Exercises for Audio and Video Signal Processing: FH OÖ Hagenberg 2011

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Exercise 1: Quantization, Dither, Noise Shaping

## 1. Quantization

- a) Consider a 100 Hz sine wave x(n) sampled with  $f_S = 44.1$  kHz, N = 1024 number of samples and w = 3 bit (word-length). What is the number of quantization levels? How is the quantization step Q when the signal is normalized to -1 <= x(n) < 1. Show graphically how quantization is performed. What is the maximum error for this 3 bit quantizer? Write a Matlab code for quantization with rounding and truncation.
- **b)** Derive the mean value, the variance and the peak factor  $P_F$  of sequence e(n), if the signal has a uniform probability density function (pdf) in the range  $-\frac{Q}{2} < e(n) < -\frac{Q}{2}$ . Derive the signal-to-noise ratio SNR for this case. What will happen if we increase our word-length by one bit?
- c) As the input signal level decreases from maximum amplitude to very low amplitudes, the error signal becomes more audible. How can you describe the error calculated above when w decreases to 1 bit? Is the classical quantization model still valid? What can be done to avoid this distortion?
- d) Write a Matlab code for a quantizer with w = 16 bit with rounding and truncation.
  - Plot the nonlinear transfer characteristic and the error signal when the input signal covers the range 3Q < x(n) < 3Q.
  - Consider the sine wave  $x(n) = A \sin(2\pi \frac{f}{f_S}n), n = 0, \dots, N-1$  with  $A = Q, \frac{f}{f_S} = 64/N$  and N = 1024. Plot the output signal  $(n = 0, \dots, 99)$  of a quantizer with rounding and truncation in the time-domain and the frequency domain.
  - Compute for both quantization types the quantization error and the SNR.

## 2. Dither

- a) What is dither and when do we have to use dither?
- **b)** How do we perform dither and which kind of dither do we have?
- c) How do we obtain a triangular high-pass dither and why do we prefer it to other dithers?
- **d)** Matlab: generate corresponding dither signals for rectangular, triangular and triangular high-pass.
- e) Plot the amplitude distribution and the spectrum of the output  $x_Q(n)$  of a quantizer for every dither type.

## 3. Noise Shaping

- a) What is noise shaping and when do we do it?
- **b)** Why is it necessary to dither during noise shaping and how do we do this?
- c) Matlab: The first noise shaper used is without dither and assumes that the transfer function in the feedback structure can be first-order  $H(z) = z^{-1}$  or second-order  $H(z) = -2z^{-1} + z^{-2}$ . Plot the output  $x_Q(n)$  and the error signal e(n) and its spectrum. Show with a plot how the error signal will be shaped.
- **d**) The same noise shaper is now used with a dither signal. Is it really necessary to dither with noise shaping? Where would you add your dither in the flow graph for achieving better results?
- e) In the feedback structure we now use a psychoacoustic-based noise shaper which uses the Wannamaker filter coefficients:

```
h_3 = [1.623, -0.982, 0.109]

h_5 = [2.033, -2.165, 1.959, -1.590, 0.6149]

h_9 = [2.412, -3.370, 3.937, -4.174, 3.353, -2.205, 1.281, -0.569, 0.0847].
```

Show with Matlab plot how the error is shaped by this filter?