

### A cost and information-based account of epistemic *must*

We show how a general model of rational inference in communication delivers the puzzlingly weak interpretation of the necessity modal *must*. At issue is the failed inference in (1): despite the necessity semantics of *must*, *must p* (1b) does not entail that *p* (1a). Why? This has been a subject of debate since (?, ?).

- (1) a. It's raining.
- b. It must be raining.

We begin with a careful comparison of the meanings of the two statements in (1), asking whether a speaker's choice between (1a) and (1b) is affected by the directness of her evidence for whether it is raining (*q*); whether listeners' interpretations of (1a) and (1b) differ with respect to the strength of their resulting belief in *q*; and whether these beliefs are determined in part by the evidence they attribute to the speaker's choice between (1a) and (1b).

In **Exp. 1 (n=40)**, we collected estimates of evidence directness. Participants on Amazon's Mechanical Turk rated the probability of *q* (e.g., of it raining) given a piece of evidence *e* (e.g., *You hear the sound of water dripping on the roof*) on a sliding scale with endpoints labeled "impossible" and "certain". These estimates were used for analysis in Exps. 2 and 3.

**Exp. 2 (n=40)** tested how likely speakers are to use the marked *must p* utterance as evidence directness decreases. On each trial, participants were presented with a piece of evidence (e.g., *You see a person come in from outside with wet hair and wet clothes*) and were asked to choose one of four utterances—bare (1a), *must p* (1b), *probably p*, *might p*—to describe the situation to a friend. Participants were more likely to choose the more marked *must* form over the bare form as the directness of evidence decreased ( $\beta=5.4$ ,  $SE=2.4$ ,  $p<.05$ ), even when controlling for evidence type (e.g., perceptual, reportative, inferential).

**Exp. 3 (n=120)** tested whether listeners' estimates of a) the probability of *q* and b) the directness of speakers' evidence for *q* differ depending on the observed utterance; i.e. whether listeners take into account their knowledge of speakers' likely utterances in different evidential states as they interpret the bare and *must* forms. On each trial, participants were presented with an utterance (e.g. *It's raining*), and were asked a) to rate the probability of *q* on a sliding scale with endpoints labeled "impossible" and "certain"; and b) to select one out of five pieces of evidence that the speaker must have had about *q*. Participants' believed *q* was less likely after observing the *must* utterance ( $\mu=.65$ ,  $sd=.21$ ) than after observing the bare utterance ( $\mu=.86$ ,  $sd=.15$ ,  $\beta=-.21$ ,  $SE=.02$ ,  $t=-10.1$ ,  $p<.0001$ ). In addition, average directness of evidence was lower after *must* ( $\mu=.78$ ,  $sd=.12$ ) than after the bare utterance ( $\mu=.87$ ,  $sd=.1$ ,  $\beta=-.08$ ,  $SE=.01$ ,  $t=-6.8$ ,  $p<.0001$ ).

Taken together, these results support an M-implicature (?, ?) account of the choice and interpretation of epistemic *must*: the longer, marked, *must* is interpreted by listeners as conveying the marked meaning that the speaker arrived at the conclusion that *q* via an evidentially less certain route than if they had chosen the shorter, unmarked, bare form. We capture these results in a lexical uncertainty model in which the semantics of the bare utterance and *must q* are relatively unconstrained, following (?, ?, ?). We define the semantics of the utterances such that  $p(q|bare) > \theta_b$  and  $p(q|must) > \theta_m$ , where the pragmatic listener is uncertain about  $\theta_b$  and  $\theta_m$  and infers the values through pragmatic reasoning. When the cost of uttering *must q* is greater than the bare form, the pragmatic listener infers that  $p(q)$  is smaller than when the utterance is the less costly *bare q*. Given the weakened certainty of *q*, the listener may then infer that the speaker has indirect or imperfect evidence of *q*. Our empirical results and computational model support this account and provide a new perspective on the meaning of *must*: its weakened meaning derives straightforwardly from an M-implicature. We discuss this model in the context of efficient production and interpretation cost tradeoffs between speakers and listeners.

## References