

QUE 1:  $S_n = \frac{n}{2}(2a + (n-1)d)$

$$340 = \frac{n}{2}(2(7) + (n-1)6)$$

$$680 = n(14 + 6n - 6)$$

$$680 = n(8 + 6n)$$

$$680 = 8n + 6n^2$$

$$6n^2 + 8n - 680 = 0$$

$$-8 \pm \sqrt{8^2 - 4(6)(-680)} \over 2(6)$$

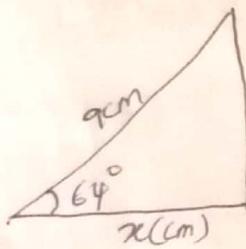
$$-8 \pm \sqrt{64 + 16320} \over 12$$

$$-8 \pm \sqrt{16384} \over 12$$

$$-8 + 128 \over 12 \quad \text{or} \quad -8 - 128 \over 12$$

$$n = 10 \quad \boxed{\text{option B}}$$

QUE 2:



$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\cos 64^\circ = \frac{x}{9}$$

$$x = 3 \cdot 9 \text{ cm} \quad \boxed{\text{option D}}$$

QUE 3:  $\frac{1+i}{1-i}$

$$\frac{1+i}{1-i} \times \frac{1+i}{1+i}$$

$$\frac{1+2i+i^2}{1+2i+2i^2} \Rightarrow \frac{2i}{2} = 0+i$$

10 marks or.

$$r(\cos \theta + i \sin \theta)$$

$$1\left(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2}\right)$$

QUE 4:  $n(Y) = 20$

$$n(S) = 16$$

$$n(h) = 12$$

$$n(S \cup h)^c = 2$$

$$n(S \cap h) = ?$$

$$n(S \cup h) = n(S) + n(h) - n(S \cap h)$$

$$n(S \cup h) = 16 + 12 - n(S \cap h)$$

$$= 28 - n(S \cap h)$$

$$n(S \cup h) + n(S \cup h)^c = n(Y)$$

$$28 - n(S \cap h) + 2 = 20$$

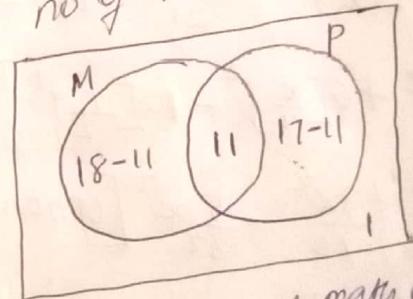
$$30 - n(S \cap h) = 20$$

$$30 - 20 = n(S \cap h)$$

$$10 = n(S \cap h) \quad \boxed{\text{option B}}$$

QUE 5: no of those who passed math = 18  
no of those who passed physics = 17  
no of those who passed both = 11

no of those who failed both = 11



no of those who passed math only = 7  
 $\boxed{\text{option B}}$

QUE 6:  $\frac{4+2i}{5-i}$

$\boxed{\text{option B}}$

$$\frac{4+2i}{5-i} \times \frac{5+i}{5+i}$$

$$\frac{20+4i+2i+2i^2}{25}$$

$$\frac{20+14i+2i^2}{25} \Rightarrow \frac{18+14i}{25}$$

$$\frac{9+14i}{25}$$

$$\text{QUE 7: } (3+2x)^6$$

$$= {}^6C_0 3^6 (2x)^0 + {}^6C_1 3^5 (2x)^1 + {}^6C_2 3^4 (2x)^2 + {}^6C_3 3^3 (2x)^3 \\ + {}^6C_4 3^2 (2x)^4 + {}^6C_5 3^1 (2x)^5 + {}^6C_6 3^0 (2x)^6$$

$$729 + 2916x + 4860x^2 + 4320x^3$$

$\therefore$  the coefficient of  $x^3$  is 4320

$$\text{Alternatively: } \sum {}^nC_r x^{n-r} y^r$$

$${}^6C_3 x^{6-3} y^3$$

$$x^3 = x^3$$

$${}^6C_3 x^3 y^3$$

$${}^6C_3 (3^3)(2x)^3$$

$$20 \times 27 \times 8x^3$$

$$= 4320x^3 \quad [\text{option A}]$$

$$\text{QUE 8: Expand } (2+x)^{-3}$$

$$\left[ 2^{-3} \left[ 1 + \frac{x}{2} \right]^{-3} \right]$$

$$\frac{1}{8} \left[ 1 + \left[ -\frac{3x}{2} \right] + \frac{-3[-3-1]}{2!} \left[ \frac{x}{2} \right]^2 + \frac{(-3)(-4)(-5)}{3!} \left[ \frac{x}{2} \right]^3 \right]$$

$$\frac{1}{8} \left[ 1 - \frac{3x}{2} + 6 \left[ \frac{x}{2} \right]^2 - 10 \left[ \frac{x}{2} \right]^3 \right]$$

$$\frac{1}{8} - \frac{3x}{16} + \frac{3x^2}{16} - \frac{5}{32} x^3 \quad [\text{option B}]$$

$$\text{QUE 9: } \Delta = b^2 - 4ac$$

$$\Delta = (-3)^2 - 4(1)(-10)$$

$$\Delta = 9 + 40$$

$$\Delta = 49$$

Roots of the equation is Real and distinct because it positive and also a perfect square.

QUE 10:  $5x^2 - 7x - 3 = 0$   
Form the equation whose roots are  $\alpha = \frac{1}{2}$  and  $\beta = \frac{1}{5}$

$$\alpha + \beta = -\frac{b}{a} = \frac{7}{5}$$

$$\alpha\beta = \frac{c}{a} = -\frac{3}{5}$$

Equation from roots =  $x^2 - [\text{sum of root}]x + \text{product}$

$$\frac{\alpha-1}{2} + \frac{\beta-1}{5}$$

$$\frac{\beta}{2}(\alpha-1) + \frac{\alpha}{5}(\beta-1)$$

$$\frac{2\beta}{5} - 2 + \beta^2 \alpha - \beta$$

$$\frac{2\beta}{5} + \beta^2 \alpha - 2\beta$$

$$4\beta[2+\beta] - [2+4\beta]$$

$$\frac{2\beta}{5} - \frac{3}{5} \left[ \frac{7}{5} \right] - \frac{1}{5}$$

$$-\frac{3}{5} \left[ \frac{7}{5} \right] - \frac{1}{5}$$

$$\frac{4\beta-1}{\beta} \times \frac{4\beta-1}{2}$$

$$\frac{2\beta^2 - 4\beta - 4\beta + 1}{2\beta}$$

$$\frac{4\beta^2 - 2\beta + 1}{2\beta}$$

$$\frac{(4\beta)^2 - 2\beta + 1}{2\beta}$$

$$\left[ \frac{-3}{5} \right]^2 - 2 \left( -\frac{3}{5} \right) + 1$$

$$-\frac{3}{5}$$

$$= -\frac{64}{25}$$

Equation of the root equals  
 $x^2 - [56/15]x + \frac{-64}{15} = 0$

$$15x^2 - 56x - 64 = 0$$

[option B]

QUE 11: Common ratio = 2

5th term:  $a r^4 = a + 45$   
 $a r^4 = a + 45$

Where  $r = 2$

$$a \cdot 2^4 = a + 45$$

$$16a = a + 45$$

$$15a = 45$$

$$a = 3$$

5th term  $= a r^4$   
 $= 3 \times 2^4$

$$= 3 \times 16 = 48$$
 [Option D]

QUE 12: Harmonic Sequence can be defined as the reciprocal of the arithmetic sequence with numbers other than zero. Therefore, Harmonic sequence can be zero. [Option D]

QUE 13: 2, 4, 6, 8, 10, 12 is an example of Arithmetic progression. The common difference shows this [Option B]

QUE 14: Series obtained by adding term of Arithmetic sequence is called Arithmetic prog. While that of division is Geometric prog [Option C]

QUE 15:  $6, \frac{1}{3}, \frac{1}{3^2}, \dots$

$$a = 1$$

$$r = \frac{1}{3}$$

$$S_n = \frac{a}{1-r}$$

$$= \frac{1}{\frac{2}{3}}$$

$$= \frac{3}{2}$$
 [Option B]

QUE 16: Arithmetic Mean  $\bar{x}$  between 2 and 3

$$\frac{a+b}{2} = \frac{2+3}{2} = \frac{5}{2}$$

Harmonic mean between 2 and 3

$$\frac{2ab}{a+b} = \frac{2(2)(3)}{2+3} = \frac{12}{5}$$

$$\bar{x} + H = \frac{\frac{12}{5}}{\frac{5}{2}} + \frac{5}{2}$$

$$= \frac{24+25}{10} = \frac{49}{10}$$

$$[Option B]$$

QUE 17: Arithmetic mean between 9 & 11

$$\frac{a+b}{2} = \frac{9+11}{2}$$

$$\bar{x} = 10$$
 [Option A]

QUE 18: Expand  $a^2 + b^2$

$$[a+b]^2 = a^2 + b^2 + 2ab$$

$$[a+b]^2 - 2ab = a^2 + b^2$$

$$[Option E] (a+b)(a-b)$$

QUE 19:  $Z_1 = 2+i$

$$Z_2 = 1+3i$$

$$[Z_1 - Z_2] = 2-1 + 3i - 1i = 1-2i$$

$$Z_1 - Z_2 = 1-2i$$

QUE 20:  $|Z_1 + Z_2| =$

$$Z_1 + Z_2 = 3+4i$$

$$|Z_1 + Z_2| = \sqrt{3^2 + 4^2}$$

$$|Z_1 + Z_2| = 5$$

$$|Z_1| = \sqrt{2^2 + 1^2}$$

$$|Z_1| = \sqrt{5}$$

$$|Z_2| = \sqrt{1^2 + 3^2}$$

$$|Z_2| = \sqrt{10}$$

$$|Z_1| + |Z_2| = \sqrt{5} + \sqrt{10}$$

$$= 5.4$$

$$\therefore |Z_1 + Z_2| \leq |Z_1| + |Z_2|$$

QUE 21: Polar form of complex number

$$r(\cos\theta + i\sin\theta)$$
 [Option C]

QUE 22: Arithmetic mean between  $x-3$  &  $x+5$

$$\frac{a+b}{2} = \frac{x-3+x+5}{2} = \frac{2x+2}{2}$$

$$\bar{x} = x+1$$

$$[Option C]$$

QUE 23: 2, 6, 18

$$a = 2$$

$$r = 3$$

$$S_{n_5} = a \left[ r^{n-1} - 1 \right] \quad \text{where } n \text{ is 5}$$

$$S_{n_5} = 2 \left[ 3^5 - 1 \right] / (3 - 1)$$

$$S_{n_5} = 2 \left[ 243 \right]$$

$$S_{n_5} = 242 \quad [\text{option C}]$$

QUE 24:  $[3+2x]^6$  Find the constant term

$${}^7 C_r x^{n-r} y^r$$

$$6 C_0 3^6 (2x)^0$$

$$= 729 \quad [\text{option A}]$$

QUE 25:  $U = \{1, 3, 3, 4\}$

$$P = \{3, 3\}$$

$$Q = \{3, 4\}$$

What is  $\{P \cap Q\}^c$

$$\{P \cap Q\}^c = 2$$

$$\{P \cap Q\}^c = \{1, 3, 4\} \quad [\text{option B}]$$

QUE 26: length = 8cm

radius = 6cm

$$L = r\theta$$

$$8 = 6\theta$$

$$\theta = 4/3$$

$$\text{Area} = \frac{r^2 \theta}{2}$$

$$= \frac{36}{2} \times \frac{4}{3}$$

$$= 24 \text{ cm}^2 \quad [\text{option C}]$$

QUE 27:  $\tan \alpha = \frac{4}{5}$   $\tan \beta = \frac{4}{19}$   $\tan \gamma = \frac{2}{5}$

value of  $\tan(\alpha + \beta + \gamma)$

$$\tan(\alpha + \beta + \gamma) = \frac{\tan \alpha + \tan \beta + \tan \gamma}{1 - \tan \alpha \tan \beta \tan \gamma}$$

$$\begin{aligned} \tan(\beta + \gamma) &= \frac{\tan \beta + \tan \gamma}{1 - \tan \beta \tan \gamma} \\ &= \frac{\frac{4}{19} + \frac{2}{5}}{1 - \frac{4}{19} \left[ \frac{2}{5} \right]} \end{aligned}$$

$$= \frac{58}{95} \times \frac{95}{87} = \frac{58}{87}$$

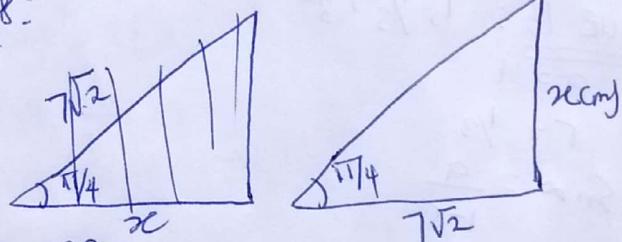
$$\tan(\alpha + \beta + \gamma) = \frac{\tan \alpha + [\tan \beta + \tan \gamma]}{1 - \tan \alpha \tan \beta \tan \gamma}$$

$$= \frac{1}{5} + \frac{58}{87} / 1 - \frac{1}{5} \left[ \frac{58}{87} \right]$$

$$= \frac{13}{15} \times \frac{15}{13} = 1$$

$$\therefore \tan(\alpha + \beta + \gamma) = 1 \quad [\text{option D}]$$

QUE 28:



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 45 = \frac{2}{7\sqrt{2}}$$

$$x = 7\sqrt{2} \text{ cm} \quad [\text{option B}]$$

QUE 29: Find the 4th term of an AP whose first term is 2 and the common difference is 0.5.

$$T_{n=4} = a + 3d$$

$$= 2 + 3[0.5]$$

$$= 3.5 \quad [\text{option C}]$$

QUE 30: Length = ?

$$\theta = \frac{150 \times \pi}{180} = \frac{5\pi}{6}$$

$$r = 12 \text{ cm}$$

$$L = r\theta$$

$$L = 12 \times \frac{5\pi}{6}$$

$$L = 10\pi \text{ cm} \quad [\text{option C}]$$

QUE 31:  $A = \{a, b, c\}$

$$B = \{a, b, c, d, e\}$$

$$C = \{a, b, c, d, e, f\}$$

Find  $(A \cup B) \cap (A \cup C)$

$$[A \cup B] = \{a, b, c, d, e\}$$

$$[A \cup C] = \{a, b, c, d, e, f\}$$

$$(A \cup B) \cap (A \cup C) = \{a, b, c, d, e\} \quad [\text{option B}]$$

QUE 32: If  $\cos 60^\circ = \frac{1}{2}$

$$\cos 60^\circ = \sin 30^\circ$$

[\text{option A}]

QUE 33: Perimeter of a sector

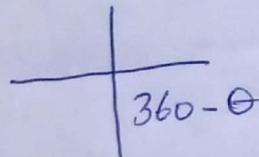
$$\frac{\theta}{360} \times 2\pi r + 2r$$

$$\frac{120}{360} \times 2 \times \frac{22}{7} \times 10.5 + 2(10.5)$$

$$\frac{55440}{2520} + 21$$

$$22 + 21 = 43 \text{ cm} \quad [\text{option C}]$$

QUE 34:  $\cos 75^\circ$  has the same value as

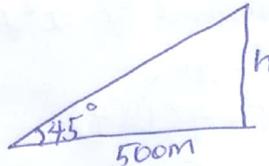


$$360 - \theta$$

$$360 - 75 = 285^\circ$$

$\therefore \cos 75^\circ$  is equivalent to  $\cos 285^\circ$   
[\text{option C}]

QUE 35:



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 45 = \frac{h}{500}$$

$$h = 500\sqrt{2} \quad [\text{option E}]$$

QUE 36: Calculate the sum to infinity

$$1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27}$$

$$a = 1$$

$$r = \frac{1}{3}$$

$$S_{n \rightarrow \infty} = \frac{a}{1-r}$$

$$S_{n \rightarrow \infty} = \frac{1}{\frac{2}{3}}$$

$$= \frac{3}{2} \quad [\text{option B}]$$

QUE 37:  $\frac{1+2i}{1-3i}$

Rationalize

$$\frac{1+2i}{1-3i} \times \frac{1+3i}{1+3i}$$

$$\frac{1+5i+6i^2}{10}$$

$$\frac{-5+5i}{10} = -\frac{1}{2} + \frac{i}{2}$$

$$\text{Modulus} = \sqrt{(-\frac{1}{2})^2 + (\frac{1}{2})^2}$$

$$= \sqrt{\frac{1}{2}}$$

$$= \frac{1}{\sqrt{2}}$$

$\arg [1+2i] = \frac{\pi}{4}$

$$\tan \theta = \frac{1}{2} \times \frac{-2}{1}$$

$$\theta = -45^\circ$$

From Argand diagram

$$\theta = -45^\circ \quad \theta = 180 - 45^\circ$$

$$\theta = 135^\circ$$

$$\left[ \frac{1}{\sqrt{2}}, \frac{\pi}{4} \right]$$

QUE 38: Discriminant of  $x^2 + 3x + 4 = 0$

$$\Delta = b^2 - 4ac$$

$$\Delta = 3^2 - 4(1)(4)$$

$$\Delta = 9 - 16$$

$$\Delta = -7 \quad [\text{option B}]$$

QUE 39:  $x^2 - 5x + 4 = 0$  Find  $\frac{1}{\alpha} - \frac{1}{\beta}$

$$\alpha + \beta = -5 \quad \text{--- (i)}$$

$$\alpha \beta = 4 \quad \text{--- (ii)}$$

$$\alpha = 4/\beta \quad \text{--- (iii)}$$

$$\frac{1}{\beta} + \beta = -5$$

$$\beta^2 + 5\beta + 4 = 0$$

$$-5 \pm \sqrt{5^2 - 4(4)}$$

$$\frac{-5 \pm \sqrt{9}}{2}$$

$$\frac{-5+3}{2} \quad \text{or} \quad \frac{-5-3}{2}$$

$$\beta = -1 \quad \text{or} \quad -4$$

$$\text{when } \beta = -1 \quad \alpha = -4$$

$$\text{or } \beta = -4 \quad \alpha = -1$$

To solve  $\frac{1}{\alpha} - \frac{1}{\beta}$  when  $\alpha$  is -1 and  $\beta$  is -4

$$\frac{1}{\alpha} - \frac{1}{\beta}$$

$$\frac{\beta - \alpha}{\alpha \beta}$$

$$\frac{-4 - (-1)}{4} = -\frac{3}{4}$$

To solve  $\frac{1}{\alpha} - \frac{1}{\beta}$  when  $\alpha = -4$  &  $\beta = -1$

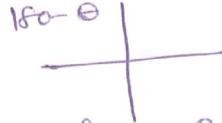
$$\frac{\beta - \alpha}{\alpha \beta}$$

$$\frac{-1 - (-4)}{4} = \frac{3}{4}$$

$$\therefore \frac{1}{\alpha} - \frac{1}{\beta} = \pm \frac{3}{4}$$

[option C]

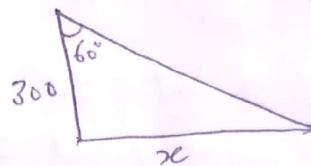
QUE 40: The value of  $\sin 210^\circ$



$$180^\circ - 210^\circ = -30^\circ$$

∴ The value of  $\sin 210^\circ = -\frac{1}{2}$

QUE 41:



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 60^\circ = \frac{x}{300}$$

$$\sqrt{3} = \frac{x}{300}$$

$$x = 300\sqrt{3}$$

QUE 42:  $S = \{1, 2, 3, 4, 5, 6\}$

$T = \{3, 4, 5, 6\}$

$R = \{1, 4, 5\}$

Find  $(S \cap T) \cup R$

$(S \cap T) = \{3, 4, 5, 6\}$

$(S \cap T) \cup R = \{1, 3, 4, 5, 6\}$

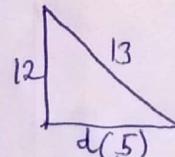
QUE 43: Write as a single fraction

$$\frac{5}{6r} - \frac{3}{4r}$$

$$\frac{10 - 9}{12r} = \frac{1}{12r} \quad [\text{option E}]$$

QUE 44: If  $\sin x = \frac{12}{13}$

Find  $1 - \cos^2 x$



$$13^2 = 12^2 + d^2$$

$$169 - 144 = d^2$$

$$d = 5$$

$$\cos x = \frac{5}{13}$$

$$1 - \left(\frac{5}{13}\right)^2 = 1 - \frac{25}{169}$$

$$= \frac{144}{169}$$

[option D]

QUE 45: BANANA

$$\frac{7!}{3!2!}$$

$$\frac{7 \times 6 \times 5 \times 4 \times 3 \times 2}{[3 \times 2 \times 1][2 \times 1]} = 720$$

[option A]

QUE 46: no of student = 40

no of physic student = 22

no of math student = 21

$$\text{no of student} = n(P) + n(M) - n(P \cap M)$$

$$40 = 22 + 21 - x$$

$$40 = 43 - x$$

$$x = 3$$

no of those who study physics =

$$n(P) - n(P \cap M)$$

$$22 - 3 = 19$$

[option D]

QUE 47:  $n(Y) = 37$

$$n(C) = 8, n(E) = 19$$

$$n(M) = 25, n(E \cap M) = 12$$

$$n(C \cap E) = 0, n(C \cap M) = ?$$

~~n(C \cap M \cap E) = ?~~

$$n(Y) = n(C) + n(M) + n(E) - [n(E \cap M) + n(C \cap E) + n(C \cap M)]$$

$$37 = 8 + 25 + 19 - [12 + 0 + x]$$

$$37 = 52 - [2 + x]$$

$$37 = 40 - x$$

$x = 3$  [option A]

QUE 48: If  $\tan \theta < 0, \sin \theta < 0$   
then angle lies at the first quadrant because all is positive at the first quadrant.

QUE 49:  $\cos(x + \alpha)$

$\cos(x + \alpha)$  is equivalent to

-  $\cos \alpha$  [option B]

QUE 50:  $\sec(\alpha - 90^\circ)$

See  $(\alpha - 90^\circ)$  is equivalent to  
 $\cos \alpha$  [option A]

QUE 51:  $\cot(90^\circ - \alpha)$

Recall that  $\cot = 1/\tan$

$\therefore \cot(90^\circ - \alpha) = \tan \alpha$   
[option A]

QUE 52:  $\sin\left[\frac{3\pi}{2} - \theta\right] =$

$\sin[270^\circ - \theta]$

= -  $\cos \theta$   
[option D]

QUE 53, 54, 55 & 56 are Rational Numbers

QUE 57: First term =  $x^2$   
Second term =  $2x + 1$   
Third term =  $2x^2$

$$4[x^2 + 2x + 1] - 3[x^2] = 4x^2 + 8x + 4 - 3x^2$$

$$4[x^2 + 4x + 4] - 3x^2 = 4x^2 + 16x + 16 - 3x^2$$

$$4x^2 + 16x + 16 - 3x^2 = 4x^2 + 12x + 16$$

$$x^2 + 12x + 16 = 2x^2 + 4x + 48$$

Collect like terms

$$x^2 + 12x + 16 = 0$$

$$12 \pm \sqrt{144 - 108}$$

$$\frac{12+6}{2} \text{ or } \frac{12-6}{2}$$

$$x = 9 \text{ or } 3$$

The values of the three consecutive numbers  
= 3, 4 & 5 or 9, 10, 11

[option A]

QUE 58: Find the sum of all numbers between 5 & 130 which are divisible by 4

$$8, 12, 16, \dots, 128$$

$$T_n = a + (n-1)d$$

$$128 = 8 + (n-1)4$$

$$128 = 8 + 4n - 4$$

$$128 = 4 + 4n$$

$$124 = 4n$$

$$n = 31$$

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

$$S_n = \frac{31}{2}(2(8) + (31-1)4)$$

$$S_n = \frac{31}{2}(16 + 120)$$

$$S_n = \frac{31}{2} \times 186$$

$$S_n = 2108 \quad [\text{option C}]$$

QUE 59: What is the coefficient of  $x^3$  in the expansion of  $(3+2x)^6$

$$\sum^n C_r x^{n-r} y^r$$

$$6C_3 3^{6-r} y^r$$

$$x^3 = x^r$$

$$\therefore r = 3$$

$$6C_3 3^{6-3} y^3 (2x)^3$$

$$20 \times 3^3 (2x)^3$$

$$20 \times 27 \times 8x^3$$

$$= 4320x^3 \quad [\text{option A}]$$

QUE 60: Find the modulus of  $1+i$

$$\text{modulus } (r) = \sqrt{1^2 + 1^2}$$

$$= \sqrt{2}$$

$$\arg(\tan \theta) = \frac{\pi}{4}$$

$$\tan \theta = 1$$

$$\theta = 45^\circ$$

$$[\sqrt{2}, 45^\circ] \quad [\text{option A}]$$

QUE 61:  $x^2 - 5x + 4 = 0$   
Solved already in Q 39

$$\text{QUE 62: } n(x) = 120$$

$$n(Y) = 75$$

$$n(I) = 60$$

$$n(Y \cap I) = ?$$

$$n(X) = n(Y) + n(I) - n(Y \cap I)$$

$$120 = 75 + 60 - x$$

$$120 = 135 - x$$

$$x = 15 \quad [\text{option C}]$$

QUE 63: Since the no of those who learned both subject is 15

$$n(I) = 60 - 15 \\ = 45 \quad [\text{option A}]$$

QUE 64: Second term  $(ar) = -\frac{1}{2}$

Third term  $(ar^2) = \frac{1}{4}$

$$ar = -\frac{1}{2}$$

$$ar^2 = \frac{1}{4}$$

$$r = \frac{1}{4} \times -\frac{2}{1}$$

$$r = -\frac{1}{2}$$

$$\text{Sum to infinity} \quad \frac{a}{1-r}$$

$$= \frac{1}{1 - (-\frac{1}{2})} = \frac{1}{1 + \frac{1}{2}}$$

$$= \frac{2}{3} \quad [\text{option D}]$$

$$\text{QUE 65: } \frac{x+5}{(x-1)(x+2)} = \frac{P}{x-1} + \frac{Q}{x+2}$$

$$x+5 = P(x+2) + Q(x-1)$$

When  $x$  is 1

$$1+5 = P(3) + Q(0)$$

$$6 = 3P \quad P = 2$$

When  $x$  is -2

$$-2+5 = P(-2+2) + Q(-3)$$

$$3 = -3Q$$

$$Q = -1 \quad P+Q = 2-1$$

$$= 1 \quad [\text{option A}]$$

QUE 66: Null/Empty set are represented by  $\emptyset$  or  $\{\}$  [option D]

QUE 67: If A and B are sets and  $A \cup B = A \cap B$

This implies that  $A = B$  [option C]

QUE 68: If X and Y are two sets then,

$$X \cap (Y \cup X)$$

$$= (X \cap Y) \cup (X \cap X)$$

$$= \emptyset$$
 [option C]

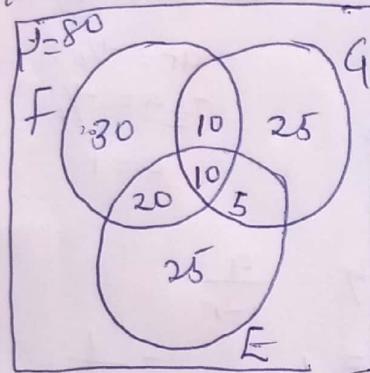
QUE 69: The number of elements in the power of the set  $\{a, b, c\}$

~~$P(A) = 2^n$~~

$$P(A) = 2^2$$

$$= 4$$
 [option B]

QUE 70:



$$n(F) = 80$$

$$n(E \cap F) = 30$$

$$n(G) = 50$$

$$n(F \cap G) = 20$$

$$n(E) = ?$$

$$n(E \cap F \cap G) = 10$$

$$80 = 80 + 60 + x - [30 + 20 + 15] + 10$$

$$80 = 60 + 50 + x - [30 + 20 + 15] + 10$$

$$80 = 110 + x - [65] + 10$$

$$80 = 110 + 10 - 65 + x$$

$$80 = 55 + x$$

$$x = 25$$

No of those who studied at least one subject

$$= 30 + 25 + 25 + 10 + 10 + 20 + 5$$

$$= 125$$

QUE 71:  $n(X) = 28$

$$n(E) = 18$$

$$n(H) = 15$$

$$n(K) = 22$$

$$n(E \cap H) = 9$$

$$n(H \cap K) = 11$$

$$n(K \cap E) = 13$$

$$n(E \cap H \cap K) = ?$$

$$28 = 18 + 15 + 22 - [9 + 11 + 13] + x$$

$$28 = 55 - [33] + x$$

$$28 = 22 + x$$

$$x = 28 - 22$$

$$x = 6$$
 [option A]

QUE 72: If the number of expert with 50% expertise is  $x$

~~$x = \frac{1}{2}(x) + \frac{2}{3}(x) - 10 + 6$~~

$$x = \frac{x}{2} + \frac{2x}{3} - \frac{4}{1}$$

$$x = \frac{3x + 4x - 24}{6}$$

$$6x = 7x - 24$$

$$24 = 7x - 6x$$

$$x = 24$$

[option C]

$\therefore$  no of expert equals 24

QUE 73: Object in a set are called Element of a set

[option A]

QUE 74: A group or collection of objects is known as Set

[option B]

QUE 75: vowels in alphabet

{a, e, i, o, u} [option B]

QUE 76: Set {x: odd numbers between 10 and 18}

{11, 13, 15, 17} [option C]

QUE 77:  $a_n = \frac{(-1)^n}{2n-1}$   $a_5 = ?$

$$a_5 = \frac{(-1)^5}{2(5)-1}$$

$$a_5 = \frac{-1}{9}$$

[option D]

Q1 QUE 79: What is the 31<sup>st</sup> term of the sequence 1, 4, 7, 10

$$a = 1 \quad d = 3$$

$$T_{31} = a + (31-1)d$$

$$T_{31} = a + 30d$$

$$T_{31} = 1 + 30(3)$$

$$T_{31} = 91 \quad [\text{option B}]$$

QUE 80:  $m-2n, m-n, m$

$$a = m-2n$$

$$d = n$$

$$\text{i.e } m-n - m-2n = d$$

$$m-n - m+2n = d$$

$$n = d$$

11<sup>th</sup> term =  $a + 10d$

$$T_{11} = m-2n + 10(n)$$

$$T_{11} = m-2n + 10n$$

$$T_{11} = m + 8n \quad [\text{option D}]$$

QUE 81: Common difference of sequence

5, 8, 11, 14 is

$$8-5 = d \\ d = 3 \quad [\text{option A}]$$

QUE 82:  $2^1 + 2^2 + 2^3 + \dots + 2^n =$   
 $2 + 4 + 8 + \dots + 2^n$   
 $r = 2$   
 $a = 2$   
 $a[r^n - 1] = 2[2^n - 1]$  [\text{option A}]

QUE 83: Second term of a sequence  
 $\text{Ans } n^2 - \frac{4}{2}$

When  $n$  is 2

$$= 2^2 - \frac{4}{2}$$

$$= 4 - \frac{4}{2}$$

$$= 2 \quad [\text{option E}]$$

QUE 84: A.P whose  $n$ th term is  $2n-1$

$$\text{when } n \text{ is } 1 = 2(1)-1 \quad \text{A.P.} = 3, 5$$

$$\text{when } n \text{ is } 2 = 2(2)-1 \quad [\text{option C/E}]$$

$$\text{when } n \text{ is } 3 = 2(3)-1 = 5$$

QUE 85: How many are there in  
 $20, 25, 30, \dots, 140$

$$T_n = a + (n-1)d$$

$$140 = 20 + (n-1)5$$

$$140 = 20 + 5n - 5$$

$$140 = 15 + 5n$$

$$125 = 5n \quad [\text{option B}]$$

$$n = 25$$

QUE 86: Find the first term of an A.P whose 8th & 12th term is 39 & 59

$$T_8 = a + 7d$$

$$T_{12} = a + 11d$$

$$a + 7d = 39$$

$$a + 11d = 59$$

$$4d = 20$$

$$d = 5$$

Sub for  $d$  in ①

$$a + 7d = 39$$

$$a + 7(5) = 39$$

$$a = 4 \quad [\text{option C}]$$

QUE 87: The 15th term of  $20, 15, 10$

$$a = 20$$

$$d = -5$$

$$T_{15} = a + 14d$$

$$T_{15} = 20 + 14(-5)$$

$$T_{15} = 20 - 70$$

$$T_{15} = -50 \quad [\text{option C}]$$

QUE 88:  $a = 5$

$$a + 2d = 15 \quad \dots \textcircled{a}$$

Sub for  $a$  in ②

$$5 + 2d = 15$$

$$2d = 10$$

$$d = 5$$

$$S_{16} = \frac{n}{2} [2a + (n-1)d]$$

$$S_{16} = \frac{16}{2} [2(5) + (16-1)5]$$

$$S_{16} = 8[10 + 75]$$

$$S_{16} = 680 \quad [\text{option D}]$$

QUE 89: How many terms are there in  
 $5, 20, 80, 320, \dots, 20480$

$a = 5$   
 $r = 4$   
 $20480 = ar^{n-1}$   
 $20480 = 5 \times 4^{n-1}$   
 $4096 = 4^{n-1}$

QUE 89: How many terms are there in  
 $5, 20, 80, 320, \dots, 20480$

$a = 5, r = 4$   
 $20480 = ar^{n-1}$   
 $20480 = 5 \times 4^{n-1}$   
 $4096 = 4^{n-1}$   
 $4^6 = 4^{n-1}$   
 $6 = n - 1$   
 $n = 7$  [option D]

QUE 90:  $x^4 - 3x + 5$  is divided by  
 $2x - 1$   
 $2x - 1 = 0$   
 $x = \frac{1}{2}$   
 $\left[\frac{1}{2}\right]^4 - 3\left[\frac{1}{2}\right] + 5 = 0$   
 $\frac{1}{16} - \frac{3}{2} + \frac{5}{1} = 0$   
 $\frac{1 - 24 + 80}{16} = 0$   
 remainder =  $\frac{57}{16}$

QUE 91: solve equation  $x^2 + 5x - 6 = 0$

$x^2 + 5x - 6 = 0$   
 $x^2 + [x^2 - 1](+6x - 6)$   
 $x[x-1] + 6[x-1]$   
 $[x+6][x-1]$   
 values of  $x$  equal  $1, -6$   
 [option B]

QUE 92: If  $a < 0$ , the function  
 $F(x) = ax^2 + bx + c$   
 has its maximum value  
 [option A]

QUE 93: If roots of  $x^2 - 5x + a = 0$   
 then  $a$  equal  
 $b = b^2 - 4ac$   
 $b = (-5)^2 - 4[1][a]$   
 $b = 25 - 4a$   
 $25 - 4a = 0$   
 $a = \frac{25}{4}$  [option C]

QUE 94: If  $w$  is imaginary root of unity, then  $w^2$  is?

$$w = \sqrt[3]{-1}$$

$$w^2 = 1$$
 [option A]

QUE 95: Discriminant =  $b^2 - 4ac$   
 [option C]

QUE 96:  $x^2 - 2x + 3$  Find the equation with roots  $\alpha + \beta$  and  $\beta + 2$   
 $\alpha + \beta = -b/a = -2$   
 $\alpha\beta = ca = 3$

Sum of roots  
 $\alpha + \beta + \beta + 2 = \alpha + 2\beta + 2$   
 Sum of roots =  $[\alpha + 2] + \beta$   
 $= 6$

Product of roots  
 $(\alpha + \beta)(\beta + 2)$   
 $\alpha\beta + 2\alpha + 2\beta + 4$   
 $\alpha\beta + 2[\alpha + 2] + 4$   
 $3 + 2[2] + 4$   
 $= 11$

equation of root  
 $x^2 - [\text{sum of root}]x + \text{product of root}$   
 $x^2 - 6x + 11 = 0$

QUE 97:  $ax^2 + bx + c = 0$   
 for root to be distinct and real the discriminant [ $b^2 - 4ac$ ] must be greater than zero  
 [option B]

QUE 98: Find the roots of  $x^2 + 2x - 15 = 0$

Using factorization method

$$[x^2 - 3x] + [5x - 15] = 0$$

$$x[x - 3] + 5[x - 3] = 0$$

$$[x - 3][x + 5]$$

Roots equal 3 & -5 [option A]

QUE 99: Find the roots of  $2x^2 + 3x - 9 = 0$

$$-b \pm \sqrt{\frac{b^2 - 4ac}{2a}}$$

$$-3 \pm \sqrt{\frac{(3)^2 - 4(2)(-9)}{2(2)}}$$

$$-3 \pm \sqrt{\frac{9 + 72}{4}}$$

$$\frac{-3 \pm 9}{4} \Rightarrow \frac{-3+9}{4} \text{ or } \frac{-3-9}{4}$$

$$\frac{6}{4} \text{ or } -\frac{12}{4}$$

$\frac{3}{2}$  or -3 [option B]

QUE 100: Which of these <sup>sub</sup> set are equal

$$L = \{5, t, s\}$$

$$N = \{t, s, t\}$$

$$D = \{s, t, s, t\}$$

[option D is correct] all subset are equal neglecting repetition.

QUE 101: Solve for  $x$  if  $5^{x^2} = 625^{x+3}$

$$5^{x^2} = 625^{x+3}$$

$$5^{x^2} = 5^{4(x+3)}$$

$$5^{x^2} = 5^{4x+12}$$

$$x^2 = 4x + 12$$

$$x^2 - 4x - 12 = 0$$

$$x^2 + 2x - 6x - 12 = 0$$

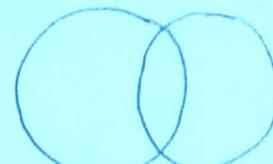
$$x[x+2] - 6[x+2] = 0$$

$$[x-6][x+2]$$

$$x = 6 \text{ & } -2$$

[option B]

QUE 102:



The overlap between two circle in Venn diagram represent the intersection of two set  
[option B]

QUE 103: no of student in Antony team = 8  
no of " in badminton team = 12  
intersection = 3

$$n(U) = ?$$

$$n(U) = n(t) + n(b) - n(t \cap b)$$

$$n(U) = 12 + 8 - 3$$

$$n(U) = 17$$
 [option B]

QUE 104: Set is the collection of a well defined objects  
[option B]

QUE 105: Anything belonging to a set is called element of the set  
[option C]

QUE 106: The null set is considered to be a \*subset\* of every set.  
[option A]

QUE 107: A set which does not contain any element is regarded as Null/empty set  
{} or  $\emptyset$  [option A]

QUE 108: Every set is a \*subset\* of itself  
{} [option B]

QUE 109: Two set are said to be Equal if they have the same number of elements  
[option A]

QUE 110:  $n(U) = 80$ ,  $n(I) = 32$ ,  $n(H) = 45$

$$80 = 32 + 45 - n(I \cap H)$$

$$80 = 77 - x$$

$$x = 17$$
 [option A]

QUE 111:  $n(V) = 80$   
 $n(G) = 65$   
 $n(E) = 50$   
 $n(ENG) = ?$

$$80 = 65 + 50 - x$$

$$80 = 115 - x$$

$$x = 115 - 80$$

$x = 35$  [option D]

QUE 112:  $\frac{\log_{10} \sqrt{125} + \log_{10} \sqrt{27} - \log_{10} \sqrt{75}}{\log_{10} 3 - \log_{10} 5}$

$$\frac{\log_{10} 5\sqrt{5} + \log_{10} 3\sqrt{3} - \log_{10} 5\sqrt{3}}{\log_{10} 3 - \log_{10} 5}$$

$$= \log_{10} \frac{15\sqrt{15}}{5\sqrt{3}} \times \log_{10} \frac{5}{3}$$

$$= \frac{5\sqrt{5} \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = \frac{5\sqrt{45}}{3} = 5\sqrt{5}$$

[option A]

QUE 113: Obtain the roots of the equation

$$x^2 - 5x + 6 = 0$$

Using factorization method

$$x^2 - 2x - 3x + 6 = 0$$

$$x[x-2] - 3[x-2] = 0$$

$$[x-3][x-2] = 0$$

roots of equation equals 2 & 3

[option C]

QUE 114: The sum of all numbers between 5 & 130 which are divisible by 4 is?

$$5, 12, 16, \dots, 128$$

$$T_n = a + (n-1)d$$

$$128 = 8 + (n-1)4$$

$$128 = 8 + 4n - 4$$

$$n = 31$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_n = \frac{31}{2} [2(8) + (30)4]$$

$$= 15.5 [16 + 120] = 2108$$

[option D]

(112)

QUE 115: Sequence is a set of quantities  $x_1, x_2, x_3$  stated in a definite order  
[option A]

QUE 116: Evaluate  $[1+i] - [1-i]$

$$1 - 1 + i - [-i] \\ 2i$$

[option A]

QUE 117: Obtain modulus  $Z = \frac{1+2i}{1-[1-i]^2}$

$$Z = \frac{1+2i}{1+2i} \times \frac{1-i}{1-i}$$

$$Z = \frac{1-i+2i-4i^2}{5}$$

$$Z = \frac{5}{5}$$

$Z = 1$  [option A]

QUE 118: Find r and ar  $ar^2 = 10$   
 $ar^6 = 6250$

divide both equations

$$\frac{ar^6}{ar^2} = \frac{6250}{10}$$

$$r^4 = 625$$

$$r = 5$$

Sub for r in eqn ①

$$a5^2 = 10$$

$$25a = 10$$

$$a = 10/25$$

$$a = 2/5$$

$$r = 5, a = 2/5$$

[option A]

QUE 119: Find the co-efficient of  $x^6$  in the expansion  $[1+x]^2$

$$[1+x][1+x]$$

$$1 + 2x + x^2$$

$$Ans = 1$$

[option A]

QUE 120:  $r = 3\text{cm}$

$$\theta = 60^\circ \approx \pi/3$$

$$L = r\theta$$

$$L = 3 \times \frac{\pi}{3}$$

$$L = \pi\text{cm}$$

[option B]

QUE 121: 12, x, y, z, -4. Find x

$$T_n = a + (n-1)d$$

$$-4 = 12 + [5-1]d$$

$$-4 = 12 + 4d$$

$$-16 = -4d$$

$$d = 4$$

To get x:

$$12 \text{ and } x-12 = 4$$

$$x = -4 + 12$$

$$x = 8 \quad [\text{option D}]$$

QUE 122: Find the value of b if

$$15, a, b, c, 3.$$

$$T_n = a + [n-1]d$$

$$3 = 15 + [4]d$$

$$3 = 15 + 4d$$

$$-12 = 4d$$

$$d = -3$$

To get b, get c first

$$3 - c = -3$$

$$3 + 3 = c$$

$$c = 6$$

$$\text{Then } 6 - b = -3$$

$$6 + 3 = b$$

$$b = 9 \quad [\text{option A}]$$

QUE 123:  $1 + \frac{1}{3} + \frac{1}{9} + \frac{1}{27} \dots$

$$a = 1$$

$$r = \frac{1}{3}$$

$$\text{Summ} \propto = \frac{a}{1-r}$$

$$= \frac{1}{1-\frac{1}{3}}$$

$$= \frac{3}{2}[1.5] \quad [\text{option B}]$$

QUE 124: What is the coefficient of  $x^3$  in the expansion of  $[1-2x]^{-2}$

$$[1^{-2} [1-2x]^{-2}]$$

$$\frac{1}{4} [1 + [-2][-2x] + \frac{-2[-3]}{2!} [-2x]^2 + \frac{-2[-3][-4]}{3!} [-2x]^3]$$

$$\frac{1}{4} [1 - 4x + 12x^2 + 32x^3]$$

$$\frac{1}{4} - x + 3x^2 + 8x^3$$

$\therefore$  the coefficient of  $x^3$  is 8  
[option E]

QUE 125:  $P = \{x : 2 \leq x \leq 4\}$

$$P = \{3, 3, 4\}$$

[option C]

QUE 126: [option B] refer to [Q101]

QUE 127: Solve for y in  $9^y - 4(3)^y + 8 = 0$

$$3^y - 4(3)^y + 8 = 0$$

$$3^y - 4(3)^y + 3 = 0$$

$$\text{Let } 3^y = P$$

$$P^2 - 4P + 3 = 0$$

$$P = 1 \text{ & } 3$$

$$\text{recall } 3^y = P$$

$$3^y = 1 \quad 3^y = 3^1$$

$$y = 0 \quad y = 1$$

[option C]

QUE 128: Find the 16th term of the sequence 3, 6, 9, 12, ...

$$a = 3 \quad d = 3$$

$$T_{16} = a + 15d$$

$$= 3 + 15[3]$$

$$= 48 \quad [\text{option E}]$$

QUE 129:  $n(A) = 12$

$$n(B) = 10$$

$$n(A \cup B) = 17$$

$$n(A \cap B) = ?$$

$$n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$17 = 12 + 10 - x$$

$$17 = 22 - x$$

$$x = 5 \quad [\text{option C}]$$

QUE 130: Simplify  $y = a^{\log_a x}$

$$\log_a y = \log_a(a^{\log_a x})$$

$$\log_a y = \log_a x \times \log_a a$$

$$\log_a a = 1$$

Then  $\log_a y = \log_a x$   
hence  $y = x$  [option A]

QUE 131: Express  $(2-3i)(1+2i)$

$$(2+4i) - 3i(1+2i)$$

$$= 2+4i - 3i - 6i^2$$

$$= 2+i+6$$

$$= 8+i$$
 [option D]

QUE 132: Find the value that satisfy the equation  $(x+iy)+i(x-y)=6+4i$

$$x+iy = 6 \quad \text{--- (1)}$$

$$x-y = 4 \quad \text{--- (2)}$$

from eqn 1  $x = 6-y$   
sub for  $x$  in (2)

$$6-y-y = 4$$

$$6-2y = 4$$

$$6-4 = 2y$$

$$2 = 2y$$

$$y = 1$$

To subs for  $y$  using (1)

$$x-1 = 4$$

$$x = 5$$

[option A]

QUE 133: If  $Z = 2+3i$  find  $Z - \frac{1}{Z}$

$$\frac{1}{Z} = \frac{1}{2+3i} \times \frac{2-3i}{2-3i}$$

$$\frac{1}{Z} = \frac{2-3i}{13}$$

$$Z - \frac{1}{Z} = \frac{2+3i}{1} - \frac{2-3i}{13}$$

$$= \frac{13(2+3i) - [2-3i]}{13}$$

$$= \frac{26+39i - 2+3i}{13}$$

$$= \frac{24+42i}{13} = \frac{24}{13}, \frac{42i}{13}$$

QUE 134: Simplify  $\frac{1+i}{1-i}$

by rationalization  $\frac{1+i}{1-i} \times \frac{1+i}{1+i}$

$$= \frac{1+i+i-1}{2}$$

$$= \frac{2i}{2}$$

$$= i$$
 [option C]

QUE 135: If  $Z_1 = 1-2i$

$$Z_2 = 3+2i$$

Find  $Z_1 Z_2$

$$(1-2i)(3+2i)$$

$$1(3+2i) - 2i(3+2i)$$

$$3+2i - 6i - 4i^2$$

$$7-4i$$

QUE 136: Find the value of  $|Z|$  in

$$Z = 3-4i$$

$$|Z| = \sqrt{3^2 + 4^2}$$

$$|Z| = 5$$
 [option A]

QUE 137: If  $Z_1 = 1-2i$

$$Z_2 = 2-i$$

Simplify  $\frac{Z_1}{Z_2}$

$$\frac{1-2i}{2-i} \times \frac{2+i}{2+i}$$

$$\frac{2+2i-3i-2i^2}{5}$$

$$\frac{5-2i}{5}$$

If  $Z_1 = 2-3i$   
then we have

$$\frac{2-3i}{2-i} \times \frac{2+i}{2+i}$$

$$\frac{4+2i-6i-3i^2}{5}$$

$$\frac{7-4i}{5}$$

[option D]

QUE 138: Polar form of  $3+4i$

$$r = \sqrt{3^2 + 4^2}$$

$$r = 5$$

$$\arg = \tan^{-1} \frac{4}{3}$$

$$\theta = 53^\circ$$

$$Z = 5[\cos 53^\circ + i \sin 53^\circ]$$

$$\text{Ques 139: } z = 1+i$$

Find the complex conjugate form of  $3z - 2$

$$3z = 3(1+i)$$

$$3z = 3+3i$$

$$3z - 2 = 3+3i - 2$$

$$= 1+3i$$

$$\text{Conjugate of } 1+3i = 1-3i \quad [\text{option C}]$$

Ques 140: Find the modulus of  $z+2$  where

$$z = 1+4i$$

$$z+2 = 1+4i+2$$

$$= 3+4i$$

$$\text{modulus} = \sqrt{3^2 + 4^2}$$

$$= \sqrt{25}$$

$$= 5 \quad [\text{option C}]$$

Ques 141: Find the value of  $x$  &  $y$

$$(2x-y) + i(x+y) = 4+2i$$

$$2x-y = 4 \quad \dots \textcircled{1}$$

$$x+y = 2 \quad \dots \textcircled{2}$$

$$x = 2-y \quad \dots \textcircled{3}$$

Substitute  $x$  in eqn (1)

$$2(2-y) - y = 4$$

$$4-2y-y = 4$$

$$4-3y = 4$$

$$4-4 = 3y$$

$$y = 0 \quad //$$

Sub for  $y$  in  $\textcircled{2}$

$$x+0 = 2 \quad [\text{option A}]$$

$$x = 2 \quad //$$

Ques 142: Simplify  $z + \frac{1}{z}$  if  $z = 1+2i$

$$\frac{1}{z} = \frac{1}{1+2i} \times \frac{1-2i}{1-2i}$$

$$= \frac{1-2i}{5}$$

$$z + \frac{1}{z} = 1+2i + \frac{1-2i}{5}$$

$$= \underline{\underline{5(1+2i)} + \frac{1-2i}{5}} \quad 5$$

$$\frac{5(1+2i) + 1-2i}{5} = \frac{6+8i}{5}$$

Ques 143: Find the conjugate form of the complex number  $z^2$  given  $z = 3-2i$

$$z^2 = (3-2i)(3-2i)$$

$$= 3(3-2i) - 2i(3-2i)$$

$$= 9-6i - 6i + 4i^2$$

$$= 9-12i - 4$$

$$= 5-12i$$

$$\text{conjugate} = 5+12i \quad [\text{option E}]$$

Ques 144: Express  $(-1+i)^2$

$$= (-1+i)(-1+i)$$

$$= -1(-1+i) + i(-1+i)$$

$$= 1-i - i + i^2$$

$$= -2i$$

$$= 0 - 2i \quad [\text{option B}]$$

Ques 145: Simplify  $i^9$

Take to the multiple of 4

$$i^4 = 1 \quad [\text{option C}]$$

Ques 146: Simplify  $i^{16}$

Take to the multiple of 4

$$i^4 = 1 \quad [\text{option B}]$$

Ques 147:  $xtiy$  and  $p+iq$  are equal

From ~~the~~<sup>first</sup> we will say ~~p~~<sup>x</sup> = p and  $y = q$

$$x = p \quad [\text{real part}]$$

$$y = q \quad [\text{imaginary part}]$$

$$[\text{option D}]$$

Ques 148: Polar form of complex no

$$z = a+bi$$

$$r(\cos\theta + i\sin\theta)$$

$$[\text{option C}]$$

Ques 149: Exponential form of complex number  $r(\cos\theta + i\sin\theta)$

$$= r e^{i\theta}$$

Since  $\theta$  is positive

$$[\text{option A}]$$

QUE 150: Exponential form of a complex number  $r(\cos\theta - i\sin\theta)$   
 $= re^{-i\theta}$

Where  $\theta$  is negative [Option A]

QUE 151: Compute the argument of

$$z = 4(1+i)$$

$$z = 4 + 4i$$

$$\text{Arg} = \tan\theta = y/x$$

$$\tan\theta = 4/4$$

$$\theta = \tan^{-1} 1$$

$$\theta = 45^\circ \quad [\text{option E}]$$

QUE 152:  $z = z_1$  and  $z = z_2$

Find the equation that satisfy

$$3z\bar{z} + 2(z - \bar{z}) = 39 + 12i$$

$$\text{remember } z\bar{z} = x^2 + y^2$$

$$\therefore \text{we have, } 3(x^2 + y^2) + 2[x + iy - (x - iy)] = 39 + 12i$$

$$3(x^2 + y^2) + 2[2iy] = 39 + 12i$$

$$3x^2 + 3y^2 + 4iy = 39 + 12i$$

$$3x^2 + 3y^2 = 39 \quad \dots \quad (1)$$

$$4y = 12 \quad \dots \quad (2)$$

$$y = 3$$

Sub for  $y$  in eqn (1)

$$3x^2 + 3y^2 = 39$$

$$x^2 + y^2 = 13 \quad \text{when you divide all through by 3}$$

$$x^2 + 9 = 13$$

$$x^2 = 4$$

$$x = \pm 2$$

$$\therefore z = 2 + 3i$$

$$\bar{z} = 2 - 3i \text{ or } -2 + 3i \quad \begin{array}{l} \text{when you multiply} \\ \text{all through by minus} \end{array} \quad [\text{option C}]$$

QUE 153:  $z = x + iy$  when  $\arg z = \pi/4$

$$\frac{\pi}{4} = 45^\circ \quad \text{remember } \tan\theta = y/x$$

$$1 = y/x$$

$$x = y$$

[option B]

QUE 154:  $z = r(\cos\theta + i\sin\theta)$  what is  $z^n$  from De Moivre's theorem

$$z = r^n [\cos n\theta + i\sin n\theta] \quad [\text{option B}]$$

QUE 155: Simplify  $(5+4i)(3+7i)(2-3i)$

$$\begin{aligned} & 5(3+7i) + 4i(3+7i) \\ & 15 + 4i + 12i + 28i^2 \\ & [-13 + 16i][2-3i] \\ & -13[2-3i] + 16i[2-3i] \\ & -26 + 39i + 32i - 48i \\ & -26 + 71i \\ & 22 + 7i \end{aligned}$$

$$\begin{aligned} & 5(3+7i) + 4i(3+7i)[2-3i] \\ & 15 + 35i + 12i + 28i^2[2-3i] \\ & [-13 + 47i][2-3i] \\ & -13[2-3i] + 47i[2-3i] \\ & -26 + 39i + 94i - 14i \\ & 115 + 133i \quad [\text{option C}] \end{aligned}$$

QUE 156:  $f(x) = 2x^2 - 2$

evaluate  $f(a-1) + f(1)$

$$\begin{aligned} f(a-1) &= 2(a-1)^2 - 2 \\ &= 2(a^2 - 2a + 1) - 2 \\ &= 2a^2 - 4a + 2 - 2 \\ &= 2a^2 - 4a \end{aligned}$$

$$\begin{aligned} f(1) &= 2(1)^2 - 2 \\ &= 2 - 2 \\ &= 0 \end{aligned}$$

$$\therefore f(a-1) + f(1)$$

$$\begin{aligned} &= 2a^2 - 4a \\ &\text{by factorizing} \end{aligned}$$

$$2a(a-2) \quad [\text{option A}]$$

QUE 157:  $Z = x + iy$  [Final] the locus is defined by  $|Z| = 5$

$$Z = \sqrt{x^2 + y^2}$$

Square both sides

where  $Z = 5$

$$5^2 = x^2 + y^2$$

$$25 = x^2 + y^2 \quad [\text{option B}]$$

QUE 158: Simplify  $\frac{ix}{1+iy} = \frac{3x+4yi}{x+3yi}$

$$x+3yi(xi) = 3xi + 3xi^2 + 4i - 4y$$

$$x^2i - 3xi = 4i - 4y$$

$$x^2 = 4 \quad \dots \text{①}$$

$$x = \pm 2$$

$$-3xi = -4y \quad (\text{bi})$$

$$3x = 4y$$

$$y = 3x/4$$

$$\text{When } x \text{ is } 2 \quad y = \frac{3}{4} = \frac{3}{2}$$

$$\therefore x = -2 \quad y = -\frac{3}{4} = -\frac{3}{2}$$

$$\therefore x = \pm 2 \quad y = \pm \frac{3}{2}$$

[option D]

QUE 159: If  $\alpha$  and  $\beta$  are roots of  $3x^2 - 7x + 2 = 0$  find the value of

$$\alpha\beta = -b/a = \frac{2}{3} \quad \frac{1}{\alpha^2 + \beta^2}$$

$$= \frac{2}{3} = \frac{2}{3}$$

$$= \frac{1}{(\alpha + \beta)^2 - 2\alpha\beta}$$

$$= \frac{1}{\left(\frac{7}{3}\right)^2 - 2\left(\frac{2}{3}\right)}$$

$$= \frac{1}{\frac{49}{9} - \frac{4}{3}}$$

$$= \frac{1}{\frac{37}{9}} = \frac{9}{37} = \frac{9}{37} \quad [\text{option C}]$$

QUE 160:  $x^2 + px + q = 0$

$$\alpha - \beta = 5$$

$$\frac{\alpha}{\beta} = \frac{1}{2}$$

Take the ratio which implies

$$\alpha = 7 \text{ and } \beta = 2 \quad \alpha\beta = 14$$

equation from the root equal

$$x^2 - 7x + 14 = 0$$

$$\therefore p = -7 \text{ and } q = 14$$

[option A]

QUE 161:  $2x^2 + 5x + 3 = 0$

Find the reciprocal of  $\frac{\alpha}{2} + \frac{\beta}{\alpha\beta}$

$$\frac{\alpha}{2} + \frac{\beta}{\alpha\beta}$$

$$\text{reciprocal} = \frac{\alpha\beta}{2 + \beta^2}$$

$$= \frac{4\beta}{(\alpha + \beta)^2 - 2\alpha\beta}$$

$$\alpha + \beta = -\frac{b}{a} = -\frac{5}{2}$$

$$\alpha\beta = \frac{c}{a} = \frac{3}{2}$$

$$= \frac{3/2}{(-5/2)^2 - 2(3/2)} = \frac{3 \times 4}{2 \times 13} = \frac{6}{13}$$

$$= \frac{6}{13}$$

QUE 162:  $U = \{x : 0 < x \leq 18\}$

$$U = \{1, 2, 3, 4, 5, \dots, 18\}$$

This mean zero is not included while 18 is included but the values must not exceed 18

$$QUE 163: U = \{1, 2, 3, 4, \dots, 18\}$$

$$A = \{2, 4, 6, 8\}$$

$$B = \{3, 4, 5, 6\}$$

$$A^C = \{1, 3, 5, 7, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18\}$$

$$B^C = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18\}$$

$$A^C \cap B^C = \{1, 2, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18\}$$

[option C]

QUE 164: U: {1, 3, 5, 6, 7, 8, 10}  $\Delta$

$$A: \{2, 4, 6, 8\}$$

$$B: \{3, 4, 5, 6\}$$

Find A - B

$$A - B = \{2, 8\} \quad [\text{option C}]$$

QUE 165: U: {1, 3, 4, 5, 6, 7, 8, 10}  $\Delta$

$$A: \{2, 4, 6, 8\}$$

$$B: \{3, 4, 5, 6\}$$

$$\text{Evaluate } A \Delta B = [A - B] \cup [B - A]$$

$$A - B = \{2, 8\}$$

$$B - A = \{3, 5\}$$

$$A \Delta B = \{3, 5, 8\} \quad [\text{option B}]$$

QUE 166: P = {-5, -4, -3, -2, -1, 0, 1, 3, 4}

Q = {-3, -1, 0, 1, 3, 4, 5, 6, 7, 8, 9}

$$P \cap Q = \{-3, -1, 0, 1, 3, 4\} \quad [\text{option A}]$$

QUE 167: n(x) = 42

$$n(y) = ?$$

$$n(x \cap y) = 84$$

$$n(x \cup y) = 36$$

$$n(x \cup y) = n(x) + n(y) - n(x \cap y)$$

$$36 = 42 + n(y) - 84$$

$$36 = -42 + n(y)$$

$$n(y) = 78 \quad [\text{option C}]$$

QUE 168: Sub set of S = {a, b, c}

$$= \{\emptyset, \{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \{a, b, c\}\}$$

[\text{option C}]

QUE 169: Complement of a set is the set of element found in a universal set but absent in its own set

$$e.g. U = \{a, b, c\}$$

$$B = \{a, c\}$$

$\therefore B^c = \{b\}$  complement of set B  
 $b \in B$  because it is present in universal set  
but absent in its own set

QUE 170: A = {-3, -2, -1, 1}

$$B = \{1, -2, 3\}$$

$$C = \{1, 3, -3\}$$

$$D = \{-1, -2, -3\}$$

$$n(A) \neq n(B)$$

no of element in A is not the same as that of element in B  
because  $n(A) = 4$  while  $n(B) = 3$ .