

ARITHMETIC PROGRESSION AND SUM TO INFINITY

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CONTRIBUTION: I'll be contributing a c++ code for the calculation of arithmetic progression and sum to infinity. Firstly, Arithmetic progression is a sequence of numbers in which each differs from the preceding one by a constant quantity. While the sum to infinity of a sequence is the sum of the infinite number of terms in a sequence.

Formula for the nth term of an AP:

$$T(n) = a + (n - 1)d$$

Sample: The first term of an AP is 2 and the common difference is 3. Calculate the 4th term

Solution

$$T(n) = a + (n - 1)d$$

$$T(4) = 2 + (4 - 1)3$$

$$T(4) = 2 + 3(3) = 2 + 9$$

$$T(4) = 11$$

Formula for sum of the nth term of an AP:

$$S(n) = n/2[2a + (n - 1)d]$$

Sample: The first term of an AP is 2 and the common difference is 3. Find the sum of the first 4 terms of the AP.

Solution

$$S(n) = n/2[2a + (n - 1)d]$$

$$S(4) = 4/2[2(2) + (4 - 1)3]$$

$$S(4) = 2[4 + 3(3)] = 2(4 + 9) = 2(13)$$

$$S(4) = 26$$

Formula for Sum to Infinity when $r > 1$:

$$S_{\infty} = a / (r - 1)$$

Sample: Find the sum to infinity if the first term is 9 and the common ratio is 4.

Solution

$$S_{\infty} = a / (r - 1)$$

$$S_{\infty} = 9 / (4 - 1)$$

$$S_{\infty} = 9 / 3$$

$$S_{\infty} = 3$$

Formula for Sum to Infinity when $r < 1$:

$$S_{\infty} = a / (1 - r)$$

Sample: Find the sum to infinity if the first term is 8 and the common ratio is 0.5.

Solution

$$S_{\infty} = a / (1 - r)$$

$$S_{\sim} = 8 / (1 - 0.5)$$

$$S_{\sim} = 8 / 0.5$$

$$S_{\sim} = 16$$