

# violations

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## outline

misc

intuition

collinearity again

heteroskedasticity

normality of residuals

endogeneity

[\*] (elements of) research design: causality

[\*] more diagnostics

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## changes from before

- ◇ dropped autocorrelation—assuming you use cross-sec data
  - not time series, not panel

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## violations

- ◇ so far we have just talked about the regressions that satisfy assumptions
- ◇ but what happens when assumptions are violated?
  - typically, they are!
- ◇ and what you can do about it ?

## practical considerations

- ◇ usually have heteroskedasticity in crosssectional data
- ◇ (and autocorrelation in time-series data) [skipped]
- ◇ (and both in panel data) [skipped]
- ◇ “unobserved heterogeneity” = LOVB
- ◇ outliers/leverage
- ◇ normality of residuals
- ◇ you should \*always\* test all of them
  - (except autocorr in unclustered cross-sectional data and normality in datasets > 1k)
- ◇ when you report reg results, it is expected and assumed you took care of all assumptions

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## we discussed collinearity earlier

- ◇ if perfect, then you cannot estimate std err
  - stata will just drop a perfectly collinear var
  - with dummies—if you incl all cat—it is so called “dummy trap”
- ◇ otherwise, collinearity does not violate any assumption
- ◇ just makes std err bigger
- ◇ it is just like “micronumerosity”
- ◇ typically, do nothing

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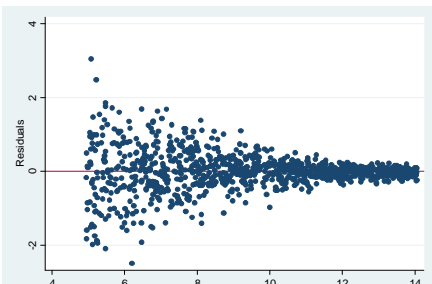
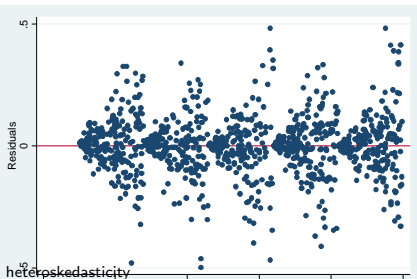
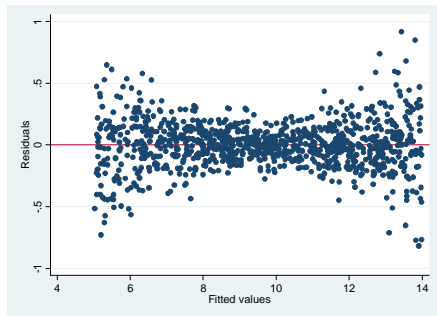
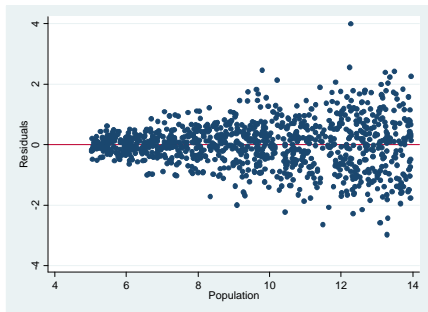
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# examples



## violation

- ◇ again, heteroskedascity=pattern in residuals
- ◇ the variance of  $Y$  conditional on  $X$  varies from one observation to another
  - eg it may depend on the values of  $X$
- ◇ if true:
  - $\hat{\beta}_j$  still unbiased
  - $s_{\hat{\beta}_j}$  is not as accurate as reported by software
  - not BLUE because not efficient

# diagnosis

- ◇ eyeball
- ◇ test
- there are many tests... eg Breush-Pagan

## solutions

- ◇ calculate robust se
- ◇ transform variables (\*if\* theoretically justifiable)
  - heteroskedasticity might indicate you are working in the wrong metric
  - a popular transformation that often works is log
  - log is popular for skewed distributions like income...
- ◇ dofile: het

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## only worry if you have small sample

- ◇ don't have to worry about this at all if sample is big
- ◇ if sample is small, after running regress
- ◇ can predict residuals `predict resid,r`
- ◇ do a histogram and plot them
- ◇ if they look very unnormal, don't be too trusting in significance
- ◇ try to get more data!



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## closely related to design!

- ◇ if you have bad design, you'll have endogeneity
- ◇ curiously, economists are obsessed with it
- ◇ but other fields aren't
- ◇ a superb and readable reference is Sorensen (2012)  
<http://people.bu.edu/tsimcoe/code/Endog-PDW.pdf>

## what is it

- ◇ technically, if  $x$  and error term are correlated
- ◇ so there is some  $Z$  that predicts  $Y$  and correlates with  $X$ 
  - (see also discussion of  $Z$  in res des sec)
- ◇ so it can be just LOVB, or unobserved heterogeneity
- ◇ unobserved heterogeneity: see Rumsfeld's unknown unknowns in res des sec

## simultaneity and self-selection

- ◇ but usually by endogeneity we mean bigger problems
- ◇ simultaneity and self-selection
- ◇ and they are bigger problems because no amount of control vars helps!
- ◇ simultaneity not only  $X \rightarrow Y$  but also  $Y \rightarrow X$ 
  - could do Granger causality or IV
- ◇ but best do an experiment, or natural experiment
- ◇ think deeply about the relationship between  $X$  and  $Y$
- ◇ one of the best ways to think deeply, i think, is to use INUS condition (res des sec)

## the bottom line

- ◇ the bottom line is that in experiment U/As are assigned to levels of X at random
- ◇ think about whether that is the case in your study (after controlling for other Xs)
- ◇ or at least if that's the case to large degree
- ◇ you want to think about selectivity and self-selection early in the process: at the research design stage
- ◇ think about **source of variability** in X
  - or data generating process as pol sci would put it

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## research design

- ◇ whether you have good or bad research design does not violate assumptions
- ◇ but it is critical for ability to argue causality
- ◇ causality is achieved with design, not with statistics (incl regression)!!
  - sure trying to get closer to it with multiple regressions, but cannot really get there with much confidence
  - indeed multiple regression results themselves (without design or at least much thought given to it), are about as good as an educated guess!!

## research design is a class itself

- ◇ research design is about designing your research
- ◇ i will just mention few things that will be important for this class
- ◇ a quick, useful and applied reference is  
<http://www.socialresearchmethods.net/kb/design.php>
- ◇ a more in-depth treatment is Lawrence B. Mohr, Impact Analysis for Program Evaluation  
[books.google.com/books?isbn=0803959362](http://books.google.com/books?isbn=0803959362)
- ◇ also see <http://knowledge.sagepub.com/view/researchdesign/SAGE.xml>
- guess have to be on campus to access it for free



## causality

- ◇ much of research design is about causality
  - want to show  $X \rightarrow Y$
- ◇ correlation is necessary for causality
  - (in rare cases suppressor var makes it unnecessary, eg (Mazur, 2011))
- ◇ but not sufficient
- ◇ <http://www.tylervigen.com/>

## INUS condition (Mackie, 1980)

- ◇ a useful way of thinking about causality:  
Insufficient but Non-redundant part of Unnecessary but Sufficient Condition
- ◇ many, if not most causes are INUS conditions
- ◇ eg a cigarette as a cause of forest fire
  - it's Insufficient, because by itself it is not enough, eg you also need oxygen, dry leaves, etc
  - it is contributing to fire, hence Non-redundant
- ◇ and along with other stuff (oxygen, dry leaves etc) it constitutes Unnecessary but Sufficient Condition
  - it's not necessary for fire, it can be lightning, etc
  - but it's sufficient – it's enough to start the fire

## basic concepts

- ◇ Y: a dependent variable, outcome
- ◇ X: an independent variable, predictor
  - (T: (treatment), like X)
- ◇ Z: some other variable
- ◇ want to show  $X \rightarrow Y$  (X affects (causes) Y)
  - and not the other way round ( $Y \rightarrow X$ )
  - and not  $Z \rightarrow Y$  ; eg X(CO<sub>2</sub>), Y(temp), Z(sun temp)
  - it is difficult to argue !
  - after all, there are unknown unknowns (Z's that we are unaware of)

## The Problem: Unknown Unknowns

- ◇ there are known knowns; there are things we know that we know
- ◇ there are known unknowns; that is to say, there are things that we now know we don't know
- ◇ but there are also unknown unknowns—there are things we do not know we don't know
- ◇ (Donald Rumsfeld)
- ◇ how do we deal with unknown unknowns?
- ◇ do an experiment!

## The Problem put another way: Counterfactual

- ◇ it all boils down to comparing what happened to what would have happened had the treatment not happened
- ◇ eg we got a new teacher and now kids perform better on SAT
  - to know whether the teacher caused better performance we would need to know what would have happened to SAT scores without this teacher (scores might have gone up due to Z),
  - and compare it to what actually happened

## The Problem put another way: Counterfactual

- ◇ the problem is that we do not observe counterfactual (we can try to infer it though)
- ◇ counterfactual is the effect of all knowns/unknowns (incl. unknown unknowns)
- ◇ how do we deal with lack of counterfactual
- ◇ do an experiment!
- ◇ (or if you cannot, try to estimate it somehow)

## the gold standard [ask IRB appr]

- ◇ the experimental design give few examples
- ◇ only with experimental design you can confidently argue causality
- ◇ and it is because randomization takes care of the known and unknown predictors of the outcome (draw a picture of 2 groups of people)
  - in other words, it establishes a counterfactual
- ◇ but wait !
  - most of the time we cannot have an experimental design because it is unethical and politically impossible  
eg we cannot randomly assign kids to bad school or to

## internal validity

- ◇ internal validity is about causality
- ◇ you have internal validity if you can claim that X causes Y
  - eg some drug X causes some disease Y to disappear
  - <http://knowledge.sagepub.com/view/researchdesign/n43.xml#n43>
  - <http://knowledge.sagepub.com/view/researchdesign/n192.xml#n192>



## threats to internal validity

- ◇ history, maturation, regression to the mean
  - something else happened that caused Y
  - things develop over time in a certain way
- ◇ selection bias, self selection
  - does smoking causes cancer ?
  - maybe less healthy people select to smoke ?
- ◇ <http://knowledge.sagepub.com/view/researchdesign/n192.xml#n192>

## spurious correlation

- ◇ you think that X causes Y, but actually it is Z
- ◇ global warming:
  - we have it—we can measure temperature
  - but what's the cause:  $CO_2$  or Sun activity?

## reverse causality

- ◇ a closely related topic to spurious correlation is reverse causality
- ◇ here, instead of some other  $Z$  that causes  $Y$  instead of  $X$
- ◇ we have  $Y$  causing  $X$ , as opposed to  $X$  causing  $Y$ ...
- ◇ what do we do ?

## reverse causality

- ◇ you may try to find some other  $X$  that measures the same or similar concept and that cannot be caused by  $Y$
  - ◇ eg instead of education  $\rightarrow$  wage; do father's education  $\rightarrow$  wage (your wage can reverse cause your education, but not your father's education)
  - ◇ find some exogenous (external) shock: policing  $\leftrightarrow$  crime
  - ◇ but terror attack/alert  $\rightarrow$  policing  $\rightarrow$  crime; we know that policing  $\rightarrow$  crime; not the other way round
- <https://www.law.upenn.edu/fac/jklick/48JLE267.pdf>

## natural experiment

- ◇ again most of the time you cannot have an experiment
- ◇ but there are natural experiments or exogenous shocks
- ◇ exogenous meaning that they are caused externally (like an experimenter's randomization) and somewhat randomly (at least with relation to a problem at hand)
  - eg earthquake (any weather, eg storm); terrorist attack; policy change (less random)
- ◇ in model simply have dummy for U/As affected storm, policy etc

## causality without experiment?

- ◇ yes! well maybe, but you need to do lots of work...
- ◇ essentially you want to exclude alternative explanations
- ◇ so you act like a devil's advocate...
- ◇ try to abolish your story / find an alt explanation
- ◇ if you cannot find any, then your story is right ...
  - until disproved
  - just use regression and “control” for other vars
- ◇ there are some designs that improve our inference greatly over having no design at all (ex post facto, observational)

## ex post facto: $X_1 Y_1$

- ◇ very common...it is \*no\* design
- ◇ non-experimental, cross-sectional, observational, correlational; you'll most likely do this
- ◇ we start investigation "after the fact"
- ◇ no time involved, don't know whether X precedes Y
- ◇ both, X and Y are observed at the same time **examples?**
  - (but X must precede Y in order to be causal)
- ◇ practically impossible to argue causality here
- ◇ but cheap and big N, and good external validity

## ex post facto: $X_1 Y_1$

- ◇ useful, many “causes” were discovered using observational studies
- ◇ eg smoking→cancer was found out using ex post facto
- ◇ and then confirm using better designs
- ◇ <http://knowledge.sagepub.com/view/researchdesign/n145.xml>
- ◇ <http://knowledge.sagepub.com/view/researchdesign/n271.xml#n271>



## **before-after (pre-post): blackboard: schematic**

- ◇ measured Y, then do X, and then measured Y again
- ◇ eg measured readership at the library , buy some cool stats books ; measured readership again
- ◇ eg measured crime rate , put more police on the streets ; measured crime again
- ◇ eg measured soup consumption , changed soup ; measured soup consumption again
- ◇ anyone did pre/post? eg working at school?
  - tried new programs, new approaches?
  - or simply pre-post without T, say to identify highest and lowest gain students

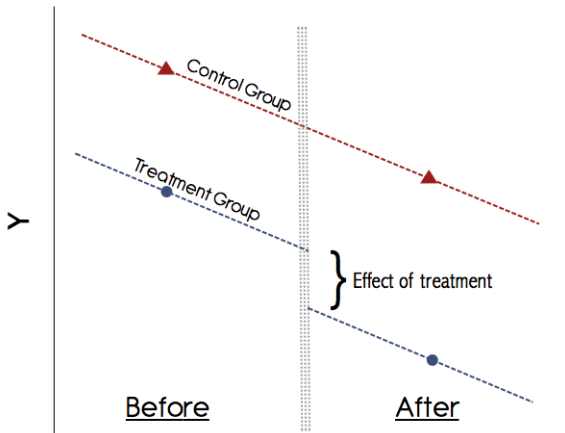
## (2 group) comparative change: $\frac{Y_{E1}X_2Y_{E3}}{Y_{C1}Y_{C3}}$

- ◇ eg  $H_0$  : police with better guns fights crime better
- ◇ measured crime rate in 2010 in Camden ( $Y_{E1}$ ) and Newark ( $Y_{C1}$ )
  - in 2011 give super guns to police in Camden ( $X_2$ ), (but not in Newark)
  - in 2012 measured crime rate Camden ( $Y_{E3}$ ) and Newark ( $Y_{C3}$ )
- ◇ if crime rate dropped more in Camden than in Newark, then we have evidence that the guns worked
- ◇ stata: see so called DID <http://www.princeton.edu/~otorres/DID101.pdf>

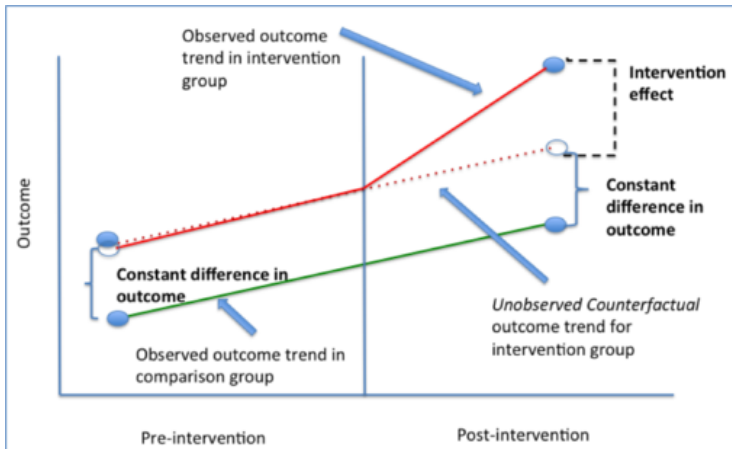
## difference in difference (p.235 Wheelan, 2013)

- ◇ just 'before after' with a comparison group
- ◇ did sth to one group, and not to the other group
  - over time (pre post) see if there is any difference
- ◇ like we discussed earlier in res\_des.pdf
- ◇ blackboard: fig: first from p236, and then from p237
  - and pictures similar to those from res\_des.pdf follow

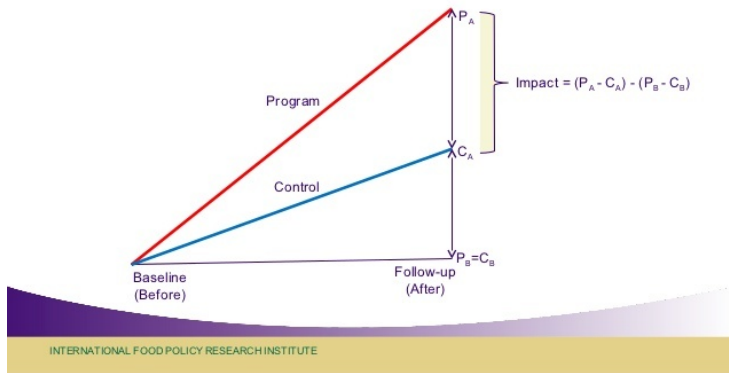
# DID



# DID



## Illustrating Difference-in-Difference Estimate of Average Program Effect



## discontinuity analysis (p.238 Wheelan, 2013)

- ◇ can use when there is some rigid cutoff for something, say:
  - remedial program for F grades
  - prison sentence for a crime
- ◇ then compare those who just made it (C-, or a ticket)
  - v those who didn't (F, prison)—but they were just above the cutoff
- ◇ the cool thing is that the two groups are similar, especially:
  - not really any difference whatsoever with respect to cause of treatment!
  - so the treatment is arbitrary (random), so we have experiment!

## example

- ◇ new jersey state government workforce profile 2010
- ◇ <http://www.nj.gov/csc/about/publications/workforce/pdf/wf2010.pdf>
- ◇ p37: minorities in state govt over time
- ◇ how increase internal validity?
- ◇ compare to PA, DE, NY etc
- ◇ factor in minority population; applications
- ◇ do experiments! many already done! again, read lit!!
  - say people with black names apply for jobs
  - students with Asian names email professors
- ◇ and both, employers and professors discriminate against!



**eg: tacit knowledge is the key!**

- ◇ if you know sth about state govt
  - you know that it is concentrated in Trenton
  - (one student said so)
- ◇ hence, the key is population characteristics
  - around Trenton!

## next step

- ◇ if you are interested in program evaluation:
  - quick <http://www.socialresearchmethods.net/kb/evaluation.php>
  - in-depth, advanced: Mohr (1995), Shadish et al. (2002)

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## Nick's modeldiag

- ◇ `http:`  
`//www.stata-journal.com/sjpdf.html?articlenum=gr0009`
- ◇ `dofile:modeldiag`

## ucla diagnostics

◇ https:

`//stats.idre.ucla.edu/stata/webbooks/reg/chapter2/  
stata-webbooksregressionwith-statachapter-2-regression-d`

◇ most useful:

- `scatter dfbeta ...`
- `lvr2plot, ml()`
- `avplot(s)`

◇ you should always do these in your research

◇ may also want to transform variables if needed: 1.5  
transforming variables https:

`//stats.idre.ucla.edu/stata/webbooks/reg/chapter1/  
regressionwith-statachapter-1-simple-and-multiple-regres`

◇ and see **help regress postestimation**

[\*] more diagnostics

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- MAZUR, A. (2011): "Does increasing energy or electricity consumption improve quality of life in industrial nations?" Energy Policy, 39, 2568–2572.
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- SORENSEN, J. B. (2012): "Endogeneity is a fancy word for a simple problem," Unpublished.
- WHEELAN, C. (2013): Naked statistics: stripping the dread from the data, WW Norton & Company.