

*I*  
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ber  
things  
*I*  
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lived  
trace  
space  
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space

$$\mathcal{S}_\tau \subseteq (R^d, \cdot)$$

*x-*  
*y-*  
vec-  
tor  
flow  
field

$$F_\tau : \mathcal{S}_\tau \longrightarrow T\mathcal{S}_\tau$$

$$R^d_{\text{dog"}}$$

$$\text{"dog"} \mapsto \vec{v}_{\text{dog}} = [0.12, -0.85, 1.03, \dots, 0.07] \in R^{768}$$

"cat"

$$\text{"cat"} \mapsto \vec{v}_{\text{cat}} = [0.11, -0.87, 1.01, \dots, 0.09] \in R^{768}$$

"dog"  
"cat"  
**What**  
gets  
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ded?  
*Elg-*  
*thing*  
 $\ell_2$   
 $\ell_2$   
 $\ell_2$   
**Close**  
to-  
gether:  
"dog"  
"puppy"  
"canine"  
 $\approx$   
0.9—  
 $\ell_2^2$   
**Far**  
apart:  
"dog"  
"quantum"  
"economics"  
 $\approx$   
4.7—  
5.3  
 $R^{768}$   
 $R^{1024}$   
*not*  
 $\ell_2$   
*an-*  
*gle*  
*of*  
*en-*  
*try*  
 ${}_1$   
*move*

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$$\begin{array}{l} \textit{mean-} \\ \textit{vec-} \\ \textit{tor-} \\ \textit{flow} \\ \textit{field} \\ F_\tau \\ \mathcal{S}_\tau \end{array}$$

$$F_\tau:\mathcal{S}_\tau\longrightarrow T\mathcal{S}_\tau$$

$$\begin{array}{l} T\mathcal{S}_\tau \\ \mathcal{S} \\ \dot{a}(t) = \\ F_\tau(a(t)) \end{array}$$

$$\vec{v}_{\rm dog}=(1.00,\;1.00,\;0.00), \vec{v}_{\rm puppy}=(1.10,\;1.00,\;0.05).$$