

**Topic:** Coefficients in quadratics**Question:** Factor the quadratic.

$$5x^2 - 3x - 2$$

**Answer choices:**

- A  $(5x + 2)(x + 1)$
- B  $(5x - 2)(x + 1)$
- C  $(5x + 2)(x - 1)$
- D  $(5x - 2)(x - 1)$



**Solution: C**

The only factors of 5 are 5 and 1, so we know we'll have

$$(5x \quad \quad)(x \quad \quad)$$

The only factors of 2 are 2 and 1, which means we'll have one of the following:

$$(5x \quad 1)(x \quad 2) \quad \quad \text{or} \quad \quad (5x \quad 2)(x \quad 1)$$

If we do the factoring the first way, we'll need to combine  $10x$  and  $x$  to get the middle term,  $-3x$ . There's no way we can do that, even if we make one or both of them negative. If we do the factoring the second way, we'll need to combine  $5x$  and  $2x$  to get  $-3x$ . If we make the  $5x$  negative and keep the  $2x$  positive, then we get  $-5x + 2x = -3x$ . Therefore, we have to use  $-1$  as the constant term in the second factor (because  $-5x = 5x \cdot -1$ ), and 2 as the constant term in the first factor (because  $2x = 2 \cdot x$ ), so we get

$$(5x + 2)(x - 1)$$



**Topic:** Coefficients in quadratics**Question:** Factor the quadratic.

$$6x^2 - 2x - 4$$

**Answer choices:**

- A  $2(3x + 2)(x + 1)$
- B  $2(3x - 2)(x - 1)$
- C  $2(3x - 2)(x + 1)$
- D  $2(3x + 2)(x - 1)$



**Solution: D**

First, we'll factor out a 2, because 2 is the factor that's common to all three terms.

$$6x^2 - 2x - 4$$

$$2(3x^2 - x - 2)$$

The only factors of 3 are 3 and 1, so we know we'll have

$$2(3x \quad )(x \quad )$$

The only factors of 2 are 2 and 1, which means we'll have one of the following:

$$2(3x - 1)(x - 2) \quad \text{or} \quad 2(3x - 2)(x - 1)$$

If we do the factoring the first way, we'll need to combine  $6x$  and  $x$  to get the middle term,  $-x$ . There's no way we can do that, even if we make one or both of them negative. If we do the factoring the second way, we'll need to combine  $3x$  and  $2x$  to get  $-x$ . If we make the  $3x$  negative and keep the  $2x$  positive, then we get  $-3x + 2x = -x$ . Therefore, we have to use  $-1$  as the constant term in the second factor in parentheses (because  $-3x = 3x \cdot -1$ ), and 2 as the constant term in the first factor in parentheses (because  $2x = 2 \cdot x$ ), so we get

$$2(3x + 2)(x - 1)$$



**Topic:** Coefficients in quadratics

**Question:** Factor the cubic polynomial, remembering to look first for a greatest common factor.

$$6x^3 + 11x^2 - 2x$$

**Answer choices:**

A  $x(6x + 1)(x - 2)$

B  $x(6x - 1)(x - 2)$

C  $x(6x - 1)(x + 2)$

D  $(6x + 1)(x + 2)$



**Solution: C**

Note that  $6x^3 + 11x^2 - 2x$  is a trinomial (a polynomial with three nonzero terms) but not a quadratic polynomial (because it has an  $x^3$  term).

However, we can factor out an  $x$ , because  $x$  is the factor that's common to all three terms.

$$6x^3 + 11x^2 - 2x$$

$$x(6x^2 + 11x - 2)$$

The only pairs of factors of 6 are (6,1) and (3,2), so we'll have one of these:

$$x(6x \quad)(x \quad) \quad \text{or} \quad x(3x \quad)(2x \quad)$$

The only factors of 2 are 2 and 1, which means we'll have one of the following four possibilities:

$$x(6x \quad 2)(x \quad 1)$$

$$x(3x \quad 2)(2x \quad 1)$$

$$x(6x \quad 1)(x \quad 2)$$

$$x(3x \quad 1)(2x \quad 2)$$

If we do the factoring as  $x(6x \quad 2)(x \quad 1)$ , we'll need to combine  $6x$  and  $2x$  to get the middle term,  $11x$ . There's no way we can do that, even if we make one or both of them negative.

If we do the factoring as  $x(3x \quad 2)(2x \quad 1)$ , we'll need to combine  $3x$  and  $4x$  to get  $11x$ . There's no way we can do that, even if we make one or both of them negative.



If we do the factoring as  $x(3x - 1)(2x - 2)$ , we'll need to combine  $6x$  and  $2x$  to get  $11x$ . There's no way we can do that, even if we make one or both of them negative.

Finally, if we do the factoring as  $x(6x - 1)(x + 2)$ , we'll need to combine  $12x$  and  $x$  to get  $11x$ , which we can do by making  $12x$  positive and  $x$  negative. Therefore, we have to use 2 as the constant term in the second factor in parentheses (because  $12x = 6x \cdot 2$ ), and  $-1$  as the constant term in the first factor in parentheses (because  $-x = -1 \cdot x$ ), so we get

$$x(6x - 1)(x + 2)$$

