```
In [2]: import numpy as np
   import pandas as pd
   from sklearn.model_selection import train_test_split
   from sklearn.metrics import accuracy_score,confusion_matrix
   import matplotlib.pyplot as plt
```

In [3]: import pandas as pd
 #imported the dataset given to us
 pid=pd.read_csv("C:\\Users\\dhima\\anaconda3\\4rth week\\pima-indians-diabetes.cs
 #made a copy of the original dataset
 pid1=pid.copy()
 print(pid1)

	pregs	plas	pres	skin	test	BMI	pedi	Age	class
0	6	148	72	35	0	33.6	0.627	50	1
1	1	85	66	29	0	26.6	0.351	31	0
2	8	183	64	0	0	23.3	0.672	32	1
3	1	89	66	23	94	28.1	0.167	21	0
4	0	137	40	35	168	43.1	2.288	33	1
763	10	101	76	48	180	32.9	0.171	63	0
764	2	122	70	27	0	36.8	0.340	27	0
765	5	121	72	23	112	26.2	0.245	30	0
766	1	126	60	0	0	30.1	0.349	47	1
767	1	93	70	31	0	30.4	0.315	23	0

[768 rows x 9 columns]

```
In [4]: #pid.columns
    #created a list of all the columns present in the dataset
    #pid_col=list(pid.columns)
    pid2=pid.copy()
    #pid_col
    #pid_col1=pid_col.copy()
    #we do not want to bring changes in the class column so we removed it from the column #pid_col1.remove('class')
    pid2.drop(["class"], axis = 1, inplace = True)
    print(pid2)
```

	pregs	plas	pres	skin	test	BMI	pedi	Age
0	6	148	72	35	0	33.6	0.627	50
1	1	85	66	29	0	26.6	0.351	31
2	8	183	64	0	0	23.3	0.672	32
3	1	89	66	23	94	28.1	0.167	21
4	0	137	40	35	168	43.1	2.288	33
763	10	101	76	48	180	32.9	0.171	63
764	2	122	70	27	0	36.8	0.340	27
765	5	121	72	23	112	26.2	0.245	30
766	1	126	60	0	0	30.1	0.349	47
767	1	93	70	31	0	30.4	0.315	23

[768 rows x 8 columns]

Ques 1 Show the performance of K-nearest neighbor (KNN) classifier for different values of K (1, 3, 5, 7, 9,

11, 13, 15, 17, 19, 21)

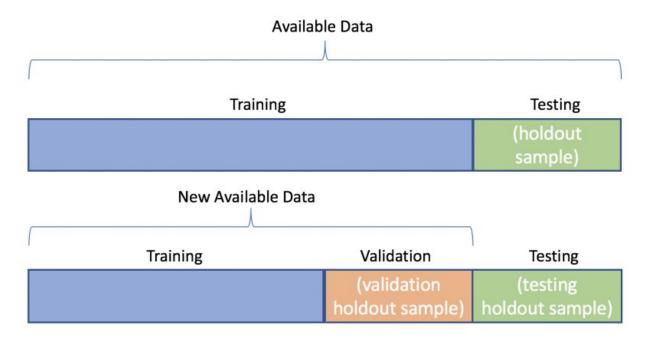
A. Find confusion matrix (use 'confusion_matrix') for each K.

B. Find the classification accuracy (You can use 'accuracy_score') for each K. Note the value of K for

which the accuracy is high.

```
In [5]: X1 = pid2
                                        # X denotes the input functions and here class defines
         print(X1)
         y1 = pid['class']
                                                 #y denotes the output functions
         print(y1)
         X1_train, X1_test, y1_train, y1_test = train_test_split(X1, y1,
                                                                    train_size=0.7,
                                                                    random state=42,
                                                                    stratify=y1)
         print(X1_train)
         print(X1 test)
         print(y1_train)
         print(y1_test)
         print(f"Numbers of train instances by class: {np.bincount(y1 train)}")
         print(f"Numbers of test instances by class: {np.bincount(y1_test)}")
                       plas
                                    skin
                                                   BMI
                                                          pedi
               pregs
                             pres
                                           test
                                                                 Age
                        148
                                72
                                       35
                                                                  50
         0
                   6
                                               0
                                                  33.6
                                                         0.627
         1
                   1
                         85
                                66
                                       29
                                              0
                                                  26.6
                                                         0.351
                                                                  31
                                                  23.3
         2
                   8
                        183
                                64
                                        0
                                              0
                                                         0.672
                                                                  32
         3
                   1
                         89
                                66
                                       23
                                             94
                                                  28.1
                                                         0.167
                                                                  21
         4
                   0
                                                                  33
                        137
                                40
                                       35
                                            168
                                                  43.1
                                                         2.288
                        . . .
                                            . . .
                                                  32.9
         763
                  10
                        101
                                76
                                       48
                                            180
                                                         0.171
                                                                  63
         764
                   2
                        122
                                70
                                       27
                                              0
                                                  36.8
                                                         0.340
                                                                  27
         765
                   5
                        121
                                                  26.2
                                                                  30
                                72
                                       23
                                            112
                                                         0.245
         766
                   1
                        126
                                60
                                        0
                                               0
                                                  30.1
                                                         0.349
                                                                  47
                   1
                         93
                                70
                                               0
                                                  30.4
                                                         0.315
                                                                  23
         767
                                       31
         [768 rows x 8 columns]
         0
                 1
         1
                 0
         2
                 1
         3
                 0
         4
                 1
                . .
         763
                 0
         764
                 0
         765
                 0
         766
                 1
         767
         Name: class, Length: 768, dtype: int64
               pregs
                      plas
                             pres
                                    skin
                                           test
                                                   BMI
                                                          pedi
                                                                 Age
         209
                   7
                        184
                                84
                                       33
                                              0
                                                  35.5
                                                         0.355
                                                                  41
         176
                   6
                         85
                                78
                                        0
                                              0
                                                  31.2
                                                         0.382
                                                                  42
         147
                   2
                        106
                                       35
                                                  30.5
                                                         1.400
                                                                  34
                                64
                                            119
         454
                   2
                        100
                                54
                                       28
                                            105
                                                  37.8
                                                         0.498
                                                                  24
                   5
                        104
                                74
                                        0
                                                  28.8
                                                         0.153
                                                                  48
         636
                                              0
         . .
                        . . .
                                                   . . .
                                                           . . .
                                                                 . . .
                                            175
         214
                   9
                        112
                                82
                                                  34.2
                                                         0.260
                                       32
                                                                  36
         113
                   4
                         76
                                62
                                        0
                                              0
                                                  34.0
                                                         0.391
                                                                  25
         556
                   1
                         97
                                70
                                       40
                                                  38.1
                                                         0.218
                                                                  30
                                               0
         759
                   6
                        190
                                92
                                        0
                                               0
                                                  35.5
                                                         0.278
                                                                  66
         107
                   4
                        144
                                58
                                       28
                                            140
                                                  29.5
                                                         0.287
                                                                  37
```

```
[537 rows x 8 columns]
     pregs
             plas
                    pres
                           skin
                                  test
                                          BMI
                                                pedi
                                                       Age
730
          3
              130
                       78
                             23
                                    79
                                         28.4
                                               0.323
                                                        34
198
          4
              109
                       64
                             44
                                    99
                                         34.8
                                               0.905
                                                        26
24
              143
                      94
                             33
                                   146
                                         36.6
                                               0.254
                                                        51
         11
417
              144
                             32
                                         38.5
                                               0.554
                                                        37
          4
                      82
                                     0
387
          8
              105
                     100
                             36
                                     0
                                        43.3
                                               0.239
                                                        45
. .
               . . .
                                                  . . .
                      . . .
                            . . .
                                          . . .
                                                        . . .
        . . .
                                   . . .
94
          2
                                        24.7
                                               0.761
              142
                      82
                             18
                                    64
                                                        21
          5
                      75
                                        29.9
437
              147
                                     0
                                               0.434
                                                        28
                              0
86
         13
              106
                      72
                             54
                                     0
                                        36.6
                                                        45
                                               0.178
221
          2
              158
                      90
                              0
                                     0
                                        31.6
                                               0.805
                                                        66
19
          1
              115
                      70
                             30
                                    96
                                        34.6
                                               0.529
                                                        32
[231 rows x 8 columns]
209
        1
176
       0
147
       0
454
       0
636
        0
       . .
214
       1
113
       0
556
       0
759
        1
107
Name: class, Length: 537, dtype: int64
730
        1
198
        1
24
        1
417
        1
387
        1
       . .
94
       0
437
       0
86
        0
        1
221
19
        1
Name: class, Length: 231, dtype: int64
Numbers of train instances by class: [350 187]
Numbers of test instances by class: [150 81]
```



```
In [6]: X1 test, X1 val, y1 test, y1 val = train test split(X1 test, y1 test,
                                                                     train size=0.5,
                                                                     random state=42,
                                                                     stratify=y1 test)
         print(X1 train)
         print(X1_val)
         print(y1 test)
         print(y1_val)
         print(f"Numbers of test instances by class: {np.bincount(y1_test)}")
         print(f"Numbers of validation instances by class: {np.bincount(y1 val)}")
                                     skin
                                            test
                                                    BMI
                                                           pedi
               pregs
                       plas
                              pres
                                                                  Age
         209
                    7
                        184
                                 84
                                       33
                                               0
                                                   35.5
                                                          0.355
                                                                   41
         176
                    6
                         85
                                 78
                                        0
                                                   31.2
                                                          0.382
                                                                   42
                                               0
         147
                    2
                        106
                                 64
                                       35
                                             119
                                                   30.5
                                                          1.400
                                                                   34
                                                                   24
         454
                    2
                        100
                                 54
                                       28
                                             105
                                                   37.8
                                                          0.498
         636
                    5
                        104
                                 74
                                        0
                                               0
                                                   28.8
                                                          0.153
                                                                   48
          . .
                  . . .
                        . . .
                                . . .
                                       . . .
                                             . . .
                                                    . . .
                                                                  . . .
         214
                    9
                        112
                                 82
                                       32
                                             175
                                                   34.2
                                                          0.260
                                                                   36
                    4
                                                   34.0
                                                                   25
         113
                         76
                                 62
                                        0
                                               0
                                                          0.391
         556
                    1
                         97
                                 70
                                       40
                                               0
                                                   38.1
                                                          0.218
                                                                   30
         759
                        190
                                 92
                                        0
                                                   35.5
                                                          0.278
                                                                   66
                    6
                                               0
         107
                    4
                        144
                                 58
                                       28
                                             140
                                                   29.5
                                                          0.287
                                                                   37
         [537 rows x 8 columns]
                       plas
                                                    BMI
               pregs
                              pres
                                            test
                                                                  Age
                                     skin
                                                           pedi
         83
                    0
                        101
                                 65
                                       28
                                               0
                                                   24.6
                                                          0.237
                                                                   22
         347
                    3
                        116
                                 0
                                        0
                                               0
                                                   23.5
                                                          0.187
                                                                   23
         52
                    5
                          88
                                 66
                                       21
                                              23
                                                   24.4
                                                          0.342
                                                                   30
                    1
                         91
                                       25
         650
                                             100
                                                   25.2
                                                          0.234
                                                                   23
                                 54
                    0
                        167
                                        0
                                                   32.3
                                                          0.839
         300
                                  0
                                               0
                                                                   30
          . .
                                                                  . . .
                  . . .
                        . . .
                                . . .
                                       . . .
                                             . . .
         422
                   0
                        102
                                       46
                                              78
                                                   40.6
                                                          0.496
                                                                   21
                                 64
         580
                    0
                        151
                                90
                                       46
                                               0
                                                   42.1
                                                          0.371
                                                                   21
         219
                    5
                        112
                                 66
                                        0
                                               0
                                                   37.8
                                                          0.261
                                                                   41
                    1
                                                                   21
         486
                        139
                                 62
                                       41
                                                   40.7
                                                          0.536
                                             480
         112
                    1
                          89
                                 76
                                       34
                                                   31.2
                                                          0.192
                                                                   23
                                              37
         [116 rows x 8 columns]
         418
                 0
         235
                  1
         373
                 0
         330
                 0
         64
                 1
         151
                 0
         535
                 1
         82
                 0
         25
                 1
         637
         Name: class, Length: 115, dtype: int64
         83
         347
                 0
         52
                 0
         650
                 0
         300
                  1
```

Name: class, Length: 116, dtype: int64 Numbers of test instances by class: [75 40] Numbers of validation instances by class: [75 41]

```
In [7]: from sklearn.neighbors import KNeighborsClassifier
        neighbors=[1,3,5,7,9,11,13,15,17,19,21]
        train accuracy = np.empty(len(neighbors))
        val accuracy = np.empty(len(neighbors))
        acc=[]
        # Loop over K values
        for i, k in enumerate(neighbors):
           knn = KNeighborsClassifier(n_neighbors=k)
           knn.fit(X1 train, y1 train)
           print('Predicted Outcomes for neighbours =',k,'are', knn.predict(X1_val))
           print('\n')
           print('Accuracy = ',knn.score(X1 val, y1 val))
           if ((knn.score(X1_val, y1_val))>=0):
               acc.append(knn.score(X1 val, y1 val))
           print('\n')
           matrix = confusion matrix(y1 val,knn.predict(X1 val))
           print('Confusion Matrix = ',matrix)
           print('\n\n')
           # Compute traning and test data accuracy
           train accuracy[i] = knn.score(X1 train, y1 train)
           val accuracy[i] = knn.score(X1 val, y1 val)
        print(acc)
        print('\n')
        print('maximum accuracy is =', max(acc)*100)
        # Generate plot
        plt.plot(neighbors, val_accuracy, label = 'Testing dataset Accuracy')
        plt.plot(neighbors, train_accuracy, label = 'Training dataset Accuracy')
        plt.legend()
        plt.xlabel('n neighbors')
        plt.ylabel('Accuracy')
        plt.show()
        Predicted Outcomes for neighbours = 1 are [0 1 0 0 1 0 0 1 1 0 0 0 1 0 1 1 1 1
        1101010001000000000
         0 0 0 0 0 0 0 1 0 0 1 0 0 0 1 0 1 0 0 1 0 1 1 0 0 0 0 0 0 0 0 1 0 0 0 0 0
        0 0 1 1 0]
        Accuracy = 0.6206896551724138
        Confusion Matrix = [[52 23]
         [21 20]]
```

Confusion Matrix = [[59 16]
 [19 22]]

Accuracy = 0.7327586206896551

Confusion Matrix = [[64 11] [20 21]]

Accuracy = 0.7413793103448276

Confusion Matrix = [[66 9] [21 20]]

Accuracy = 0.7327586206896551

```
Confusion Matrix = [[64 11] [20 21]]
```

Accuracy = 0.7068965517241379

```
Confusion Matrix = [[64 11] [23 18]]
```

Accuracy = 0.7413793103448276

```
Confusion Matrix = [[66 9]
  [21 20]]
```

Accuracy = 0.7672413793103449

```
Confusion Matrix = [[68 7] [20 21]]
```

Accuracy = 0.7586206896551724

Confusion Matrix = [[67 8] [20 21]]

Accuracy = 0.7672413793103449

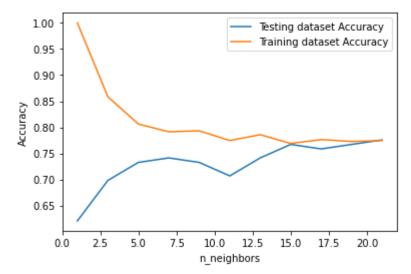
Confusion Matrix = [[67 8]
 [19 22]]

Accuracy = 0.7758620689655172

Confusion Matrix = [[68 7]
 [19 22]]

[0.6206896551724138, 0.6982758620689655, 0.7327586206896551, 0.741379310344827 6, 0.7327586206896551, 0.7068965517241379, 0.7413793103448276, 0.7672413793103449, 0.7586206896551724, 0.7672413793103449, 0.7758620689655172]

maximum accuracy is = 77.58620689655173



```
In [8]: from sklearn.neighbors import KNeighborsClassifier
      neighbors=[1,3,5,7,9,11,13,15,17,19,21]
      #train accuracy = np.empty(len(neighbors))
      #val accuracy = np.empty(len(neighbors))
      acc=[]
      # Loop over K values
      for i, k in enumerate(neighbors):
         knn = KNeighborsClassifier(n_neighbors=k)
         knn.fit(X1 train, y1 train)
         print('Predicted Outcomes for neighbours =',k,'are', knn.predict(X1_test))
         y_pred=knn.predict(X1_test)
         y_pred
         print('Accuracy = ',knn.score(X1_test, y1_test))
         if ((knn.score(X1 test, y1 test))>=0):
             acc.append(knn.score(X1 test, y1 test))
         print('\n')
         matrix = confusion matrix(y1 test,knn.predict(X1 test))
         print('Confusion Matrix = ',matrix)
         print('\n')
      print(acc)
      print('\n')
      print('maximum accuracy is =', max(acc)*100)
      Predicted Outcomes for neighbours = 1 are [0 1 0 1 1 0 0 0 1 0 0 0 1 0 1 0 1 0
      0010101000101000110
       0\; 1\; 0\; 0\; 0\; 0\; 1\; 1\; 0\; 1\; 0\; 0\; 0\; 0\; 1\; 0\; 0\; 0\; 0\; 1\; 0\; 1\; 0\; 1\; 1\; 1\; 1\; 0\; 0\; 0\; 1\; 0\; 1\; 0
       1 0 0 0]
      Accuracy = 0.7130434782608696
      Confusion Matrix = [[60 15]
       [18 22]]
      Predicted Outcomes for neighbours = 3 are [0 1 0 1 1 0 0 0 1 0 0 0 0 0 0 0 0
      0010101000000000110
       1 0 0 0]
      Accuracy = 0.7130434782608696
      Confusion Matrix = [[64 11]
       [22 18]]
      Predicted Outcomes for neighbours = 5 are [0 1 0 1 1 0 0 0 1 0 0 0 0 0 0 0 0
      0010101000010000111
```

```
1 0 0 0]
Accuracy = 0.7043478260869566
Confusion Matrix = [[61 14]
[20 20]]
Predicted Outcomes for neighbours = 7 are [0 1 0 1 1 0 0 0 1 0 0 0 0 0 0 0 0
0010101000110000111
1 0 0 01
Accuracy = 0.7391304347826086
Confusion Matrix = [[63 12]
[18 22]]
Predicted Outcomes for neighbours = 9 are [0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 1
1010101000110000111
1 0 0 0]
Accuracy = 0.7130434782608696
Confusion Matrix = [[61 14]
[19 21]]
Predicted Outcomes for neighbours = 11 are [0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0
1010101000010000100
1 0 0 01
Accuracy = 0.7043478260869566
Confusion Matrix = [[62 13]
[21 19]]
Predicted Outcomes for neighbours = 13 are [0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0
1010101000110000100
1 0 0 01
Accuracy = 0.7217391304347827
Confusion Matrix = [[63 12]
[20 20]]
```

Predicted Outcomes for neighbours = 15 are [0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0

```
1010101000011000100
1 0 0 01
Accuracy = 0.7130434782608696
Confusion Matrix = [[63 12]
[21 19]]
Predicted Outcomes for neighbours = 17 are [0 1 0 0 0 0 0 1 0 0 0 0 0 0 0 0 0
1010101000110000100
1 0 0 01
Accuracy = 0.7130434782608696
Confusion Matrix = [[64 11]
[22 18]]
Predicted Outcomes for neighbours = 19 are [0 1 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0
1010101000110000100
0\;1\;0\;0\;0\;0\;0\;0\;1\;0\;0\;0\;0\;1\;1\;0\;1\;0\;0\;0\;0\;1\;1\;0\;1\;0\;0\;0\;1\;0\;1\;0
1000]
Accuracy = 0.7043478260869566
Confusion Matrix = [[61 14]
[20 20]]
Predicted Outcomes for neighbours = 21 are [0 1 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0 0
1010101000111000100
0 0 0 0]
Accuracy = 0.7130434782608696
Confusion Matrix = [[62 13]
[20 20]]
[0.7130434782608696, 0.7130434782608696, 0.7043478260869566, 0.739130434782608
6, 0.7130434782608696, 0.7043478260869566, 0.7217391304347827, 0.71304347826086
96, 0.7130434782608696, 0.7043478260869566, 0.7130434782608696]
maximum accuracy is = 73.91304347826086
```

Ques.2 Build a Bayes classifier with Multi-modal Gaussian distribution (GMM) with Q components (modes) as class

conditional density for each class. Show the performance for different values of Q (2, 4, 8, 16).

Estimate the parameters of the Gaussian Mixture Model (mixture coefficients, mean vectors and covariance matrices) using maximum likelihood method.

A. Find confusion matrix (use 'confusion_matrix') for each Q.

- B. Find the classification accuracy (You can use 'accuracy_score') for each Q.
- C. Observe the values in the covariance matrix in each case and comment.
- D. Compare the results with that obtained using Bayes classifier with unimodal Gaussian distribution

(Q = 1).

Clustering methods such as K-means have hard boundaries, meaning a data point either belongs to that cluster or it doesn't. On the other hand, clustering methods such as Gaussian Mixture Models (GMM) have soft boundaries, where data points can belong to multiple cluster at the same time but with different degrees of belief. e.g. a data point can have a 60% of belonging to cluster 1, 40% of belonging to cluster 2.

Apart from using it in the context of clustering, one other thing that GMM can be useful for is outlier detection: Due to the fact that we can compute the likelihood of each point being in each cluster, the points with a "relatively" low likelihood (where "relatively" is a threshold that we just determine ourselves) can be labeled as outliers.

This is the exact situation we're in when doing GMM. We have a bunch of data points, we suspect that they came from K different guassians, but we have no clue which data points came from which guassian. To solve this problem, we use the EM algorithm. The way it works is that it will start by placing guassians randomly (generate random mean and variance for the guassian). Then it will iterate over these two steps until it converges.

E step: With the current means and variances, it's going to figure out the probability of each data point xi coming from each guassian. M step: Once it computed these probability assignments it will use these numbers to re-estimate the guassians' mean and variance to better fit the data points.

That could be a problem for datasets with large number of dimensions (e.g. text data), because with the number of parameters growing roughly as the square of the dimension, it may quickly

become impossible to find a sufficient amount of data to make good inferences. One common way to avoid this problem is to fix the covariance matrix of each component to be diagonal (off-diagonal value will be 0 and will not be updated). To achieve this, we can change the covariance_type parameter in scikit-learn's GMM to diag.

```
In [9]: X2 = pid2
                                        # X denotes the input functions and here class defines
         print(X2)
         y2 = pid['class']
                                                  #y denotes the output functions
         print(y2)
         X2_train, X2_test, y2_train, y2_test = train_test_split(X2, y2,
                                                                     train_size=0.7,
                                                                     random state=42,
                                                                     stratify=y2)
         print(X2_train)
         print(X2 test)
         print(y2_train)
         print(y2_test)
                       plas
                                     skin
                                            test
                                                    BMI
                                                           pedi
                                                                  Age
               pregs
                              pres
                                       35
         0
                    6
                        148
                                 72
                                               0
                                                   33.6
                                                          0.627
                                                                   50
         1
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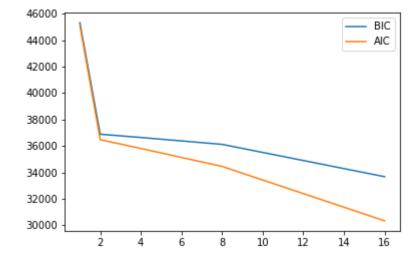
```
In [10]: import numpy as np
    from sklearn.mixture import GaussianMixture
    gm = GaussianMixture(n_components=2,covariance_type='full',max_iter=1000,n_init=2
    clf=gm.fit(X2_train, y2_train)
    y_pred=gm.predict(X2_test) #NB classifier assumes that all the features are
    print(y_pred)
```

```
In [12]: print(clf.bic(pid2))
print(clf.aic(pid2))
```

36949.88963138758 36536.59234513744

```
In [13]: n_estimators=[1,2,4,8,16]
    clfs=[GaussianMixture(n ).fit(pid2) for n in n_estimators]
    bics=[clf.bic(pid2) for clf in clfs]
    aics=[clf.aic(pid2) for clf in clfs]
    print(clfs)
    print(bics)
    print(aics)
    plt.plot(n_estimators, bics, label="BIC")  #low value of both aic and bic is print(plot(n_estimators, aics, label="AIC")
    plt.legend();
```

[GaussianMixture(), GaussianMixture(n_components=2), GaussianMixture(n_components=4), GaussianMixture(n_components=8), GaussianMixture(n_components=16)] [45311.82212435199, 36884.02231564019, 36637.73973732567, 36116.433283252394, 3 3669.879740016106] [45107.49537609349, 36470.72502939005, 35806.50137509224, 34449.31276905238, 30 330.99492188293]



```
In [14]: import numpy as np
          from sklearn.mixture import GaussianMixture
          gm = GaussianMixture(n components=16,covariance type='full',max iter=1000,n init
          clf=gm.fit(X2 train, y2 train)
          y pred=gm.predict(X2 test)
                                            #NB classifier assumes that all the features are
          print(y_pred)
          print('\n\n')
          print(gm.means )
          print('\n\n')
          print(gm.score(pid2, y=None))
          print('\n\n')
          probs = gm.predict_proba(pid2)
          print(probs)
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           [2.56096203e+00 1.02477466e+02 6.85442609e+01 2.63139563e+01
            7.97271661e+01 3.10383569e+01 4.09326960e-01 2.66711606e+01]
           [5.20000000e+00 1.65600000e+02 7.24000000e+01 3.26000000e+01
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            0.00000000e+00 2.35038960e+01 4.51625088e-01 2.38118098e+01]
           [7.00000000e+00 1.44000000e+02 8.10000000e+01 3.40000000e+01
            4.45000000e+01 2.87750000e+01 4.92750000e-01 5.35000000e+01]
           [4.45929422e+00 1.17714813e+02 9.94917866e-01 2.99682373e+00
            1.03637278e+00 2.54156772e+01 4.23465426e-01 3.23777928e+01
           [3.80009513e+00 1.62905133e+02 7.59982751e+01 3.00003433e+01
            2.81800955e+02 3.67902014e+01 5.92580977e-01 4.05010866e+01]
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            1.22479032e+02 3.42512948e+01 6.85807018e-01 2.80835182e+01]
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           [4.26388802e+00 1.13186016e+02 7.35388708e+01 3.05317231e+01
            0.00000000e+00 3.34120599e+01 4.12666647e-01 3.50534934e+01]
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           [5.70094030e+00 1.60061105e+02 7.52280570e+01 2.95928260e+01
            1.40629935e+02 3.27365471e+01 5.63938687e-01 3.76315845e+01]
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```

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[3.25000000e+00 4.42500000e+01 7.60000000e+01 2.35000000e+01 5.75000000e+00 3.04750000e+01 8.91750000e-01 2.95000000e+01]]
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-20.868892014013216

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[2.53194702e-30 5.51066358e-23 0.00000000e+00 ... 8.65024706e-56 0.00000000e+00 0.0000000e+00]
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[1.30155539e-39 1.12438212e-20 0.00000000e+00 ... 2.30566179e-43 0.00000000e+00 0.00000000e+00]
[2.46643591e-41 9.46508124e-06 0.00000000e+00 ... 1.20813143e-50 0.00000000e+00 0.00000000e+00]
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