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Hypothesis Representation

We could approach the classification problem ignoring the fact that y is discrete-valued, and use our old linear regression algorithm to try to predict y given x. However, it is easy to construct examples where this method performs very poorly. Intuitively, it also doesn't make sense for $h_{\theta}(x)$ to take values larger than 1 or smaller than 0 when we know that $y \in \{0, 1\}$. To fix this, let's change the form for our hypotheses $h_{\theta}(x)$ to satisfy $0 \le h_{\theta}(x) \le 1$. This is accomplished by plugging $\theta^T x$ into the Logistic Function.

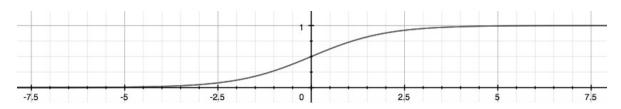
Our new form uses the "Sigmoid Function," also called the "Logistic Function":

$$h_{ heta}\left(x
ight)=g\left(heta^{T}x
ight)$$

$$z = heta^T x$$

$$g\left(z\right)=\frac{1}{1+e^{-z}}$$

The following image shows us what the sigmoid function looks like:



The function g(z), shown here, maps any real number to the (0, 1) interval, making it useful for transforming an arbitrary-valued function into a function better suited for classification.

 $h_{\theta}\left(x\right)$ will give us the **probability** that our output is 1. For example, $h_{\theta}\left(x\right)=0.7$ gives us a probability of 70% that our output is 1. Our probability that our prediction is 0 is just the complement of our probability that it is 1 (e.g. if probability that it is 1 is 70%, then the probability that it is 0 is 30%).

$$egin{aligned} h_{ heta}\left(x
ight) &= P\left(y=1|x; heta
ight) = 1 - P\left(y=0|x; heta
ight) \ P\left(y=0|x; heta
ight) + P\left(y=1|x; heta
ight) = 1 \end{aligned}$$

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