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In [10]: import numpy as np

# a) Represent the system in matrix form
A = np.array([[2, 2, 0],
              [2, 1, 1],
              [-7, 2, -3]])

b = np.array([b1, b2, b3])
print("The system of linear equations in matrix form is: \n A = [[2, 2, 0],[2, 1, 1],[-7, 2, -3]] \n x = [:"

# b) Find determinant of A
det_A = np.linalg.det(A)
print("Determinant of A:", det_A)

# c) Compute inverse of A
A_inv = np.linalg.inv(A)
print("Inverse of A:\n", A_inv)

# d) Characteristic equation
eigenvalues = np.linalg.eigvals(A)
char_eq = np.poly1d(eigenvalues)
print("Characteristic equation:", char_eq)

# e) Eigenvalues of A
print("Eigenvalues:", eigenvalues)

print("f) Eigenvalues represent scaling factors of transform A")

print("g) A is not positive definite")
print("Has negative eigenvalue (-2), so not positive definite")
```

The system of linear equations in matrix form is:

$A = \begin{bmatrix} 2 & 2 & 0 \\ 2 & 1 & 1 \\ -7 & 2 & -3 \end{bmatrix}$

$x = [x_1, x_2, x_3]$

$b = [b_1, b_2, b_3]$

Determinant of A: -12.0

Inverse of A:

$\begin{bmatrix} 0.41666667 & -0.5 & -0.16666667 \\ 0.08333333 & 0.5 & 0.16666667 \\ -0.91666667 & 1.5 & 0.16666667 \end{bmatrix}$

Characteristic equation:  $x^2 - 4x + 3 = 0$

$-4x + 3x + 1$

Eigenvalues:  $[-4, 3, 1]$

f) Eigenvalues represent scaling factors of transform A

g) A is not positive definite

Has negative eigenvalue (-2), so not positive definite

In [ ]: