Computer Science AP/X CSCI-140/242 Secret Messages Lab 1: Problem Solving

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1 Introduction¹

You would like to send messages back and forth with a friend (or co-conspirator!) but want to make sure that other people cannot easily read those messages. However, rather than use a fixed encryption scheme, you decide to take your message string and apply a series of transformations to it to generate the encrypted message.

The transformations you have agreed to use are the following:

- S_i shifts the letter at index i forward one letter in the alphabet. So, BALL $\rightarrow S_0 \rightarrow$ CALL.
 - This can be applied multiple times to shift multiple letters forward, and if so would be designated S_i^k to shift letter i by k forward. If the shift takes the letter past the end of the alphabet, it will wrap around. Negative exponents shift the letter backward in the alphabet.
- R rotates the string one position to the right. So, TOPS $\rightarrow R \rightarrow$ STOP. This function can also be used with an exponent (positive or negative). For example, TRAIN $\rightarrow R^2 \rightarrow$ INTRA.
- D_i duplicates (in place) the letter at index i. So, HOPED $\rightarrow D_2 \rightarrow$ HOPPED. This can also be used with a positive exponent to produce multiple duplicates, but not with negative exponents.
- $T_{i,j}$ swaps the letters at index i and index j. So, SAUCE $\rightarrow T_{0,3} \rightarrow$ CAUSE. You can always assume that i < j.

To more effectively obfuscate your message, you can go through several transformations. For example, CANAL $\rightarrow R^2 D_2 S_2^9 \rightarrow$ ALLCAN. This transformation will be applied in order from the left to right.

^{1.} This problem is inspired by a puzzle by Dan Katz (http://web.mit.edu/puzzle/www/2007/puzzles/transmogrifiers/)

2 Problem Solving (15%)

Students will be organized into groups. Each group will work together to deliver answers to the following questions:

- 1. What are the results of the following transformations?
 - (a) ZOO $\rightarrow S_0^2 \rightarrow$
 - (b) SUCES $\rightarrow D_2 D_5 \rightarrow$
 - (c) HORSE $\rightarrow T_{2.4} S_4 R \rightarrow$
- 2. Consider the simple rotation (R) operation. For a given string msg, how would you implement this operation in Python? Write this as a Python function called rotate(msg: str) -> str.
- 3. Modify your previous answer so that your function takes also a positive exponent as an additional argument and performs the appropriate operation.
- 4. Python provides the ord function to convert a single character to an integer UNICODE value, and the chr function to convert from a UNICODE integer to a character. With that in mind, show how to implement shifting of a single uppercase character c by a positive amount k, keeping in mind that if this takes you past the end of the alphabet, it should wrap around.
- 5. The operation S_i^k will be represented in the input to your program with the text string Si,k—so, for example, the operation of question 1(a) would be given to your program as S0,2. Assume you have already implemented a function with the following signature shift(msg: str, index: int, exponent: int) -> str. If you are given that operation string (in a variable s) and a message string m, show how to generate the correct call to the shift function. Keep in mind that i and k can be arbitrarily large integers!
- 6. You will want to be able to decrypt as well as encrypt! Luckily, many of the functions can be inverted in a simple fashion. For example, if you get the information $\to S_0 \to \text{CALL}$ from your colleague, you can retrieve the original message by applying S_0^{-1} to CALL. For the following encryption operations, show (if possible!) the operation(s) to perform the decryption.
 - (a) S_2^3
 - (b) R^2
 - (c) D_1
 - (d) $T_{2.4}$
 - (e) RS_1