#### **KEY**

# Section 1: Algebra

**1.3** 
$$N(H) = H$$

**1.6** Any two linearly independent elements in W. Example:

$$\left[\begin{array}{ccc} 0 & 1 & -1 \\ -1 & 0 & 0 \\ 1 & 0 & 0 \end{array}\right], \left[\begin{array}{ccc} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{array}\right]$$

**1.9** Any functional of the form 
$$ax - ay + cz$$
, where  $3c - a = 1$ 

### Section 2: Analysis

2.9 
$$-\frac{2\pi i}{a}$$

## Section 3: Topology

# Section 4: Calculus & Differential Equations

4.1 
$$-\frac{4}{\pi^2}$$

4.2 
$$\frac{12\pi}{5}$$

**4.3** 
$$\frac{3}{4}\sqrt{\pi}$$
.

**4.4** 
$$y = c_1 e^{c_2 x}$$

**4.5** 
$$y'' = g - c(y')^2$$
 for  $t > 0$ ;  $y(0) = y'(0) = 0$ .

$$1.6$$
  $\sqrt{g}$ 

**4.6** 
$$\sqrt{\frac{g}{c}}$$
  
**4.7**  $y' = u$ ;  $u' = v$ ;  $v' = v - x^2u^2$ 

**4.10** 
$$[-(t+1), (t+1)]$$

### Section 5: Miscellaneous

**5.1** a. 
$$E \cup F$$
; b.  $F$ 

**5.2** 
$$E = \bigcap_{n=1}^{\infty} \cup_{m=n}^{\infty} E_m$$

**5.3** 
$$2^n(2n-1)+1$$

5.5 
$$\frac{10}{24}$$

5.5 
$$\frac{10}{21}$$

5.5 
$$\frac{10}{21}$$
  
5.6 Semi-major axis = 1; semi-minor axis =  $\frac{1}{3}$ 

5.7 
$$\frac{1}{2} \log \frac{3}{2}$$

$$\left(|a|^{\frac{3}{2}}+|b|^{\frac{3}{2}}+|c|^{\frac{3}{2}}\right)^{\frac{2}{3}}$$

Note: Please accept any correct equivalent form of the answers.