

# regression

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## outline

intuition of inference (inferential statistics)

multivariate ols: intuition

wages example

interpretation and practice

violations (Wheelan, ch12)

## ps3, ps4

- everyone saw individual comments on canvass, rt?
- yes lit rev can be humbling; out of sudden you'll realize how much is out there and how much you didnt know
- have bigger font, not more than like 12 lines per slide!
- can get housing prices at census tract and over-time
- around philly affordable! eg room for \$500
- no experiment unless random assignment to treatment!!!
- avoid data collection/irb bureaucracy; just download it  
<https://www.icpsr.umich.edu/web/pages/ICPSR/ssvd/>

- review INUS, most people screwed it up
- N: it is not Necessary, but Non-redundant! nothing on its own is Necessary (if anything along with other stuff)
- remember lit rev
  - <https://theaok.github.io/generic/howToGoogSch.html>
- still pretty much everyone summarizes, not synthesizes

## old: ps3/ps4

- overwhelmed, all over the place—normal!! again 3 bulletpoints res\_des.pdf; and build on some published study, just add little from yourself
- get hands dirty with data! enough of plans and outlines, just do it! if you keep on just planing/outlining, you'll keep on going in circles and confusisng/overwhelming yourself
- or if you just do literature review, and no study, then just say it, and just do it as well
- be clear about what YOU are doing, not about what we remotely know about the topic, what other did
- background info is cool, but cut to the chase asap!

## old: ps3/ps4

- lit review is always critical!
- sometimes it is all that you'll do in this class
- need to be comprehensive, ideally 50+ studies
- again, need to synthesize/criticize, tell a story, have a value added from YOU; not just summarize
- refer to <http://theaok.github.io/generic/howToGoogSch.html>
- the goal of the lit rev is not just to get to know
- it is to build foundation for your study, to find out the gap, that your study will fill
- again, be rather modest, take a little step ahead, not save the world

old: ps3/ps4

- ideally find a study or few studies you really like and just replicate adding little twist from yourself, maybe just for locality, maybe just update with recent data, focus and elaborate on specific angle
- again, try to find a lit review published—saves time, does much of work for you in one paper!

- many people talk about experiments that are not!! need random assignment!! (and it needs to be feasible/ethical)
- intervention or treatment without random assign fine, can still do before/after but don't call it experiment!!
- experiment: a specific design of random assignment to treatment; not a synonym for any study or research as in colloquial everyday language
- lets discuss, give me several examples
- nobody will conduct experiment (IRB, time consuming, etc), but you can plan one for future



## old: ps3/ps4

- it always helps to define precisely your X, Y, U/A !!
- internal and external validities—specifically about causality and generalizability—should have been more specific and answer the question more directly
- external validity: need to say if sample was random!
- internal validity: discuss some threats
  - really need experiment or at least a quasi experiment
- don't say increased, large etc—use numbers, esp graphs, be specific!
- INUS again: first be clear  $X \rightarrow Y$  !, and then how is X: I,N,U,S (spell out!)—someone give a good example?

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multivariate ols: intuition

wages example

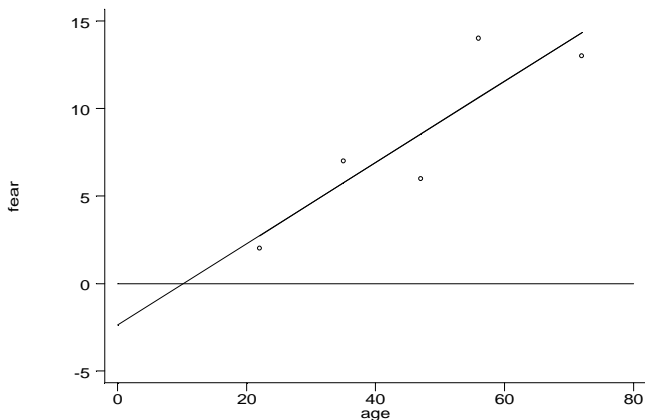
interpretation and practice

violations (Wheelan, ch12)

## finding answers

- got hypothesis?
- now it's time to analyze the data
- inference: making inferences from data
- this is what we want to know after all!
- just use regression and “control” for other variables  
[elaborate later]
- we have research questions, turn them into hypotheses
  - (a brief clear testable statement)
- say have a survey measuring people's fear of crime (0-15)
  - H1: fear of crime increases with age

## example: age and fear



●  $\hat{Y}_i = \hat{\beta}_1 + \beta_2 X_i = -2.365 + .232X_i$

○ eg pre fear at 40yo

## examples

- the regression advantage: use multiple vars at once  
eg life expectancy <https://www.blueprintincome.com/tools/life-expectancy-calculator-how-long-will-i-live/>

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## multivariate OLS

- multiple (multivariate) reg: very common tool in soc sci
- finds effect of a var of interest (X) on the dependent var (Y) **controlling/holding constant other vars**
- a stat trick that makes it as if sample equal on all Xs controlled for; imitates experimental setting (randomization)
  - again, in experiment you randomize into treatment and control groups so that both groups are on average the same and then we apply treatment (e.g. drug) to treatment group and see if had effect as compared to control group

## multivariate OLS

- most of the time cannot do experiment:
  - tell some people to smoke and some not
  - give college to some and not others
- but can use regression!
- eg: study effect of education ( $X$ ) on income ( $Y$ )
  - but it may not be the same for males and females?
  - just control for gender in regression
- and the effect is as if everybody had the same gender!



# multivariate OLS

- $X \rightarrow Y$  can say that X affects Y
- $Y = f(X)$  or: Y is a function of X (same thing)
- $Y = f(X_1, X_2, \dots, X_n, u)$
- in soc sci **always** many Xs

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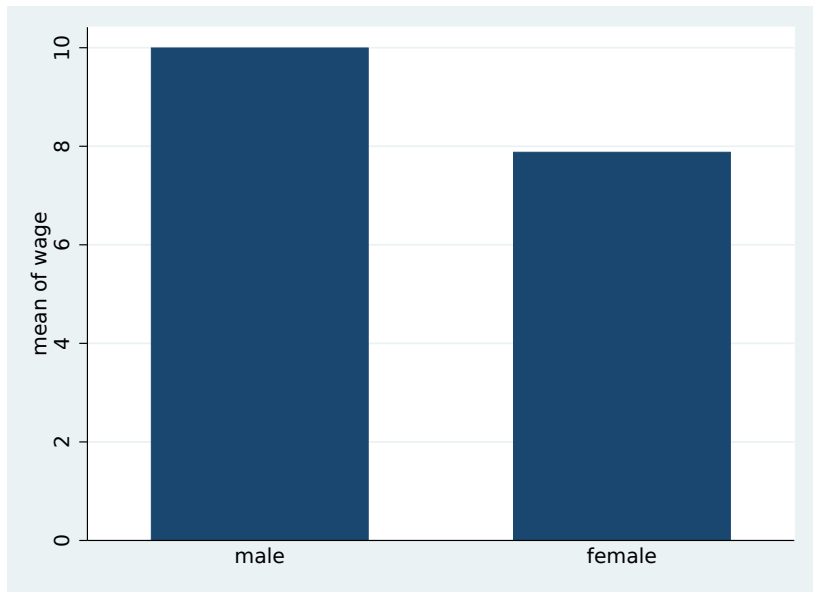
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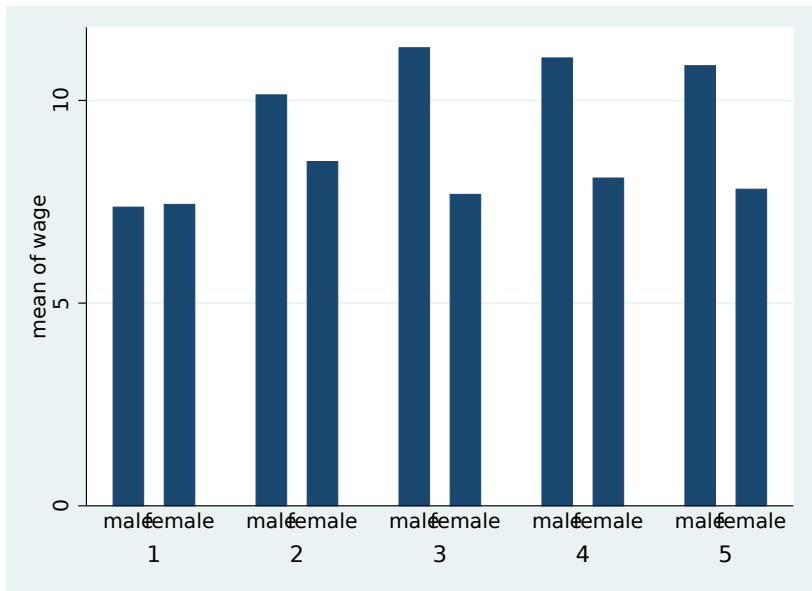
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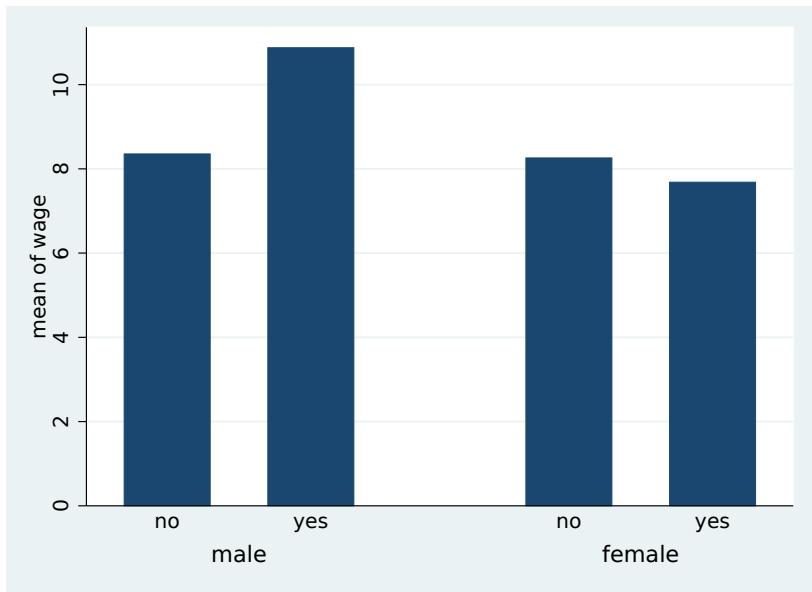
## wages (never do reg w/o des sta)



## wages by quintile of experience



## wages by marital status and gender



## descriptive stats



| Variable    | Obs | Mean  | Std. Dev. | Min | Max  |
|-------------|-----|-------|-----------|-----|------|
| -----+----- |     |       |           |     |      |
| wage        | 534 | 9.02  | 5.1       | 1   | 44.5 |
| educ        | 534 | 13.01 | 2.6       | 2   | 18   |
| exp         | 534 | 17.82 | 12.3      | 0   | 55   |

|             |  |      |       |      |
|-------------|--|------|-------|------|
|             |  | wage | educ  | exp  |
| -----+----- |  |      |       |      |
| wage        |  | 1.00 |       |      |
| educ        |  | 0.38 | 1.00  |      |
| exp         |  | 0.08 | -0.35 | 1.00 |

## interpreting coefficients

- pretty much only one way to interpret reg correctly
- 1 unit (\$ % etc) increase in  $X$  leads to  $\beta$  unit (\$ % etc) increase/decrease in  $Y$  ( $> 1X$ : remember ceteris paribus!)
- and as per Wheelan ch11: focus on:
  - sign
  - size
  - significance:
    - t-stat,  $t = \text{coeff}/\text{se}$ , sig if  $|t| > 2$
    - $p$  is prob of getting this result or larger if no assoc (Wheelan p198), sig if  $p < .05$
    - $95\%CI = \pm 2 * se$

## multivariate ols



| wage        |  | Coef.    | Std. Err. | t     | P> t  |
|-------------|--|----------|-----------|-------|-------|
| -----+----- |  |          |           |       |       |
| educ        |  | .9188352 | .081526   | 11.27 | 0.000 |
| exp         |  | .0986602 | .0178812  | 5.52  | 0.000 |
| married     |  | .5704847 | .4357421  | 1.31  | 0.191 |
| _cons       |  | -5.07037 | 1.224631  | -4.14 | 0.000 |
| -----       |  |          |           |       |       |



## now let's turn to cars!

- let's say we want to explain price with mpg and weight
- research Q: fuel efficient cars are actually cheaper
- hypothesis: the higher the mpg, the lower the price

●

●



## interpret: $\beta$ , p, t, CI; predict price for 10mpg

•

| price       |  | Coef.    | Std. Err. | t     | P> t  | [95% Conf. Interval] |
|-------------|--|----------|-----------|-------|-------|----------------------|
| -----+----- |  |          |           |       |       |                      |
| mpg         |  | -49.5186 | .15       | -0.57 | 0.567 | -221, 122            |
| weight      |  | 1.746    | .64       | 2.72  | 0.008 | .46, 3               |
| _cons       |  | 1946     | 3597      | 0.54  | 0.590 | -5226, 9118          |
| -----       |  |          |           |       |       |                      |

## predicted values (p200 Wheelan, 2013)

- $\text{weight} = -118 + 4.3 * (\text{height in}) + .12 * (\text{age}) - 4.8 * (\text{female})$
- 53yo female who is 5'5:
  - $-118 + (4.3 * 65) + (.12 * 53) - (4.8 * 1) = 163$
- 35yo male who is 6'3:
  - $-118 + (4.3 * 75) + (.12 * 35) - (4.8 * 0) = 209$
- remember life expectancy game? same thing!!
- banks, insurance companies, etc
  - use such models to predict if you pay debt, die, etc
  - and hence how risky you are, and what's the price

## a “complete” explanation

- $wage = f(\text{native ability, education, family background, age, gender, race, height, weight, strength, attitudes, neighborhood influences, family connections, interactions of the above, chance encounters, ...})$
- multiple regression will tell you the effect of one variable while controlling for the effect of other variables (again, as if everybody was the same on other vars)
- $wage_i = \beta_1 + \beta_2 X_{2i} + \beta_3 X_{3i} + \dots + \beta_n X_{ni} + u_i$

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## practice regressions interpretations

- Happy Tourists, Unhappy Locals <http://link.springer.com/article/10.1007/s11205-016-1436-9>

## do scatterplots

- it is useful to produce a scatterplot
  - you'd see outliers
    - and whether the relationship is due to them
  - **blackboard**: relationships biased due to outliers
  - say marriage rate and divorce rate across states



## think about it

- always interpret results!
- give it some thought
- ask yourself whether results make sense and why
- think about measurement and what it means
  - eg does marriage cause divorce or sth about NV?
- and as always, remember design principles:
  - INUS condition
  - threats to validity
- and note that in addition to regression
  - it is critical to have theory/logic/mechanism
  - see Wheelan (2013, p207)

## Wheelan in ch11 mentions Whitehall studies

- fascinating stuff!
- high status causes better health!
- great book 'Status Syndrome' <http://a.co/jaUwT7>
- say nobel prize or oscar boosts one's health and longevity
- these successful folks live longer and in better health
- than exact same people (income, lifestyle, etc) but without status

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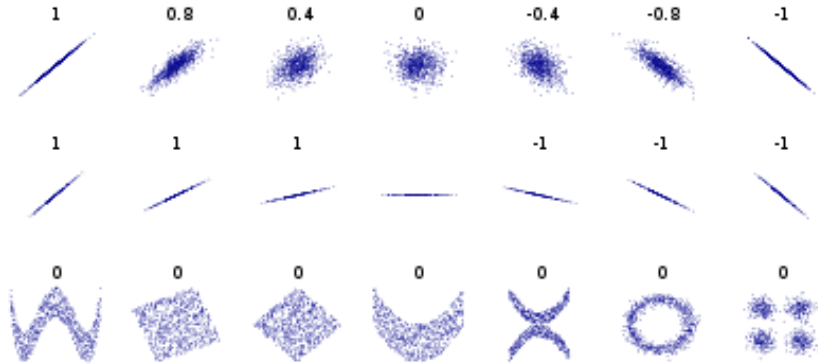
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## don't kill with regressions (p212 Wheelan, 2013)

- tens of thousands of females killed or made sick with estrogen, because regressions showed estrogen was good
- regression estimates are never causal by themselves!
- remember the gold standard: experiment!
- again, INUS, unknown unknowns,  $\text{corr} \neq \text{causation}$ , etc

## nonlinear relationships



- like corr, won't detect nonlinear relationships!
- example of nonlinear rel? extra credit!

## what to do about nonlinear rel?

- just break it up into subsets/subsamples! dig deeper!
  - say for males and females separately
  - say for low and hi val separately
- that's a quick way to see nonlinear relationship!
- eg it may first rise and then fall

## reverse causality (p216 Wheelan, 2013)

- more lessons—  $\rightarrow$  bad golf, or
- bad golf—  $\rightarrow$  more lessons
- solution:
  - lag variable: bad golf last month—  $\rightarrow$  more lessons now
  - use exogenous shock—remember from res\_des.pdf:
  - (terrorist attack—  $\rightarrow$ ) policing—  $\rightarrow$  crime
- or think about it! miserable people choose cities?
- then i looked at only people who were born in urban/rural

## omitted variable bias (p217 Wheelan, 2013)

- golf— > heart disease and cancer?
- control for age!
- age is killing people, not golf!



## extrapolate beyond data (p220 Wheelan, 2013)

- only interpret within range of data!
- remember regression of fear on age?
- and reg line hits y-axis at -3

## data mining (p221 Wheelan, 2013)

- if you torture your data enough, it will confess
- likewise, if you throw enough variables, will find significant relationships
- remember: you need theory, causal mechanism/path, story!

LEVITT, S. D. AND S. J. DUBNER (2010): Freakonomics, vol. 61, Sperling & Kupfer.

WHEELAN, C. (2013): Naked statistics: stripping the dread from the data, WW Norton & Company.