Topic: Testing for functions

Question: Does the equation represent a function?

$$2x^2 + 2y^2 = 18$$

Answer choices:

- A Yes, because there are values of x that will give multiple values for y.
- B No, because there are values of x that will give multiple values for y.
- C No, because every value of x will give a unique value for y.
- D Yes, because every value of x will give a unique value for y.



Solution: B

Solve the equation for y.

$$2x^2 + 2y^2 = 18$$

$$x^2 + y^2 = 9$$

$$y^2 = 9 - x^2$$

$$y = \pm \sqrt{9 - x^2}$$

Now that we have the equation in this form, we can find values of x that return multiple y-values. For instance, at x=1,

$$y = \pm \sqrt{9 - 1^2}$$

$$y = \pm \sqrt{8}$$

$$y = \pm 2\sqrt{2}$$

Because the equation takes on the values $y=-2\sqrt{2}$ and $y=2\sqrt{2}$ at the single value x=1, we know the equation doesn't represent a function.



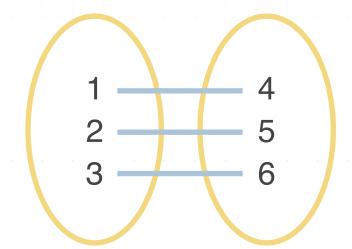
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Question: Which of these could represent a function?

Answer choices:

$$A$$
 (-1, -1), (2,0), (3,1), (-1,2)

- B The relation whose graph consists of the points with coordinates (1,2), (1,3), and (1,4).
- C (-2, -1), (-3,0), (-3, -3), (3,2)



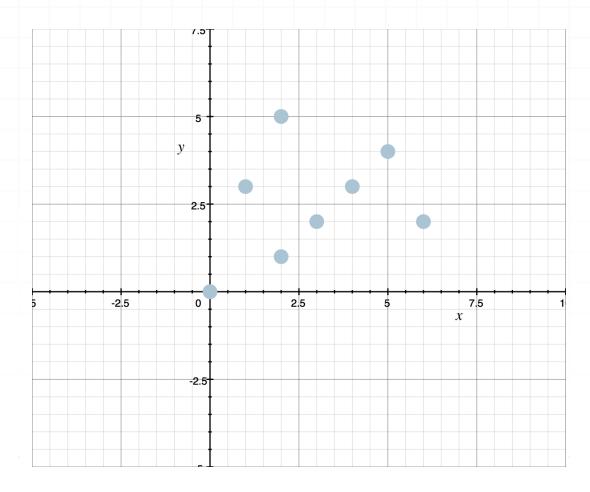
Solution: D

Answer choice D is the only expression that could represent a function, because it's the only answer choice that shows just one y-value for every x -value.



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Question: The graph shows eight points that define a relation between x and y. Identify the pair of points which prove that the relation is not a function.



Answer choices:

- A (1,3) and (4,3)
- B (5,4) and (2,1)
- C (3,2) and (6,2)
- D (2,1) and (2,5)

Solution: D

If one *x*-value gives two different *y*-values, then the relation is not a function.

Answer choice D shows x = 2, y = 1 and x = 2, y = 5. In other words, the same x-value but two different y-values. Therefore, we know that the relation is not a function.

