

- See Chandru Grading Comments from 11/4/23 below

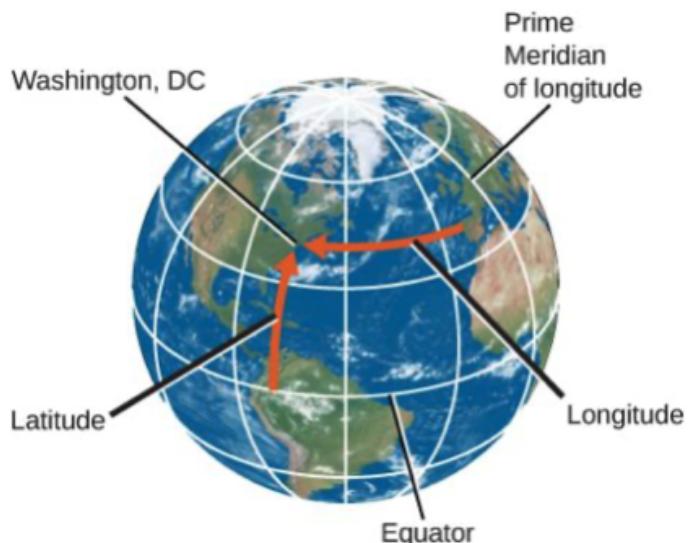
1. Nice work!

- ✓ You have a 100% grade on this notebook

- ✓ Correct Any Errors identified above for an improved grade

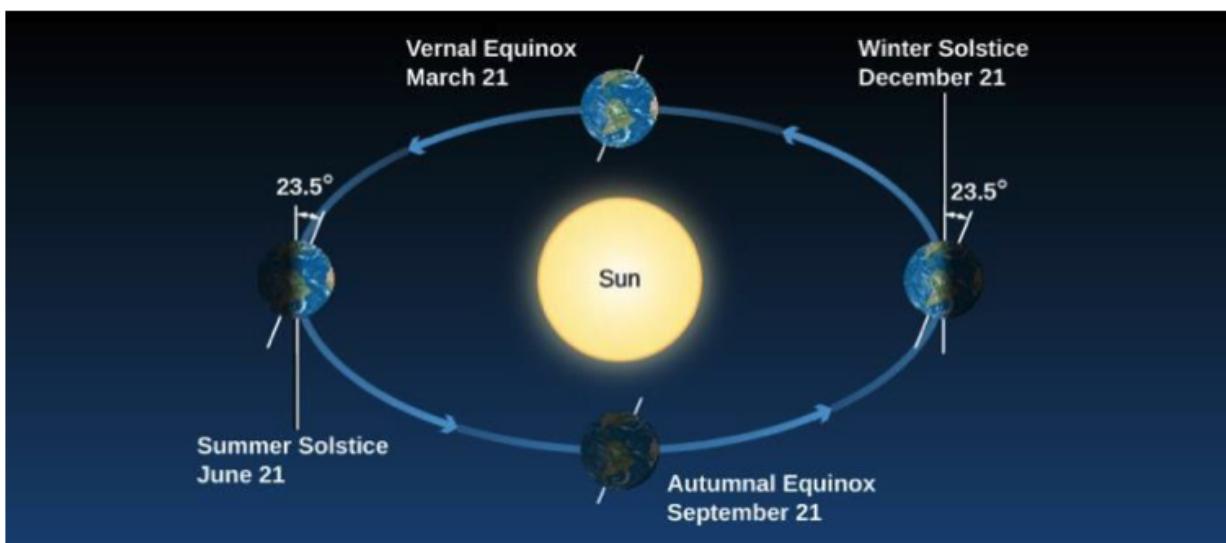
Earth Seasons and Sun Angle Calculations for Seattle and other cities for a given date

FIGURE 4.2



Latitude and Longitude of Washington, DC. We use latitude and longitude to find cities like Washington, DC, on a globe. Latitude is the number of degrees north or south of the equator, and longitude is the number of degrees east or west of the Prime Meridian. Washington, DC's coordinates are 38° N and 77° W.

FIGURE 4.5



Seasons. We see Earth at different seasons as it circles the Sun. In June, the Northern Hemisphere “leans into” the Sun, and those in the North experience summer and have longer days. In December, during winter in the Northern Hemisphere, the Southern Hemisphere “leans into” the Sun and is illuminated more directly. In spring and autumn, the two hemispheres receive more equal shares of sunlight.

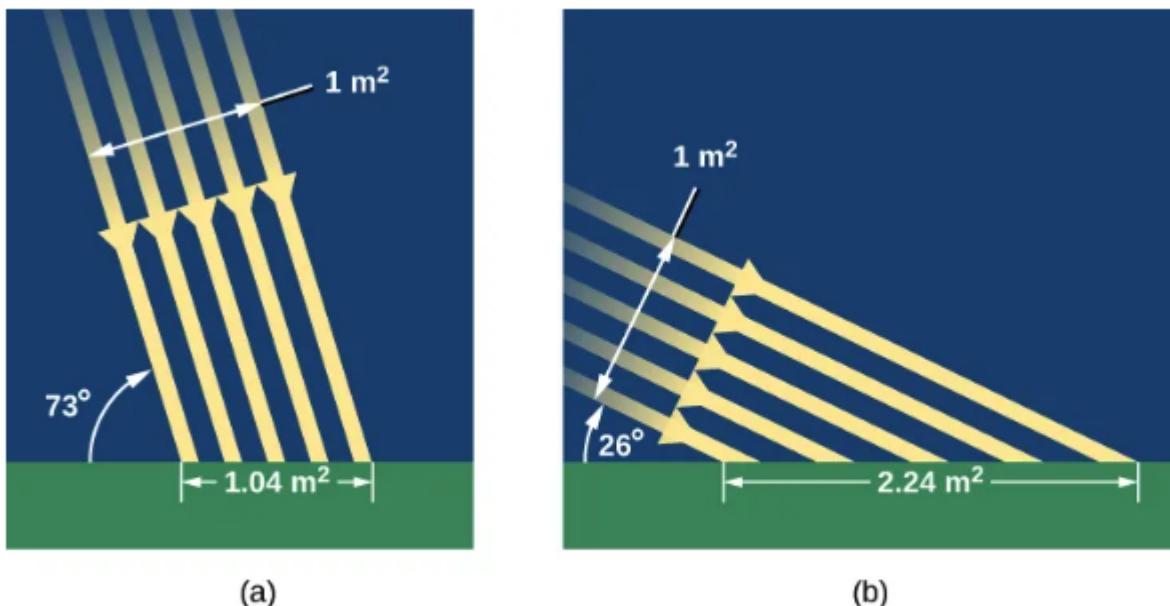
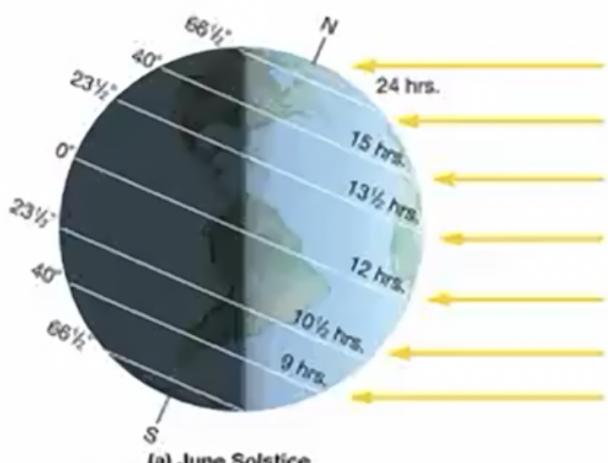
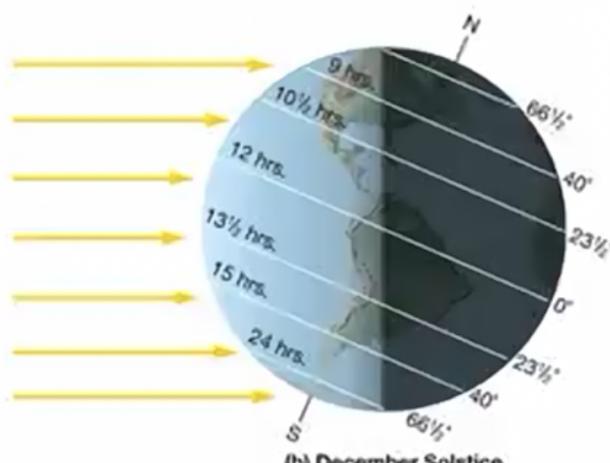


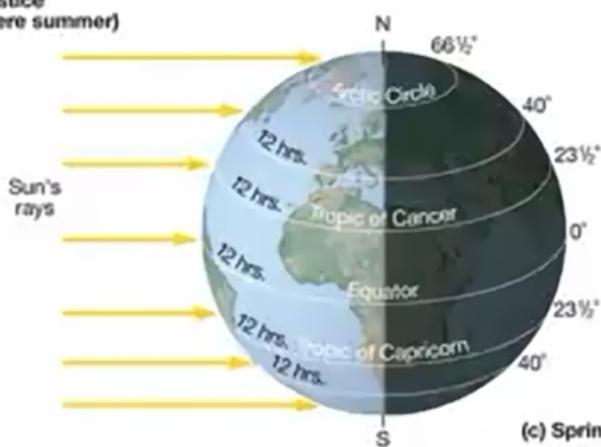
Figure 4.6 The Sun's Rays in Summer and Winter. (a) In summer, the Sun appears high in the sky and its rays hit Earth more directly, spreading out less. (b) In winter, the Sun is low in the sky and its rays spread out over a much wider area, becoming less effective at heating the ground.



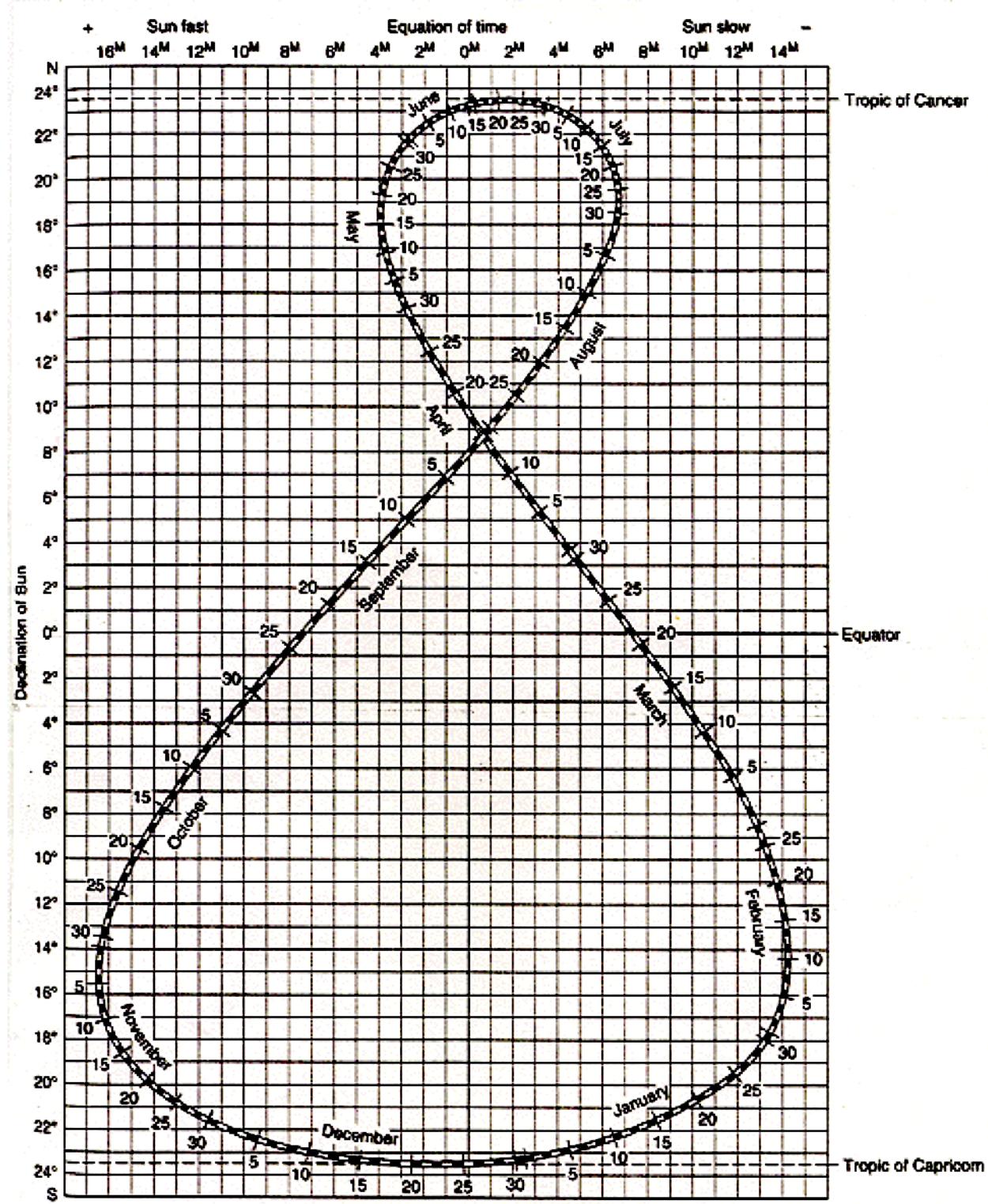
(a) June Solstice
(Northern Hemisphere summer)



(b) December Solstice
(Northern Hemisphere winter)



(c) Spring/Fall Equinox



The analemma. Data courtesy of U.S. Coast and Geodetic Survey.

Analemma by US Coast and Geodetic Survey

Data:

Location: 40° N

Date: December 22

Location of 90° Sun: $23\frac{1}{2}^{\circ}$ S
Sun is directly Overhead at this Latitude

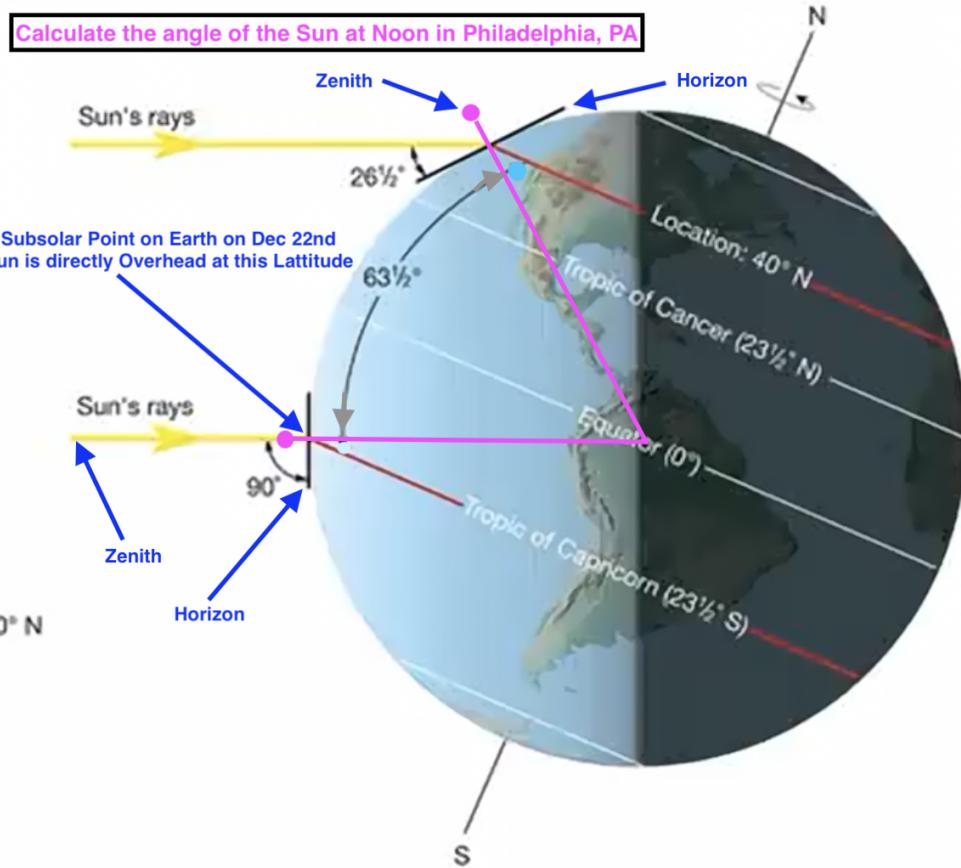
Calculations:

Step 1:

Distance in degrees between
 $23\frac{1}{2}^{\circ}$ S and 40° N = $63\frac{1}{2}^{\circ}$

Step 2:

$$\frac{90 - 63\frac{1}{2}^{\circ}}{26\frac{1}{2}^{\circ}} = \text{Noon Sun angle at } 40^{\circ} \text{ N on December 22}$$



Sun Angle Calculator: Repeat tasks 1, 2 & 3 above for calculating Sun Elevation at:

- Philadelphia at Winter Solstice in the Northern Hemisphere (See above)
- Seattle on Autumnal Equinox in the Northern Hemisphere (Complete in-class)
- An Equatorial city of your choice at Autumnal Equinox
- Stockholm at Winter Solstice in the Northern Hemisphere
- Sydney at Summer Solstice in the Southern Hemisphere
- A city of your choice in the Tropic of Capricorn at Vernal Equinox

A. Calculate Sun's Altitude in Philadelphia, PA on Dec 22nd which is the Winter Solstice in Northern Hemisphere

TASK 1: Let's store the Latitude and Longitude of Philadelphia below in decimal degrees for computing

Philadelphia Latitude: $39^{\circ} 57' 9.3''$ N Philadelphia Longitude: $75^{\circ} 9' 54.8''$ W

- Note: North Latitudes are considered Positive and South Negative

- Note: East Longitudes are considered Positive and West Negative

Philadelphia Latitude = 39.95 degrees

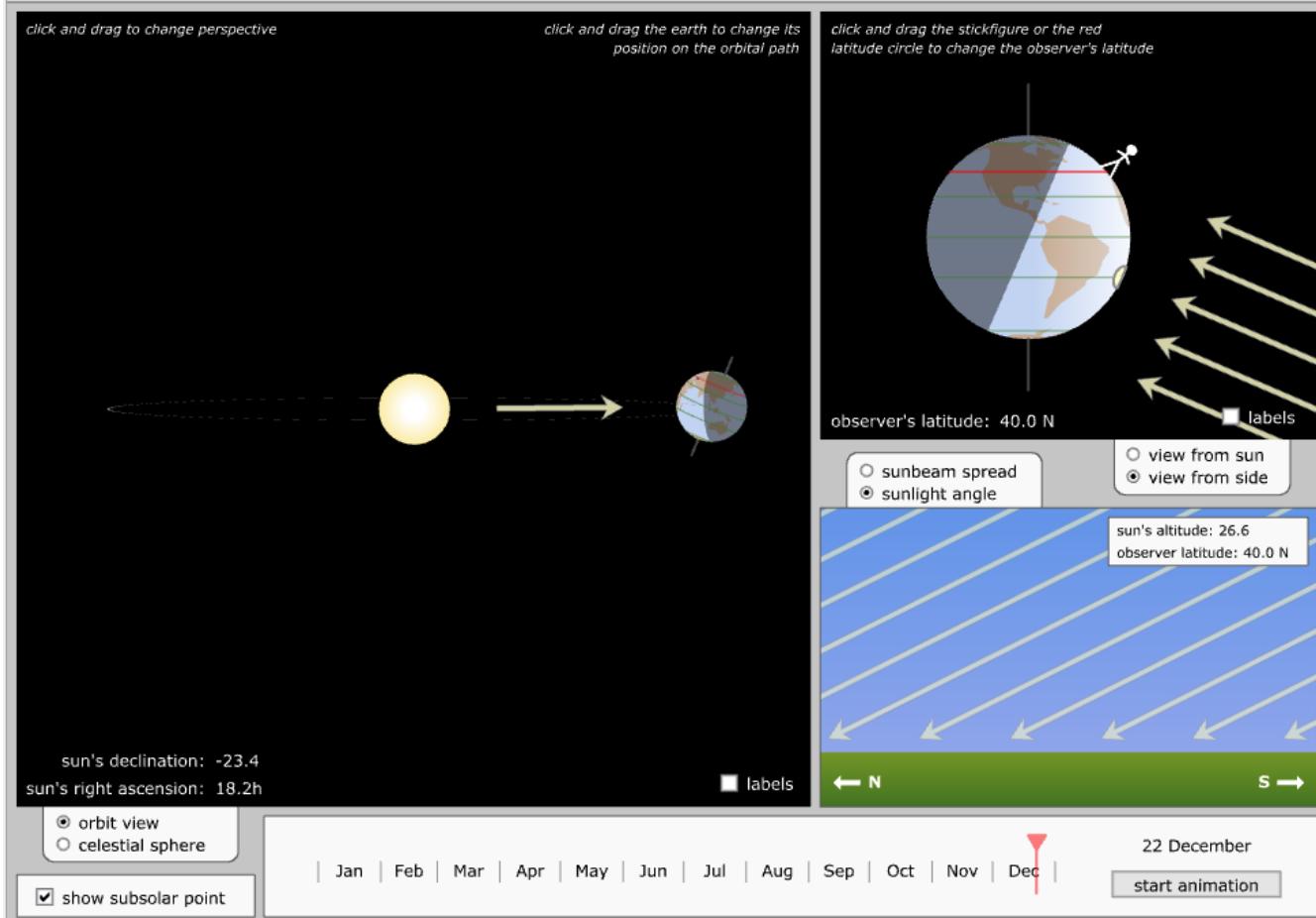
Philadelphia Longitude = -75.17 degrees

TASK 2: Let's calculate the altitude of the Sun above the horizon in Philadelphia at Winter Solstice in the Northern Hemisphere

1. To do this we first need ***Philadelphia's latitude which is calculated above to be +39.95***
2. We then need the ***latitude of the sub-solar point*** on Earth on Dec 22nd. In other words, this is the latitude at which the Sun is directly overhead.
3. At Winter Solstice in NH, Sun is directly overhead any city on the Tropic of Capricorn. At other dates, we can refer to the Analemma chart above.
4. The ***latitude of the sub-solar point is -23.5 deg*** as read from the Analemma chart
5. We then find the ***angular separation or angular distance between these two latitudes***
6. Finally the ***Sun Altitude*** or Sun Elevation above the horizon on Dec 22nd is calculated to be ***90 - angular distance*** for locations in NH and ***90 + angular distance*** for locations in SH

Sun Altitude in Philadelphia at Winter Solstice (Dec 22nd) = 26.55 deg

TASK 3: Using the [Seasons Simulator linked here](#) snapshot a picture of the summer solstice in the Northern hemisphere. Validate the computer Sun Altitude with your calculation above within 5% accuracy.



Percent Error in calculating Sun Altitude = 0.20%

B. Calculate Sun's Altitude in Seattle, WA on Sep 21

TASK 1: Let's store the Latitude and Longitude of Seattle below in decimal degrees for computing

Seattle Latitude: 47° 7' N Seattle Longitude: 122° 2' W

- Note: North Latitudes are considered Positive and South Negative
- Note: East Longitudes are considered Positive and West Negative

Seattle Latitude = 47.12 degrees

Seattle Longitude = -122.03 degrees

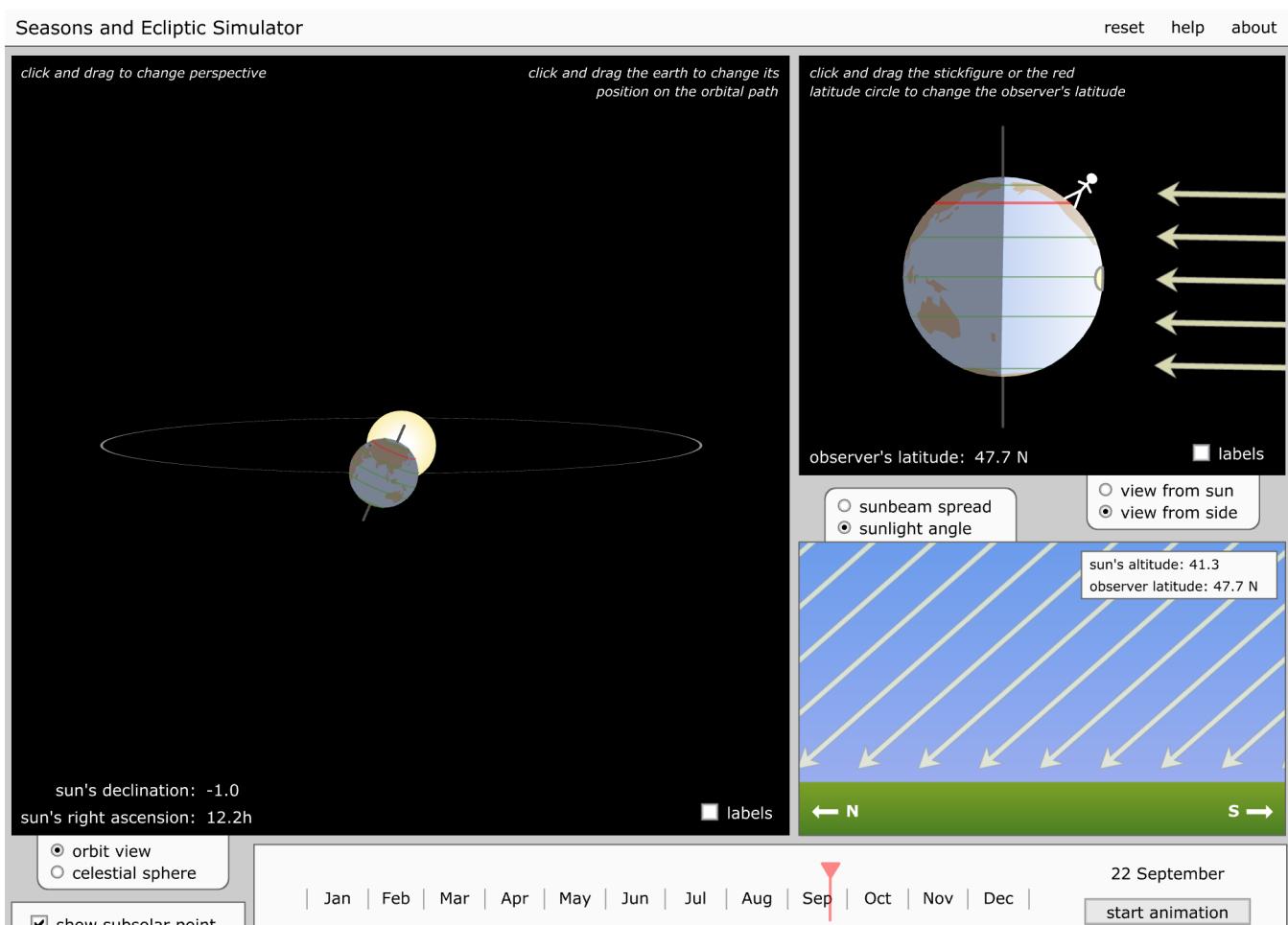
TASK 2: Let's calculate the altitude of the Sun above the horizon in Seattle at Autumnal Equinox in the Northern Hemisphere

1. To do this we first need **Seattle's latitude which is calculated above to be +47.12**
2. We then need the **latitude of the sub-solar point** on Earth on Sep 21st. In other words, this is the latitude at which the Sun is directly overhead.

3. Let's refer to the Analemma chart above for the subsolar point on Sep 21st.
4. The **latitude of the sub-solar point is +1 deg** as read from the Analemma chart
5. We then find the **angular separation or angular distance between these two latitudes**
6. Finally the **Sun Altitude** or Sun Elevation above the horizon on Dec 22nd is calculated to be **90 - angular distance** for locations in NH and **90 + angular distance** for locations in SH

Sun Altitude in Seattle at Autumnal Equinox = 43.38 deg

TASK 3: Using the Seasons Simulator linked here snapshot a picture of the summer solstice in the Northern hemisphere. **You can also get a more accurate value from the US Naval Observatory here.** Validate the computer Sun Altitude with your calculation above within 5% accuracy.



Percent Error in calculating Sun Altitude = 1.84%

C. Calculate Sun's Altitude in Cali, CO on the Autumnal Equinox

TASK 1: Let's store the Latitude and Longitude of Seattle below in decimal degrees for computing

Cali Latitude: 3.45° 7' N Cali Longitude: 76.5° 59'W

- Note: North Latitudes are considered Positive and South Negative
- Note: East Longitudes are considered Positive and West Negative

Cali Latitude = 3.57 degrees

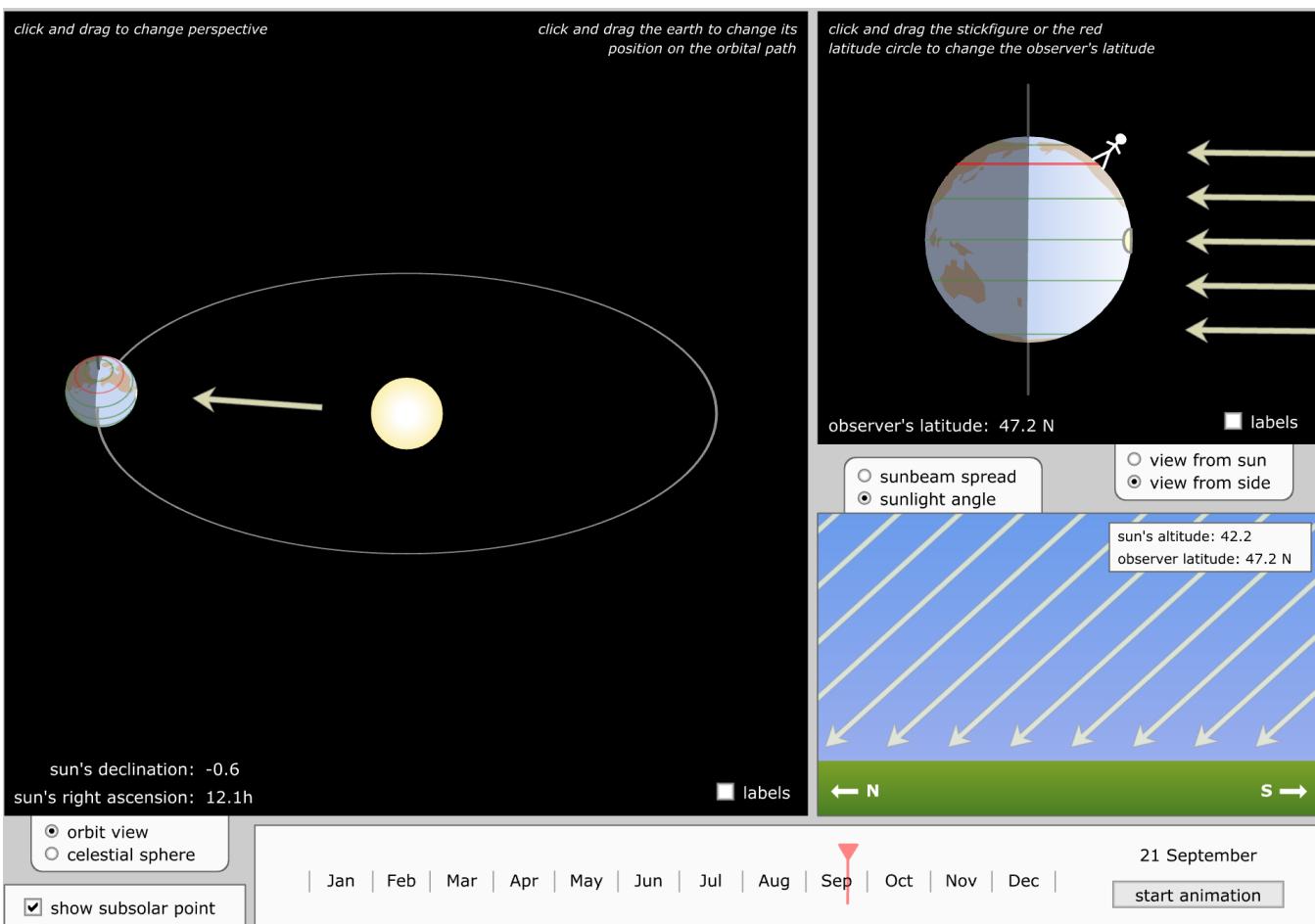
Cali Longitude = -122.03 degrees

TASK 2: Let's calculate the altitude of the Sun above the horizon in Cali at Autumnal Equinox

1. To do this we first need ***Seattle's latitude which is calculated above to be +47.12***
2. We then need the ***latitude of the sub-solar point*** on Earth on Sep 21st. In other words, this is the latitude at which the Sun is directly overhead.
3. At (Autumnal Equinox) in NH, ***Sun is directly overhead any city on the Equator. At other dates, we can refer to the Analemma chart above.***
4. The ***latitude of the sub-solar point is 1 deg*** as read from the Analemma chart
5. We then find the ***angular separation or angular distance between these two latitudes***
6. Finally the ***Sun Altitude*** or Sun Elevation above the horizon on Sep 21st is calculated to be ***90 - angular distance***

Sun Altitude in Cali at Autumnal Equinox (Sep 21nd) = 86.93 deg

TASK 3: Using the [Seasons Simulator linked here](#) snapshot a picture of the summer solstice in the Northern hemisphere. Validate the computer Sun Altitude with your calculation above within 5% accuracy.



Percent Error in calculating Sun Altitude = 2.80%

D. Calculate Sun's Altitude in Stockholm, SE on Dec 22nd which is the Winter Solstice in Northern Hemisphere

TASK 1: Storing Latitude and Longitude of Stockholm below in decimal degrees for computing

Stockholm Latitude: 59° 20' N Stockholm Longitude: -18° 3' W

- Note: North Latitudes are considered Positive and South Negative
- Note: East Longitudes are considered Positive and West Negative

Stockholm Latitude = 59.33 degrees

Stockholm Longitude = -18.05 degrees

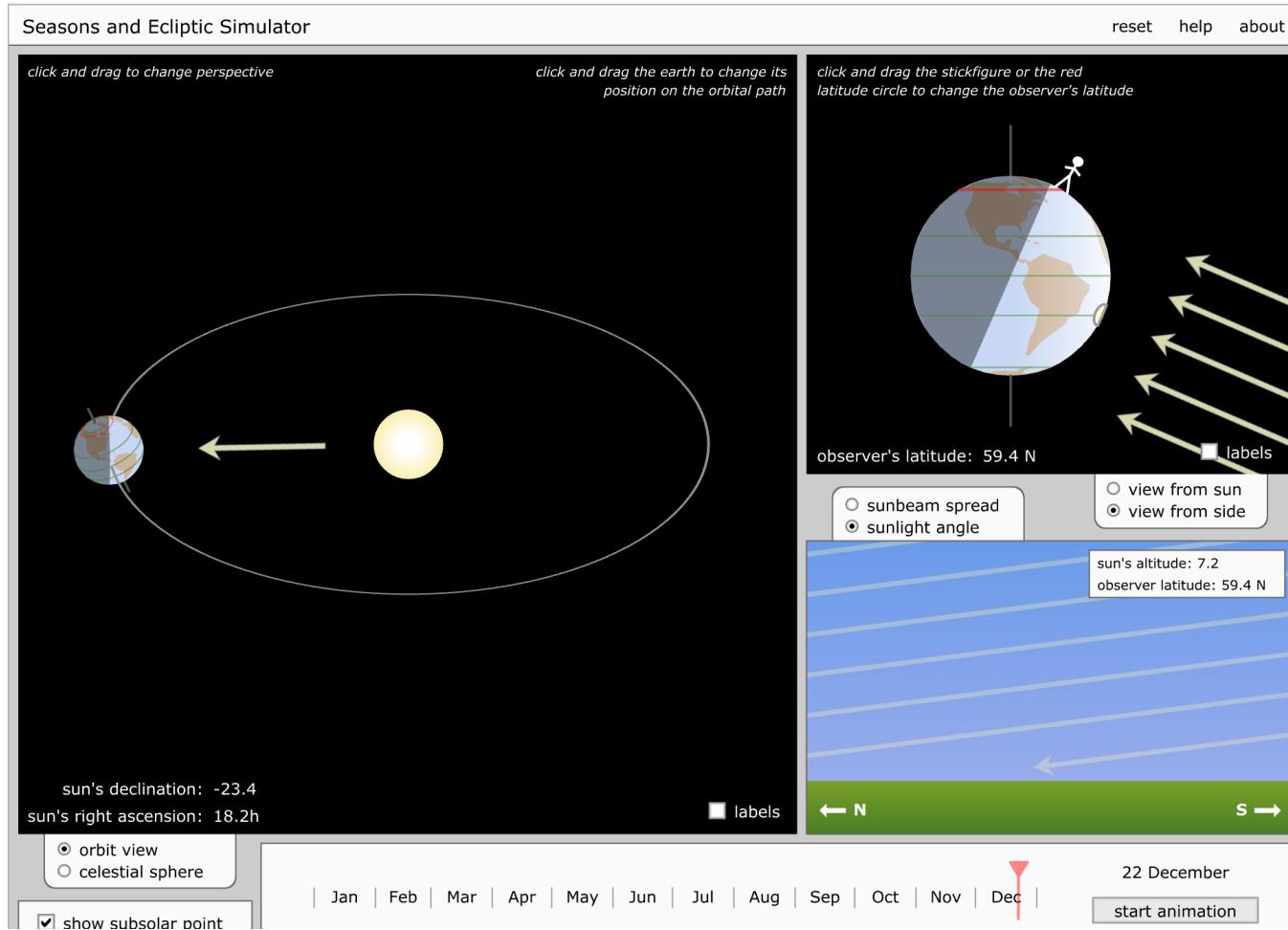
TASK 2: Let's calculate the altitude of the Sun above the horizon in Stockholm at Winter Solstice in the Northern Hemisphere

1. To do this we first need **Stockholm's latitude which is calculated above to be +59.33**
2. We then need the **latitude of the sub-solar point** on Earth on Dec 22nd. In other words, this is the latitude at which the Sun is directly overhead.

3. At Winter Solstice, Sun is directly overhead any city on the Tropic of Capricorn. At other dates, we can refer to the Analemma chart above.
4. The **latitude of the sub-solar point is -23.5 deg** as read from the Analemma chart
5. We then find the **angular separation or angular distance between these two latitudes**
6. Finally the **Sun Altitude** or Sun Elevation above the horizon on Dec 22nd is calculated to be **90 - angular distance** for locations in NH and **90 + angular distance** for locations in SH

Sun Altitude in Stockholm at Winter Solstice (Dec 22nd) = 7.17 deg

TASK 3: Screenshot of Seasons Simulator



Percent Error in calculating Sun Altitude = 0.46%

E. Calculate Sun's Altitude in Sydney, WA on Summer Solstice in the SH (Dec 21)

TASK 1: Let's store the Latitude and Longitude of Sydney below in decimal degrees for computing

Sydney Latitude: 33° 52' 11" S Sydney Longitude: 151° 12'30" E

- Note: North Latitudes are considered Positive and South Negative

- Note: East Longitudes are considered Positive and West Negative

Sydney Latitude = -33.87 degrees

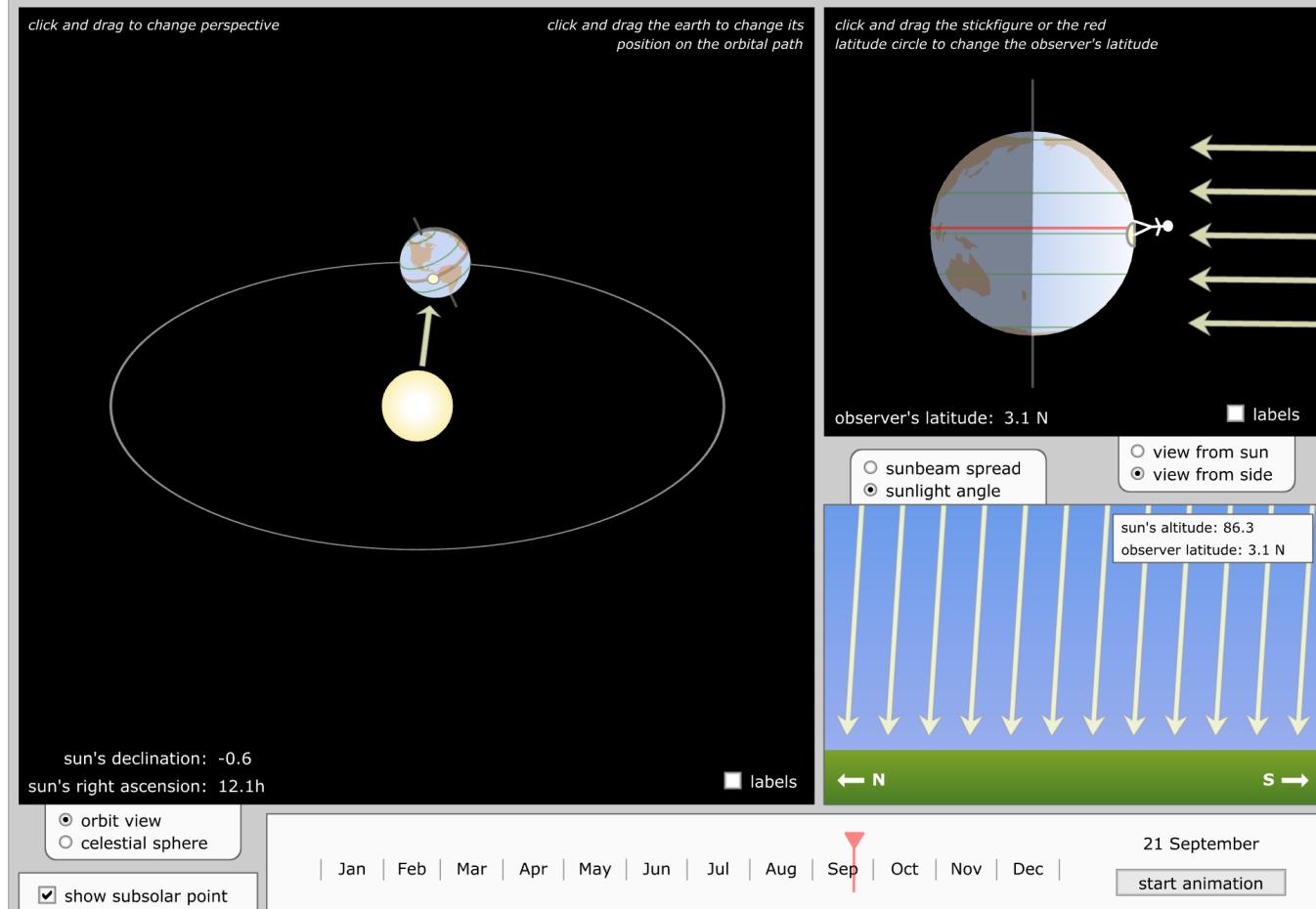
Sydney Longitude = 151.21 degrees

TASK 2: Let's calculate the altitude of the Sun above the horizon in Sydney at Summer Solstice in the Southern Hemisphere

1. To do this we first need ***Sydney's latitude which is calculated above to be -33.87***
2. We then need the ***latitude of the sub-solar point*** on Earth on Dec 21st. In other words, this is the latitude at which the Sun is directly overhead.
3. Let's refer to the Analemma chart above for the subsolar point on Dec 21st.
4. The ***latitude of the sub-solar point is -23.5 deg*** as read from the Analemma chart
5. We then find the ***angular separation or angular distance between these two latitudes***
6. Finally the ***Sun Altitude*** or Sun Elevation above the horizon on Dec 22nd is calculated to be ***90 - angular distance*** for locations in NH and ***90 + angular distance*** for locations in SH

Sun Altitude in Sydney at Summer Solstice in SH = 79.63 deg

TASK 3: Using the [Seasons Simulator linked here](#) snapshot a picture of the summer solstice in the Northern hemisphere. [You can also get a more accurate value from the US Naval Observatory here](#). Validate the computer Sun Altitude with your calculation above within 5% accuracy.



Percent Error in calculating Sun Altitude = 0.73%

F. Calculate Sun's Altitude in Alice Springs, AU on the Vernal Equinox(March 21)

TASK 1: Let's store the Latitude and Longitude of Alice Springs below in decimal degrees for computing

Alice springs(AS) Latitude: $23^{\circ} 42' \text{ N}$ * Alice springs(AS) Longitude: $-133^{\circ} 52' \text{ W}$ *

- Note: North Latitudes are considered Positive and South Negative
- Note: East Longitudes are considered Positive and West Negative

Alice Springs Lattitude = 23.70 degrees

Alice Springs Longitude = -133.87 degrees

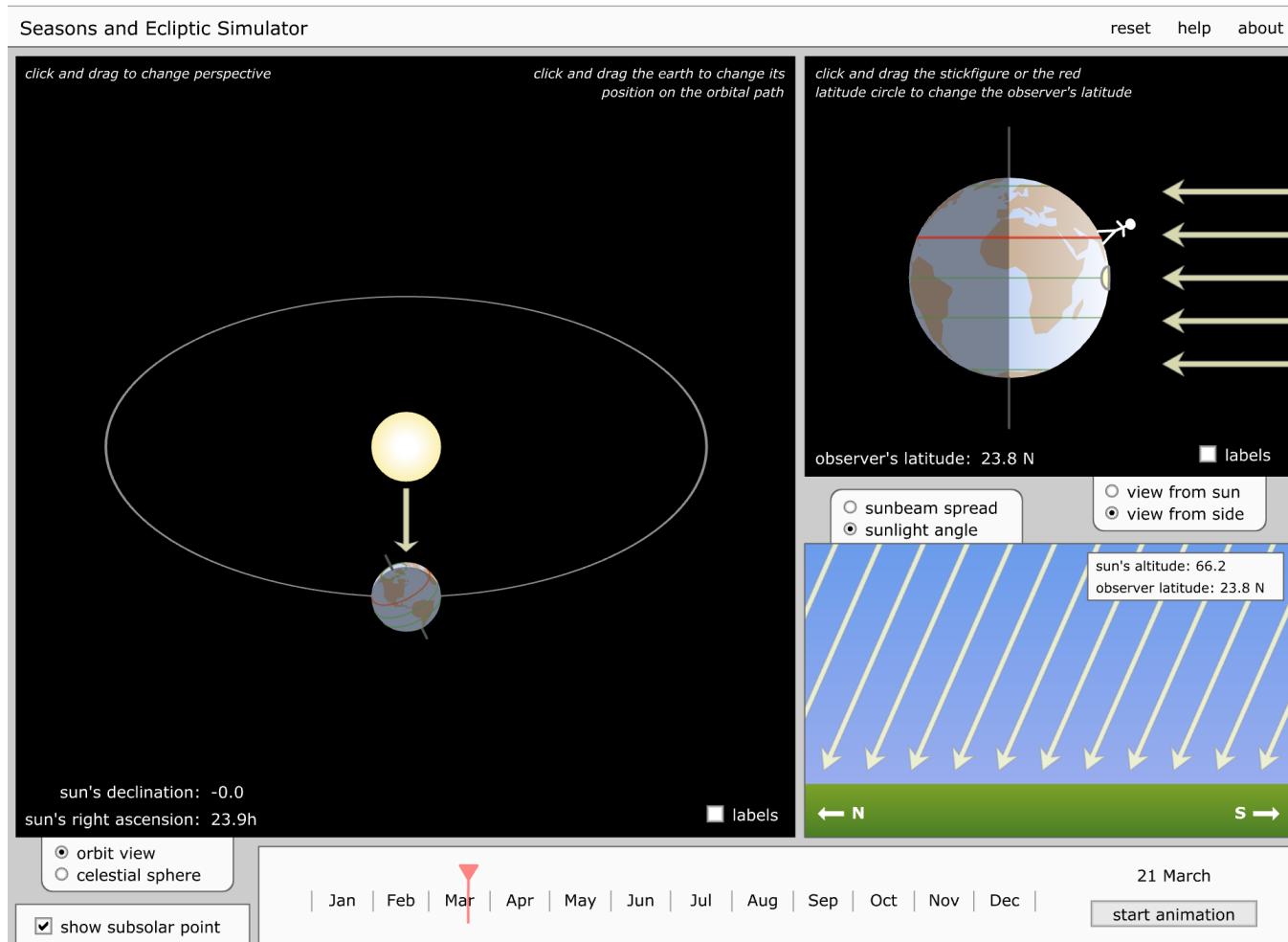
TASK 2: Let's calculate the altitude of the Sun above the horizon in Philadelphia at Winter Solstice in the Northern Hemisphere

1. To do this we first need **Philadelphia's latitude which is calculated above to be $+39.95$**

2. We then need the **latitude of the sub-solar point** on Earth on Dec 22nd. In other words, this is the latitude at which the Sun is directly overhead.
3. At Winter Solstice in NH, Sun is directly overhead any city on the Tropic of Capricorn. At other dates, we can refer to the Analemma chart above.
4. The **latitude of the sub-solar point is -23.5 deg** as read from the Analemma chart
5. We then find the **angular separation or angular distance between these two latitudes**
6. Finally the **Sun Altitude** or Sun Elevation above the horizon on Dec 22nd is calculated to be **90 - angular distance** for locations in NH and **90 + angular distance** for locations in SH

Sun Altitude in Alice Springs at Vernal Equinox(March 21) = 66.30 deg

TASK 3: Using the [Seasons Simulator linked here](#) snapshot a picture of the summer solstice in the Northern hemisphere. Validate the computer Sun Altitude with your calculation above within 5% accuracy.



Percent Error in calculating Sun Altitude = 0.15%