

# FIT2086 Assignment 1

## Question 1

- a. Finding a pattern can be accomplished by using regression, which finds how much each variable is different from each other.
- b. A behaviour of a person can be predicted using forecasting which makes prediction in future.
- c. Predicting the data in future should use forecasting as the same reason in previous question.
- d. Classifying a sub-type from a sample based on their characteristics should use clustering.

## Question 2.

- a. Using the following R code.

```
1 setwd("C:/Users/yjb13/OneDrive/Monash Uni/Year 2/FIT2086 Modelling for Data Analysis/Assignment1")
2 PA <- read.csv("port.adelaide.csv", header = FALSE)$V1
3 PA
4 previous0_0 <- 0 ← the frequency of losing previous game and lose the following
5 previous0_1 <- 0
6 previous1_0 <- 0
7 previous1_1 <- 0
8 for (i in 3:length(PA)) {
9   if (PA[i-1] == 0) {
```

```

1 setwd("C:/Users/yjb13/OneDrive/Monash Uni/Year 2/FIT2086 Modelling for Data Analysis/Assignment1")
2 PA <- read.csv("port.adelaide.csv", header = FALSE)$V1
3 PA
4 previous0_0 <- 0 ← the frequency of losing previous game and lose the following
5 previous0_1 <- 0 game.
6 previous1_0 <- 0
7 previous1_1 <- 0
8 for (i in 3:length(PA)) {
9   if (PA[i-1] == 0) {
10     if (PA[i] == 0) {
11       previous0_0 <- previous0_0 + 1
12     } else {
13       previous0_1 <- previous0_1 + 1
14     }
15   }
16   if (PA[i-1] == 1) {
17     if (PA[i] == 0) {
18       previous1_0 <- previous1_0 + 1
19     } else {
20       previous1_1 <- previous1_1 + 1
21     }
22 }
23 }
24
25 previous0_0 = 20
26 previous0_1 = 12
27 previous1_0 = 13
28 previous1_1 = 22

```

divide by total number of game (68) to get the probability of these event occurred.

According to the output, the table should be:

	$W_t = 0$	$W_t = 1$
$W_{t-1} = 0$	$\frac{20}{67}$	$\frac{12}{67}$
$W_{t-1} = 1$	$\frac{13}{67}$	$\frac{22}{67}$

b. Marginal probability of PA winning a game:

$$P(W_t = 1) = \frac{12}{67} + \frac{22}{67} = \frac{34}{67}$$

c. The probability of PA win given they won previous one:

$$P(W_t = 1 | W_{t-1} = 1) = \frac{P(W_t = 1, W_{t-1} = 1)}{P(W_{t-1} = 1)}$$

$$= \frac{\frac{22}{67}}{\frac{13}{67} + \frac{22}{67}}$$

$$= \frac{\frac{22}{67}}{\frac{13}{67} + \frac{22}{67}} \\ = \frac{22}{35}$$

d. The probability of PA win given they lost previous one:

$$P(W_t = 1 | W_{t-1} = 0) = \frac{P(W_t = 1, W_{t-1} = 0)}{P(W_{t-1} = 0)} \\ = \frac{\frac{12}{67}}{\frac{20}{67} + \frac{12}{67}} \\ = \frac{3}{8}$$

e. To verify if  $W_t$  and  $W_{t-1}$  are independent,

$$P(W_t = 1, W_{t-1} = 1) = P(W_t = 1) P(W_{t-1} = 1)$$

$$P(W_t = 1, W_{t-1} = 1) = \frac{22}{67}$$

$$P(W_t = 1) = \frac{12}{67} + \frac{22}{67} = \frac{34}{67}$$

$$P(W_{t-1} = 1) = \frac{13}{67} + \frac{22}{67} = \frac{35}{67}$$

$$P(W_t = 1) \cdot P(W_{t-1} = 1) = \frac{1140}{4489}$$

$$\therefore P(W_t = 1, W_{t-1} = 1) \neq P(W_t = 1) P(W_{t-1} = 1)$$

$\therefore W_t$  and  $W_{t-1}$  are not independent.

f. The probability of losing given they won previous game is:

$$P(W_t = 0 | W_{t-1} = 1) = \frac{P(W_t = 0, W_{t-1} = 1)}{P(W_{t-1} = 1)} \\ = \frac{\frac{13}{67}}{\frac{12}{67} + \frac{22}{67}}$$

$$= \frac{\frac{12}{67}}{\frac{12}{67} + \frac{22}{67}} \\ = \frac{12}{34}$$

The probability of losing next game given losing this one:

$$P(W_t = 0 | W_{t-1} = 0) = \frac{P(W_t = 0, W_{t-1} = 0)}{P(W_{t-1} = 0)} \\ = \frac{\frac{20}{67}}{\frac{20}{67} + \frac{12}{67}} \\ = \frac{20}{32} \\ = \frac{5}{8}$$

$\therefore$  The probability of PA losing their next two game given that they won their previous is

$$\frac{13}{34} \times \frac{5}{8} = \frac{65}{272}$$

### Question 3

$$\begin{aligned} a. E[S] &= E[X_1 + X_2] = E[X_1] + E[X_2] = 2E[X_1] \\ &= (1 \times \frac{1}{6} + 2 \times \frac{1}{6} + 3 \times \frac{1}{6} + 4 \times \frac{1}{6} + 5 \times \frac{1}{6} + 6 \times \frac{1}{6}) \times 2 \\ &= 3.5 \times 2 \\ &= 7 \end{aligned}$$

$$\begin{aligned}V[S] &= [E[S^2] - E[S]]^2 \\&= 54.83 - 49 \\&= 5.83\end{aligned}$$

### b. The Uniform Distribution

This distribution can be used to model discrete numerical and categorical data.

$$c. P(S | 2, 12) = \frac{1}{12-2+1}, S \in \{2, \dots, 12\}$$

d.  $\because S$  is uniformly distributed.

$$\therefore E[S] = \frac{a+b}{2} = \frac{14}{2} = 7$$

$$E[\bar{s}] = \frac{\sqrt{a} + \sqrt{b}}{2} = \frac{\sqrt{2} + \sqrt{14}}{2} = 2.58$$

e.  $\because S$  is uniformly distributed.

if roll three dice,

$$S \in \{3, \dots, 18\}$$

$$\therefore E[S] = \frac{3+18}{2} = 10.5$$

$$E[S^2] = \frac{3^2+18^2}{2} = 166.5$$

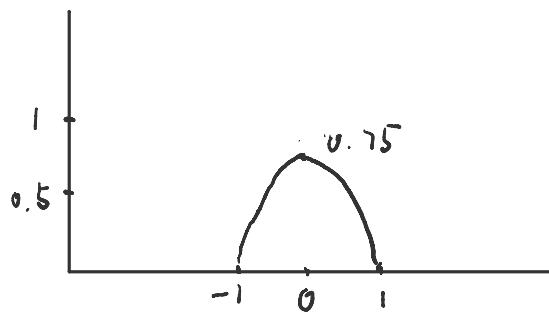
### Question 4

a. when  $S = 1$

$$(3, 1, 2, 1, \dots, 1, 1)$$

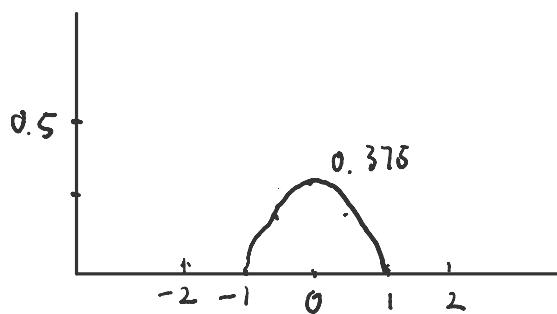
a. when  $s = 1$

$$P(x|1) = \begin{cases} \frac{3}{4}(1-x^2), & \text{for } x \in (-1, 1) \\ 0, & \text{otherwise} \end{cases}$$



when  $s = 2$

$$P(x|2) = \begin{cases} \frac{3}{8}(1-x^2), & \text{for } x \in (-2, 2) \\ 0, & \text{otherwise} \end{cases}$$



$$b. E[x] = \int_a^b x f(x) dx$$

$$= \int_{-s}^s \frac{3x}{4s} (1 - (\frac{x}{s})^2) dx$$

$$= \frac{3}{4s} \left( \frac{x^2}{2} - \frac{x^4}{4s^2} \right) \Big|_{-s}^s$$

$$= \frac{3}{4s} \left( \frac{s^2}{2} - \frac{s^4}{4s^2} \right) - \frac{3}{4s} \left( \frac{(-s)^2}{2} - \frac{(-s)^4}{4s^2} \right)$$

$$= 0$$

$$C. V[x] = E[(x-\mu)^2] = E[x^2] - E[x]^2$$

$$= \int_{-s}^s \frac{3x^2}{4s} \left(1 - \left(\frac{x}{s}\right)^2\right) dx - \left[ \int_{-s}^s \frac{3x}{4s} \left(1 - \left(\frac{x}{s}\right)^2\right) dx \right]^2$$

d. cdf is

$$P(X \leq x) = \int_{-\infty}^x P(x') dx' , \quad x \in (-s, s)$$

$$e. E[|x|] = \int_a^b |x| f(|x|) dx$$

$$= \int_{-s}^s \frac{3x}{4s} \left(1 - \left(\frac{x}{s}\right)^2\right) dx$$

$$= \frac{3}{4s} \left( \frac{x^2}{2} - \frac{x^4}{4s^2} \right) \Big|_{-s}^s$$

$$= \frac{3}{4s} \left( \frac{s^2}{2} - \frac{s^4}{4s^2} \right) - \frac{3}{4s} \left( \frac{|s|^2}{2} - \frac{|s|^4}{4s^2} \right)$$

$$= 0$$

Question 5.

a. Using the following R code.

```

1 my_estimates <- function(x)
2 {
3   n = length(x)
4   retval = list()
5   # Calculate the sample mean
6   retval$mu_m1 = sum(x)/n
7 }
```

```

1 my_estimates <- function(x)
2 {
3   n = length(x)
4
5   retval = list()
6
7   # calculate the sample mean
8   retval$mu_ml = sum(x)/n
9
10  # calculate the squared deviations around the mean
11  e2 = (x - retval$m)^2
12
13  # calculate the two estimates of variance
14  retval$var_ml = sum(e2)/n
15  retval$var_u = sum(e2)/(n-1)
16
17  return(retval)
18 }
19
20 # 3.2 Estimate from training data
21 db <- read.csv("dogbites.total.csv")
22
23 est = my_estimates(db$daily.dogbites)
24 est
25 est$mu_ml
26 est$var_ml
27 est$var_u
28 sqrt(est$var_ml)
29 sqrt(est$var_u)
30

```

According to the result:

$$\hat{\lambda}_{ML} = est\$mu\_ml = 4.505$$

b.

i.

Using the following R code

$$ppois(1, lambda = 4.505) = 0.061$$

$\therefore$  The probability of at most 1 dog-bite in a day is 0.061

ii.

The number of dog-bites occurred in a day should be the expected value 4 E.g.

The number of dog-bites occurred in a day should be the expected value 4.505.

iii.

- ∴ The expected dog-bites occurred in a day is 4.505
- ∴ The expected dog-bites occurred in 4 weeks is  $28 \times 4.505 = 126.14$
- ∴ The hospital system expect to see 126.14 dog-bites in 4 weeks

iv.

Probability of seeing 6 or more dog-bites in 28 days:

Using the following code in R.

c.