

$$\begin{aligned}
 & \textcircled{1} \quad A + \bar{A}B + (\bar{A} + B)C + (\bar{A} + B + C)D \\
 & \quad A + \bar{A}B + (\bar{A} + B)C + \bar{A} \cdot \bar{B} \cdot \bar{C} \cdot D \\
 & \quad A + \bar{A}B + \bar{A}BC + \bar{A}\bar{B}\bar{C}D \\
 & \quad A + \bar{A}(B + \bar{B}C + \bar{B}\bar{C}D) \\
 & \quad A + \bar{A}(B + C + \bar{B}\bar{C}D) \rightarrow C + \bar{C} \quad \text{X} \\
 & \quad A + \bar{A}(B + C + \bar{B}D) = C + \bar{C} \\
 & \quad \quad \quad B + \bar{B}D = B + D \\
 & \quad A + \bar{A}(B + D + C) = B + D \\
 & \quad A + \bar{A}(B + D + C) = \\
 & \quad \quad \boxed{A + B + D + C}
 \end{aligned}$$

$$\begin{aligned}
 & \textcircled{2} \quad A[(B + C)(D + \bar{A})] \\
 & \quad A[B + CD + \bar{A}C] \\
 & \quad \overline{A[B + CD + \bar{A}C]} = \overline{AB + ACD + \bar{A}C} = \\
 & \quad \overline{AB} \cdot \overline{ACD} \cdot \overline{\bar{A}C} = (\bar{A} + B)(\bar{A} + \bar{C} + \bar{D}) = \\
 & \quad \bar{A}\bar{A} + \bar{A}\bar{C} + \bar{A}\bar{D} + \bar{A}\bar{B} + \bar{B}\bar{C} + \bar{B}\bar{D} \\
 & \quad \bar{A} + \bar{A}\bar{C} + \bar{A}\bar{D} + \bar{A}\bar{B} + \bar{B}\bar{C} + \bar{B}\bar{D} \\
 & \quad \bar{A}(1 + \bar{C} + \bar{D} + \bar{B}) + \bar{B}\bar{C} + \bar{B}\bar{D} \\
 & \quad \quad \boxed{\bar{A} + \bar{B}\bar{C} + \bar{B}\bar{D}}
 \end{aligned}$$

$$\textcircled{3} \quad \overline{\bar{A}B\bar{C}} = \bar{A} + \bar{B} + \bar{C} \therefore \boxed{A + B + C}$$

$$\begin{aligned}
 & \textcircled{4} \quad \bar{A}B\bar{C} + A\bar{B}\bar{C} + B\bar{C}D \\
 & \quad \bar{B}\bar{C}(\bar{A} + A + D) = \boxed{B\bar{C}}
 \end{aligned}$$

$$\begin{aligned}
 & \textcircled{5} \quad A\bar{B}\bar{C} + A\bar{B}C + ABC \\
 & \quad A(\bar{B}\bar{C} + \bar{B}C + BC) \quad \bar{B} + B\bar{C} \\
 & \quad A(\bar{B}(\bar{C} + C) + BC) = \bar{B} + C \\
 & \quad A(\bar{B} + C) = \boxed{AB + AC}
 \end{aligned}$$