

Topic: Rationalizing complex denominators**Question:** Use the conjugate method to simplify the expression.

$$\frac{\sqrt{-3}\sqrt{-3} - 2i^3}{i + 3}$$

Answer choices:

A $\frac{7}{10} + \frac{9i}{10}$

B $-\frac{7}{10} + \frac{9i}{10}$

C $\frac{7}{10} - \frac{9i}{10}$

D $-\frac{7}{10} - \frac{9i}{10}$



Solution: B

Remember that

$$i = \sqrt{-1}$$

and

$$i^2 = -1$$

First, we'll rewrite the numerator using $\sqrt{-3} = \sqrt{3(-1)} = \sqrt{3}\sqrt{-1} = \sqrt{3}(i)$ and $i^2 = -1$.

$$\frac{\sqrt{-3}\sqrt{-3} - 2i^3}{i + 3}$$

$$\frac{\sqrt{3}(i) \cdot \sqrt{3}i - 2i^3}{i + 3}$$

$$\frac{(\sqrt{3} \cdot \sqrt{3})(i^2) - 2i^3}{i + 3}$$

$$\frac{3(-1) - 2i^3}{i + 3}$$

$$\frac{-3 - 2i^3}{i + 3}$$

We can use the conjugate method to get the imaginary number i out of the denominator.

$$\frac{-3 - 2i^3}{i + 3} \cdot \frac{3 - i}{3 - i}$$



$$\frac{(-3 - 2i^3)(3 - i)}{(i + 3)(3 - i)}$$

Now that we have a binomial multiplication problem, we need to make sure that (in the numerator and denominator separately) we multiply the first terms, outer terms, inner terms, and last terms.

$$\frac{-9 + 3i - 6i^3 + 2i^4}{3i - i^2 + 9 - 3i}$$

$$\frac{2i^4 - 6i^3 + 3i - 9}{-i^2 + 9}$$

Replacing i^2 with -1 , we get

$$\frac{2(-1)(-1) - 6(-1)i + 3i - 9}{-(-1) + 9}$$

$$\frac{2 + 6i + 3i - 9}{10}$$

$$\frac{9i - 7}{10}$$

Split the fraction.

$$\frac{9i}{10} - \frac{7}{10}$$

$$-\frac{7}{10} + \frac{9i}{10}$$



Topic: Rationalizing complex denominators**Question:** Use the conjugate method to simplify the expression.

$$\frac{3i - i^2}{2i^2 - i^3}$$

Answer choices:

A $\frac{1}{5} - \frac{7}{5}i$

B $-\frac{2}{3} - \frac{10}{3}i$

C $\frac{2}{3} - \frac{10}{3}i$

D $-10 + 3i$



Solution: A

Remember that

$$i = \sqrt{-1}$$

and

$$i^2 = -1$$

First, we'll rewrite the expression using $i^3 = i^2i$ and $i^2 = -1$.

$$\frac{3i - i^2}{2i^2 - i^3}$$

$$\frac{3i - i^2}{2i^2 - i^2i}$$

$$\frac{3i - (-1)}{2(-1) - (-1)i}$$

$$\frac{3i + 1}{-2 + i}$$

Now we can use the conjugate method to get the imaginary number i out of the denominator.

$$\frac{3i + 1}{-2 + i} \cdot \frac{-2 - i}{-2 - i}$$

$$\frac{(3i + 1)(-2 - i)}{(-2 + i)(-2 - i)}$$



Now that we have a binomial multiplication problem, we need to make sure that (in the numerator and denominator separately) we multiply the first terms, outer terms, inner terms, and last terms.

$$\frac{-6i - 3i^2 - 2 - i}{4 + 2i - 2i - i^2}$$

$$\frac{-3i^2 - 7i - 2}{4 - i^2}$$

Replacing i^2 with -1 , we get

$$\frac{-3(-1) - 7i - 2}{4 - (-1)}$$

$$\frac{3 - 7i - 2}{4 + 1}$$

$$\frac{1 - 7i}{5}$$

$$\frac{1}{5} - \frac{7i}{5}$$

$$\frac{1}{5} - \frac{7}{5}i$$



Topic: Rationalizing complex denominators

Question: Use the conjugate method to simplify the expression.

$$\frac{4 + 4i}{5 - 3i}$$

Answer choices:

A $\frac{4 + 16i}{17}$

B $\frac{1 + 4i}{2}$

C $\frac{16 + 16i}{17}$

D $\frac{1 + 4i}{4}$



Solution: A

The complex conjugate of the denominator of

$$\frac{4 + 4i}{5 - 3i}$$

is $5 + 3i$, so we multiply the numerator and denominator by that and simplify.

$$\frac{4 + 4i}{5 - 3i} \cdot \frac{5 + 3i}{5 + 3i}$$

$$\frac{20 + 12i + 20i + 12i^2}{25 + 15i - 15i - 9i^2}$$

$$\frac{20 + 32i - 12}{25 + 9}$$

$$\frac{8 + 32i}{34}$$

$$\frac{4 + 16i}{17}$$

