

re-  
mem-  
ber  
things  
I  
never  
lived  
trace  
spa-  
tial  
se-  
man-  
tic  
space

$$\mathcal{S}_\tau \subseteq (R^d, \cdot)$$

x-  
y  
vec-  
tor  
flow  
field

$$F_\tau : \mathcal{S}_\tau \longrightarrow T\mathcal{S}_\tau$$

$R^d$   
"dog"

$$\text{"dog"} \mapsto \vec{v}_{\text{dog}} = [0.12, -0.85, 1.03, \dots, 0.07] \in R^{768}$$

"cat"

$$\text{"cat"} \mapsto \vec{v}_{\text{cat}} = [0.11, -0.87, 1.01, \dots, 0.09] \in R^{768}$$

"dog"  
"cat"

What  
gets  
em-  
bed-  
ded?  
Every-  
thing

$\ell_2$

$\ell_2$

$\ell_2$

Close

to-  
gether:

"dog"

"puppy"

"canine"

$\tilde{0.9}$

$\tilde{1.2}$

Far

apart:

"dog"

"quantum"

"economics"

$\approx 4.7$

$\approx 5.3$

$R^{768}$

$R^{1024}$

not

$\ell_2$

an-

gle

of

en-

try

$\frac{1}{2}$

move

Cosine

dis-

tance,

hy-

per-

bolic

met-

rics,

or

task-

specific

learned

sim-

i-

lar-

*se-*  
*man-*  
*tic*  
*vec-*  
*tor*  
*flow*  
*field*  
 $F_\tau$   
 $S_\tau$

$$F_\tau : \mathcal{S}_\tau \longrightarrow T\mathcal{S}_\tau$$

$$\begin{array}{l} T\mathcal{S}_\tau \\ S_\tau \\ \dot{a}(t) = \\ F_\tau(a(t)) \end{array}$$

$$\vec{v}_{\text{dog}} = (1.00, \; 1.00, \; 0.00), \vec{v}_{\text{puppy}} = (1.10, \; 1.00, \; 0.05).$$