```
Queues
```

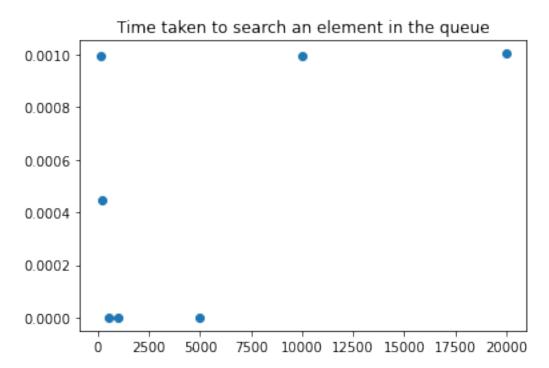
```
import matplotlib.pyplot as plt
import random as rn
import time
def enque (arr,x):
    arr.append(x)
    #return arr
def deque (arr):
    if (len(arr)==0):
        print("Queue is empty")
        return
    else:
        for i in range (len(arr)-1):
            arr[i]=arr[i+1]
        arr.pop()
        #return arr
size=[100,200,500,1000,5000,10000,20000]
timeEngue=[]
timeDeque=[]
for j in range (len(size)):
        queue=[]
        for i in range (size[j]):
            queue.append(rn.randint(1,20))
        start=time.time()
        enque (queue, 25)
        stop=time.time()
        timeEnque.append(stop-start)
        start=time.time()
        deque(queue)
        timeDeque.append(stop-start)
plt.scatter(size,timeEngue)
plt.title('Time taken to enque elements for different array sizes')
plt.show()
```

```
Time taken to enque elements for different array sizes
   0.04
   0.02
   0.00
  -0.02
  -0.04
          0
              2500
                    5000
                           7500 10000 12500 15000 17500 20000
def searchQueue(arr,x):
    k=-1
    for i in range (len(arr)):
        if (arr[i]==x):
            k=i
            break
    if (k==-1):
        print("The element is not present in the queue")
        return
    else:
        print("The element is present at the index ",k)
        return
timeSearch=[]
for j in range (len(size)):
    queue=[]
    queue=[]
    for i in range (size[j]-1):
        queue.append(rn.randint(1,20))
    queue.append(25)
    start=time.time()
    searchQueue(queue, 25)
    stop=time.time()
```

timeSearch.append(stop-start)

```
print(timeSearch)
The element is present at the index
                                     99
The element is present at the index
                                     199
The element is present at the index
                                     499
The element is present at the index
                                     999
The element is present at the index
                                     4999
The element is present at the index
                                     9999
The element is present at the index
                                     19999
[0.0009968280792236328, 0.0004448890686035156, 0.0, 0.0, 0.0,
0.0009963512420654297, 0.001003265380859375
```

```
plt.scatter(size,timeSearch)
plt.title('Time taken to search an element in the queue')
plt.show()
```



Time complexity

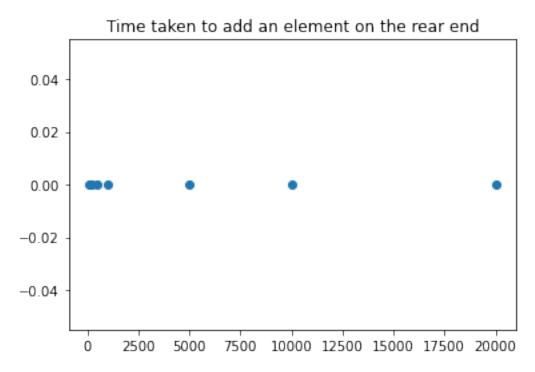
- 1) For insertion or enque the element is added directly to the end of the queue. Hence the time complexity for enque is O(1).
- 2) For deletion or dequeing the element at 0 index is removed and the other n-1 elements are all shifted to the left by 1 index. Hence the time taken for deletion is O(n).
- 3) For searching, the search technique is similar to that of linear search i.e. all the elements are checked one by one till the element desired is obtained. Hence the time complexity of searching is O(n)

```
Double ended queues
def pushBack (arr,x):
    arr.append(x)
    #return arr
def popBack(arr):
    if (len(arr)==0):
        print("queue is empty")
        return
    else:
        arr.pop()
        #return arr
def pushFront(arr,x):
    if (len(arr)==0):
        arr.append(x)
        return
    else:
        temp=arr[len(arr)-1]
        for i in range (len(arr)-1):
            arr[i+1]=arr[i]
        arr.append(temp)
        arr[0]=x
        #return arr
def popFront(arr):
    if (len(arr)==0):
        print("Queue is empty")
        return
    else:
        for i in range (len(arr)-1):
            arr[i]=arr[i+1]
        arr.pop()
        #return arr
def searchQueue(arr,x):
    for i in range (len(arr)):
        if (arr[i]==x):
            k=i
            break
    if (k==-1):
```

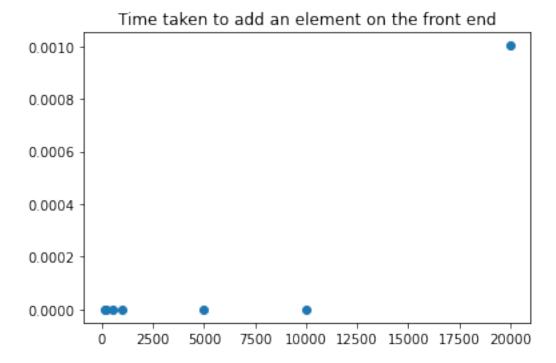
```
print("The element is not present in the queue")
        return
    else:
        print("The element is present at the index ",k)
        return
timePushBack=[]
timePushFront=[]
timePopBack=[]
timePopFront=[]
timeSearch=[]
for j in range (len(size)):
    queue=[]
    for i in range (size[i]):
        queue.append(rn.randint(1,20))
    start=time.time()
    pushBack(queue,25)
    stop=time.time()
    timePushBack.append(stop-start)
    start=time.time()
    popBack(queue)
    stop=time.time()
    timePopBack.append(stop-start)
    start=time.time()
    pushFront(queue, 25)
    stop=time.time()
    timePushFront.append(stop-start)
    start=time.time()
    popFront(queue)
    stop=time.time()
    timePopFront.append(stop-start)
    queue.append(25)
    start=time.time()
    searchQueue(queue, 25)
    stop=time.time()
    timeSearch.append(stop-start)
The element is present at the index
                                      100
                                      200
The element is present at the index
The element is present at the index
                                      500
The element is present at the index
                                      1000
The element is present at the index
                                      5000
```

```
The element is present at the index 10000
The element is present at the index 20000

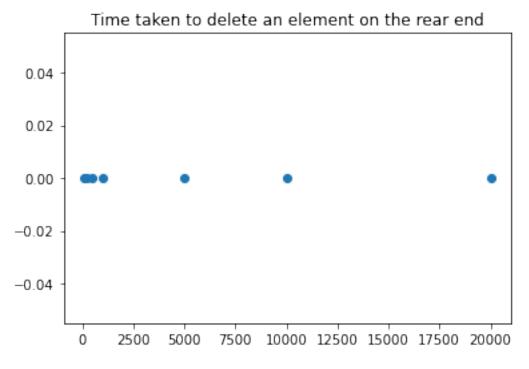
plt.scatter(size,timePushBack)
plt.title('Time taken to add an element on the rear end')
plt.show()
```



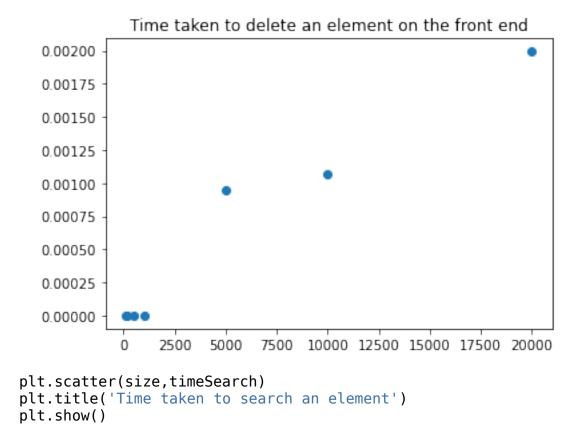
plt.scatter(size,timePushFront)
plt.title('Time taken to add an element on the front end')
plt.show()

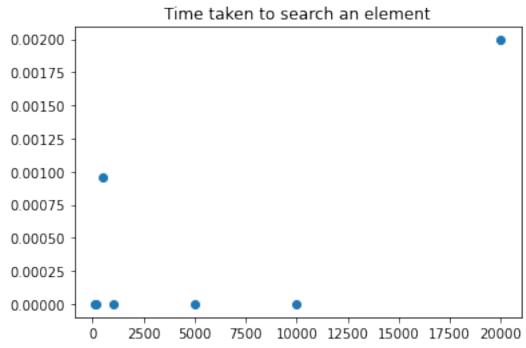


plt.scatter(size,timePopBack)
plt.title('Time taken to delete an element on the rear end')
plt.show()



plt.scatter(size,timePopFront)
plt.title('Time taken to delete an element on the front end')
plt.show()





Time Complexity

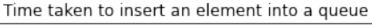
1) For push back we add the elements from the rear side and hence the complexity is O(1)

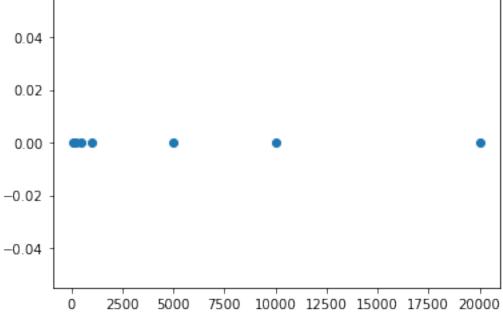
- 2) For pop back we delete the elements from the back and hence the complexity is O(1)
- 3) For push front we shift the n elements to the right by 1 index and add the element in the front. Hence the complexity is O(n)
- 4) For pop front we delete the first element and shift the n elements to the left by 1 index . Hence the time complexity is O(n)
- 5) For searching, the search technique is similar to that of linear search i.e. all the elements are checked one by one till the element desired is obtained. Hence the time complexity of searching is O(n)

```
Priority queues
def enque (arr,x):
    arr.append(x)
    #return arr
def deque (arr):
    if (len(arr)==0):
        print("Queue is empty")
        return
    else:
        minimum=arr[0]
        minIndex=0
        for i in range (len(arr)):
            if (arr[i]<minimum):</pre>
                minimum=arr[i]
                minIndex=i
        for i in range (minIndex,len(arr)-1):
            arr[i]=arr[i+1]
        arr.pop()
    #return arr
def searchQueue(arr,x):
    k=-1
    for i in range (len(arr)):
        if (arr[i]==x):
            k=i
            break
    if (k==-1):
        print("The element is not present in the queue")
```

```
return
```

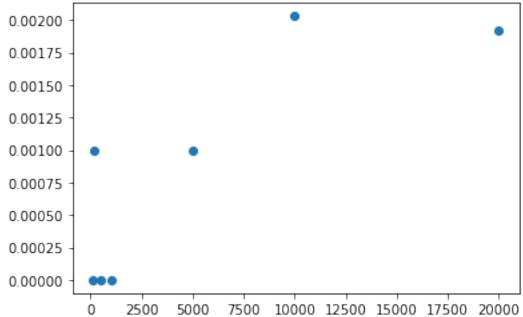
```
else:
        print("The element is present at the index ",k)
        return
timeEnguep=[]
timeDequep=[]
timeSearchp=[]
for j in range (len(size)):
    queue=[]
    for i in range (size[j]):
        queue.append(rn.randint(1,20))
    queue.append(25)
    start=time.time()
    enque(queue, rn. randint(1,10))
    stop=time.time()
    timeEnquep.append(stop-start)
    start=time.time()
    deque(queue)
    stop=time.time()
    timeDequep.append(stop-start)
    start=time.time()
    searchQueue(queue, 25)
    stop=time.time()
    timeSearchp.append(stop-start)
The element is present at the index
                                     99
The element is present at the index
                                     199
The element is present at the index
                                     499
The element is present at the index
                                     999
The element is present at the index
                                    4999
The element is present at the index 9999
The element is present at the index
                                    19999
plt.scatter(size,timeEnquep)
plt.title('Time taken to insert an element into a queue')
plt.show()
```



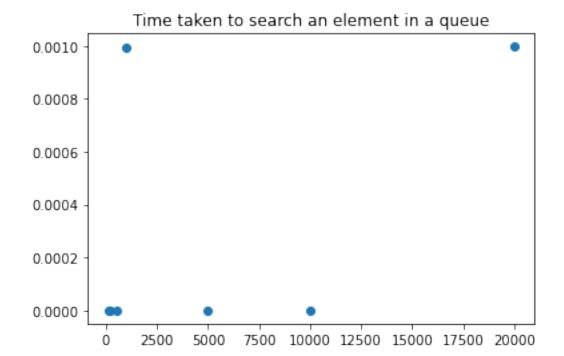


plt.scatter(size,timeDequep)
plt.title('Time taken to delete an element from a queue')
plt.show()





```
plt.scatter(size,timeSearchp)
plt.title('Time taken to search an element in a queue')
plt.show()
```



Time Complexity

- 1) For insertion or enque the element is added directly to the end of the queue. Hence the time complexity for enque is O(1).
- 2) For dequeueing or deletion of an element in a priority queue, we first need to search the element with the highest priority (i.e. the minimum value in the queue), and then delete it. After that we have to shift all the elements after it 1 index to the left. Searching has a time complexity of O(n) and shifting also has a time complexity of O(n). Hence the net time complexity is O(n)+O(n)=O(n).
- 3) For searching, the search technique is similar to that of linear search i.e. all the elements are checked one by one till the element desired is obtained. Hence the time complexity of searching is O(n)

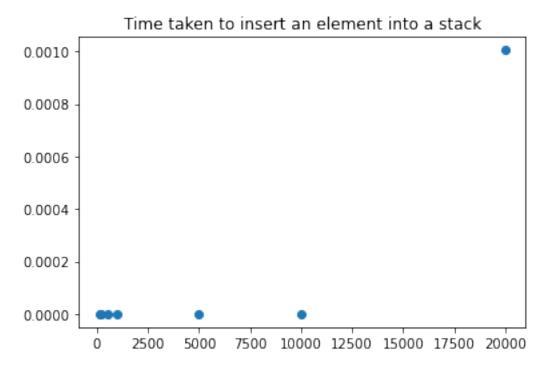
Stack

```
def push(arr,x):
    arr.append(x)
    return

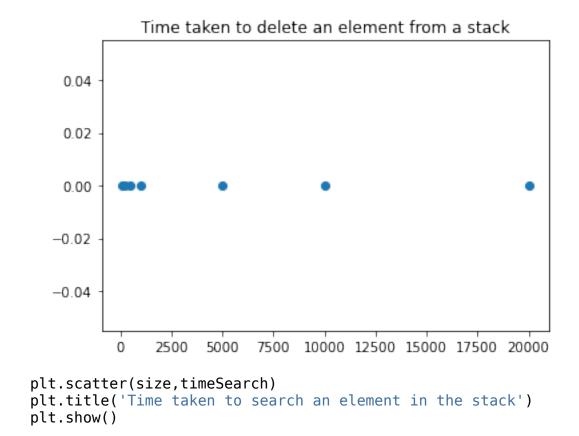
def pop(arr):
    if (len(arr)==0):
        print("The stack is empty")
        return
    else:
```

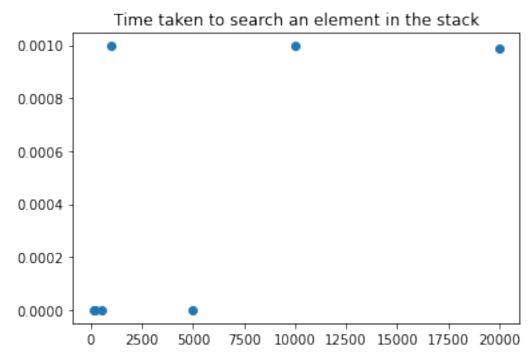
```
arr.pop()
        return
def search(arr,x):
    k=-1
    for i in range (len(arr)):
        if (arr[i]==x):
            k=i
            break
    if (k==-1):
        print("The element is not present in the stack")
        return
    else:
        print("The element is present at the index ",k)
        return
timePush=[]
timePop=[]
timeSearch=[]
for j in range (len(size)):
    stack=[]
    for i in range (size[i]):
        stack.append(rn.randint(1,20))
    start=time.time()
    pop(stack)
    stop=time.time()
    timePop.append(stop-start)
    start=time.time()
    push(stack, 25)
    stop=time.time()
    timePush.append(stop-start)
    start=time.time()
    search(stack, 25)
    stop=time.time()
    timeSearch.append(stop-start)
The element is present at the index
                                     99
The element is present at the index
                                     199
The element is present at the index 499
The element is present at the index
                                     999
The element is present at the index 4999
The element is present at the index
                                     9999
The element is present at the index
                                     19999
```

```
print(timePush)
[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.001004934310913086]
plt.scatter(size,timePush)
plt.title('Time taken to insert an element into a stack')
plt.show()
```



plt.scatter(size,timePop)
plt.title('Time taken to delete an element from a stack')
plt.show()





Time Complexity

1) The elements are added at the end. Hence the time complexity for insertion is O(1).

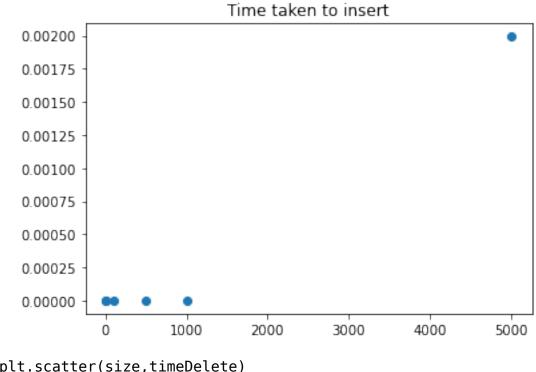
- 2) The elements are deleted from the end and hence the time complexity for deletion is O(1)
- 3) For searching, the search technique is similar to that of linear search i.e. all the elements are checked one by one till the element desired is obtained. Hence the time complexity of searching is O(n)

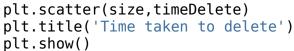
Linked lists

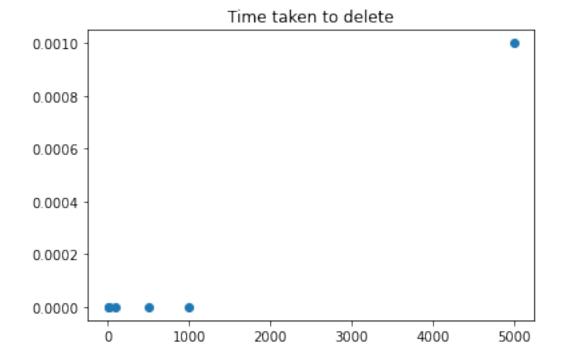
```
class Node:
    def __init__(self, data=None, next=None):
        self.data = data
        self.next = next
class linkedList:
    def init (self):
        \overline{\text{self.head}} = \text{None}
    def print(self):
        if self.head is None:
            print("Linked list is empty")
            return
        itr = self.head
        llstr = ''
        while itr:
            llstr += str(itr.data)+' , '
            if itr.next else str(itr.data)
            itr = itr.next
        print(llstr)
    def length(self):
        count = 0
        itr = self.head
        while itr:
            count+=1
            itr = itr.next
        return count
    def insertBeginning(self, data):
        node = Node(data, self.head)
        self.head = node
    def insertEnd(self, data):
        if self.head is None:
             self.head = Node(data, None)
             return
```

```
itr = self.head
    while itr.next:
        itr = itr.next
    itr.next = Node(data, None)
def insert(self, index, data):
    if index<0 or index>self.length():
        print("invalid input")
        return
    if index==0:
        self.insertBeginning(data)
        return
    count = 0
    itr = self.head
    while itr:
        if count == index - 1:
            node = Node(data, itr.next)
            itr.next = node
            break
        itr = itr.next
        count += 1
def delete(self, index):
    if index<0 or index>=self.length():
        print("Invalid Index")
        return
    if index==0:
        self.head = self.head.next
        return
    count = 0
    itr = self.head
    while itr:
        if count == index - 1:
            itr.next = itr.next.next
            break
        itr = itr.next
        count+=1
```

```
def search(self,value):
        if self.head is None:
            print("Linked list is empty")
        itr = self.head
        llstr = ''
        while itr:
            llstr += str(itr.data)+' , '
            if itr.next else str(itr.data)
            itr = itr.next
timeInsert=[]
timeDelete=[]
size=[5,10,100,500,1000,5000]
for j in range (len(size)):
    ll=linkedList()
    for i in range (size[j]):
        ll.insertEnd(rn.randint(1,20))
        ll.insertEnd(25)
    start=time.time()
    ll.insert(size[j],23)
    stop=time.time()
    timeInsert.append(stop-start)
    start=time.time()
    ll.delete(size[j])
    stop=time.time()
    timeDelete.append(stop-start)
print(timeInsert,timeDelete)
[0.0, 0.0, 0.0, 0.0, 0.0, 0.0019927024841308594] [0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]
0.0, 0.0010001659393310547]
plt.scatter(size,timeInsert)
plt.title('Time taken to insert')
plt.show()
```







Time complexity

1) For inserting an element we need to move the pointer to the desired index and then add the node. To move the pointer to the desired location time Complexity is O(n) and time

taken to create and add the node is O(1). Hence the total time complexity for inserting is O(n).

2) For deleting an element we need to move the pointer to the desired index and then delete the node. To move the pointer to the desired location time Complexity is O(n) and time taken to delete the node is O(1). Hence the total time complexity for deleting O(n).