

Cryptography Assignment 1

1.

2.

Elements in Z_5 are $\{1, 2, 3, 4\}$

The multiplicative inverse of the following are: $\{1, 2, 3, 4\}$

Elements in Z_{11} are $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

The multiplicative inverse of the following are: $\{10, -5, 4, 3, 2, 2, 3, -4, 5, 1\}$

3.

GCD of 56425, 43159 = 1

$q = 1$

old_r, r 43159 13266

old_s, s 0 1

old_t, t 1 -1

$q = 3$

old_r, r 13266 3361

old_s, s 1 -3

old_t, t -1 4

$q = 3$

old_r, r 3361 3183

old_s, s -3 10

old_t, t 4 -13

$q = 1$

old_r, r 3183 178

old_s, s 10 -13

old_t, t -13 17

$q = 17$

old_r, r 178 157

old_s, s -13 231

old_t, t 17 -302

q= 1

old_r, r 157 21

old_s, s 231 -244

old_t, t -302 319

q= 7

old_r, r 21 10

old_s, s -244 1939

old_t, t 319 -2535

q= 2

old_r, r 10 1

old_s, s 1939 -4122

old_t, t -2535 5389

q= 10

old_r, r 1 0

old_s, s -4122 43159

old_t, t 5389 -56425

4.

$$\phi(3^4) = 3^4 - 3^3 = 54$$

$$\phi(2^{10}) = 2^{10} - 2^9 = 512$$

5.

$$100 = 2^6 + 2^5 + 2^2$$

$$3^{2^0} \bmod 31319 = 3 \bmod 31319$$

$$3^{2^1} \bmod 31319 = 9 \bmod 31319$$

$$3^{2^2} \bmod 31319 = 81 \bmod 31319$$

$$3^{2^3} \bmod 31319 = 6561 \bmod 31319$$

$$3^{2^4} \bmod 31319 = 14415 \bmod 31319$$

$$3^{2^5} \bmod 31319 = 21979 \bmod 31319$$

$$3^{2^6} \bmod 31319 = 12185 \bmod 31319$$

$$\begin{aligned} \text{Therefore, } 3^{100} \bmod 31319 &= 12185 \times 21979 \times 81 \bmod 31319 \\ &= 25879 \bmod 31319 \end{aligned}$$

