# **DOUBLEROOT**

## **Truth Tables**

### Laws

# Conjunction: p ∧ q

p	q	<b>p</b> ∧ <b>q</b>
Т	Т	Т
Т	F	F
F	Т	F
F	F	F

### **Double Negation Law**

$$\sim$$
( $\sim$ p)  $\equiv$  p

### **Identity Laws**

p	٧	F	≡	p
p	Λ	T	≡	p

# Disjunction: p V q

р	q	<b>p</b> ∨ <b>q</b>
Т	Т	Т
Т	F	Т
F	Т	Т
F	F	F

# **Idempotent Laws**

$$p \lor p \equiv p$$
$$p \land p \equiv p$$

# Negation: ∼p

р	~p
Т	F
F	Т

### **Annihilation Laws**

$$p \lor T \equiv T$$
$$p \land F \equiv F$$

# Implication: $p \Rightarrow q$

р	q	$\mathbf{p}\Rightarrow\mathbf{q}$
T	T	T
Т	F	F
F	Т	T
F	F	Т

# Commutative Laws



#### Related:

Converse:  $q \Rightarrow p$ Inverse:  $\sim p \Rightarrow \sim q$ Contrapositive:  $\sim q \Rightarrow \sim p$ 

### Associative Laws

$$p \lor (q \lor r) \equiv (p \lor q) \lor r$$
  
 $p \land (q \land r) \equiv (p \land q) \land r$ 

## Biconditional: $p \Leftrightarrow q$

р	q	<b>p</b> ∨ <b>q</b>
Т	Т	T
Т	F	F
F	Т	F
F	F	Т

#### Distributive Laws

$$p \lor (q \land r) \equiv (p \lor q) \land (p \lor r)$$
$$p \land (q \lor r) \equiv (p \land q) \lor (p \land r)$$

# Exclusive Or: $p \oplus q$

р	q	p⊕q
Т	Т	F
Т	F	Т
F	Т	Т
F	F	F

### **Absorption Laws**

$$p \lor (p \land q) \equiv p$$
$$p \land (p \lor q) \equiv p$$

## De Morgan's Laws

$$\sim (p \lor q) \equiv \sim p \land \sim q$$
  
 $\sim (p \land q) \equiv \sim p \lor \sim q$