

## Assignment - Day 6: 2-D Dynamic Programming Problems

### Assignment Problems:

#### 1. 1. Unique Paths II (LeetCode 63)

Link: <https://leetcode.com/problems/unique-paths-ii/>

Objective: Find the total number of unique paths from the top-left corner to the bottom-right corner of a grid with obstacles.

Hint:

- Define a recursive function  $f(i, j)$  that returns the number of ways to reach cell  $(i, j)$ .
- Recursive Step:  $f(i, j) = f(i-1, j) + f(i, j-1)$
- Store results in a  $dp[i][j]$  cache before returning.

#### 2. 2. Dungeon Game (LeetCode 174)

Link: <https://leetcode.com/problems/dungeon-game/>

Objective: Find the knight's minimum initial health needed to rescue the princess starting from  $(0, 0)$ .

Hint:

- Define a recursive function  $f(i, j)$  that returns the minimum health required from cell  $(i, j)$  to reach the destination.

#### 3. 3. Minimum Distance to Type a Word Using Two Fingers (LeetCode 1320)

Link: <https://leetcode.com/problems/minimum-distance-to-type-a-word-using-two-fingers/>

Objective: Find the minimum total distance needed to type a word using two fingers.

Hint :

- Define a recursive function  $f(\text{index}, \text{left}, \text{right}) \rightarrow$  minimum distance to type substring starting from index given left and right finger positions.

#### 4. 4. Minimum Falling Path Sum II (LeetCode 1289)

Link: <https://leetcode.com/problems/minimum-falling-path-sum-ii/>

Objective: Find the minimum sum of a falling path through a grid such that no two consecutive elements come from the same column.

Hint (Memoization Approach):

- Define  $f(i, j)$  = minimum path sum starting from cell  $(i, j)$  to the bottom.
- Base Case: If  $i$  is the last row  $\rightarrow$  return  $grid[i][j]$ .
- Recursive Step:  $f(i, j) = grid[i][j] + \min(f(i+1, k))$  for all  $k \neq j$ .
- Store results in  $dp[i][j]$  to avoid recomputation.

#### 5. 5. Optimal Division (LeetCode 553)

Link: <https://leetcode.com/problems/optimal-division/>

Objective: Find an expression that yields the maximum result by placing parentheses optimally.

### Key Concepts to Revise:

Before attempting these problems, ensure you understand:

1. How recursion breaks problems into smaller overlapping subproblems.
2. Defining recursive states with multiple parameters.
3. Using a memo dictionary or 2D array to cache results.

### Submission Instructions:

- Solve and submit all five required problems using recursion + memoization.
- Avoid direct tabulation unless explicitly discussed.
- Submit your code via the Google Form.
- Deadline: 13 November 2025 (02:00 am).

### Note:

Memoization allows you to visualize recursion with caching — focus on understanding state parameters, base cases, and recursive transitions. Tabulation is simply the next step of converting your memoized recursion into iteration.

Best regards,  
Training Team