



Student Name: \_\_\_\_\_

Reg. No: \_\_\_\_\_

Course Title: Differential Equations

Course Code: \_\_\_\_\_

Course Instructor: Fatima Asif

Exam Type: Assignment # 4

Q.1) Compute Transforms Directly

- $t^2$
- $e^{-5t}$
- $\sinh 3t$

Use Properties and Basic Transforms to find Laplace Transform of the following:

- $\sin(5t + 2)$
- $e^{-t} \sin 2t$
- $t \sin t$

Find Inverse Laplace Transform

- $\frac{s-2}{s^2+3}$
- $\frac{3}{s(s^2+4)}$

Solve the initial value problems

- $y'' + 2y' + 5y = 0, y(0) = 1, y'(0) = 1$
- $y'' + 9y = \sin 3t, y(0) = 1, y'(0) = 0$

Q.2) Can the following IVP be solved using Laplace Transform? Explain your answer.

$$2y''' + 3y'' - 3y' - 2y = e^{-t} ; \quad y(0) = 0 ; \quad y'(0) = 0 ; \quad y''(1) = 2$$

If **yes**, then solve it. If **no**, then fix the problem and solve it.

Q.3) Solve the following differential equation using power series.

- $y'' - xy = \sin x$
- $y'' - xy = x^2 ; \quad y(0) = 1, y'(0) = 0$