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## **Decision Boundary**

In order to get our discrete 0 or 1 classification, we can translate the output of the hypothesis function as follows:

$$egin{aligned} h_{ heta}\left(x
ight) &\geq 0.5 
ightarrow y = 1 \ h_{ heta}\left(x
ight) &< 0.5 
ightarrow y = 0 \end{aligned}$$

The way our logistic function g behaves is that when its input is greater than or equal to zero, its output is greater than or equal to 0.5:

$$g\left(z
ight)\geq0.5$$
 when  $z\geq0$ 

Remember.

$$egin{aligned} z = 0, e^0 &= 1 \Rightarrow g\left(z
ight) = 1/2 \ z o \infty, e^{-\infty} &\to 0 \Rightarrow g\left(z
ight) = 1 \ z o -\infty, e^{\infty} &\to \infty \Rightarrow g\left(z
ight) = 0 \end{aligned}$$

So if our input to g is  $\theta^T X$ , then that means:

$$egin{aligned} h_{ heta}\left(x
ight) &= g\left( heta^Tx
ight) \geq 0.5 \ when \; heta^Tx &\geq 0 \end{aligned}$$

From these statements we can now say:

$$egin{aligned} heta^T x &\geq 0 \Rightarrow y = 1 \ heta^T x &< 0 \Rightarrow y = 0 \end{aligned}$$

The **decision boundary** is the line that separates the area where y = 0 and where y = 1. It is created by our hypothesis function.

## Example:

$$egin{aligned} heta &= egin{bmatrix} 5 \ -1 \ 0 \end{bmatrix} \ y &= 1 \ if \ 5 + (-1) \ x_1 + 0 x_2 \geq 0 \ 5 - x_1 \geq 0 \ - x_1 \geq -5 \ x_1 \leq 5 \end{aligned}$$

In this case, our decision boundary is a straight vertical line placed on the graph where  $x_1 = 5$ , and everything to the left of that denotes y = 1, while everything to the right denotes y = 0.

Again, the input to the sigmoid function g(z) (e.g.  $\theta^T X$ ) doesn't need to be linear, and could be a function that describes a circle (e.g.  $z = \theta_0 + \theta_1 x_1^2 + \theta_2 x_2^2$ ) or any shape to fit our data.