

Assignment - Day 5: 1-D Dynamic Programming Problems

Dear Students,

This assignment focuses on building a strong foundation in 1-D Dynamic Programming (DP).

Assignment Problems:

1. Calculate nCr (GeeksforGeeks)

Link: <https://www.geeksforgeeks.org/problems/nCr1019/1>

Objective: Calculate the value of nCr (n choose r) using modular arithmetic ($\text{mod } 10^9 + 7$).

Hint:

- Use the recursive relation: $nCr = n-1Cr-1 + n-1Cr$
- Implement with DP or memoization to avoid recomputation.
- Consider handling edge cases when $r > n$.

2. Tribonacci Number (LeetCode 1137)

Link: <https://leetcode.com/problems/n-th-tribonacci-number/>

Objective: Find the N -th Tribonacci number where $T(n) = T(n-1) + T(n-2) + T(n-3)$ with base cases $T(0)=0$, $T(1)=1$, $T(2)=1$.

Hint:

- Solve recursively first, then optimize using memorization.
- Observe the similarity to Fibonacci and note how DP reduces time complexity.

3. Min Cost Climbing Stairs (LeetCode 746)

Link: <https://leetcode.com/problems/min-cost-climbing-stairs/>

Objective: Given an array where each element represents cost on a step, return the minimum cost to reach the top of the floor.

Hint:

- Define $dp[i]$ as the minimum cost to reach step i .
- Recurrence: $dp[i] = \text{cost}[i] + \min(dp[i-1], dp[i-2])$
- Try solving via both recursion + memorization.

4. Boredom (Codeforces 455A)

Link: <https://codeforces.com/problemset/problem/455/A>

Objective: Given an array of integers, choose numbers such that no two chosen numbers differ by 1, and maximize the sum of chosen numbers.

Hint:

- Sort or compress input into frequency map.
- Use recurrence similar to 'House Robber': $dp[i] = \max(dp[i-1], dp[i-2] + i * \text{freq}[i])$
- Think about transitions in terms of 'choose or skip'.

Key Concepts to Revise:

Before attempting the assignment, make sure to review:

1. Memoization conversion.
2. Base cases and transition design (Recurrence) in DP.
3. Difference between recursion tree and DP array visualization.

Submission Instructions:

- Solve and submit all four problems.
- Use recursion → memoization approaches for understanding.
- Submit your solution files via the Google Form.
- Deadline: 12 November 2025 (02:00 am)

Note:

Understanding 1-D DP is the stepping stone to advanced 2-D problems — focus on how overlapping subproblems are handled and how recursive calls map to DP states.

Best regards,
Training Team