

We know that,

Bellman's equation

$$V_{\pi}(s) = \sum_a \pi(a|s) \sum_{s', R} p(s', R | s, a) [R + \gamma V_{\pi}(s')]$$

Given,

|          |          |          |          |
|----------|----------|----------|----------|
| $a_{11}$ | $a_{12}$ | $a_{13}$ | $a_{14}$ |
| $a_{21}$ | $a_{22}$ | $a_{23}$ | $a_{24}$ |
| $a_{31}$ | $a_{32}$ | $a_{33}$ | $a_{34}$ |
| $a_{41}$ | $a_{42}$ | $a_{43}$ | $a_{44}$ |

binomial

$$\Rightarrow a_1 = \left(\frac{1}{2}\right)(0 + \gamma(1)) = \frac{\gamma}{2}$$

$$\Rightarrow a_2 = \left(\frac{1}{2}\right)(0 + \gamma(1)) = \frac{\gamma}{2}$$

$$\Rightarrow a_3 = \left(\frac{1}{2}\right)(0 + \gamma(a_2)) + \left(\frac{1}{2}\right)(0 + \gamma(a_1))$$

$$\Rightarrow a_3 = \frac{\gamma^2}{2}$$



$$\Rightarrow a_4 = \left(\frac{1}{2}\right)(0 + \gamma a_2) + \frac{1}{2}(0 + \gamma a(-1))$$

$$\Rightarrow a_4 = \frac{\gamma^2 - \gamma}{4}$$

$$\Rightarrow a_5 = \frac{1}{3}(0 + \gamma a_4) = \frac{\gamma^3 - \gamma^2}{12}$$

$$\Rightarrow a_6 = \frac{1}{4}(0 + \gamma(-1)) + \left(\frac{1}{2}\right)(0 + \gamma(a_5))$$

$$\Rightarrow a_6 = \frac{\gamma^4 - \gamma^3 - 6\gamma}{24}$$

$$\Rightarrow a_7 = \frac{1}{2}(0 + \gamma a_1) = \frac{\gamma}{2}$$

$$\Rightarrow a_8 = \frac{1}{4}(0 + \gamma a_3) + \frac{1}{3}(0 + \gamma a_7)$$

$$\Rightarrow a_8 = \frac{\gamma^3}{8} - \frac{\gamma^2}{6}$$

$$\Rightarrow a_9 = \frac{1}{4}(0 + \gamma a_8) + \frac{1}{4}(0 + \gamma(-1))$$

$$\Rightarrow a_9 = \frac{\gamma^4}{32} - \frac{\gamma^3}{24} - \frac{\gamma}{4}$$



$$\Rightarrow a_{10} = \frac{1}{4}(0 + \gamma a_9) + \frac{1}{3}(0 + \gamma a_8)$$

$$\Rightarrow a_{10} = \frac{\gamma^5}{128} - \frac{\gamma^4}{96} - \frac{\gamma^2}{16} + \frac{\gamma^4 - \gamma^3 - 6\gamma}{72}$$

$$\Rightarrow a_{11} = \frac{\gamma a_9}{3}$$

$$\Rightarrow a_{12} = \frac{\gamma a_{11}}{2} + \frac{\gamma a_8}{4}$$

$$\Rightarrow a_{13} = \frac{\gamma a_{12}}{2} + \frac{\gamma a_7}{4}$$

$$\Rightarrow a_{14} = \frac{\gamma a_{13}}{2} + \frac{\gamma a_{10}}{3}$$