

STIX tutorial - Amplitude imaging

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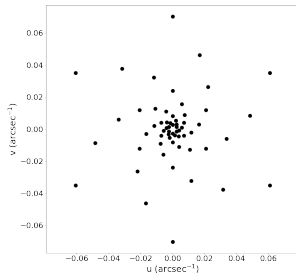
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STIX imaging problem: overview

- ▶ STIX measures V_1, \dots, V_{30} visibilities



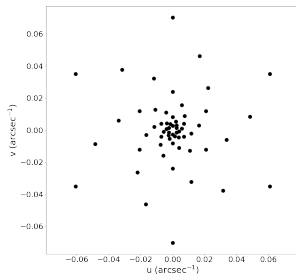
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- ▶ STIX measures V_1, \dots, V_{30} visibilities
- ▶ The imaging problem is

$$\mathcal{F}\varphi = V$$

where

- \mathcal{F} is the Fourier transform
- φ is the image of the X-ray emission
- $V = (V_1, \dots, V_{30})$



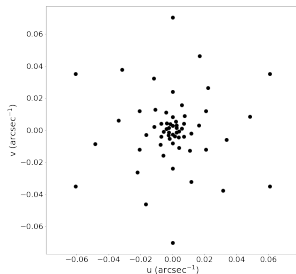
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Algorithms for calibrated data (RHESSI legacy)¹:

- | | |
|------------------|--|
| ▶ backprojection | ▶ Expectation Maximization (count-based) |
| ▶ CLEAN | ▶ uv_smooth |
| ▶ MEM_GE | ▶ VIS_CS and VIS_WV |
| ▶ VIS_FWDFIT | ▶ Bayes |

¹<https://hesperia.gsfc.nasa.gov/rhessi3/software/imaging-software/image-algorithm-summary/index.html>

Amplitude imaging (Massa., P., et al., (2021))

**The visibility amplitudes only are available for imaging
(visibility phases will come soon)**

Imaging problem from visibility amplitudes:

$$|\mathcal{F}\varphi| = A ,$$

where $A = |V|$

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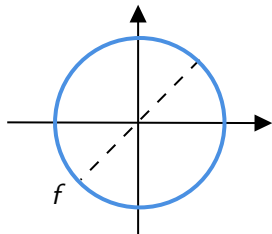
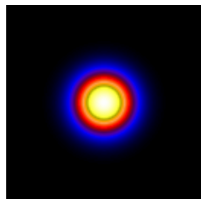
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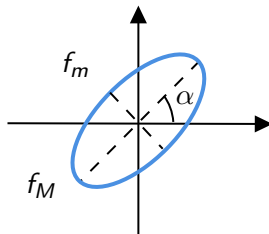
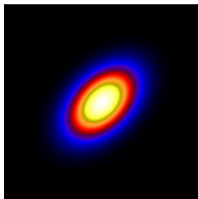
Amplitudes \Rightarrow information on dimension, orientation and relative position

Amplitude imaging (Massa., P., et al., (2021))

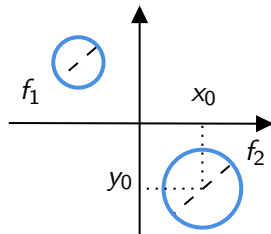
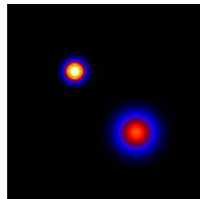
Approach: parametrized source shapes



$$\theta = (\phi, f)$$



$$\theta = (\phi, f_M, f_m, \alpha)$$



$$\theta = (x_0, y_0, \phi_1, f_1, \phi_2, f_2)$$

Particle Swarm Optimization (PSO) (Massa., P., et al., (2021))

How it works:

- ▶ choose the configuration (circular Gaussian, elliptical Gaussian, double circular Gaussian)
- ▶ find with PSO the parameters θ^* such that

$$\theta^* = \arg \min_{\theta} \chi^2(\theta) ,$$

where

$$\chi^2(\theta) = \sum_i \frac{(|(\mathcal{F}\varphi(\theta))_i| - A_i)^2}{\sigma_i^2}$$

- ▶ estimate the parameter uncertainties with the *confidence strip* approach (optional)





Sequential Monte Carlo (SMC)²_{(Massa., P., et al., (2021))}

How it works:

- ▶ choose the configuration (circular Gaussian, elliptical Gaussian, double circular Gaussian)
- ▶ approximate with SMC the probability distribution $p(\theta|A)$
- ▶ compute θ^* as the mean value of the probability distribution
- ▶ compute the parameter uncertainties as the standard deviation of the probability distribution

²Sciacchitano, F., et al. (2018)

References

-  Krucker, S., et al., *The Spectrometer/Telescope for Imaging X-rays (STIX)*, Astronomy & Astrophysics, 642 (2020)
-  Massa, P., et al., *Imaging from STIX visibility amplitudes*, submitted to Astronomy & Astrophysics (2021)
-  Sciacchitano, F., et al., *Identification of multiple hard X-ray sources in solar flares: A Bayesian analysis of the 2002 February 20 event*, The Astrophysical Journal, 862 (2018)
-  Battaglia, A. F. et al., *STIX X-ray microflare observations during the Solar Orbiter commissioning phase*, to appear on Astronomy & Astrophysics (2021)

Do you want to try it out? Find the code at
https://github.com/sgarbarino/Sparse_Bayesian_Imaging_RHESSI/tree/2021_rhessi_workshop_TUTORIAL

Thank you for the attention!