

```cpp
int solve(vector<int> &nums) {
    int n = nums.size();
    vector<int> dp(n, 0);

    dp[0] = nums[0];

    for(int i = 1; i < n; i++) {
        int incl = dp[i - 2] + nums[i];
        int excl = dp[i - 1];
        dp[i] = max(incl, excl);
    }
    return dp[n - 1];
}

int maximumNonAdjacentSum(vector<int> &nums){
    return solve(nums);
}
```

```cpp
int solve(vector<int> &nums) {
    int n = nums.size();
    int prev2 = 0;
    int prev1 = nums[0];

    for(int i = 1; i < n; i++) {
        int incl = prev2 + nums[i];
        int excl = prev1;
        int ans = max(incl, excl);
        prev2 = prev1;
        prev1 = ans;
    }
    return prev1;
}

int maximumNonAdjacentSum(vector<int> &nums){
    return solve(nums);
}
```

House Robbery

You are given an integer 'N' denoting the length of the rod. You need to determine the maximum number of segments you can make of this rod provided that each segment should be of the length 'X', 'Y', or 'Z'.

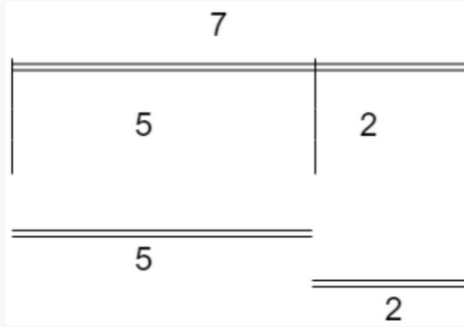**Detailed explanation** (Input/output format, Notes, Images)

Sample Input 1:

```
2
7 5 2 2
8 3 3 3
```

Sample Output 1:

```
2
0
```

Explanation For Sample Input 1:

In the first test case, cut it into 2 parts of 5 and 2.

In the second case, there is no way to cut into segments of 3 length only as the length of the rod is less than the given length.

Count Dearrangements

A Derangement is a permutation of 'N' elements, such that no element appears in its original position. For example, an instance of derangement of {0, 1, 2, 3} is {2, 3, 1, 0}, because 2 present at index 0 is not at its initial position which is 2 and similarly for other elements of the sequence.
Given a number 'N', find the total number of derangements possible of a set of 'N' elements.
Note:

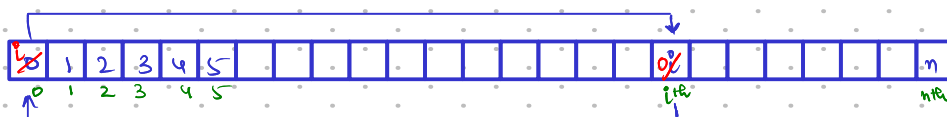The answer could be very large, output answer %(10 ^ 9 + 7).

→ Approach :-
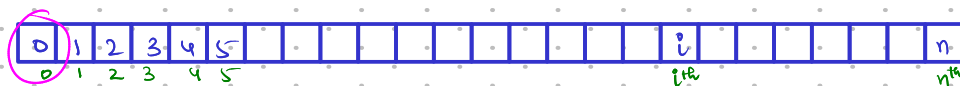
No. of ways to keep 0 is : $(n-1)$

Total dearrangements possible $= (n-1) * (sol^n \text{ of subproblems})$
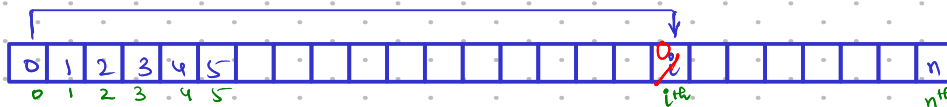
→ Two cases of subproblems :-

(I) i & 0 gets swapped :-

⇒ We have $(n-2)$ indexes left and $(n-2)$ numbers to be filled.
∴ The subproblem becomes $f(n-2)$.

(II)

0 toh i^{th} index me gaya, but main i ko 0th index pe nhi dalna chahta hu. Na hi 1 ko 1st index pe, 2 ko 2nd index pe and so on

→ Indexes $= n-1$
& Numbers $= n-1$ } Because 0 is fixed at i^{th} index.

∴ Subproblem is $f(n-1)$

$$f(n) = (n-1) * \{ f(n-1) + f(n-2) \}$$

→ Recursion :-

```cpp
long long int countDerangements(int n) {
    if (n == 1)
        return 0;
    if (n == 2)
        return 1;

    return ((n - 1) * (((countDerangements(n - 1)) % MOD + (countDerangements(n - 2)) % MOD)) % MOD) % MOD;
}
```

→ Memoization :-

```cpp
#define MOD 1000000007

long long int solveMem(int n, vector<long long int> &dp) {
    if (n == 1)
        return 0;
    if (n == 2)
        return 1;

    if(dp[n] != -1) return dp[n];

    int ans = ((n - 1) * (( (solveMem(n - 1, dp))% MOD + (solveMem(n - 2, dp)) % MOD )) % MOD) % MOD;
    dp[n] = ans;
    return ans;
}

long long int countDerangements(int n) {
    vector<long long int> dp(n + 1, -1);
    return solveMem(n, dp);
}
```

→ Tabulation :-

```cpp
long long int solveTab(int n) {
    vector<long long int> dp(n + 1, 0);

    dp[1] = 0;
    dp[2] = 1;

    for(int i = 3; i <= n; i++) {
        long long int first = dp[i - 1] % MOD;
        long long int second = dp[i - 2] % MOD;
        long long int sum = (first + second) % MOD;
        long long int ans = ( ( i - 1) * sum) % MOD;
        dp[i] = ans;
    }
    return dp[n];
}

long long int countDerangements(int n) {
    return solveTab(n);
}
```

→ Space Optimization :-

```cpp
long long int solveTab(int n) {
    long long int prev2 = 0;
    long long int prev1 = 1;

    for(int i = 3; i <= n; i++) {
        long long int first = prev1 % MOD;
        long long int second = prev2 % MOD;
        long long int sum = (first + second) % MOD;
        long long int ans = ( ( i - 1) * sum) % MOD;
        prev2 = prev1;
        prev1 = ans;
    }
    return prev1;
}

long long int countDerangements(int n) {
    return solveTab(n);
}
```

Painting Fence Algorithm

Ninja has given a fence, and he gave a task to paint this fence. The fence has 'N' posts, and Ninja has 'K' colors. Ninja wants to paint the fence so that not more than two adjacent posts have the same color.
Ninja wonders how many ways are there to do the above task, so he asked for your help.
Your task is to find the number of ways Ninja can paint the fence. Print the answer modulo 10^9 + 7.

Example:

Input: 'N' = 3, 'K' = 2
Output: 6

Say we have the colors with the numbers 1 and 0. We can paint the fence with 3 posts with the following different combinations.

110
001
101
100
010
011

Detailed explanation (Input/output format, Notes, Images) ⌄

Constraints :

1 <= 'T' <= 10
1 <= 'N' <= 10^5
1 <= 'K' <= 10^5
Time Limit: 1 sec

→ Approach :-

Solve(n) → In how many different ways we can paint the post such that not more than 2 consecutive post have the same colour.
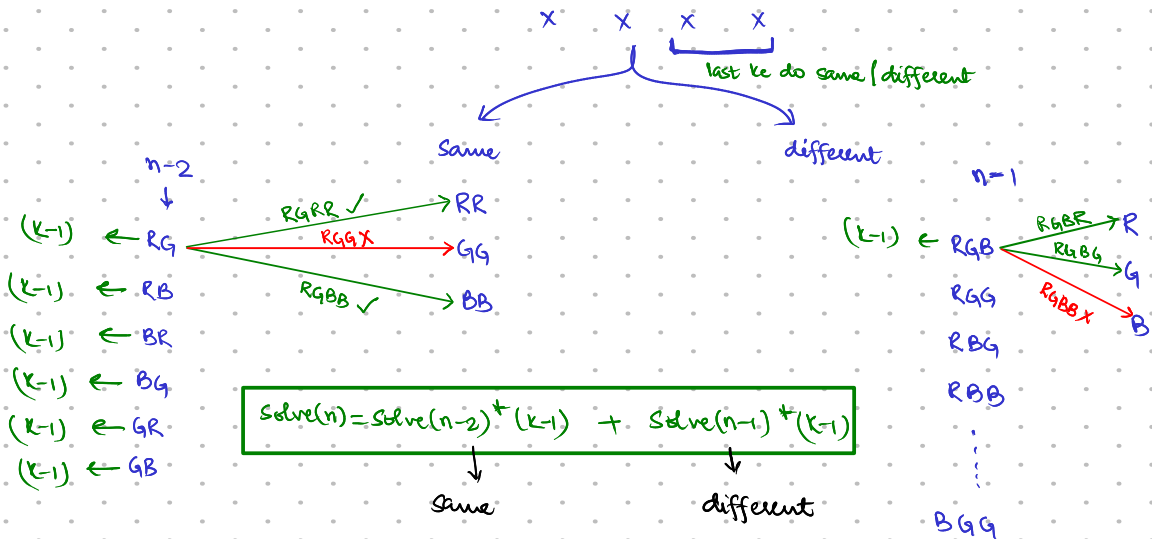
$k = 3$ (RGB)

	n=2 xx	n=3 xxx	n=4

Same colour on last two post	RR
	GG ③
	BB ↓
	    k
		RGG BRR
		RBB BGG
		GRR GBB
		         ⑥
			18

different colour on last two posts	RG BR ⑥ RB BG ↓ GR GB $k*(k-1)$	RR GB→k-1 GG BG→k-1 BB RG BR $9*(k-1)$ RB $=18$ GR	24 × k-1
$\sum$	9	24	66

Solve(2) = $k + k*(k-1) = k^2$

→ If n = 4

1st way → last 2 post colour will be different

2nd way → last 2 post colour will be same.

x   x   x   x
         ⎴
       last ke do same / different

Same ⟵   ⟶ different

n=2
↓
(k-1) ⟵ RG   RGRR ✓ → RR
                RGG X → GG
(k-1) ⟵ RB   RGBB ✓ → BB
(k-1) ⟵ BR
(k-1) ⟵ BG
(k-1) ⟵ GR
(k-1) ⟵ GB

n-1
(k-1) ⟵ RGB   RGBR → R
                RGBG → G
RGG   RGBB X → B
RBG
RBB
⋮
BGG

$$\boxed{Solve(n) = Solve(n-2)*(k-1) + Solve(n-1)*(k-1)}$$

Same ↓   different ↓

```cpp
#include <bits/stdc++.h>
#define MOD 1000000007

int add(int a, int b) {
    return (a % MOD + b % MOD) % MOD;
}

int mul(int a, int b) {
    return ((a % MOD) * (b % MOD)) % MOD;
}

int solve(int n, int k) {
    if(n == 1) return k;
    if(n == 2) return add(k, mul(k, k - 1));

    int ans = add(mul(solve(n - 2, k), k - 1), mul(solve(n - 1, k), k - 1));
    return ans;
}

int numberOfWays(int n, int k) {
    return solve(n, k);
}
```

```cpp
#include <bits/stdc++.h>
#define MOD 1000000007

int add(int a, int b) { return (a % MOD + b % MOD) % MOD; }

int mul(int a, int b) { return ((a % MOD) * 1LL * (b % MOD)) % MOD; }

int solve(int n, int k, vector<int> &dp) {
    if (n == 1)
        return k;
    if (n == 2)
        return add(k, mul(k, k - 1));

    if (dp[n] != -1)
        return dp[n];

    dp[n] = add(mul(solve(n - 2, k, dp), k - 1), mul(solve(n - 1, k, dp), k - 1));
    return dp[n];
}

int numberOfWays(int n, int k) {
    vector<int> dp(n + 1, -1);
    return solve(n, k, dp);
}
```

```cpp
#include <bits/stdc++.h>
#define MOD 1000000007

int add(int a, int b) { return (a % MOD + b % MOD) % MOD; }

int mul(int a, int b) { return ((a % MOD) * 1LL * (b % MOD)) % MOD; }

int solve(int n, int k) {

    vector<int> dp(n + 1, -1);

    dp[1] = k;
    dp[2] = add(k, mul(k, k - 1));

    for (int i = 3; i <= n; i++) {
        dp[i] = add(mul(dp[i - 2], k - 1), mul(dp[i - 1], k - 1));
    }
    return dp[n];
}

int numberOfWays(int n, int k) {
    return solve(n, k);
}
```

```cpp
#include <bits/stdc++.h>
#define MOD 1000000007

int add(int a, int b) { return (a % MOD + b % MOD) % MOD; }

int mul(int a, int b) { return ((a % MOD) * 1LL * (b % MOD)) % MOD; }

int solve(int n, int k) {
    int prev2 = k;
    int prev1 = add(k, mul(k, k - 1));

    for (int i = 3; i <= n; i++) {
        int ans = add(mul(prev2, k - 1), mul(prev1, k - 1));
        prev2 = prev1;
        prev1 = ans;
    }
    return prev1;
}

int numberOfWays(int n, int k) {
    return solve(n, k);
}
```