



STIX challenges

Università di Genova
DIMA | Dipartimento di Matematica

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Dolomites Research Week on Approximation and Applications
September, 2023



Outline

1. Calibration
2. New imaging method
3. Electron visibilities

STIX - Spectrometer/Telescope for Imaging X-rays

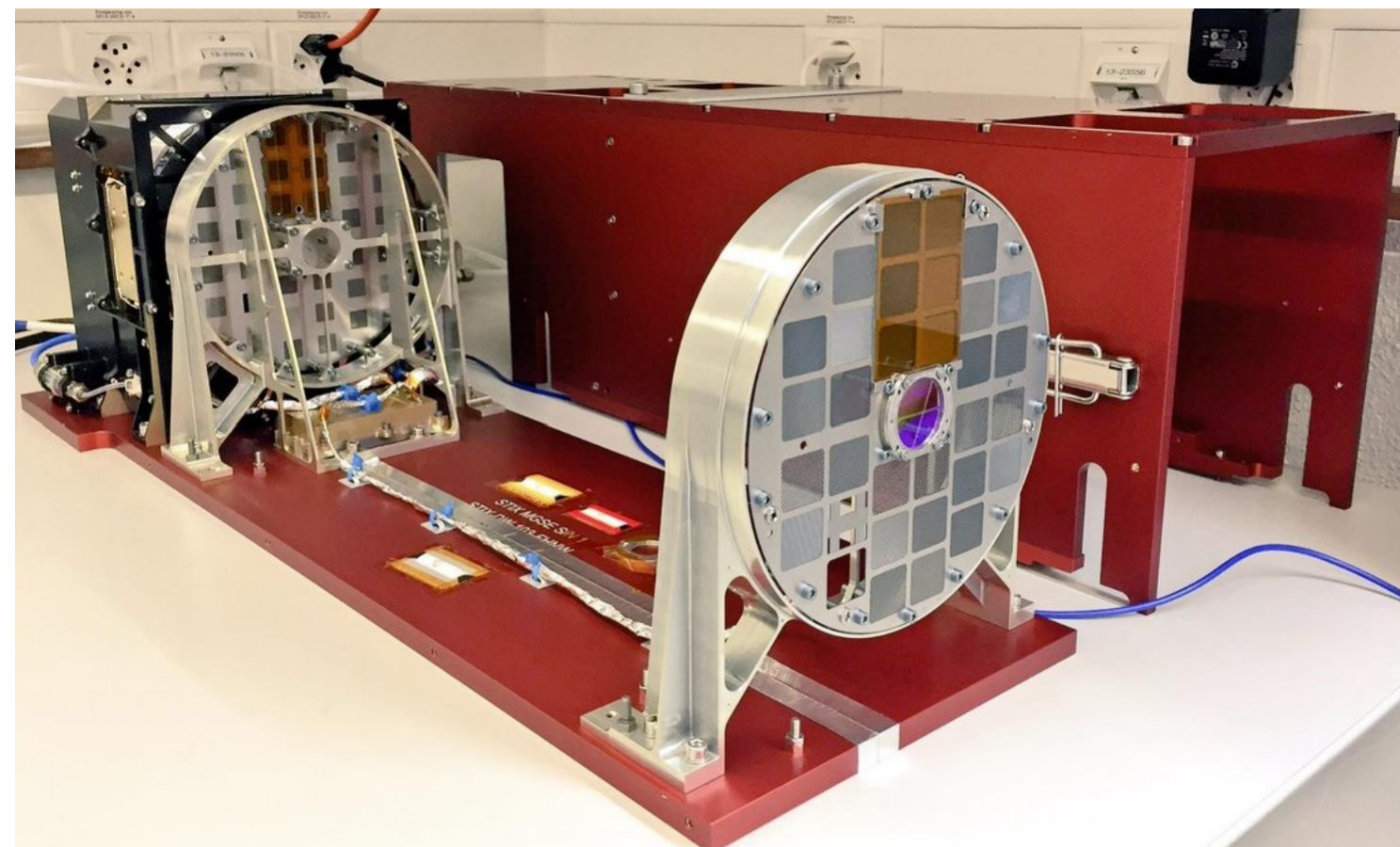


Figure: STIX before being assembled on Solar Orbiter
(Krucker et al., 2020).

Massa P., et al. *STIX imaging I--Concept*. *arXiv preprint arXiv*, 2023.

STIX - Spectrometer/Telescope for Imaging X-rays

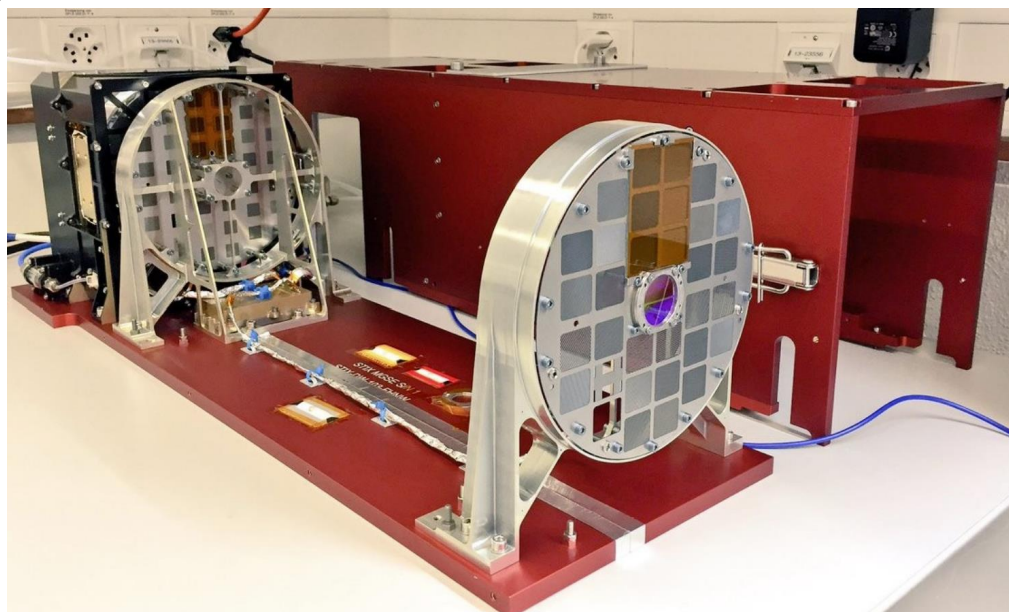


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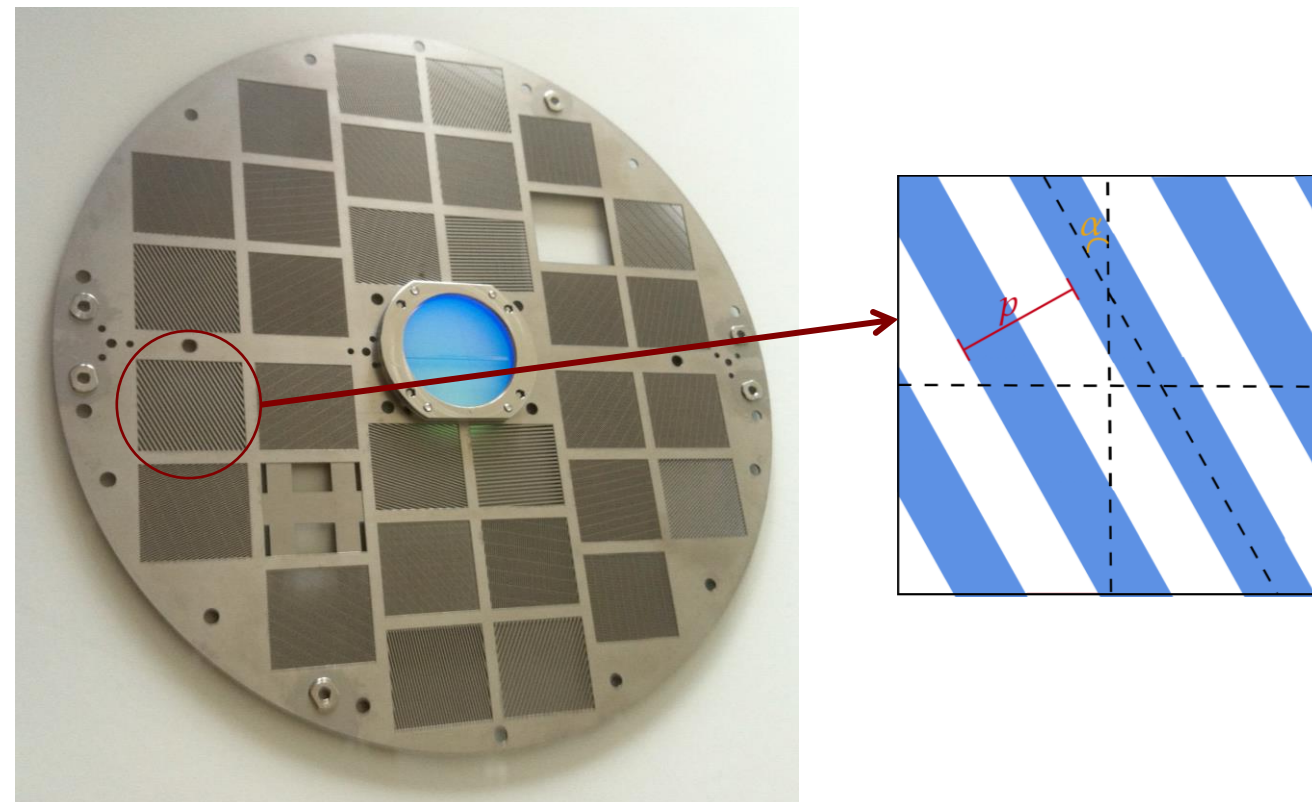


Figure: front and the rear grids before being assembled on the spacecraft (*left panel*), schematic of a grid window (*right panel*).

STIX - Spectrometer/Telescope for Imaging X-rays

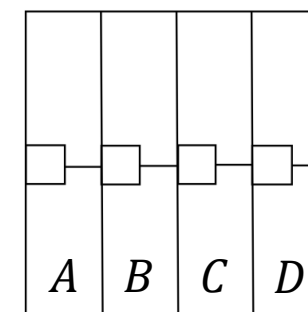
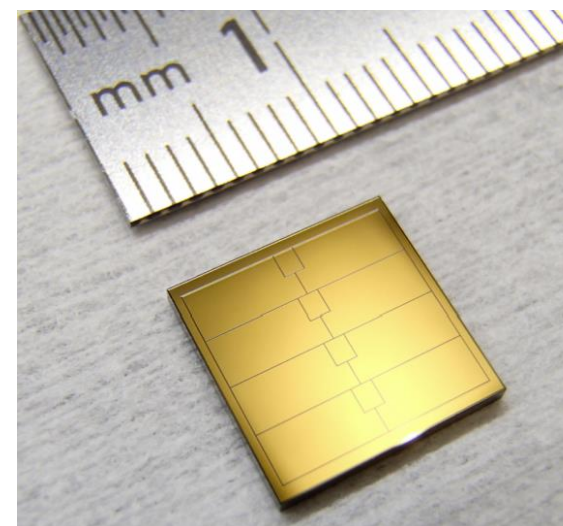
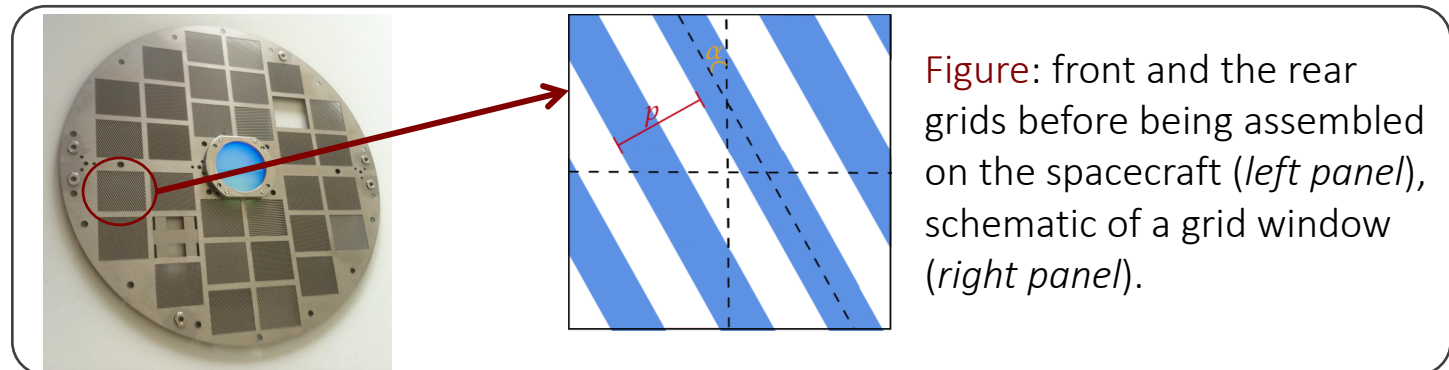


Figure: STIX detector (*left panel*) schematic of a detector (*right panel*).

STIX - Spectrometer/Telescope for Imaging X-rays

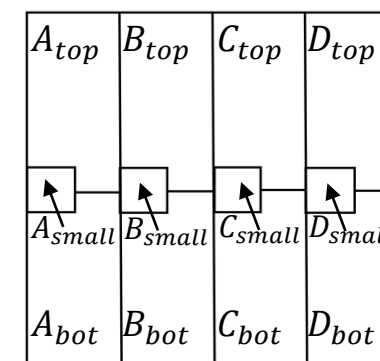
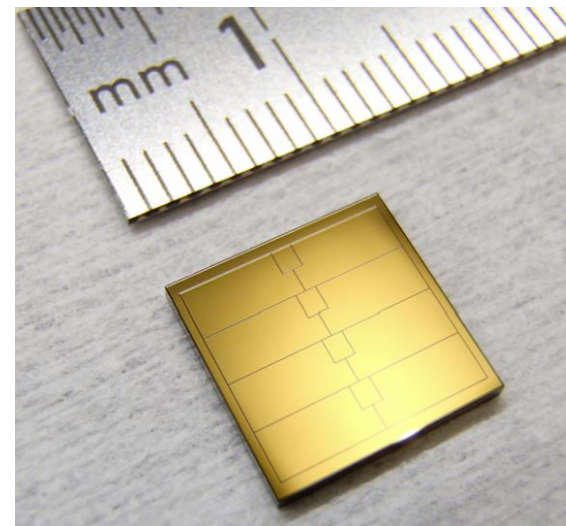
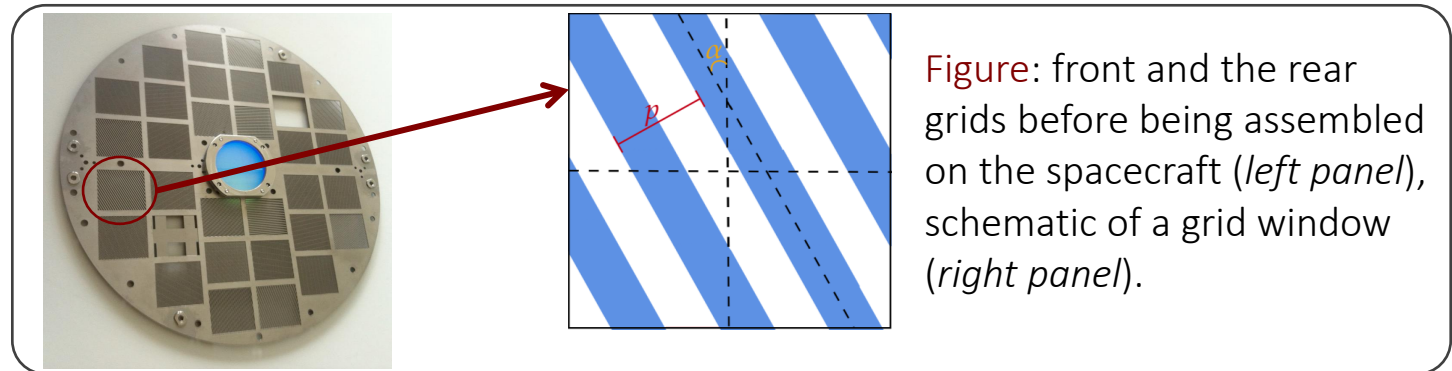


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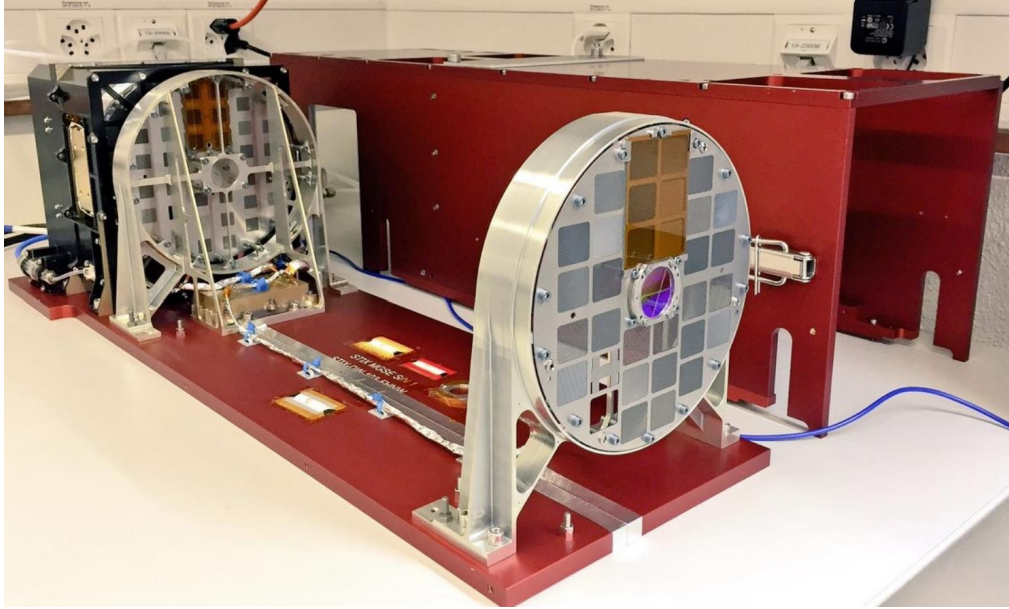


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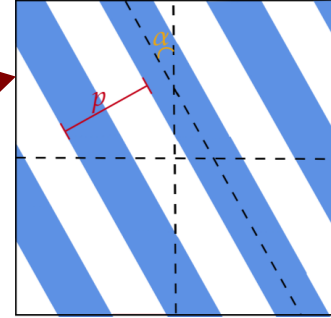
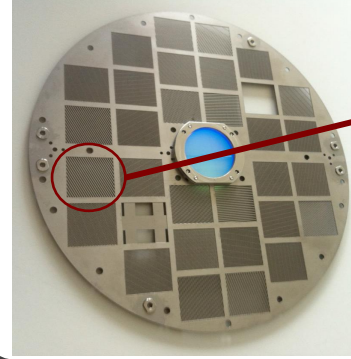


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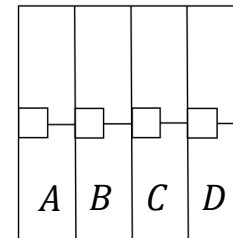
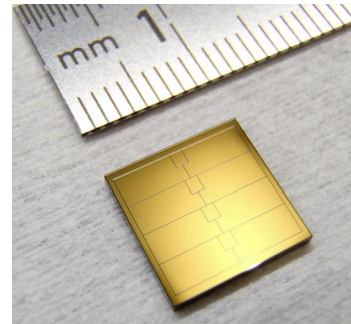


Figure: STIX detector (*left panel*) schematic of a detector (*right panel*).

Front grid

+

Rear grid

+

detector

Sub-collimator

STIX data formation process

Image reconstruction problem for STIX:

$$\mathcal{F}\phi = V \quad (1)$$

STIX data formation process

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$$\mathcal{F}\phi = V \tag{1}$$

Intensity of the X-ray photon flux
emitted from (x, y) on the Sun

STIX data formation process

Image reconstruction problem for STIX:

$$\mathcal{F}\phi = \mathbf{V} \quad (1)$$

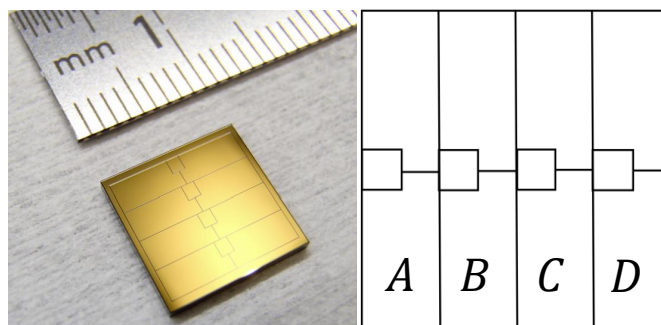


Figure: STIX detector (*left panel*)
schematic of a detector (*right panel*).

Array containing the N_V complex values of the visibilities measured by STIX

$$|V| \propto \sqrt{(C - A)^2 + (D - B)^2}$$

$$\psi = \text{atan}\left(\frac{D - B}{C - A}\right) + 45^\circ + \psi_{\text{calib}}$$

STIX data formation process

Image reconstruction problem for STIX:

$$\mathcal{F}\phi = V \quad (1)$$

The Fourier Transform defined by:

$$(\mathcal{F}\phi)_k = \iint \phi(x, y) \exp(2\pi i(xu_k + yv_k)) dx dy \quad k = 1, \dots, N_v$$

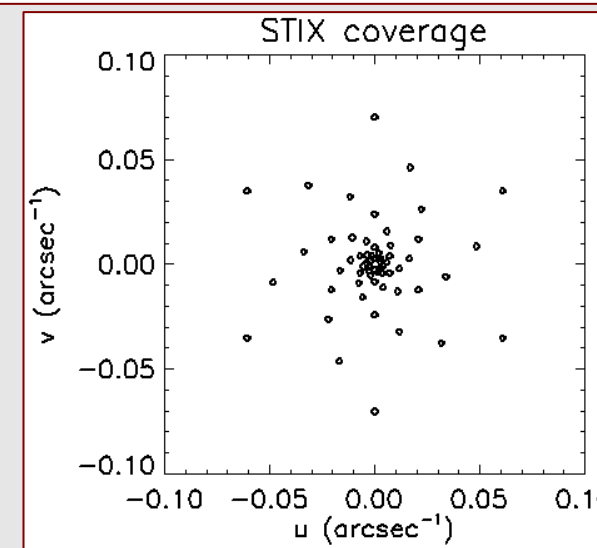


Figure: (u, v) frequencies sampled by STIX sub-collimators.

Massa P., et al. *STIX imaging I--Concept*. *arXiv preprint arXiv*, 2023.

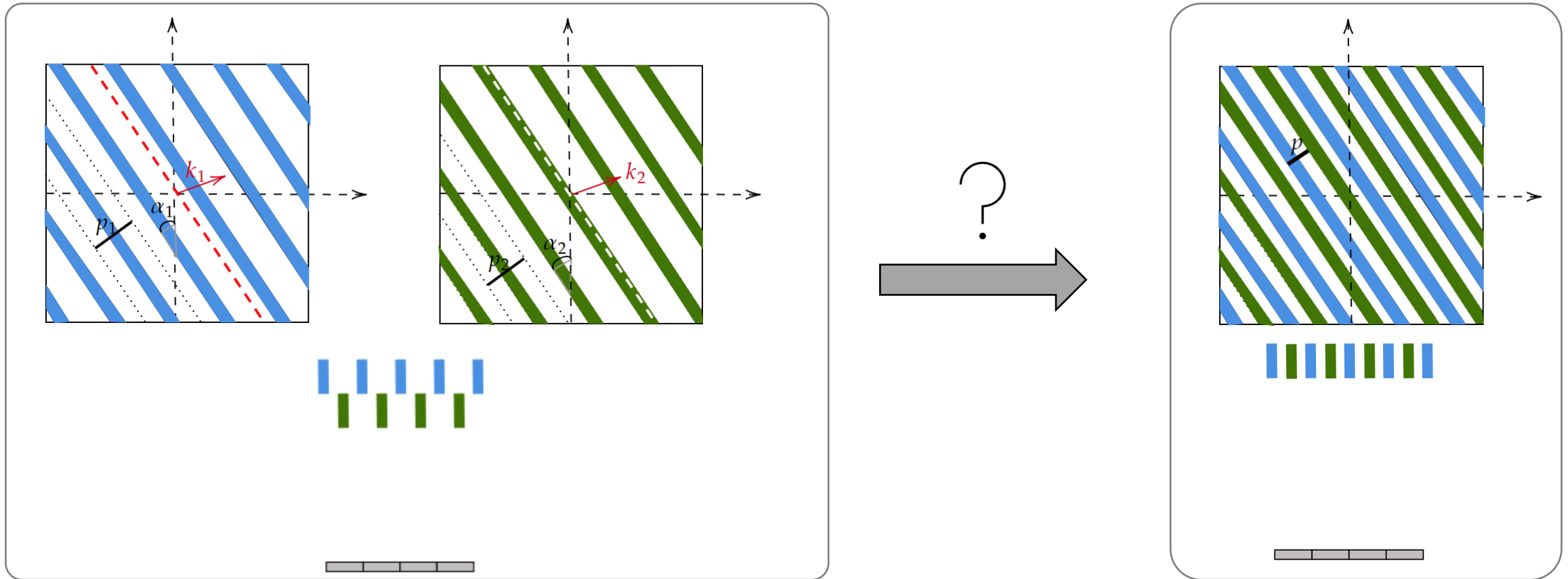
Outline

- 1. Calibration**
2. New imaging method
3. Electron visibilities

Two layers grid parameters

GOAL:

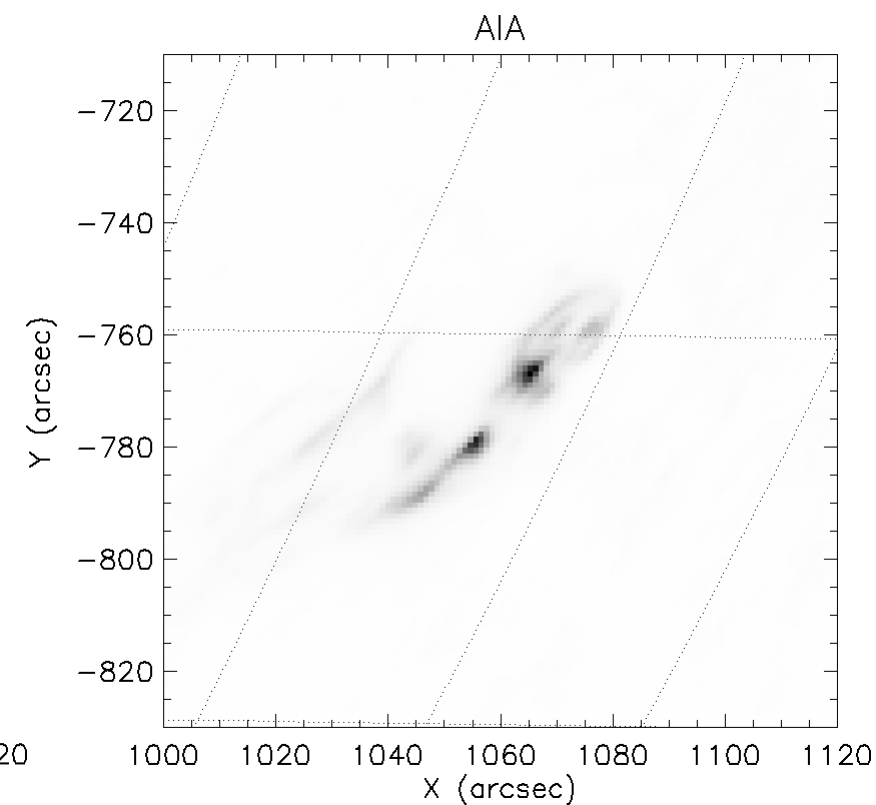
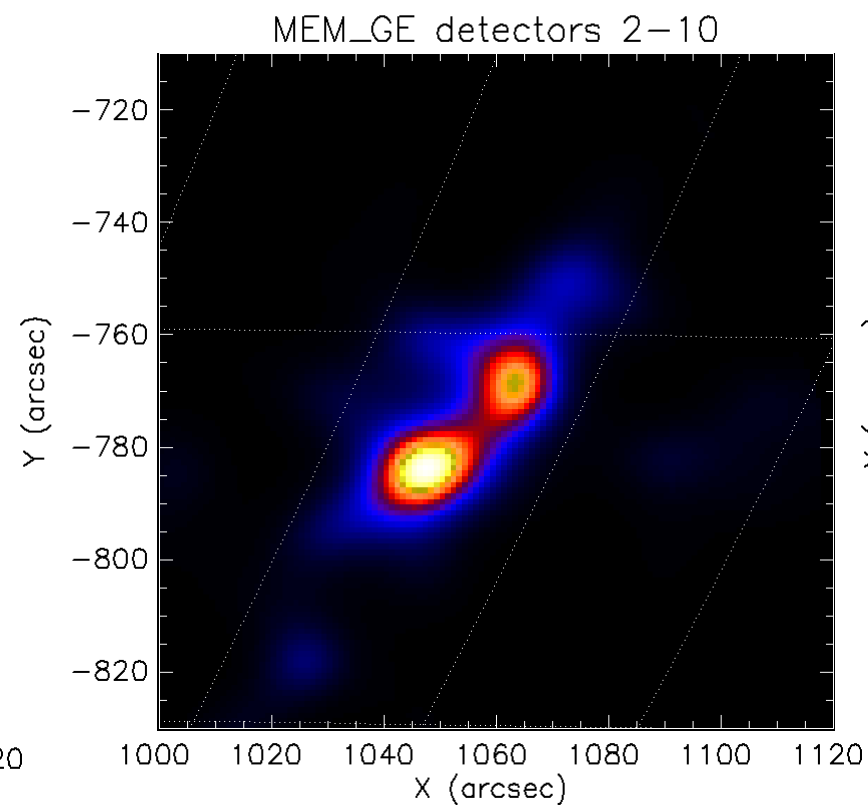
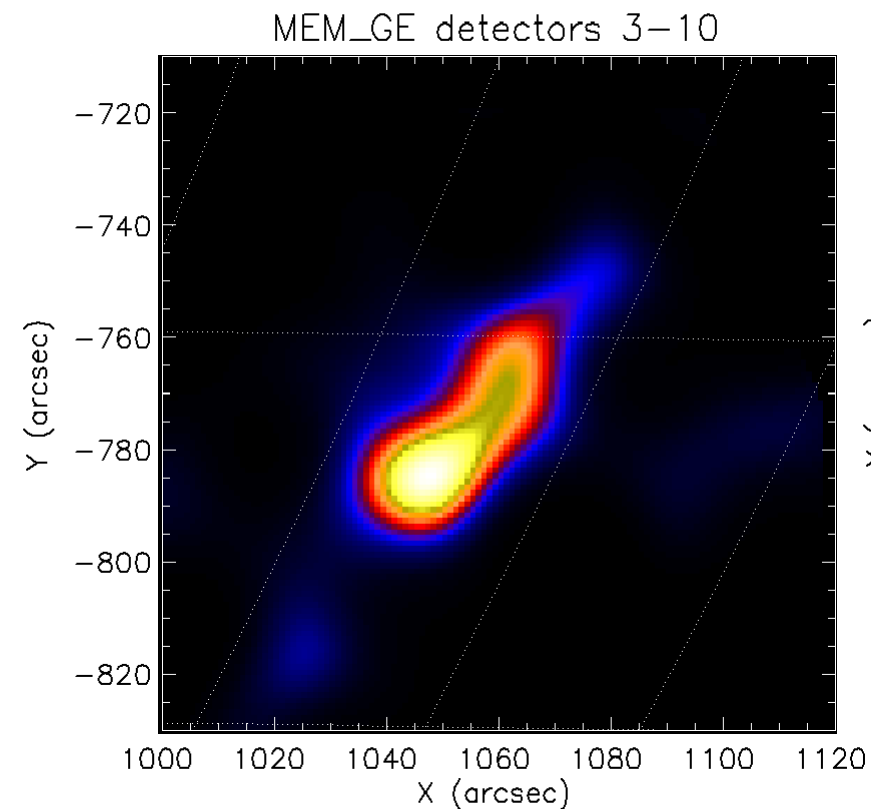
Derive the parameters of the double (and triple) layers grids in order to treat them as single-layer grids.



Test imaging – August 26, 2021

Time Interval: 23:18:00 – 23:20:00 UT

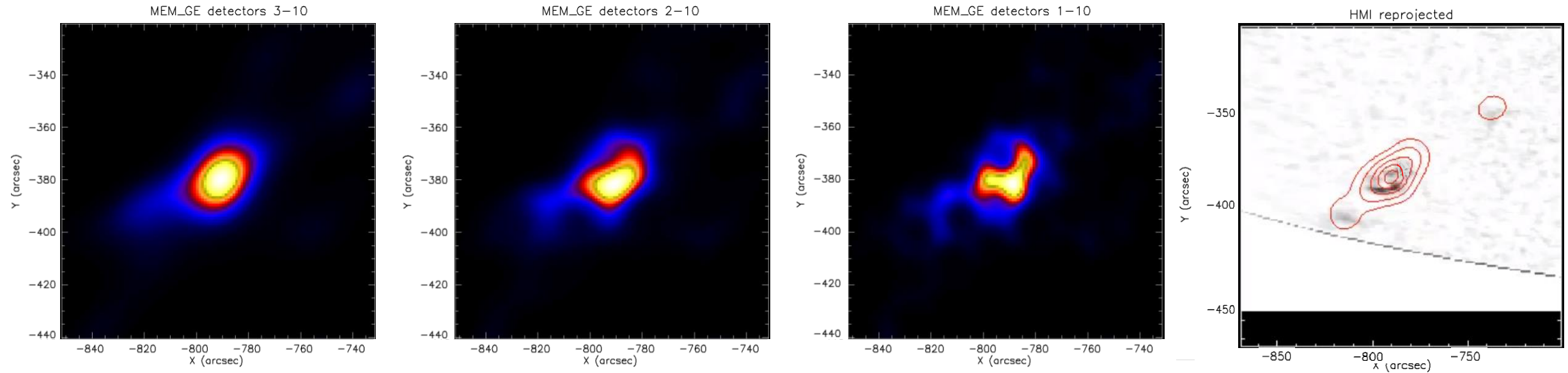
Energy Range: 15 – 25 keV



Test imaging – January 6, 2023

Time_range = 00:55:00 – 00:57:00 UT

Energy Range = 22 – 28 keV



Total flux – Measured slit

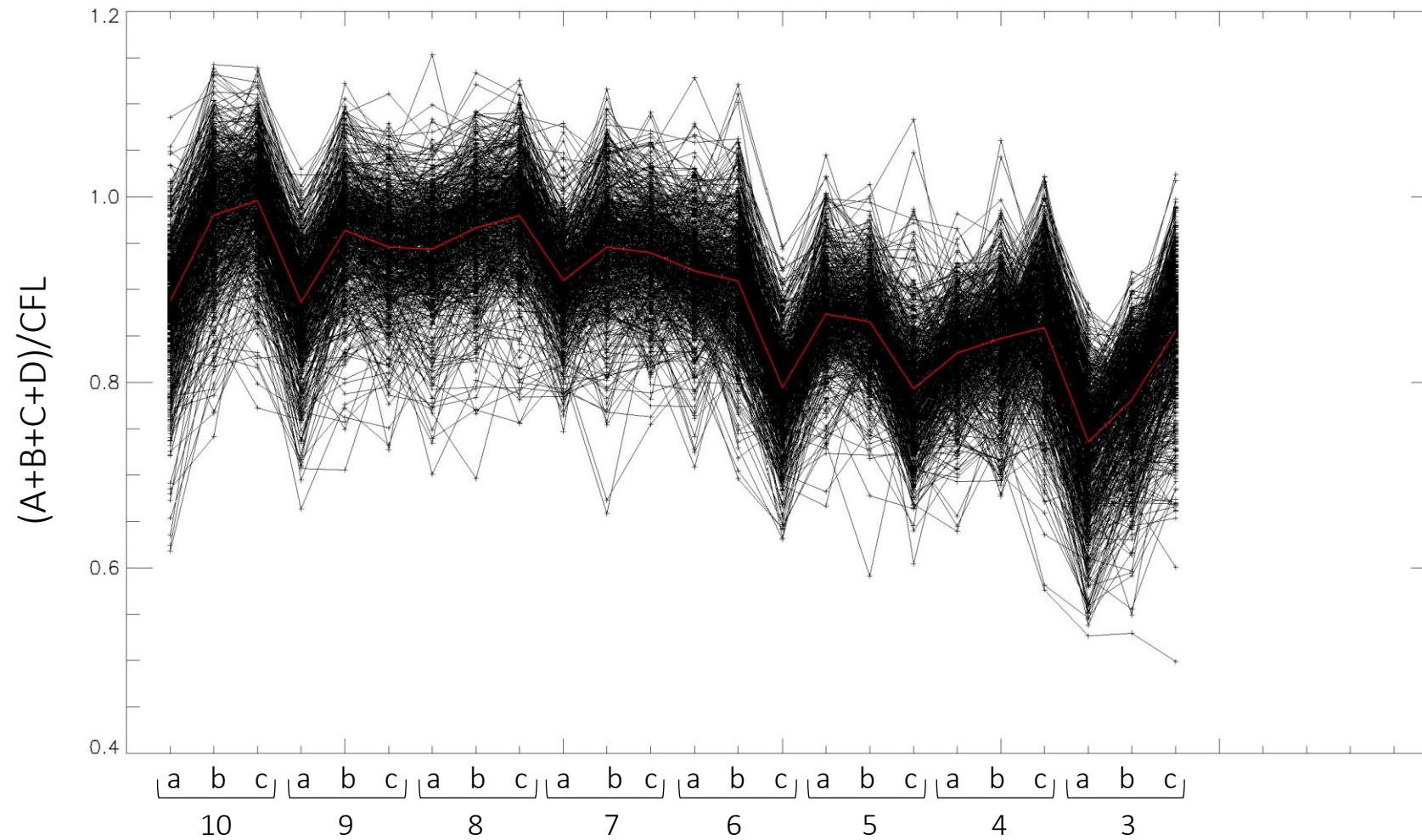


Figure: ratio between the total flux recorded by detectors from 3 to 10 and the flux recorded by CFL, for 700 events.

Total flux – Measured slit

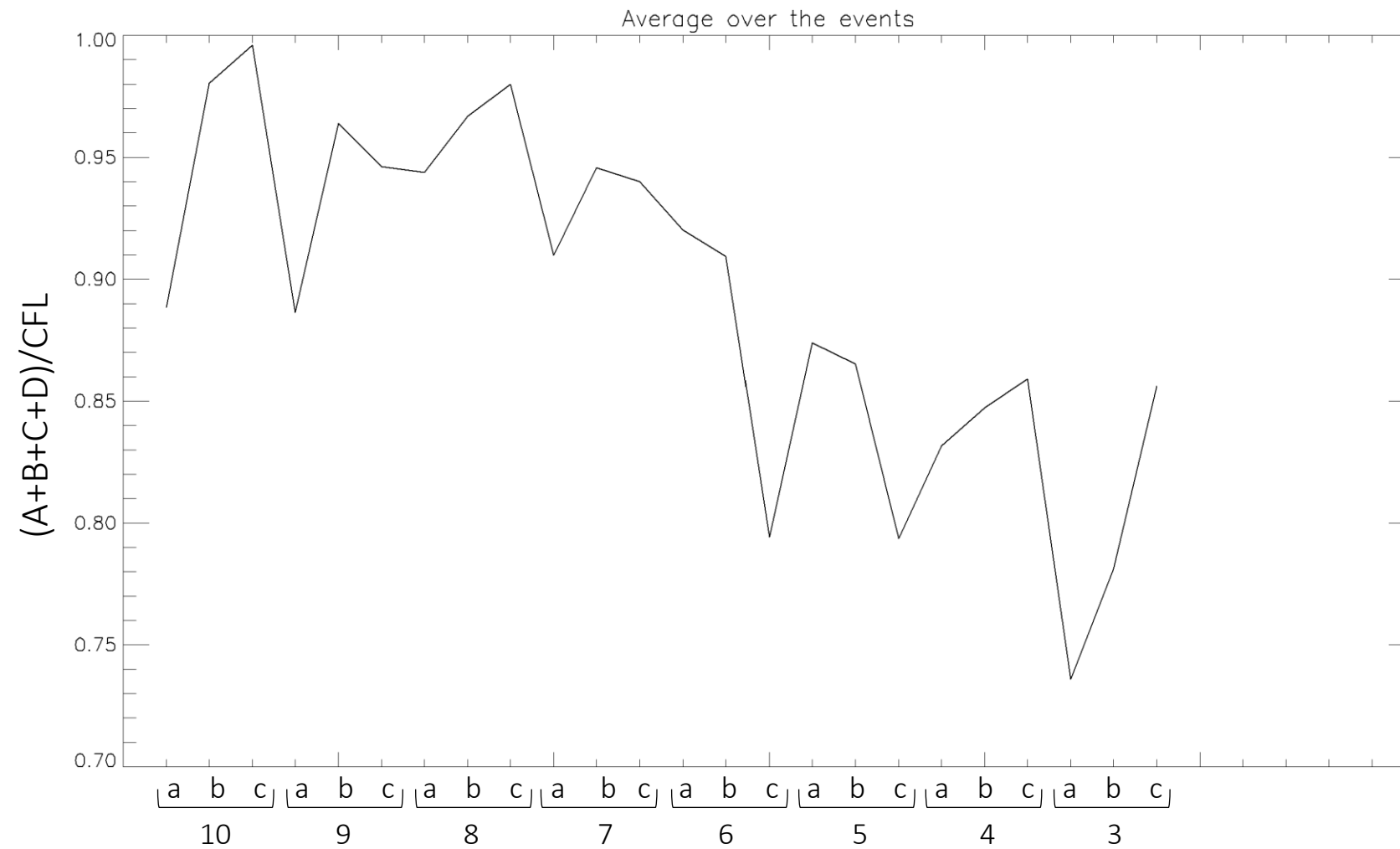


Figure: average of the ratio between the total flux recorded by detectors from 3 to 10 and the flux recorded by CFL, for 700 events.

Total flux – Measured slit

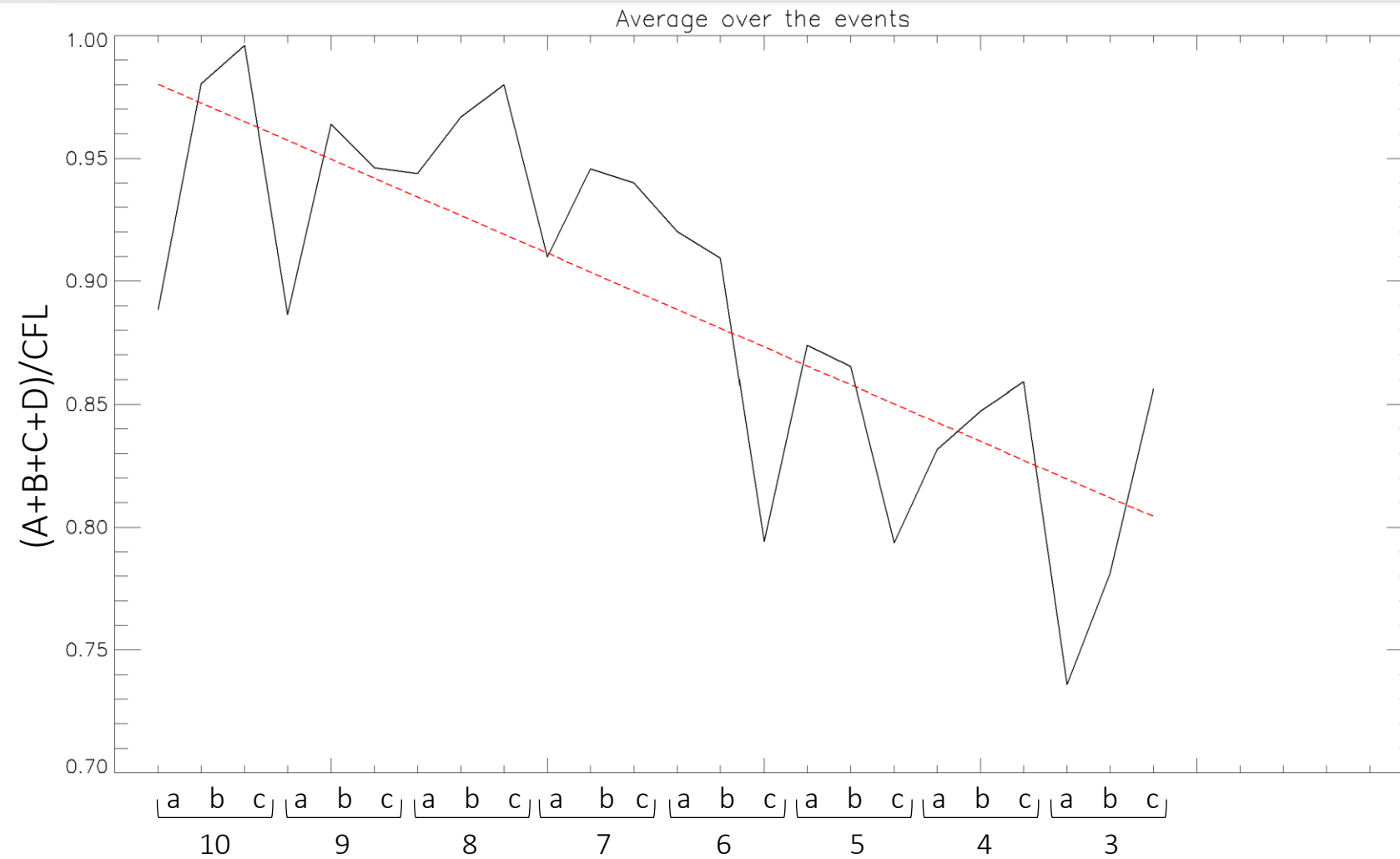


Figure: average of the ratio between the total flux recorded by detectors from 3 to 10 and the flux recorded by CFL, for 700 events.

Total flux – Effective slit

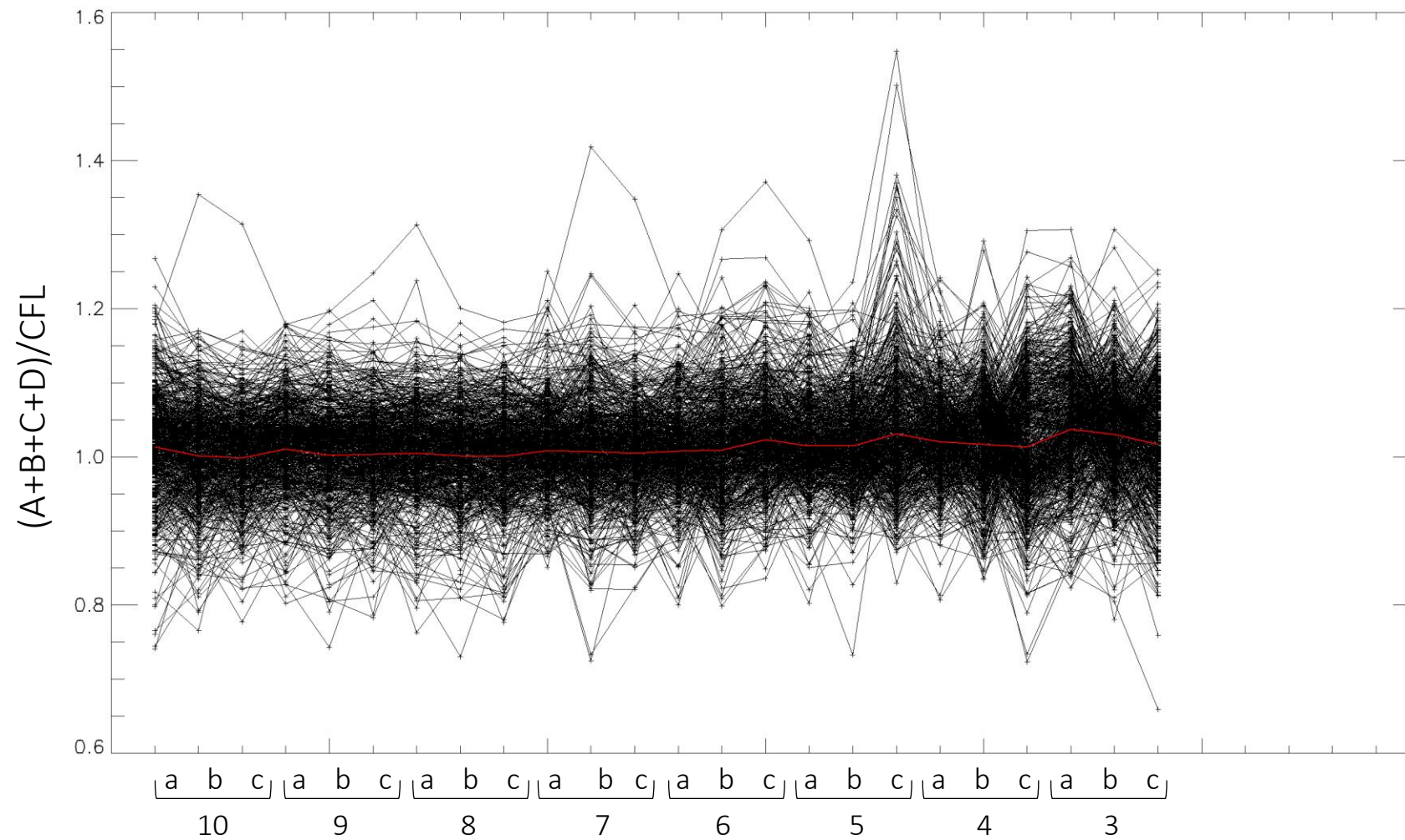


Figure: ratio between the total flux recorded by detectors from 3 to 10 and the flux recorded by CFL.

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MULTISCALE CLEAN

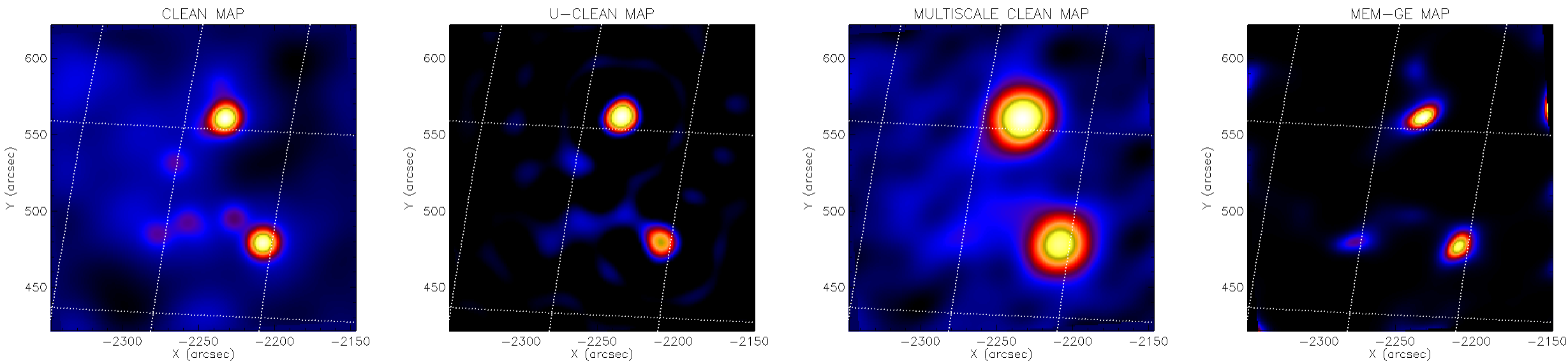


Figure: March 31, 2022 event; energy range: 25 – 50 keV. From left to right, reconstruction provided by CLEAN, U-CLEAN, MULTISCALE CLEAN and MEM_GE, respectively.

	CLEAN	U-CLEAN	MULTISCALE CLEAN	MEM-GE
Time elapsed (s)	44.066	14.904	10.482	27.454
χ^2	23.73	7.24	6.14	4.21

MULTISCALE CLEAN

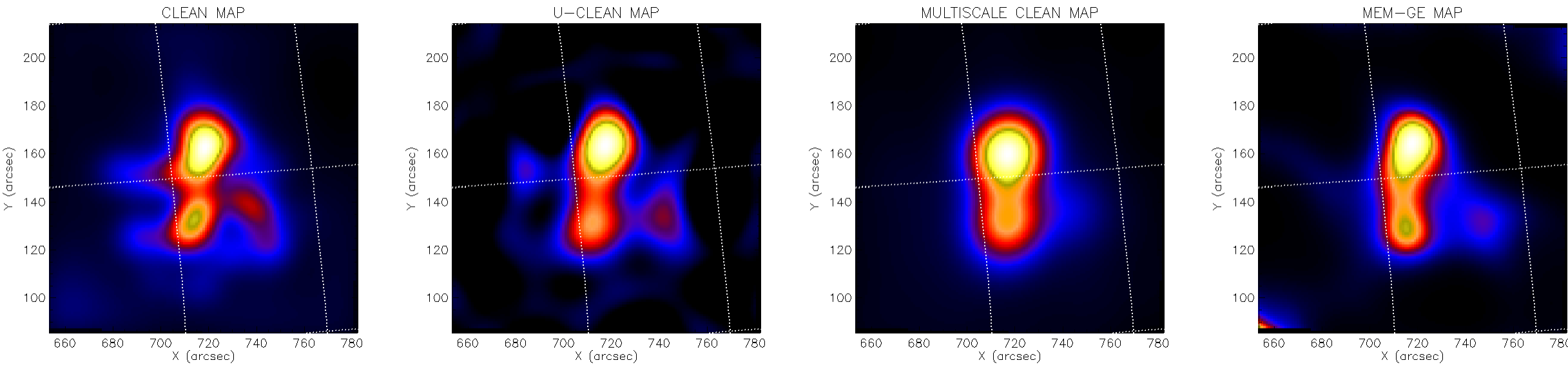


Figure: November 11, 2022 event; energy range: 6 – 10 keV. From left to right, reconstruction provided by CLEAN, U-CLEAN, MULTISCALE CLEAN and MEM_GE, respectively.

	CLEAN	U-CLEAN	MULTISCALE CLEAN	MEM-GE
Time elapsed (s)	38.440	4.799	18.672	6.342
χ^2	6.94	2.14	5.45	1.39

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From photon to electron visibilities

Bremsstrahlung equation for visibilities:

$$V(u, v; \epsilon) = \int_{\epsilon}^{\infty} W(u, v; E) Q(\epsilon, E) dE \quad (2)$$

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Photon visibilities

	ε_1	ε_2	ε_N
(u_1, v_1)	$V_{1,1}$	$V_{1,2}$	$V_{1,N}$
(u_2, v_2)	$V_{2,1}$	$V_{2,2}$	$V_{2,N}$
\vdots	\vdots	\vdots	\ddots	\vdots
(u_{N_V}, v_{N_V})	$V_{N_V,1}$	$V_{N_V,2}$	$V_{N_V,N}$

From photon to electron visibilities

Bremsstrahlung equation for visibilities:

$$V(u, v; \epsilon) = \int_{\epsilon}^{\infty} W(u, v; E) Q(\epsilon, E) dE \tag{2}$$

Spectral inversion via regularized inversion technique (Tikhonov)

Photon visibilities

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(u_1, v_1)	$V_{1,1}$	$V_{1,2}$	$V_{1,N}$
(u_2, v_2)	$V_{2,1}$	$V_{2,2}$	$V_{2,N}$
⋮	⋮	⋮	⋮	⋮
(u_{N_V}, v_{N_V})	$V_{N_V,1}$	$V_{N_V,2}$	$V_{N_V,N}$



Electron visibilities

	E_1	E_2	E_M
(u_1, v_1)	$W_{1,1}$	$W_{1,2}$	$W_{1,M}$
(u_2, v_2)				
⋮	⋮	⋮	⋮	⋮
(u_{N_V}, v_{N_V})				

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(u_{N_V}, v_{N_V})	$V_{N_V,1}$	$V_{N_V,2}$	$V_{N_V,N}$

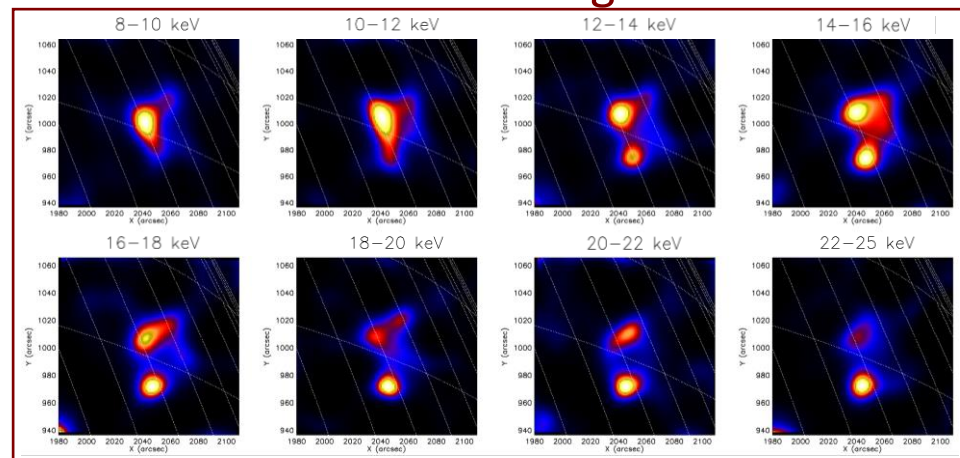


Electron visibilities

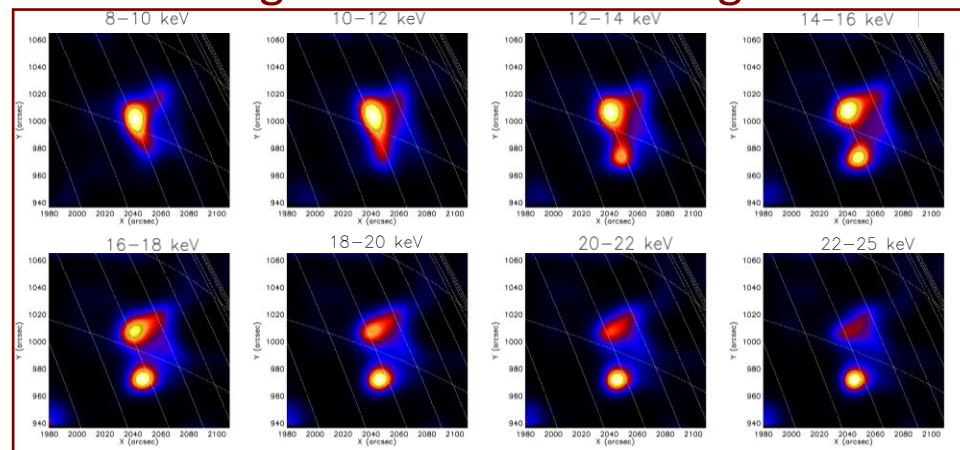
	E_1	E_2	E_M
(u_1, v_1)	$W_{1,1}$	$W_{1,2}$	$W_{1,M}$
(u_2, v_2)	$W_{2,1}$	$W_{2,2}$	$W_{2,M}$
⋮	⋮	⋮	⋮	⋮
(u_{N_V}, v_{N_V})	$W_{N_V,1}$	$W_{N_V,2}$	$W_{N_V,M}$

Products

Photon images



Regularized Photon images



Electron flux images

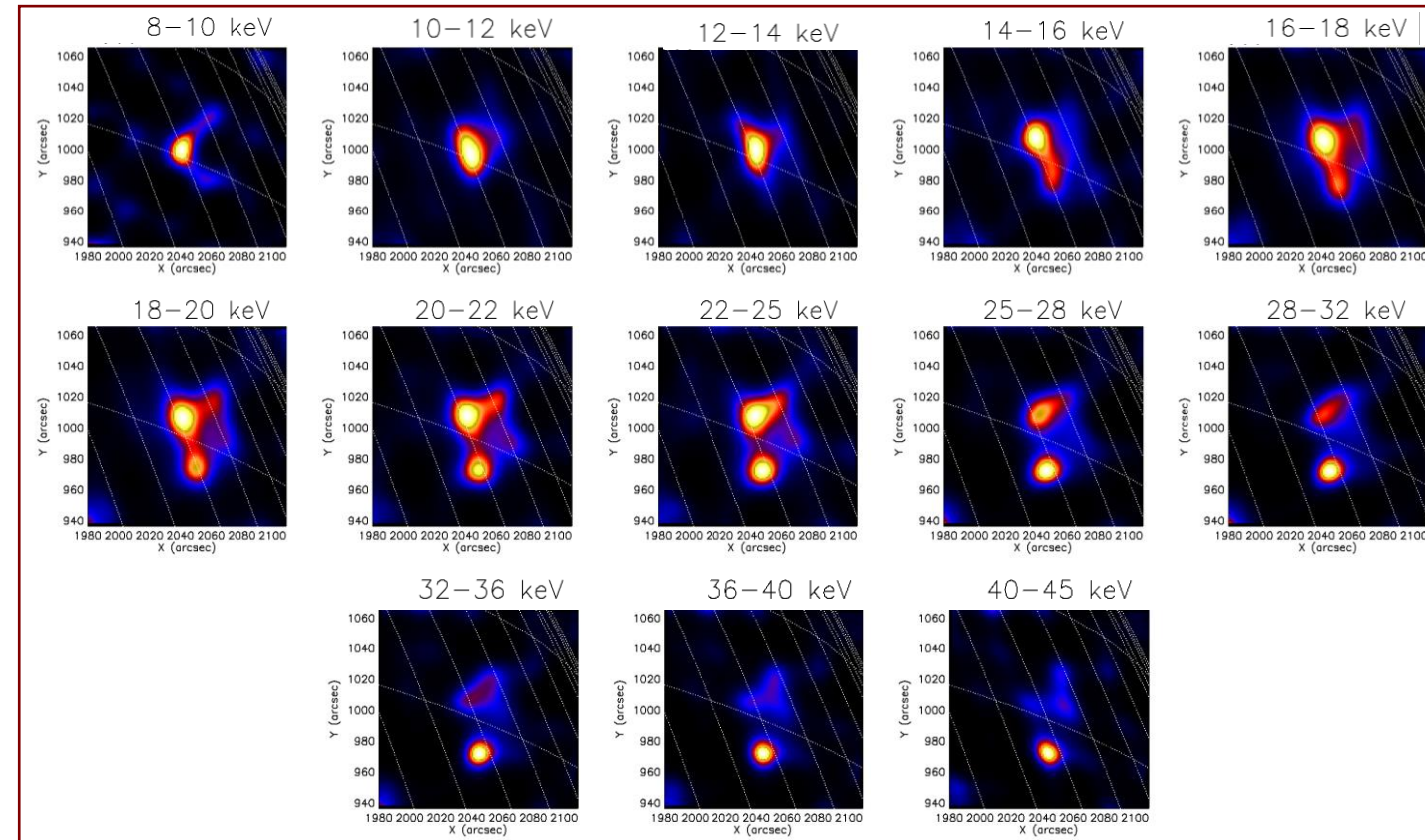


Figure: September 29, 2022 event. Photon images (*top left panels*) compared with the regularized photon maps (*bottom left panels*) in the same energy intervals, and electron flux images corresponding to the regularized electron visibilities (*right panels*) for the energy intervals shown. The maps are produced using the MEM-GE algorithm.

Products

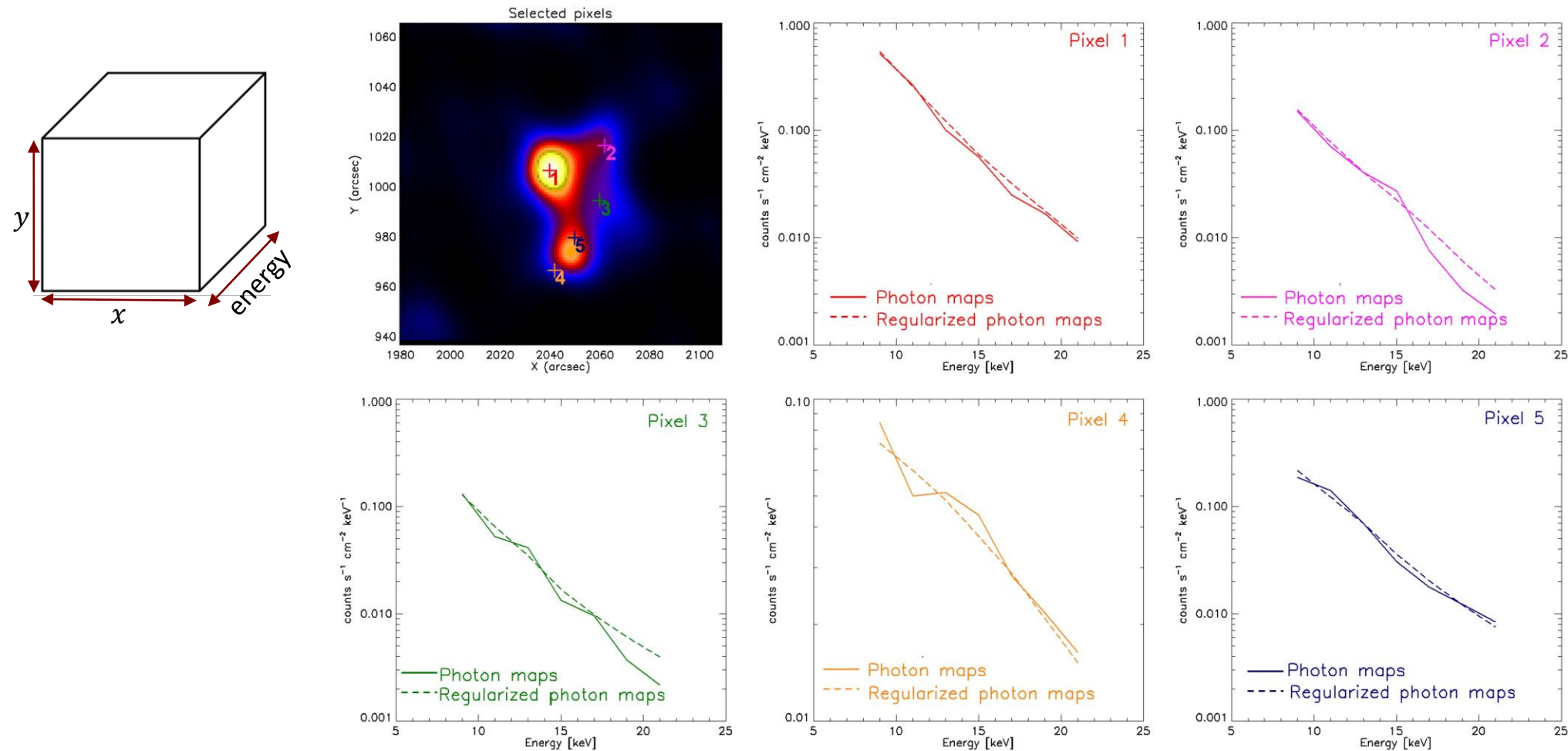


Figure: Pixel-wise spectrum obtained from photon maps and regularized photon maps. *Top left panel:* selected pixels are indicated with colored crosses. The other panels show the pixel-wise spectrum obtained from photon maps (*solid line*) and regularized photon maps (*dotted line*). The pixels selected in the top left panel and their respective spectra are indicated with the same colour. Plots are logarithmic scaled on the y-axis.

Validation

Event	OSPEX	electron maps	photon maps	regularized photon maps
May 08, 2021	$\gamma = 5.25$	$\delta = 4.53$	$\gamma = 4.94$	$\gamma = 5.50$
August 26, 2021	$\gamma = 5.47$	$\delta = 4.59$	$\gamma = 5.27$	$\gamma = 5.57$
January 20, 2022	$\gamma = 6.35$	$\delta = 4.91$	$\gamma = 6.25$	$\gamma = 6.36$
August 28, 2022	$\gamma = 6.94$	$\delta = 4.97$	$\gamma = 6.88$	$\gamma = 6.81$
September 29, 2022	$\gamma = 4.49$	$\delta = 3.68$	$\gamma = 4.24$	$\gamma = 4.42$

Table: Global spectral indices provided by OSPEX, electron maps, photon maps, and regularized photon maps.

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STIX vs RHESSI

	STIX	RHESSI
Distance from the Sun	Variable	Fixed
Energy sampling	Non-uniform	Uniform
Gaps	provides its set of visibility values at all count energies → no (u, v) point gaps	gaps due to insufficient signal-to-noise as the visibility value in question → different energy bins have different number of samples

Table: Differences between STIX and RHESSI inversion software.

STIX vs RHESSI

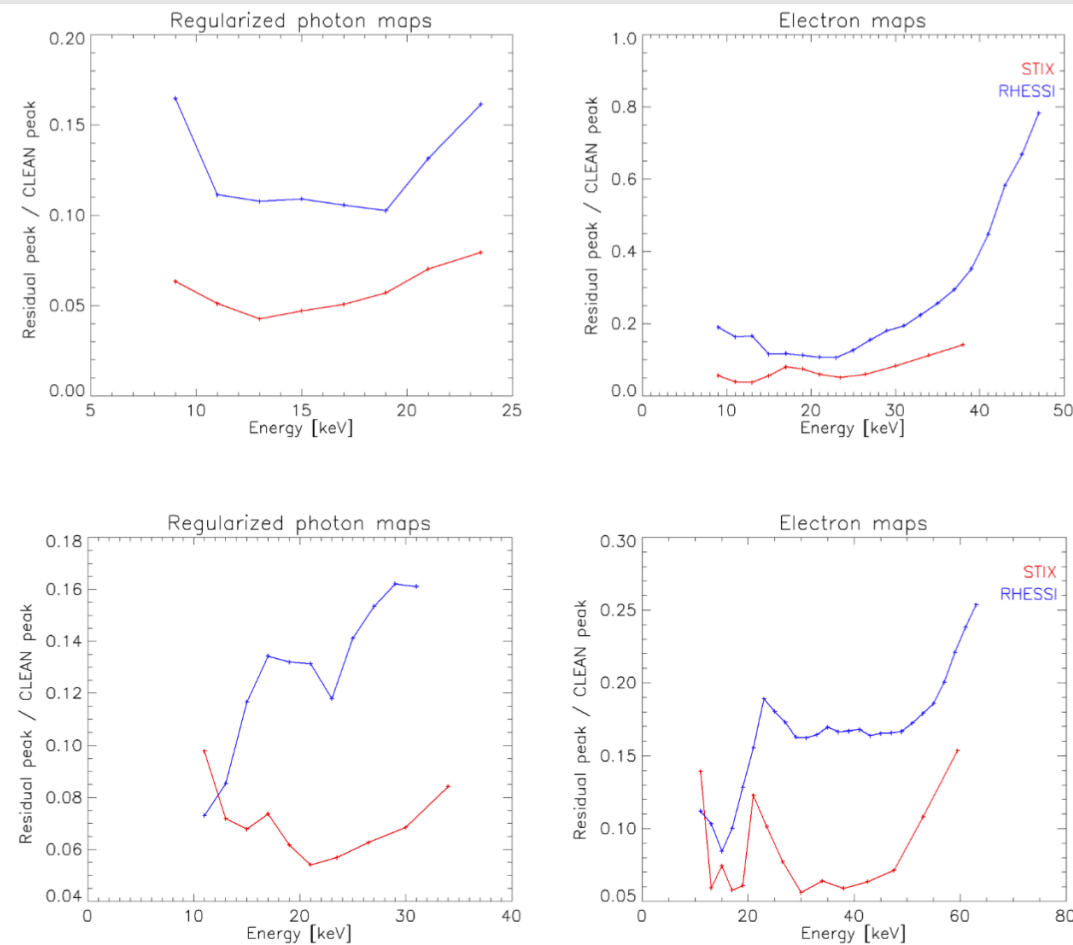


Figure: Ratio between the maximum of the residual map and the maximum of the Clean map at different energies. Red: STIX; blue: RHESSI. *Top row:* Comparison between January 11, 2023 event (STIX) and December 02, 2003 event (RHESSI). *Bottom row:* Comparison between November 11, 2022 event (STIX) and February 20, 2002 event (RHESSI)

Future works

Calibration

- ☐ Effective slit as a function of the energy;
- ☐ Apply the same strategy also for grids 1 and 2.

Imaging methods

- ☐ Test multiscale-Clean;
- ☐ Compare different methods;
- ☐ Error maps.

Electron maps

- ☐ Analyze the electron transport effects to obtain:
 - the average density along the line of sight;
 - number spectrum of accelerated electrons.



THANK YOU FOR THE ATTENTION!

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Università di Genova
DIMA | Dipartimento di Matematica
MIDA group



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