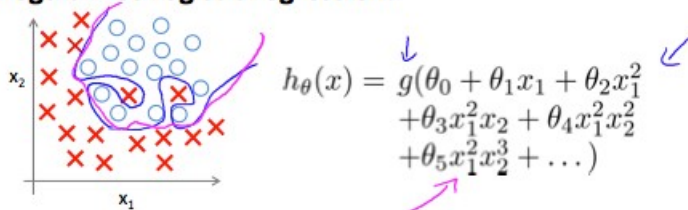


## Regularized Logistic Regression

We can regularize logistic regression in a similar way that we regularize linear regression. As a result, we can avoid overfitting. The following image shows how the regularized function, displayed by the pink line, is less likely to overfit than the non-regularized function represented by the blue line:

### Regularized logistic regression.



Cost function:

$$\rightarrow J(\theta) = - \left[ \frac{1}{m} \sum_{i=1}^m y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)})) \right] + \frac{\lambda}{2m} \sum_{j=1}^n \theta_j^2$$

$\theta_1, \theta_2, \dots, \theta_n$

### Cost Function

Recall that our cost function for logistic regression was:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^m [y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))]$$

We can regularize this equation by adding a term to the end:

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^m [y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))] + \frac{\lambda}{2m} \sum_{j=1}^n \theta_j^2$$

The second sum,  $\sum_{j=1}^n \theta_j^2$  means to explicitly exclude the bias term,  $\theta_0$ . I.e. the  $\theta$  vector is indexed from 0 to  $n$  (holding  $n+1$  values,  $\theta_0$  through  $\theta_n$ ), and this sum explicitly skips  $\theta_0$ , by running from 1 to  $n$ , skipping 0. Thus, when computing the equation, we should continuously update the two following equations:

### Gradient descent

Repeat {

$$\rightarrow \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

$$\rightarrow \theta_j := \theta_j - \alpha \left[ \underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}}_{\substack{j = 1, 2, 3, \dots, n \\ \theta_1, \dots, \theta_n}} + \frac{\lambda}{m} \theta_j \right]$$

}

$$\frac{\partial}{\partial \theta_j} J(\theta)$$

$$h_{\theta}(x) = \frac{1}{1 + e^{-\theta^T x}}$$