

Table 3. Survey of measurements on woodwinds

d_1 = inner diameter of main tube (mm).
 l_G = distance to tip of reed or to centre of embouchure-hole (mm).
 d_H = hole diameter or its smallest value (mm). For oval holes, smallest and largest values are given.
 l_H = minimum hole length (mm).
 h = mean distance of cup to hole end, in opened position (mm).

R_0 = radius of curvature of bended part of the bore.
 $+$ denotes undercutting of a hole.
 $-$ in the h-column, denotes that the hole is not covered by a key.
 $-$ denotes no hole present.
 $()$ tube diameters between brackets are estimates obtained via volume-measurements.

A. FLUTES

Gemeinhardt		Reiner		Hofinger		Kohlert		Selmer		Gaillard		Hamig		Old	piccolo	old	flute
d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G
17	26	16.8	20	16.6	63	16.5	61	16.9	40.8	16.9	23	10.85	7.1	10.35	7	18.8	0
16.2	16	17.0	12	17.0	28	16.9	23.5	17.2	25.8	17.0	13	10.85	64.1	10.35	61	18.8	132
16.65	14	17.5	19.9	17.6	22	17.8	26.5	17.8	19	17.3	7	10.7	64.1	11.2	61	15.2	340
17.0	24	17.4	20	17.7	32	17.9	36.5	17.9	29	17.5	17	10.5	73.4	11.2	67	13.5	452
18.0	34	17.8	30	17.9	42	18.1	46.5	18.1	39	17.65	27	10.25	83.1	10.0	67	11.2	583
18.1	44	17.9	40	17.9	52	18.3	56.5	18.2	49	17.85	37	10.0	99.7	9.75	72.5		
18.3	54	18.0	49.4	18.1	62	18.4	66.5	18.3	59	17.95	47	9.75	111.4	9.5	83.1		
18.45	64	18.0	50	18.2	72	18.6	76.5	18.5	69	18.05	57	9.5	122.5	9.25	97.5		
18.55	74	18.25	60	18.3	82	18.8	86.5	18.6	79	18.25	67	9.25	139.0	9.0	109.1		
18.60	84	18.4	70	18.4	92	18.8	96.5	18.7	89	18.4	77	9.0	151.9	8.75	124.7		
18.65	94	18.5	78.2	18.5	102	19.0	106.5	18.9	99	18.5	87	8.75	166.6	8.5	134.8		
18.8	104	18.55	80	18.95	152	18.8	156.5	19.0	109	18.65	97	8.5	176.8	8.25	145.7		
18.85	114	18.68	90	19.05	465	18.9	156.5	18.9	159	18.95	107	8.25	193.6	8.0	155.8		
18.9	154	18.75	100	18.9	594.4	18.9	599.7	18.9	604	18.95	601	8.0	204.7	7.75	172.6		
18.9	603	18.8	110									7.75	224.6	7.5	189.7		
		19	160									7.75	240.9	7.25	207.1		
		19	596.4									8.0	247.4	7.3	262.5		
												8.25	251.3				
												8.5	254.3				
												8.75	256.6				
												9.0	258.6				
												9.2	259.6				

hole		Gemeinhardt				Reiner				Hofinger				Kohlert ^{a)}				Selmer ^{a)}				Gaillard ^{a)}			
no	function	d_H	l_H	h	l_G	d_H	l_H	h	l_G	d_H	l_H	h	l_G	d_H	l_H	h	l_G	d_H	l_H	h	l_G	d_H	l_H	h	l_G
16	emb.	10.3	5	=	0	10.4	5.7	=	0	10.2	4.3	=	0	10.6	5	=	0	10.5	4.5	=	0	10.3	?	=	0
15		12.2				12.2				12.2				12.0				12.5				12.2			
14A		7.7	2	1.1	199.0	7.2	2.2	1.5	196.7	7.8	2	2.5	190.9	7.3	2	195.9	7.3	1.5	200.1	7.7	2	199.5			
14		7.7	2	1.1	215.0	8.0	2.0	1.5	211.1	7.8	2	2.5	206.1	7.3	2	212.4	7.3	1.5	215.9	7.7	2	216.6			
13	C-C#	7.5	2	1.7	234.0	7.2	2.0	1.5	231.4	7.2	2	3	229.2	6.9	2	230.2	6.7	2	233.9	7.0	2	233.0			
12	B-C	13.6	3	2.7	265.0	12.7	1.6	2.8	261.5	12.4	3	3	258.8	13.8	3	262.4	13.1	3	265.9	12.5	3	262.0			
11	A#-B	13.8	3	1.8	285.0	13.6	1.4	2.8	282.4	13.8	3	2	280.4	13.4	3	283.9	13.1	3	285.8	13.0	3	284.5			
10	A-A#	13.8	3	1.8	305.5	13.6	1.4	2.8	302.9	13.8	3	2	301.2	13.4	3	302.9	13.1	3	307.1	13.0	3	305.2			
9	G-A	13.8	3	2.1	328.5	13.6	1.4	2.8	325.9	13.2	3	3	323.8	13.3	3	326.4	13.1	3	329.1	13.0	3	328.5			
8	G-G#	13.8	3	2.1	351.0	13.4	1.4	1.8	348.3	12.8	3	2.5	344.4	13.2	3	349.1	13.1	3	353.5	12.5	3	349.5			
7	F#-G	13.8	3	2.1	351.0	13.6	1.4	2.8	348.4	13.2	3	3	347.4	13.3	3	348.9	13.1	3	353.5	13.0	3	352.0			
6	F-F#	14.4	3	2.2	401.5	14.0	1.4	3.7	397.7	13.8	3	3	397.6	14.0	3	399.7	14.1	3	403.0	14.0	3	401.5			
5	E-F	14.4	3	2.2	428.5	14.0	1.4	3.7	425.0	13.8	3	3.2	426.2	14.0	3	425.2	14.1	3	431.2	14.0	3	430.5			
4	D-E	14.4	3	2.2	458.0	14.0	1.4	3.7	455.2	13.8	3	3	453.6	14.0	3	455.2	14.1	3	460.5	13.8	3	458.0			
3	D-D#	15.3	3.5	1.7	492.0	15.2	1.5	2.8	486.2	15.5	3.5	3.8	487.8	14.8	3.5	489.7	15.1	3	493.4	15.5	3.5	492.0			
2	C#-D	15.3	3.5	3	526.0	15.3	1.5	3.5	519.6	15.4	4.5	3.5	518.8	14.8	3.5	522.2	15.1	3	525.9	15.5	3.5	523.5			
1	C-C#	15.3	3.5	2	560.5	15.3	1.5	3.5	553.3	15.4	4.5	3.5	553.2	14.8	3.5	557.2	15.1	3	560.6	15.5	3.5	558.0			

a) h was not measured

hole		Hamig			
no	function	d_H	l_H	h	l_G
15	emb.	8.6	5	=	0
14		10.3			
13		4.7	3.0	2.2	96.1
12	C-C#	4.7	2.8	2.2	105.9
11	B-C	4.2	3.1	2.0	111.2
10		4.2	2.8	1.5	122.1
9	A#-B	4.3	2.7	1.5	132.2
8	A-A#	5.0	2.7	1.8	132.1
7	G-A	5.8	2.6	1.8	143.7
6	G-G#	6.1	2.6	2.1	156.0
5	F#-G	6.0	2.5	2.1	166.7
4	F-F#	6.0	2.4	2.1	167.6
3	E-F	6.5	2.2	1.8	179.5
2	D-E	6.6	2.1	1.8	191.6
1	D-D#	7.0	2.0	1.8	207.1
		7.8	1.6	2.0	223.0
		8.2	1.3	1.8	236.1

hole		old piccolo			
no	function	d_H	l_H	h	l_G
13	emb.	8.6	4.5	=	0
12	B-C#	9.7			
11	B-C	4.8	3.8	3	87.9
10	A-B	4.8	4.3	=	115.3
9	A-A#	3.9	4.0	2	122.3
8	A-B	5.0	4.5	=	132.3
7	G-A	4.0	4.0	2.5	140.3
6	G-G#	4.5	4.6	=	148.8
5	F#-G	3.8	4.0	1.7	162.1
4	F-F#	4.7	4.5	=	175.5
3	E-F	5.0	4.4	=	192.5
2	D-E	4.5	4.0	2.5	202.5
1	D-D#	4.5	4.0	2.5	202.5
		4.4	4.7	=	212.8
		5.0	3.7	2.5	235.3

hole		old flute		
no	function	d_H	l_H	l_G
13	emb.	10.9	?	0
12	B-C#	7.1	4.3	220
11	A-B	6.1	4.3	235
10	A-A#	4.8	4.3	270
9	E-A	7.1	4.3	288
8	G-E#	4.6	4.3	312
7	F#-G	7.6	4.3	349
6	F-F#	10.2	4.3	382
5	E-F	7.6	4.3	400
4	D-E	5.6	4.3	420
3	D-D#	11.7	4.3	474
2	C#-D	11.2	4.3	505
1	C-C#	10.2	4.3	540

b) estimated

B. CLARINETS

Dolnet				S.M.L.				hole				Dolnet				S.M.L.			
d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G	no		d_H	l_H	d_H	l_H	d_H	l_H	d_H	l_H	d_H	l_H
mouth + piece				mouth + piece				24	G - G#	3.0	12.5	1.8	155	3.1	12.5	3.2	155.0		
(0)				(0)				23	G# - A	4.5+	7.0	2.2	169	5.3	6.5	3	167.0		
14.0 44.1				13.5 36				22	G - G#	6.2+	6.5	2	194	5.9	6.4	1.5	194.8		
14.25 47.6				14 39.5				21	F# - G	5.3+	7.0	2	204	5.5	6.7	2.5	203.5		
14.5 66.6				14.25 59.5				20	F - F#	5.0+	7.0	2.7	215	5.4	6.5	5	214.5		
14.75 84.6				14.75 76.5				19	D# - F	4.6+	5.5	2.3	231	5.2	5.0	2.8	230.8		
15.0 89.6				15.0 83.7				18	D - E	7.8	10.5	=	238.5	7.7	11.0	=	241.0		
tube				15.1 88.5				17	D# - E	5.0+	7.0	2.0	243	5.4	6.7	3	243.5		
1.8 89.6	30.0	60.7		tube				16	D - D#	5.0+	9.3	=	253	5.4	8.4	=	254.2		
14.8 450	32.0	613		15.1 88.5				15	C - D	5.0+	7.0	2	272	5.4	6.8	2.8	271.8		
15.0 473	34.0	618		15.1 430				14	G# - C#	6.4++	9.3	=	286	7.0	8.2	=	287.0		
15.25 486	38.0	627		15.25 467				13	C - C#	6.0	7.0	2.5	288.5	6.0	6.6	2.8	288.8		
15.5 498	40.0	632		15.5 487				12	C - C#	6.0	6.5	2	290	6.0	6.6	2.2	288.8		
15.75 510	46.0	645		15.75 496				11	A# - C	7.1++	7.3	=	308	8.3	6.8	=	309.0		
16.0 522	53.0	650						10	A# - B	5.1++	7.3	3	321.5	5.3	6.5	3	320.0		
17.0 539	59.0	663						9	G# - A#	7.8+	6.3	2	347	8.5	6.0	3.1	350.2		
17.5 546	60.0	664						8	G - A	8.7+	9.0	=	363	8.7	8.0	=	366.0		
								7	G# - A	8.0+	6.3	2	369	8.0	6.5	3	368.5		
								6	G - G#	7.8+	9.0	=	387	8.7	7.7	=	391.5		
								5	F - G	9.1+	9.0	=	410	9.3	7.7	=	414.0		
								4	F - F#	10.0+	5.3	3.2	442	11.4	5.5	3	445.2		
								3	E - F	12.4+	5.3	3	470	12.2	5.5	3	470.0		
								2	D# - E	11.0+	5.3	4	502	12.4	5.0	3.5	503.5		
								1	D - D#	12.3+	5.0	4	540	11.4	4.8	3.5	537.5		

a) mouthpiece volume = $10.5 \pm 0.1 \text{ cm}^3$ b) mouthpiece volume = $11.0 \pm 0.1 \text{ cm}^3$

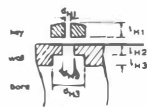
C. OBOES

Monnig				Buffet			
d_1	l_G	d_1	l_G	d_1	l_G	d_1	l_G
reed + staple +				reed + staple +			
(0.75) 0				(0.75) 0			
2.4 24.0				2.4 24.0			
3.3 37.5				3.3 37.5			
3.5 40.5				3.5 40.5			
3.7 44.9				3.7 44.9			
4.0 49.0				4.0 49.0			
4.2 53.6				4.2 53.6			
4.5 58.2				4.5 58.2			
4.8 66.0				4.8 66.0			
tube				tube			
4.0 66.0				4.0 66.0			
4.2 74.0				4.2 75.0			
4.5 82.2				4.5 84.0			
4.75 92.2				4.75 92.2			

c) volume of reed + staple = $58.0 \pm 10 \text{ mm}^3$

Monnig			
no	hole	d_H	l_H
22		0.3	77
21		0.3	77
20	C - D	3.1	6
19	B - C#	3.0	6
18		4.2	6
17	+16 A# - C	3.6	6
16	A - B	4.8	8.5
15	+13 F# - A#	4.2	6
14	A - A#	4.2	6
13	G - A	4.7	8.5
12	G - G#	5.0+	6
11	F# - G	7.0+	5.5
10	E - F#	4.6	6
9	D# - F	5.6+	6
8	E - F	7.3+	6
7	D - E	6.7+	8.5
6	D - D#	7.6	5.5
5	(D - D#)	8.5++	4.8
4	C - D	9.7	4.5
3	C - C#	7.6+	5.4
2	B - C	9.8	4.5
1	A# - B	10.8	4.5

Buffet			
no	hole	d_H	l_H
22		0.5	77
21		0.5	77
20	C - D	3.2	7.2
19	B - C#	3.2	7.2
18		6	2
17	+16 A# - C	2.8	7.0
16	A - B	6.2	2
15	+14 F# - A#	3.8	6.4
14	G - A	6.4	2
13	G - G#	4.8	7.0
12	F# - G	8.4	2
11	E - F#	3.7	5.5
10	D# - F	8.4	1.8
9	E - F	6.4	6.6
8	D - E	8.4	1.8
7	D - D#	5.7	6.4
6	(D - D#)	7.2	6.8
5	C - D	9.7	5.7
4	C - C#	7.1	6.3
3	B - C	10.4	5.4
2	A# - B	11.3	5
1	A#	4.4	6.8



D. SAXOPHONES

Schenkeleers tenor				Rascio tenor				Schenkeleers alto				Selmer soprano				Schenkeleers soprano				Solotone soprano			
d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G	d_H	l_G
mouth-piece a)				mouth-piece b)				mouth-piece c)				mouth-piece d)				mouth-piece e)				mouth-piece f)			
38.0	542	39.5	570	35.6	498	38.2	546	29.0	364	31.0	382	24.0	277	25.0	294	14.5	61	26.0	314	10.3	41	29.0	346
40.4	586	41.8	615	40.1	572	42.1	620	31.0	399	33.0	416	26.0	311	27.0	327	14.5	27	25.0	299	14.2	61	31.0	383
12.75	50.5	13.7	64	12.0	44.3	13.3	64	12.0	44.3	13.3	64	12.0	44.3	13.3	64	12.0	44.3	13.3	64	12.0	44.3	13.3	64
17.5	102.5	18.5	122.5	17.5	102.5	18.5	122.5	17.5	102.5	18.5	122.5	17.5	102.5	18.5	122.5	17.5	102.5	18.5	122.5	17.5	102.5	18.5	122.5
17.7	117	18.7	137	17.7	117	18.7	137	17.7	117	18.7	137	17.7	117	18.7	137	17.7	117	18.7	137	17.7	117	18.7	137
crook				crook				crook				crook				crook				crook			
12.0	72	12.5	97	12.0	72	12.5	97	12.0	72	12.5	97	12.0	72	12.5	97	12.0	72	12.5	97	12.0	72	12.5	97
13.3	122	13.7	147	13.3	122	13.7	147	13.3	122	13.7	147	13.3	122	13.7	147	13.3	122	13.7	147	13.3	122	13.7	147
15.3	147	15.7	172	15.3	147	15.7	172	15.3	147	15.7	172	15.3	147	15.7	172	15.3	147	15.7	172	15.3	147	15.7	172
17.3	172	17.7	197	17.3	172	17.7	197	17.3	172	17.7	197	17.3	172	17.7	197	17.3	172	17.7	197	17.3	172	17.7	197
21.4	222	21.8	247	21.4	222	21.8	247	21.4	222	21.8	247	21.4	222	21.8	247	21.4	222	21.8	247	21.4	222	21.8	247
23.5	247	23.9	272	23.5	247	23.9	272	23.5	247	23.9	272	23.5	247	23.9	272	23.5	247	23.9	272	23.5	247	23.9	272
24.6	276	25.0	301	24.6	276	25.0	301	24.6	276	25.0	301	24.6	276	25.0	301	24.6	276	25.0	301	24.6	276	25.0	301
26.0	300	26.4	325	26.0	300	26.4	325	26.0	300	26.4	325	26.0	300	26.4	325	26.0	300	26.4	325	26.0	300	26.4	325
26.0	325	26.4	350	26.0	325	26.4	350	26.0	325	26.4	350	26.0	325	26.4	350	26.0	325	26.4	350	26.0	325	26.4	350
tube				tube				tube				tube				tube				tube			
66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080	66.1	1080
67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146	67.2	1146
69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325	69.6	1325
72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220	72.5	1220
74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245	74.1	1245
80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298	80.1	1298
82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326	82.5	1326
86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358	86.3	1358
89	1388	89	1388	89	1388	89	1388	89	1388	89	1388	89	1388	89	1388	89	1388	89	1388	89	1388	89	1388
93	1423	93	1423	93	1423	93	1423	93	1423	93	1423	93	1423	93	1423	93	1423	93	1423	93	1423	93	1423
151	1441	151	1441	151	1441	151	1441	151	1441	151	1441	151	1441	151	1441	151	1441	151	1441	151	1441	151	1441

a) volume = $20.4 \pm 0.1 \text{ cm}^3$. c) volume = $16.0 \pm 0.1 \text{ cm}^3$. e) volume = $14.9 \pm 0.1 \text{ cm}^3$. g) volume = $7.0 \pm 0.1 \text{ cm}^3$. h) volume = $7.4 \pm 0.1 \text{ cm}^3$. j) volume = $6.7 \pm 0.1 \text{ cm}^3$.
 b) $R_0 = 48 \text{ mm}$. d) $R_0 = 45 \text{ mm}$. f) $R_0 = 42 \text{ mm}$.

hole	no	tenor				soprano k)			
		Schenkeleers				Schenkeleers			
		d_H	l_H	h	l_G	d_H	l_H	h	l_G
24		2.5+	5	2	177	1.7+	3	3	93
23		3.0+	9	2	363	2.3+	4	2	174
22	D-D#	12.5	2.2	2.5	354	15.0	3.7	2	172
21	C#-D	13.0	2.2	4.5	380	15.2	3.7	3	183
20	C-C#	13.5	2.2	4	408	15.2	3.2	4	194
19	B-C	15.5	2.2	3	444	17.8	3.6	4	205
18	A-B	11.5	2.2	5	465	12.5	2.5	3	218
17	A#-B	24.4	2.2	5	506	26.0	2.5	3	234
16	A-A#	23.1	2.2	3	525	25.0	4	4	242.5
15	A	21.8	2.2	5	558	25.0	2.5	3	256.5
14	G-G#	23.5	2.5	5	601	23.0	2.2	5	276.5
13	F-G	21.0	2.5	4	600	22.8	2.8	4	293
12	F-G	30.2	2.5	5	645	32.4	2.5	4	306.5
11	D#-F	25.0	2.5	5	693	24.6	3.7	3	328
10	D-E	33.6	2.6	5	791	33.5	2.7	3	379
9	D#-E	25.4	2.5	5	786	—	—	—	381.5
8	D	26.4	2.6	5	850	30.5	3	4	408
7	C-D	39.5	2.6	5	910	38.0	2.5	4	439.5
6	C-C#	30.6	3.5	5	967	29.5	3.5	4	474
5	A#-C	36.8	3.0	9	1032	34.0	4.5	6	508
4	A-B	33.1	3.0	3	1118	35.0	4	5	542
3	A#-B	42.0	3.5	7	1197	43.4	5	10	582
2	G-A	41.3	3.5	7	1269	43.2	5	10	624

hole	no	Schenkeleers			
		d_H	l_H	h	l_G
24		2.5+	4.9	2	131
23		2.5+	7.4	2	265
22	G-G#	12.3	2.3	4	276
21	F#-G	12.2	2.3	5	291
20	F-F#	12.2	2.3	3	305
19	E-F	12.2	2.3	2.5	324
18	D-E	9.3	2.3	4	344
17	C-E	20.2	2.3	4	364
16	D-D#	18.8	2.3	2	375.5
15	C-D	14.8	2.3	4.5	398.5
14	A-C#	20.9	2.3	4.5	434.5
13	C-C#	19.0	2.3	3	437.5
12	A#-C	25.0	2.3	5	468.5
11	A#-B	20.9	2.3	3.5	503.5
10	G#-A#	21.0	2.3	4.5	537.5
9	G-A	29.6	2.3	4.5	576
8	G#-A	19.3	2.3	4	569
7	G-G#	25.0	2.3	4.5	623.5
6	F-G	34.8	2.3	5	667.5
5	F-F#	31.8	2.5	4	712
4	D#-F	34.1	2.5	9	757
3	D#-E	30.7	2.5	4	835
2	D-D#	38.2	2.2	8.5	886
1	C#-D	39.0	2.2	8.5	944

k) On soprano saxophones, the key mechanism is such that high B on the second register is formed with hole 18 closed, holes 16 and 17 being open. On the Selmer, besides that, the key on hole 18 is perforated with a hole of diameter 4 mm and length 6 mm; the last hole can be closed on low register by a second key hanging 4 mm above the perforated first key.

Table 4. Data on Musical Scales.

A. Frequency of musical notes, expressed in hertz (number of complete oscillations per second)

European notation	C''	C'	C	c	c'	c''	c'''	c''''	c'''''
American notation	C ₀	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇	C ₈
C	16.3516	32.7032	65.4064	130.813	261.626	523.251	1046.50	2093.00	4186.01
	17.3239	34.6478	69.2957	138.591	277.183	554.365	1108.73	2217.46	4434.92
D	18.3540	36.7081	73.4162	146.832	293.665	587.330	1174.66	2349.32	4698.64
	19.4454	38.8909	77.7817	155.564	311.127	622.254	1244.51	2489.02	4978.03
E	20.6017	41.2034	82.4069	164.814	329.628	659.255	1318.51	2637.02	5274.04
F	21.8268	43.6535	87.3071	174.614	349.228	698.457	1396.91	2793.83	5587.65
	23.1247	46.2493	92.4986	184.997	369.994	739.989	1479.98	2959.96	5919.91
G	24.4997	48.9994	97.9989	195.998	391.995	783.991	1567.98	3135.96	6271.93
	25.9565	51.9131	103.8262	207.652	415.305	830.609	1661.22	3322.44	6644.88
A	27.5000	55.0000	110.0000	220.000	440.000	880.000	1760.00	3520.00	7040.00
	29.1352	58.2705	116.5409	233.082	466.164	932.328	1864.66	3729.31	7458.62
B	30.8677	61.7354	123.4708	246.942	493.883	987.767	1975.53	3951.07	7902.13

B. Period or reciprocal of frequency, in millisecond

	C ₀	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇	C ₈
C	61.1561	30.5781	15.2890	7.64451	3.82226	1.91113	0.955564	0.477782	0.238891
	57.7237	28.8618	14.4309	7.21546	3.60773	1.80386	0.901932	0.450966	0.225483
D	54.4839	27.2419	13.6210	6.81049	3.40524	1.70262	0.851311	0.425655	0.212828
	51.4259	25.7130	12.8565	6.42824	3.21412	1.60706	0.803530	0.401765	0.200883
E	48.5396	24.2698	12.1349	6.06745	3.03373	1.51686	0.758432	0.379216	0.189608
F	45.8153	22.9077	11.4538	5.72691	2.86346	1.43173	0.715864	0.357932	0.178966
	43.2439	21.6219	10.8110	5.40549	2.70274	1.35137	0.675686	0.337943	0.168922
G	40.8168	20.4084	10.2042	5.10210	2.55105	1.27553	0.637763	0.318881	0.159441
	38.5259	19.2630	9.6315	4.81574	2.40787	1.20394	0.601968	0.300984	0.150492
A	36.3636	18.1818	9.0909	4.54545	2.27273	1.13636	0.568182	0.284091	0.142046
	34.3227	17.1614	8.5807	4.29034	2.14517	1.07258	0.536292	0.268146	0.134073
B	32.3963	16.1982	8.0991	4.04954	2.02477	1.01238	0.506193	0.253096	0.126548

C. Acoustical length for a sound velocity of 346 m/s (in mm)

Clarinets	C ₀	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇	C ₈
Others	C ₁	C ₂	C ₃	C ₄	C ₅	C ₆	C ₇	C ₈	C ₉
C	5290.00	2645.00	1322.50	661.250	330.625	165.313	82.6563	41.3281	20.6641
	4993.10	2496.55	1248.27	624.137	312.069	156.034	78.0172	39.0086	19.5043
D	4712.86	2356.43	1178.21	589.107	294.554	147.277	73.6384	36.8192	18.4096
	4448.34	2224.17	1112.09	556.043	278.022	139.011	69.5054	34.7527	17.3763
E	4198.68	2099.34	1049.67	524.835	262.417	131.209	65.6043	32.8022	16.4011
F	3963.02	1981.51	990.76	495.378	247.689	123.845	61.9223	30.9611	15.4806
	3740.60	1870.30	935.15	467.575	233.787	116.894	58.4468	29.2234	14.6117
G	3530.65	1765.33	882.66	441.332	220.666	110.333	55.1665	27.5832	13.7916
	3332.49	1666.25	833.12	416.562	208.281	104.140	52.0702	26.0351	13.0176
A	3145.45	1572.73	786.36	393.182	196.591	98.296	49.1477	24.739	12.2869
	2968.91	1484.46	742.23	371.114	185.557	92.779	46.3893	23.1946	11.5973
B	2802.28	1401.14	700.57	350.285	175.143	87.571	43.7856	21.8928	10.9464

Table 5.

Relative frequency shift $g = \Delta f / f$ as a function of the number of semitones ν .

ν	g	ν	g
-1	-0.056126	1	0.059463
-2	-0.109101	2	0.122462
-3	-0.159104	3	0.189207
-4	-0.206299	4	0.259921
-5	-0.250846	5	0.334840
-6	-0.292893	6	0.414214
-7	-0.332580	7	0.498307
-8	-0.370040	8	0.587401
-9	-0.405396	9	0.681793
-10	-0.438769	10	0.781797
-11	-0.470268	11	0.887749
-12	-0.500000	12	1.000000

Table 6. Data of closed side-holes

Co-ordinates (L_A, y_A) and (L_B, y_B) of the terminal points of the best straight line through the points $y = \Sigma V_H / S_1$ as a function of the acoustical length L .

Dimensions in mm. ϵ is the penetration factor.

	y_A	L_A	y_B	L_B	ϵ
flute	0	310	20.8	650	0.5
piccolo	0	150	18	290	0.11
clarinet	0	200	40	580	0.13
tenor sax	0	580	32	1666	0.5
alto sax	0	440	34	1248	0.5
soprano sax	0	320	25	833	0.5
oboe	0	275	44	730	0.07
bassoon	0	925	62	2140	0.2
	62	2140	68	3100	0.04