# Informatics 1 – Introduction to Computation Functional Programming Tutorial 10

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### Week 11 due 4pm Tuesday 29 November 2022 tutorials on Thursday 1 and Friday 2 December 2022

You will not receive credit for your coursework unless you attend the corresponding tutorial session. Please email kendal.reid@ed.ac.uk if you cannot join your assigned tutorial.

Good Scholarly Practice: Please remember the good scholarly practice requirements of the University regarding work for credit. You can find guidance at the School page

http://web.inf.ed.ac.uk/infweb/admin/policies/academic-misconduct.

This also has links to the relevant University pages. Please do not publish solutions to these exercises on the internet or elsewhere, to avoid others copying your solutions.

```
div, mod :: Integral a => a -> a -> a
even, odd :: Integral a => a -> Bool
(+), (*), (-), (/) :: Num a => a -> a -> a
(<), (<=), (>), (>=) :: Ord => a -> a -> Bool
(==), (/=) :: Eq a => a -> a -> Bool
(&&), (||) :: Bool → Bool → Bool
not :: Bool -> Bool
max, min :: Ord a => a -> a -> a
isAlpha, isAlphaNum, isLower, isUpper, isDigit :: Char -> Bool
toLower, toUpper :: Char -> Char
ord :: Char -> Int
chr :: Int -> Char
                           Figure 1: Basic functions
sum, product :: (Num a) => [a] -> a
                                               and, or :: [Bool] -> Bool
sum [1.0,2.0,3.0] = 6.0
                                               and [True, False, True] = False
product [1,2,3,4] = 24
                                               or [True, False, True] = True
maximum, minimum :: (Ord a) \Rightarrow [a] \rightarrow a
                                               all, any :: (a \rightarrow Bool) \rightarrow [a] \rightarrow Bool
maximum [3,1,4,2] = 4
                                               all odd [1,2,3] = False
minimum [3,1,4,2] = 1
                                               any odd [1,2,3] = True
                                               (++) :: [a] -> [a] -> [a]
concat :: [[a]] -> [a]
                                               "good" ++ "bye" = "goodbye"
concat ["go","od","bye"] = "goodbye"
(!!) :: [a] -> Int -> a
                                               length :: [a] -> Int
[9,7,5] !! 1 = 7
                                               length [9,7,5] = 3
head :: [a] -> a
                                               tail :: [a] -> [a]
head "goodbye" = 'g'
                                               tail "goodbye" = "oodbye"
init :: [a] -> [a]
                                               last :: [a] -> a
init "goodbye" = "goodby"
                                               last "goodbye" = 'e'
takeWhile :: (a\rightarrow Bool) \rightarrow [a] \rightarrow [a]
                                               take :: Int -> [a] -> [a]
takeWhile isLower "goodBye" = "good"
                                               take 4 "goodbye" = "good"
dropWhile :: (a\rightarrow Bool) \rightarrow [a] \rightarrow [a]
                                               drop :: Int -> [a] -> [a]
dropWhile isLower "goodBye" = "Bye"
                                               drop 4 "goodbye" = "bye"
elem :: (Eq a) => a -> [a] -> Bool
                                               replicate :: Int -> a -> [a]
elem 'd' "goodbye" = True
                                               replicate 5 '*' = "****"
zip :: [a] \rightarrow [b] \rightarrow [(a,b)]
zip [1,2,3,4] [1,4,9] = [(1,1),(2,4),(3,9)]
```

Figure 2: Library functions

For this tutorial exercise, *basic functions* refers to functions in Figure 1 and *library functions* refers to functions in Figure 2 on the preceding page.

1. (a) Say that a string is *ok* if it consists only of lower case letters and has length less than six. Write a function ok :: String -> Bool that identifies ok strings. For example:

```
ok "a" = True
ok "zzzzz" = True
ok "Short" = False
ok "longer" = False
ok "???" = False
```

You may use any functions you wish.

(b) Write a function f:: [String] -> String that finds the smallest ok string, where "smallest" refers to dictionary order. If no string is ok, return "zzzzz". For example:

```
f ["a","bb","ccc","dddd","eeeee","fffffff"] = "a"
f ["uuuuuu","vvvvv","wwww","xxx","yy","z"] = "vvvvv"
f ["Short","longer","???"] = "zzzzz"
```

Use basic functions, list comprehension, and library functions, but not recursion. You may use your answer to 1(a).

- (c) Write a function g:: [String] -> String that behaves like f, this time using basic functions and recursion, but not list comprehension or library functions from Figure 2. You may use your answer to 1(a).
- (d) Write a function h :: [String] -> String that also behaves like f, this time using one or more of the following higher-order functions:

```
map :: (a -> b) -> [a] -> [b]
filter :: (a -> Bool) -> [a] -> [a]
foldr :: (a -> b -> b) -> b -> [a] -> b
```

You may use basic functions but do not use recursion, list comprehension or library functions from Figure 2. You may use your answer to 1(a).

2. (a) Write a function i :: [a] -> [a] that takes two non-empty lists and returns the tail of the first followed by the head of the second. For example:

```
i "abc" "def" = "bcd"
i "def" "ghi" = "efg"
i "ghi" "abc" = "hia"
```

You may use any functions you wish.

(b) Write a function j :: [[a]] -> [[a]] that takes a non-empty list of non-empty lists, and moves the first element of each list to become the last element of the preceding list. The first element of the first list becomes the last element of the last list. For example:

```
j ["abc","def","ghi"] = ["bcd","efg","hia"]
j ["once","upon","a","time"] = ["nceu","pona","t","imeo"]
j ["a","b","c"] = ["b","c","a"]
j ["a"] = ["a"]
```

Use basic functions, list comprehension, and library functions, but not recursion. You may use your answer to 2(a). Hint: you may wish to use i twice in your solution.

(c) Write a function  $k :: [[a]] \rightarrow [[a]]$  that behaves like j, this time using basic functions and recursion, but not list comprehension or library functions from Figure 2. You may use your answer to 2(a).

3. The following data type represents propositions with two possible variables, X and Y, constants true and false, and connectives for negation, conjunction, disjunction, and implication.

The template file provides instances

```
(==) :: Prop -> Prop -> Bool
show :: Prop -> String
```

to compare two propositions for equality and to convert a proposition into a readable format. It also provides code that enables QuickCheck to generate arbitrary values of type Prop, to aid testing.

(a) Write a function eval :: Bool -> Bool -> Prop -> Bool that takes boolean values for X and Y and returns the boolean value of the proposition. For example:

```
eval False False ((X :->: Y) : \&\&: (Not Y :||: X)) = True eval False True ((X :->: Y) : \&\&: (Not Y :||: X)) = False eval True False ((X :->: Y) : \&\&: (Not Y :||: X)) = False eval True True ((X :->: Y) : \&\&: (Not Y :||: X)) = True
```

(b) We call a proposition *simple* if it does not contain T or F as proper subterms. Write a function **simple** :: Prop -> Bool that determines whether a proposition is simple. For example:

(c) Write a function simplify:: Prop -> Prop that converts a proposition to an equivalent proposition which is simple, using the following laws:

```
Not T
Not F
             Τ
          =
F : \&\&: p = p : \&\&: F =
T : \&\&: p = p : \&\&: T
                        = p
F : | | : p = p : | | : F
T : | | : p = p : | | : T = T
F :->: p = p :->: T = T
T :->: p = p
p :->: F = Not p
For example:
simplify T
                                             Τ
                                            F
simplify F
simplify ((T : | | : X) : -> : (T : \&\&: Y)) = Y
simplify ((X : | | : F) : -> : (X : \&\&: F)) = Not X
simplify ((X : | | : Y) : -> : (X : \&\&: Y)) = ((X : | | : Y) : -> : (X : \&\&: Y))
```

## **Optional: Parsing Propositions**

Following the Common Marking Scheme, a student with good mastery of the material is expected to get 3/4 points. This section is for demonstrating exceptional mastery of the material. It is optional and worth 1/4 points.

The template file for solutions for this part of the coursework is Prop.hs. The file defines a datatype for propositions, the same as the definition above, and an appropriate show function. It makes reference to the file MyParser.hs which contains code for monadic parsing.

### Exercise 1

Write a parser

```
parseProp :: Parser Prop
```

that can read a proposition from a string. It should be the inverse to the provided show function.

### Exercise 2

Write a QuickCheck property

```
prop_roundtrip :: Prop -> Bool
```

that checks that if you show a proposition to convert it to a string and parse the string to convert it back to a proposition then the result is the original proposition.