- Linking hypothesis and number of response options modulate inferred scalar implicature rate
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Abstract

The past 15 years have seen increasing experimental investigations of core pragmatic 13 questions in the ever more active and lively field of experimental pragmatics. Within 14 experimental pragmatics, many of the core questions have relied on the operationalization of 15 the theoretical notion of 'implicature rate'. Implicature rate based results have informed the 16 work on acquisition, online processing, and scalar diversity, inter alia. Implicature rate has 17 typically been quantified as the proportion of 'pragmatic' judgments in two-alternative 18 forced choice truth value judgment tasks. Despite its theoretical importance, this linking 19 hypothesis from implicature rate to behavioral responses has never been extensively tested. Here we show that two factors dramatically affect the 'implicature rate' inferred from truth 21 value judgment tasks: a) the number of responses provided to participants; and b) the linking hypothesis about what constitutes a 'pragmatic' judgment. We argue that it is time 23 for the field of experimental pragmatics to engage more seriously with its foundational

assumptions about how theoretical notions map onto behaviorally measurable quantities,

and present a sketch of an alternative linking hypothesis that derives behavior in truth value

judgment tasks from probabilistic utterance expectations.
 Keywords: scalar implicature; methodology; linking hypothesis; experimental
 pragmatics; truth value judgment task

Word count: 9037

Linking hypothesis and number of response options modulate inferred scalar implicature rate

32 Introduction

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The past 15 years have seen the rise and development of a bustling and exciting new
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   field at the intersection of linguistics, psychology, and philosophy: experimental pragmatics
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   (Barner, Brooks, & Bale, 2011; Bonnefon, Feeney, & Villejoubert, 2009; Bott & Chemla,
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   2016; Bott & Noveck, 2004; Breheny, Ferguson, & Katsos, 2013; Breheny, Katsos, &
   Williams, 2006; Chierchia et al., 2001; De Neys & Schaeken, 2007; Degen & Tanenhaus, 2015,
   2016; Geurts & Pouscoulous, 2009; Grodner, Klein, Carbary, & Tanenhaus, 2010; Huang &
   Snedeker, 2009; Katsos & Bishop, 2011; I. A. Noveck & Reboul, 2008; Noveck & Posada,
   2003; Papafragou & Tantalou, 2004; van Tiel, van Miltenburg, Zevakhina, & Geurts, 2016;
   Tomlinson, Bailey, & Bott, 2013). Experimental pragmatics is devoted to experimentally
   testing theories of how language is used in context. How do listeners draw inferences about
   the – often underspecified – linguistic signal they receive from speakers? How do speakers
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   choose between the many utterance alternatives they have at their disposal?
        The most prominently studied phenomenon in experimental pragmatics is undoubtedly
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   scalar implicature. Scalar implicatures arise as a result of a speaker producing the weaker of
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two ordered scalemates (Geurts, 2010; Grice, 1975; Hirschberg, 1985; Horn, 1972). Examples

- 9 (1) Some of her pets are cats.
- 50 Implicature: Some, but not all, of her pets are cats.
- $Scale: \langle all, some \rangle$

are provided in (1-2).

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- (2) She owns a cat or a dog.
- Implicature: She owns a cat or a dog, but not both.
- Scale: $\langle and, or \rangle$

A listener, upon observing the utterances in (1-2) typically infers that the speaker intended to convey the meanings listed as *Implicatures*, respectively. Since Grice (1975), the agreed-upon abstract rationalization the listener could give for their inference goes something like this: the speaker could have made a more informative statement by producing the stronger alternative (e.g., *All of her pets are cats* in (1)). If the stronger alternative is true, they should have produced it to comply with the Cooperative Principle. They chose not to. Assuming the speaker knows whether the stronger alternative is true, it must not be true. The derivation procedure for ad hoc exhaustivity inferences such as in (3) is assumed to be calculable in the same way as for scalar implicatures, though the scale is assumed to be contextually driven.

65 (3) She owns a cat.

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- 66 Implicature: She owns only a cat.
- Scale: $\langle \text{cat and dog, cat} \rangle$

Because the basic reconstruction of the inference is much more easily characterized for scalar implicatures than for other implicatures, scalar implicatures have served as a test bed for many questions in experimental pragmatics, including, but not limited to:

- 1. Are scalar inferences default inferences, in the sense that they arise unless blocked by (marked) contexts (Degen, 2015; Horn, 1984; Levinson, 2000)?
- 2. Are scalar inferences default inferences, in the sense that they are computed
 automatically in online processing and only cancelled in a second effortful step if
 required by context (Bott & Noveck, 2004; Breheny et al., 2006; Degen & Tanenhaus,
 2016; Grodner et al., 2010; Huang & Snedeker, 2009; Politzer-Ahles & Fiorentino, 2013;
 Tomlinson et al., 2013)?
- 3. What are the (linguistic and extra-linguistic) factors that affect whether a scalar implicature is derived (Bergen & Grodner, 2012; Bonnefon et al., 2009; Breheny et al.,

- 2013, 2006; Chemla & Spector, 2011; De Neys & Schaeken, 2007; Degen, 2015; Degen
 & Goodman, 2014; Degen & Tanenhaus, 2015, 2016; Marneffe & Tonhauser, 2016;
 Potts, Lassiter, Levy, & Frank, 2015; Zondervan, 2010)?
- 4. How much diversity is there across implicature types, and within scalar implicatures across scale types, in whether or not an implicature is computed (Doran, Ward, Larson, McNabb, & Baker, 2012; van Tiel et al., 2016)?
- 5. At what age do children acquire the ability to compute implicatures (Barner et al., 2011; Horowitz, Schneider, & Frank, 2017; Katsos & Bishop, 2011; Musolino, 2004; Noveck, 2001; Papafragou & Tantalou, 2004; Stiller, Goodman, & Frank, 2015)?
- In addressing all of these questions, it has been important to obtain estimates of implicature rates. For 1., implicature rates from experimental tasks can be taken to inform whether scalar implicatures should be considered default inferences. For 2., processing measures on responses that indicate implicatures can be compared to processing measures on responses that indicate literal interpretations. For 3., contextual effects can be examined by comparing implicature rates across contexts. For 4., implicature rates can be compared across scales (or across implicature types). For 5., implicature rates can be compared across age groups.
- A standard measure that has stood as a proxy for implicature rate across many studies is the proportion of "pragmatic" judgments in truth value judgment paradigms (Bott & Noveck, 2004; Chemla & Spector, 2011; De Neys & Schaeken, 2007; Degen & Goodman, 2014; Degen & Tanenhaus, 2015; Geurts & Pouscoulous, 2009; Noveck, 2001; Noveck & Posada, 2003). In these kinds of tasks, participants are provided a set of facts, either presented visually or via their own knowledge of the world. They are then asked to judge whether a sentence intended to describe those facts is true or false (or alternatively, whether it is right or wrong, or they are asked whether they agree or disagree with the sentence). The crucial condition for assessing implicature rates in these kinds of studies typically

consists of a case where the facts are such that the stronger alternative is true and the target 107 utterance is thus also true but underinformative. For instance, Bott and Noveck (2004) 108 asked participants to judge sentences like "Some elephants are mammals", when world 109 knowledge dictates that all elephants are mammals. Similarly, Degen and Tanenhaus (2015) 110 asked participants to judge sentences like "You got some of the gumballs" in situations where 111 the visual evidence indicated that the participant received all the gumballs from a gumball 112 machine. In these kinds of scenarios, the story goes, if a participant responds "FALSE", that 113 indicates that they computed a scalar implicature, e.g. to the effect of "Not all elephants are 114 mammals" or "You didn't get all of the gumballs", which is (globally or contextually) false. 115 If instead a participant responds "TRUE", that is taken to indicate that they interpreted the 116 utterance literally as "Some, and possibly all, elephants are mammals" or "You got some, 117 and possibly all, of the gumballs".

Using the proportion of "FALSE" responses on true but underinformative trials as a 119 proxy for implicature rate is common in experimental pragmatics. For example, in one of the 120 first studies to investigate scalar implicatures experimentally, Noveck (2001) tested adults' 121 and children's interpretations of the scalar items might and some. The dependent measure in 122 Noveck (2001) was the rate of "logically correct responses", i.e. responding "ves" to 123 statements such as Some giraffes have long necks or There might be a parrot [in the box] 124 when there had to be a parrot in the box. He found that children responded "yes" more 125 frequently than adults, and concluded that children interpret scalar items some and might 126 more logically (i.e. literally). Similarly in another landmark study, Papafragou and Musolino 127 (2003) tested children and adults interpretation of the following set of scalar items: $\langle two, \rangle$ 128 three>, < some, all>, and < finish, start>. The dependent measure in this study was the proportion of "No" responses to a puppet's underinformative statement. The study 130 concluded that "while adults overwhelmingly rejected infelicitous descriptions, children 131 almost never did so". Furthermore, the study compared implicature rates across scales and 132 concluded that "children also differed from from adults in that their rejection rate on the 133

numerical scale was reliably higher than on the two other scales." In their final experiment, 134 Papafragou and Musolino (2003) modified their task to invite scalar inferences more easily. 135 They reported that this manipulation resulted in a significantly higher rejection rates. Based 136 on these results, they concluded that children's ability to compute implicatures is affected by 137 the type of scalar item as well as children's awareness of the task's goals. Since these early 138 pioneering studies, the rate of "FALSE" (or "No", "Wrong", "Disagree") responses on 139 underinformative trials in truth-value judgment tasks has become a commonplace dependent 140 measure (Doran et al (2012), Geurts and Pouscoulous (2009), Potts, Lassiter, Levy, and Frank (2016), inter alia.) 142

Given the centrality of the theoretical notion of "implicature rate" to much of 143 experimental pragmatics, there is to date a surprising lack of discussion of the basic 144 assumption that it is adequately captured by the proportion of "FALSE' responses in truth 145 value judgment tasks (but see Benz and Gotzner (2014); Geurts and Pouscoulous (2009); Degen and Goodman (2014); Katsos and Bishop (2011); Sikos et al (this issue)). Indeed, the 147 scalar implicature acquisition literature was shaken up when Katsos and Bishop (2011) 148 showed that simply by introducing an additional response option, children started looking 149 much more pragmatic than had been previously observed in a binary judgment paradigm. Katsos and Bishop (2011) allowed children to distribute a small, a big, or a huge strawberry 151 to a puppet depending on "how good the puppet said it". The result was that children gave 152 on average smaller strawberries to the puppet when he produced underinformative 153 utterances compared to when he produced literally true and pragmatically felicitous 154 utterances, suggesting that children do, in fact, display pragmatic ability even at ages when 155 they had previously appeared not to. 156

But this raises an important question: in truth value judgment tasks, how does the
researcher know whether an interpretation is literal or the result of an implicature
computation? The binary choice task typically used is appealing in part because it allows for
a direct mapping from response options—"TRUE" and "FALSE"—to interpretations—literal

and pragmatic. That the seeming simplicity of this mapping is illusory becomes apparent 161 once a third response option is introduced, as in the Katsos and Bishop (2011) case. How is 162 the researcher to interpret the intermediate option? Katsos and Bishop (2011) grouped the 163 intermediate option with the negative endpoint of the scale for the purpose of categorizing 164 judgments as literal vs. pragmatic, i.e., they interpreted the intermediate option as 165 pragmatic. But it seems just as plausible that they could have grouped it with the positive 166 endpoint of the scale and taken the hard line that only truly "FALSE' responses constitute 167 evidence of a full-fledged implicature. The point here is that there has been remarkably little 168 consideration of linking hypotheses between behavioral measures and theoretical constructs 169 in experimental pragmatics, a problem in many subfields of psycholinguistics (Tanenhaus, 170 2004). We argue that it is time to engage more seriously with these issues. 171

We begin by reporting an experiment that addresses the following question: do the 172 number of response options provided in a truth value judgment task and the way that 173 responses are grouped into pragmatic ("SI") and literal ("no SI") change inferences about 174 scalar implicature rates? Note that this way of asking the question assumes two things: first, 175 that whatever participants are doing in a truth value judgment task, the behavioral measure 176 can be interpreted as providing a measure of interpretation; and second, that listeners either do or do not compute an implicature on any given occasion. In the General Discussion we 178 will discuss both of these issues. Following Degen and Goodman (2014), we will offer some remarks on why truth value judgment tasks are better thought of as measuring participants' 180 estimates of speakers' production probabilities. This will suggest a completely different class 181 of linking hypotheses. We then discuss an alternative conception of scalar implicature as a 182 probabilistic phenomeonen, a view that has recently rose to prominence in the subfield of 183 probabilistic pragmatics (Franke & Jäger, 2016; Goodman & Frank, 2016). This alternative 184 conception of scalar implicature, we argue, affords developing and testing quantitative 185 linking hypotheses in a rigorous and motivated way. 186

Consider a setup in which a listener is presented a card with a depiction of either one

or two animals (see Figure 1 for an example). As in a standard truth value judgment task, 188 the listener then observes an underinformative utterance about this card (e.g., "There is a 189 cat or a dog on the card") and is asked to provide a judgment on a scale with 2, 3, 4, or 5 190 response options, with endpoints "wrong" and "right." In the binary case, this reproduces 191 the standard truth value judgment task. Figure 1 exemplifies (some of) the researcher's 192 options for grouping responses. Under what we will call the "Strong link" assumption, only 193 the negative endpoint of the scale is interpreted as evidence for a scalar implicature having 194 been computed. Under the "Weak link" assumption, in contrast, any response that does not 195 correspond to the positive endpoint of the scale is interpreted as evidence for a scalar 196 implicature having been computed. Intermediate grouping schemes are also possible, but 197 these are the ones we will consider here. Note that for the binary case, the Weak and Strong 198 link return the same categorization scheme, but for any number of response options greater than 2, the Weak and Strong link can in principle lead to differences in inferences about 200 implicature rate. 201

Let's examine an example. Assume three response options (wrong, neither, right). 202 Assume further that each of the three responses was selected by a third of participants, i.e., 203 the distributions of responses is 1/3, 1/3, and 1/3. Under the Strong link, we infer that this 204 task yielded an implicature rate of 2/3. Under the Weak link, we infer that this task yielded 205 an implicature rate of 1/3. This is quite a drastic difference if we are, for instance, interested 206 in whether scalar implicatures are inference defaults and we would like to interpret an 207 implicature rate of above an arbitrary threshold (e.g., 50%) as evidence for such a claim. 208 Under the Strong link, we would conclude that scalar implicatures are not defaults. Under 209 the Weak link, we would conclude that they are. In the experiment reported in the following 210 section, we presented participants with exactly this setup. We manipulated the number of 211 response options between participants and analyzed the results under different linking 212

¹An open question concerns the extent to which the labeling of points on the scale affects judgments (e.g., "wrong"-"right" vs. "false"-"true" vs. "disagree"-"agree"). Studies vary in the labeling of scale points.

hypothesis.²

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Experiment

Participants played an online card game in which they were asked to judge descriptions 215 of the contents of cards. Different groups of participants were presented with different 216 numbers of response options. On critical trials, participants were presented with descriptions for the cards that typically result in exhaustivity implicatures ("There is a cat on the card" 218 when there was a cat and a dog) or scalar implicatures ("There is a cat or a dog on the card" 219 when there was a cat and a dog). We categorized their responses on such trials according to 220 the Weak and the Strong link introduced above, and tested whether the number of response options and the linking hypothesis led to different conclusions about the rate of computed 222 implicatures in the experimental task. 223

Methods

200 participants were recruited via Amazon Mechanical Turk. They Participants. optionally provided demographic information at the end of the study. Participants' mean age was 35. We also asked participants if they had any prior training in logic. 40 participants reported that they did, while 160 had no prior training in logic. All participants' data was

²Researchers may vary with respect to which linking hypothesis (Weak vs. Strong, or others) they consider most plausible. Supporters of the Weak link may argue that there are three theoretically motivated categories of judgments: false, true but infelicitous, true and felicitous. Under such an account, it is plausible that false and true+felicitous responses occupy the ends of the false/true scale while true but infelicitous responses occupy the mid portion. On critical trials, participants judge underinformative statements that are true but infelicitous and therefore the mid portion of the scale can provide evidence for implicature computation. However, supporters of the Strong link may argue that if a participant computes an implicature, their response in the task should show the commitment to that interpretation by judging the underinformative utterance as false. Any other response shows that they have not truly computed an implicature. So far, these discussions have remained largely informal. In this paper we stay neutral with respect to the plausibility of each link and only aim to demonstrate the consequences of assuming them.

29 included in the final analysis.³

Materials and procedure. The study was administered online through Amazon 230 Mechanical Turk.⁴ Participants were first introduced to the set of cards we used in the study 231 (Figure 2). Each card depicted one or two animals, where an animal could be either a cat, a 232 dog, or an elephant. Then participants were introduced to a blindfolded fictional character 233 called Bob. Bob was blindfolded to avoid violations of ignorance expectations associated with 234 the use of disjunction (Chierchia et al., 2001; Sauerland, 2004). Participants were told that 235 Bob would guess the contents of the cards and their task was to indicate whether Bob's guess 236 was wrong or right. On each trial, participants saw a card and a sentence representing Bob's 237 guess. For example, they saw a card with a cat and read the sentence "There is a cat on the 238 card." They then provided an assessment of Bob's guess. The study ended after 24 trials. 239

Two factors were manipulated within participants: card type and guess type. There 240 were two types of cards, cards with only one animal on them and cards with two animals. 241 There were three types of guesses: simple (e.g. There is a cat), conjunctive (e.g. There is a 242 cat and a doq), and disjunctive (e.g. There is a cat or a doq). Crossing card type and guess 243 type yielded trials of varying theoretical interest (see Figure 3): critical underinformative 244 trials that were likely to elicit pragmatic inferences (either scalar or exhaustive) and control 245 trials that were either unambiguously true or false. Each trial type occurred three times with 246 randomly sampled animals and utterances that satisfied the constraint of the trial type. 247 Trial order was randomized. 248

On critical trials, participants could derive implicatures in two ways. First, on trials on which two animals were present on the card (e.g., cat and dog) but Bob guessed only one of them (e.g. "There is a cat on the card"), the utterance could have a literal interpretation ("There is a cat and possibly another animal on the card") or an exhaustive interpretation

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³This study was carried out in accordance with the recommendations of the Common Rule, Federal Office for Human Research Protections. The protocol was approved by the Stanford University IRB 2 (non-medical research). All subjects gave Informed consent, documentation was waived by the IRB.

⁴The experiment can be viewed here.

("There is only a cat on the card"). We refer to these trials as "exhaustive". Second, on trials 253 on which two animals were on the card (e.g., a cat and a dog) and Bob used a disjunction 254 (e.g., "There is a cat or a dog on the card"), the utterance could have the literal, inclusive, 255 interpretation, or a pragmatic, exclusive interpretation. We refer to these trials as "scalar". 256 In order to assess the effect of the number of response options on implicature rate, we 257 manipulated number of response options in the forced choice task between participants. We 258 refer to the choice conditions as "binary" (options: wrong, right), "ternary" (options: wrong, 259 neither, right), "quaternary" (options: wrong, kinda wrong, kinda right, right), and "quinary" 260 (wrong, kinda wrong, neither, kinda right, right). Thus, the endpoint labels always remained 261 the same. If there was an uneven number of response options, the central option was neither. 262 Participants were randomly assigned to one of the four task conditions. 263

64 Results and discussion

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The collected dataset contains 50 participants in the binary task, 53 in the ternary task, 43 in the quaternary task, and 54 in the quinary task. Figures 4 to 7 show the proportions of response choices in each of the 8 trial types on each of the four response tasks, respectively. We report the relevant patterns of results qualitatively before turning to the quantitative analysis of interest.

Qualitative analysis. In the binary task, participants were at or close to ceiling in 270 responding "right" and "wrong" on unambiguously true and false trials, respectively (see 271 Figure 4). However, on underinformative trials (i.e. a "cat" or "cat or dog" description for a 272 card with both a cat and a dog), we observe pragmatic behavior: on exhaustive trials, 273 participants judged the utterance "wrong" 14% of the time; on scalar trials, participants 274 judged the utterance "wrong" 38% of the time. That is, both under the Weak and Strong 275 link assumptions introduced in the Introduction, inferred implicature rate on exhaustive 276 trials is 14% and on scalar trials 38%. 277

In the ternary task, participants were also at or close to ceiling in responding "right"

and "wrong" on unambiguously true and false trials, respectively (see Figure 5). And again, 279 on underinformative trials (a "cat" and "cat or dog" description for a card with both a cat 280 and a dog), we observed pragmatic behavior: on exhaustive trials, participants considered 281 the guess "wrong" 8% of the time and neither wrong nor right 12% of the time. On scalar 282 trials, participants judged the guess "wrong" 23% of the time and "neither" 11% of the time. 283 This means that the Weak and Strong link lead to different conclusions about implicature 284 rates on the ternary task. Under the Weak link, inferred implicature rate on exhaustive trials 285 is 20%; under the Strong link it is only 8%. Similarly, under the Weak link, inferred 286 implicature rate on scalar trials is 34%; under the Strong link it is only 23%. 287

In the quaternary task (Figure 6), participants were again at or close to ceiling in 288 responding "right" and "wrong" on 4 of the 6 unambiguously true and false trials. However, 289 with four response options, two of the control conditions appear to be showing signs of 290 pragmatic infelicity: when a conjunction was used and only one of the animals was on the 291 card, participants considered the guess "wrong" most of the time (46%), but they often 292 considered it "kinda wrong" (32%) or even "kinda right" (19%). This suggests that perhaps 293 participants considered the notion of a partially true or correct statement in our experimental setting. Disjunctive descriptions of cards with only one animal, while previously at ceiling for "right" responses, were downgraded to only "kinda right" 26% of the 296 time, presumably because these utterances are also underinformative, though the degree of 297 underinformativeness may be less egregious than on scalar trials. 298

On underinformative exhaustive trials, we observed pragmatic behavior as before:
participants judged the guess "wrong" 2% of the time, "kinda wrong" 5% of the time, and
wkinda right" 66% of the time. On scalar trials, participants judged the guess "wrong" 6% of
the time, "kinda wrong" 12% of the time, and "kinda right" 43% of the times.

Thus, we are again forced to draw different conclusions about implicature rates
depending on whether we assume the Weak link or the Strong link. Under the Weak link,
inferred implicature rate on exhaustive trials is 73%; under the Strong link it is only 2%.

Similarly, under the Weak link, inferred implicature rate on scalar trials is 61%; under the Strong link it is only 6%.

Finally, Figure 7 shows the proportion of responses in the quinary task. Performance on the 4 pragmatically felicitous control trials was again at floor and ceiling, respectively.

The 2 control conditions in which the quaternary task had revealed pragmatic infelicity again displayed that pragmatic infelicity in the quinary task, suggesting that this is a robust type of pragmatic infelicity that, nonetheless, requires fine-grained enough response options to be detected experimentally.

On underinformative exhaustive trials, we observed pragmatic behavior as before:
participants judged the guess "wrong" 2% of the time, "kinda wrong" 1 and 1% of the time,
ineither" 1 and 1% of the time, and "kinda right" 72% of the time. On scalar trials,
participants judged the guess "wrong" 6% of the time, "kinda wrong" 4% of the time,
ineither" 1% of the time, and "kinda right" 52% of the time.

Thus, we would again draw different conclusions about implicature rates depending on whether we assume the Weak link or the Strong link. Under the Weak link, inferred implicature rate on exhaustive trials is 76 and 76%; under the Strong link it is only 2%.

Similarly, under the Weak link, inferred implicature rate on scalar trials is 63%; under the Strong link it is only 6%.

Quantitative analysis. Our primary goal in this study was to test whether the
estimated implicature rate in the experimental task is affected by the linking hypothesis and
the number of response options available to participants. To this end, we only analyzed the
critical trials (exhaustive and scalar). In particular, we classified each data point from
critical trials as constituting an implicature (1) or not (0) under the Strong and Weak link.
Figure 8 shows the resulting implicature rates by condition and link. It is immediately
apparent that there is variability in inferred implicature rate. In particular, the Weak link
appears to result in greater estimates of implicature rates in tasks with four or five response
options, compared to the Strong link. For the binary and ternary task, the assumed link

333 appears to play a much smaller role.

To analyze the effect of link and response options on inferred implicature rate, we used 334 a Bayesian binomial mixed effects model using the R packge "brms" (Bürkner & others, 335 2016) with weakly informative priors.⁵ The model predicted the log odds of implicature over 336 no implicature from fixed effects of response type (binary, ternary, quaternary, quinary – 337 dummy-coded with binary as reference level), link (strong vs. weak – dummy-coded with 338 strong as reference level), and trial type (exhaustive vs. scalar – dummy-coded, with 339 exhaustive as reference level), as well as their two-way and three-way interactions. Following Barr, Levy, Scheepers, and Tily (2013), we included the maximal random effects structure 341 justified by the design: random intercepts for items (cards) and participants, random by-participant slopes for link, trial type, and their interaction, and random by-item slopes for link, trial type, response type, and their interactions. Since the number of response options 344 was a between-participant variable we did not include random slopes of response options for participants. Four chains converged after 2000 iterations each (warmup = 1000). Table 1 346 summarizes the mean parameter estimates and their 95% credible intervals. $\hat{R} = 1$ for all 347 estimated parameters. All the analytical decisions described here were pre-registered⁶. 348 The model provided evidence for the following effects: First, there was a main effect of 349 trial type such that scalar trials resulted in greater implicature rates than exhaustive trials 350 (Mean Estimate = 6.09, 95% Credible Interval=[1, 12.29]). Second, there was an interaction 351 between link and number of response options such that the quaternary task (Mean Estimate 352 = 14.03, 95% Credible Interval=[7.24, 21.88]) and the quinary task (Mean Estimate = 17.28, 353 95% Credible Interval=[10.64, 25.80]) resulted in greater implicature rates with a weak link 354 than with a strong link, but there was no evidence of a link-dependent difference in inferred 355 implicature rate for the binary and ternary task. Finally, there was a three-way interaction between link, trial type, and number of response options, driven by the binary/quinary 357 contrast (Mean Estimate = -7.74, 95\% Credible Interval=[-16.59, -0.16]). Simple effects 358

⁵For more information about the default priors of the "brms" package, see the brms package manual.

⁶Our preregistration can be accessed at https://aspredicted.org/tq3sz.pdf

analysis on only the binary and and quinary trials, separately for the exhaustive and scalar 359 subset of the data, revealed that the three-way interaction is driven by a different effect of 360 number of response options under the Weak vs Strong link for the two inference types. 361 Specifically, on exhaustive trials, number of response options (2 vs. 5) only resulted in 362 greater implicature rates under the Weak ($\beta = .2, p < .0001$), but not the Strong link ($\beta =$ 363 -.8, p < .82). In contrast, on scalar trials, number of response options (2 vs. 5) resulted in 364 greater implicature rates under the Weak ($\beta = 3.6, p < .005$) link, and in lower implicature 365 rates under the Strong link (β = -4.0, p < .0007). In sum, both number of response options and link affected the inferred implicature 367 rate, as did the type of inference (exhaustive vs. scalar).

General Discussion

370 Summary and methodological discussion

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In this paper we asked whether linking hypothesis and number of response options 371 available to participants in truth value judgment tasks affects inferred implicature rates. The 372 results presented here suggest they do. A linking assumption that considered the highest 373 point on the scale literal and any lower point pragmatic (Weak link) resulted in higher 374 implicature rates in tasks with 4 or 5 response options compared to the standard two options. 375 A linking hypothesis that considered the lowest point on the scale pragmatic and any higher 376 point literal (Strong link) reported lower implicature rates in tasks with 4 or 5 options 377 compared to the standard two options. The results suggest that the choice of linking 378 hypothesis is a crucial analytical step that can significantly impact the conclusions drawn 379 from truth value judgment tasks. In particular, there is danger for pragmatic ability to be 380 both under- and overestimated. 381 While the binary truth value judgement task avoids the analytic decision between 382 Strong and Weak linking hypothesis, the results reported here suggest that binary tasks can 383 also underestimate participants' pragmatic competence. In binary tasks, participants are 384

often given the lowest and highest points on a scale ("wrong" vs. "right") and are asked to report pragmatic infelicities using the lowest point (e.g. "wrong"). The study reported here 386 showed that on trials with true but pragmatically infelicitous descriptions, participants often 387 avoided the lowest point on the scale if they were given more intermediate options. Even 388 though the option "wrong" was available to participants in all tasks, participants in tasks 389 with intermediate options chose it less often. In computing implicature rate, this pattern 390 manifested itself as a decrease in implicature rate under the Strong link when more response 391 options were provided, and an increase in implicature rate under the Weak link when more 392 response options were provided. These observations are in line with Katsos and Bishop 393 (2011)'s argument that pragmatic violations are not as severe as semantic violations and 394 participants do not penalize them as much. Providing participants with only the extreme 395 ends of the scale (e.g. wrong/right, false/true) when pragmatic violations are considered to be of an intermediate nature risks misrepresentation of participants' pragmatic competence. It further suggests that in studies that use binary tasks to investigate response-contingent processing, proportions of "literal" responses may be a composite of both literal and 399 pragmatic underlying interpretations that just happen to get mapped differently onto 400 different response options by participants.

This study did not investigate the effect of response labels on the inferred implicature 402 rate. However, the results provided suggestive evidence that some options better capture participant intuitions of pragmatic infelicities than others. Among the intermediate options, 404 "kinda right" was chosen most often to report pragmatic infelicities. The option "neither" 405 was rarely used in the ternary and quinary tasks (where it was used as a midpoint), 406 suggesting that participants interpreted pragmatic infelicities as different degrees of being 407 "right" and not "neither right nor wrong." Therefore, options that capture degrees of being 408 "right" like "kinda right" may prove most suitable for capturing infelicity in the long run. 409 We leave this as a methodological issue for future research. 410

The study had three further design features worth investigating in future work. First,

the utterances were ostensibly produced by a blindfolded character. This was an intentional 412 decision to control for violation of ignorance expectations with disjunction. A disjunction 413 such as "A or B" often carries an implication or expectation that the speaker is not certain 414 which alternative actually holds. Future work should investigate how the violation of the 415 ignorance expectation interacts with link and number of response options in inferred 416 implicature rate. Second, in this study we considered exhaustive and scalar implicatures 417 with or. If the observed effects of link and number of response options hold in general, they 418 should be observable using other scales, e.g., on implicatures with *some*. Finally, our 419 experiment was designed as a guessing game and the exact goal or task-relevant Question 420 Under Discussion of the game was left implicit. Given the past literature on QUD effects on 421 scalar implicature, we expect that different goals – e.g., to help the character win more 422 points vs. to help the character be more accurate – would affect how strict or lenient participants are with their judgments and ultimately affect implicature rate in the task (Degen & Goodman, 2014; Zondervan, 2010). Future work should systematically vary the goal of the game and explore its effects on the inferred implicature rate. But crucially, it's 426 unlikely that the observed effects of number of response options and linking hypothesis on 427 inferred implicature rate are dependent on any of the discussed design choices.

Revisiting the linking hypothesis

On the traditional view of the link between implicature and behavior in sentence
verification tasks, scalar implicature is conceptualized as a binary, categorical affair – that is,
an implicature is either "calculated" or it isn't, and the behavioral reflexes of this categorical
interpretation process should be straightforwardly observed in experimental paradigms. This
assumption raises concerns for analyzing variation in behavior on a truth value judgment
task; for example, why did the majority of respondents in the binary condition of our
experiment answer "right" to an utterance of the underinformative "There is a cat or dog"
when the card had both a cat and a dog on it? And why did a sizeable minority nonetheless

choose "wrong" in this same condition?

To explain these data on the traditional view, we are forced to say that a) not all 439 participants calculated the implicature; or that b) some participants who calculated the implicature did not choose the anticipated (i.e., "wrong") response due to some other 441 cognitive process which overrode the "correct" implicature behavior; or some mixture of (a) 442 and (b). We might similarly posit that one or both of these factors underlie the variation in 443 the ternary, quaternary, and quinary conditions. However, without an understanding of how 444 to quantitatively specify the link between implicature calculation and its behavioral 445 expression, the best we can hope for on this approach is an analysis which predicts general 446 qualitative patterns in the data (e.g. a prediction of relatively more "right" responses than 447 "wrong" responses in a given trial of our binary truth value judgment task, or a prediction of 448 a rise in the rate of response of "right"/"wrong" between two experimental conditions, given 440 some contextual manipulation). However, we should stress that to the best of our knowledge, 450 even a qualitative analysis of this kind of variation in behavior on sentence verification tasks – 451 much less the effect of the number of response choices on that behavior – is largely 452 underdeveloped in the scalar implicature literature. 453

We contrast the above view of implicature and its behavioral reflexes with an 454 alternative linking hypothesis. Recent developments in the field of probabilistic pragmatics 455 have demonstrated that pragmatic production and comprehension can be captured within 456 the Rational Speech Act (RSA) framework (Bergen, Levy, & Goodman, 2016; Degen, Franke, 457 & Jäger, 2013; Degen, Tessler, & Goodman, 2015; Frank & Goodman, 2012; Franke & Jäger, 458 2016; Goodman & Frank, 2016; Goodman & Stuhlmüller, 2013; Kao, Wu, Bergen, & Goodman, 2014; Qing & Franke, 2015). Much in the spirit of Gricean approaches to pragmatic competence, the RSA framework takes as its point of departure the idea that individuals are rational, goal-oriented communicative agents, who in turn assume that their interlocutors similarly behave according to general principles of cooperativity in 463 communication. Just as in more traditional Gricean pragmatics, pragmatic inference and

pragmatically-cooperative language production in the RSA framework are, at their core, the product of counterfactual reasoning about alternative utterances that one might produce (but does not, in the interest of cooperativity). However, the RSA framework explicitly and quantitatively models cooperative interlocutors as agents whose language production and comprehension is a function of Bayesian probabilistic inference regarding other interlocutors' expected behavior in a discourse context.

Specifically, in the RSA framework we model pragmatically competent listeners as 471 continuous probabilistic distributions over possible meanings (states of the world) given an 472 utterance which that listener observes. The probability with which this listener L_1 ascribes a 473 meaning s to an utterance u depends upon a prior probability distribution of potential states 474 of the world P_w , and upon reasoning about the communicative behavior of a speaker S_1 . S_1 in turn is modeled as a continuous probabilistic distribution over possible utterances given 476 an intended state of the world the speaker intends to communicate. This distribution is 477 sensitive to a rationality parameter α , the production cost C of potential utterances, and the 478 informativeness of the utterance, quantified via a representation of a literal listener L_0 whose 479 interpretation of an utterance is in turn a function of that utterance's truth conditional 480 content [[u]](s) and her prior beliefs about the state of the world $P_w(s)$. 481

482
$$P_{L_1}(s|u) \propto P_{S_1}(u|s) * P_w(s)$$

483 $P_{S_1}(u|s) \propto exp(\alpha(log(L_0(s|u)) - C(u)))$
484 $P_{L_0}(s|u) \propto [[u]](s) * P_w(s)$

This view contrasts with the traditional view in that it is rooted in a quantitative formalization of pragmatic competence which provides us a continuous measure of pragmatic reasoning. In the RSA framework, individuals never categorically draw (or fail to draw) pragmatic inferences about the utterances they hear. For example, exclusivity readings of disjunction are represented in RSA as relatively lower posterior conditional probability of a conjunctive meaning on the P_L distribution given an utterance of "or", compared to the prior probability of that meaning. Thus, absent auxiliary assumptions about what exactly

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would constitute "implicature", it is not even possible to talk about rate of implicature
calculation in the RSA framework. The upshot, as we show below, is that this view of
pragmatic competence does allow us to talk explicitly and quantitatively about rates of
observed behavior in sentence verification tasks.

We take inspiration from the RSA approach and treat participants' behavior in our 496 experimental tasks as the result of a soft-optimal pragmatic speaker in the RSA framework. 497 That is, following Degen and Goodman (2014), we proceed on the assumption that behavior 498 on sentence verification tasks such as truth value judgment tasks, is best modeled as a 490 function of an individual's mental representation of a cooperative speaker (S_1) in the 500 language of RSA) rather than of a pragmatic listener who interprets utterances (P_{L_1}) . In 501 their paper, Degen & Goodman show that sentence verification tasks are relatively more 502 sensitive to contextual features like the Question Under Discussion than are sentence 503 interpretation tasks, and that this follows if sentence interpretation tasks – but not sentence 504 verification tasks – require an additional layer of counterfactual reasoning about the 505 intentions of a cooperative speaker.

A main desideratum of a behavioral linking hypothesis given the RSA view of pragmatic competence is to transform continuous probability distributions into categorical outputs (e.g. responses of "right"/"wrong" in the case of the binary condition of our experiment). For a given utterance u and an intended communicated meaning s, $S_1(\mathbf{u} \mid \mathbf{s})$ outputs a conditional probability of u given s. For example, in the binary condition of our experiment where a participant evaluated "There is a cat or a dog" when there were both animals on the card, the participant has access to the mental representation of S_1 and hence

⁷Degen and Goodman (2014) argue that sentence verification is more plausibly construed as a production task rather than as an interpretation task because participants, unlike in natural language comprehension, are provided with the ground truth about the state of the world that a speaker is describing. Thus, participants are in essence being asked to assess the quality of a speaker's utterance. In contrast, Degen and Goodman argue, true interpretation tasks are characterized by the listener inferring what the state of the world is that the speaker is describing, for instance by selecting from one of multiple interpretation options.

to the S_1 conditional probability of producing the utterance "cat or dog" given a dog and cat card: S_1 ("cat or dog" | cat and dog). According to the linking hypothesis advanced here, the participant provides a particular response to u if the RSA speaker probability of u lies within a particular probability interval. We model a responder, R, who in the binary condition responds "right" to an utterance u in world s just in case $S_1(u|s)$ exceeds some probability threshold θ :

```
520 R(u, w, \theta)

521 = "right" iff S_1(u \mid s) > \theta

522 = "wrong" otherwise
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The model of a responder in the binary condition is extended intuitively to the 523 condition where participants had three response options. In this case, we allow for two 524 probability thresholds: θ_1 , the minimum standard for an utterance in a given world state to 525 count as "right", and θ_2 , the minimum standard for "neither". Thus, in the ternary 526 condition, R(u, s, θ_1 , θ_2) is "right" iff $S_1(\mathbf{u} \mid \mathbf{s}) > \theta_1$ and "neither" iff $\theta_1 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_2$. To 527 fully generalize the model to our five experimental conditions, we say that R takes as its 528 input an utterance u, a world state s, and a number of threshold variables dependent on a variable c, corresponding to the experimental condition in which the participant finds 530 themself (e.g. the range of possible responses available to R).

```
Given c = "ternary"
532
               R(u, w, \theta_1, \theta_2)
533
               = "right" iff S_1(\mathbf{u} \mid \mathbf{s}) > \theta_1
534
                = "neither" iff \theta_1 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_2
535
                = "wrong" otherwise
536
                Given c = "quaternary"
537
               R(u, w, \theta_1, \theta_2, \theta_3)
538
                = "right" iff S_1(\mathbf{u} \mid \mathbf{s}) > \theta_1
539
                = "kinda right" iff \theta_1 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_2
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= "kinda wrong" iff \theta_2 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_3
541
           = "wrong" otherwise
542
           Given c = "quinary"
543
          R(u, w, \theta_1, \theta_2, \theta_3, \theta_4)
           = "right" iff S_1(\mathbf{u} \mid \mathbf{s}) > \theta_1
545
           ="kinda right" iff \theta_1 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_2
546
           = "neither" iff \theta_2 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_3
547
           = "kinda wrong" iff \theta_3 > S_1(\mathbf{u} \mid \mathbf{s}) > \theta_4
548
           = "wrong" otherwise
549
           In an RSA model, S_1(\mathbf{u} \mid \mathbf{s}) will be defined for any possible combination of possible
550
    utterance and possible world state. One consequence of this is that for the purposes of our
551
    linking hypothesis, participants are modeled as employing the same decision criterion – does
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    S_1(\mathbf{u} \mid \mathbf{s}) exceed the threshold? – in both "implicature" and "non-implicature" conditions of
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    a truth value judgment task experiment. That is, participants never evaluate utterances
    directly on the basis of logical truth or falsity: for example, our blindfolded character Bob's
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    guess of "cat and dog" on a cat and dog card trial is "right" to the vast majority of
556
    participants not because the guess is logically true but because S_1 ("cat and dog" | cat and
557
    dog) is exceedingly high.
558
           For further illustration, we use our definition of a pragmatically-competent speaker S_1
559
    (as defined above) to calculate the speaker probabilities of utterances in states of the world
560
    corresponding to our experimental conditions (i.e., for "cat", "dog", "cat and dog", and
561
    "elephant", given either a cat on the card, or both a cat and a dog on the card). In
    calculating these probabilities, we assume that the space of possible utterances is the set of
    utterances made by Bob in our experiment (i.e. any possible single, disjunctive, or
564
    conjunctive guess involving "cat", "dog", or "elephant"). For the purposes of our model, we
565
    assume a uniform cost term on all utterances. We furthermore assume that the space of
566
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possible meanings corresponds to the set of possible card configurations that a participant

may have seen in our experiment, and that the prior probability distribution over these world states is uniform. Lastly, we set α – the speaker rationality parameter – to 1. The resulting speaker probabilities are shown in Figure 9.⁸

The linking hypothesis under discussion assumes that speaker probabilities of utterance 571 given meaning are invariant across a) our four different experimental conditions, b) across 572 participants, and c) within participants (that is, participants do not update their S_1 573 distribution in a local discourse context). We note that the assumption (b) may conceivably 574 be relaxed by allowing one or more of the parameters in the model – including the prior 575 probability over world states P_w , the cost function on utterances C, or the rationality 576 parameter α – to vary across participants. We also note that assumption (c) in particular is 577 in tension with a growing body of empirical evidence that semantic and pragmatic 578 interpretation is modulated by rapid adaptation to the linguistic and social features of one's 579 interlocutors (Fine, Jaeger, Farmer, & Qian, 2013; Kleinschmidt & Jaeger, 2015; Yildirim, 580 Degen, Tanenhaus, & Jaeger, 2016). 581

However, if we should like to keep the above simplifying assumptions in place, then this 582 linking hypothesis commits us to explaining variation in the data in terms of the threshold 583 parameters of our responder model R. Consider first the variation in response across 584 different experimental conditions on a given trial, e.g. evaluation of a guess of "cat and dog" 585 when the card contains both a cat and a dog. The variation in the proportion of responses of 586 "right" on this trial between the binary, ternary, quaternary, and quinary conditions indicates 587 that the threshold value for "right" responses must vary across conditions; that is, we predict 588 that the θ of the binary condition will differ from, e.g., the θ_1 of the ternary condition as well 580 as the θ_1 of the quaternary condition. We also observed variation in response on this trial 590 within a single condition (for example, a sizeable minority of participants responded "wrong" 591

⁸Note that the probabilities in each facet don't sum to 1 because the model considers all possible disjunctive, conjunctive, and simple utterances, while we are only visualizing the ones corresponding to the experimental conditions.

to this trial in the binary condition). Thus, this linking hypothesis is committed to the notion that threshold values may vary across participants, such that a speaker probability of utterance $S_1(\mathbf{u} \mid \mathbf{s})$ can fall below θ for some subset of participants while $S_1(\mathbf{u} \mid \mathbf{s})$ itself remains constant across participants.

Lastly, for two utterances of the same conditional probability and in the same 596 experimental condition, participants in our experiment sometimes provided a judgment of 597 "right" to one utterance but "wrong" to the other. That is, there was within-subject 598 variation in this experiment. One way to represent such variation would be to posit that the 599 parameterization of threshold values proceeds stochastically and that threshold values are 600 recalibrated for every individual sentence verification task. Rather than representing a 601 threshold as a discrete value N between 0 and 1, we can represent that threshold as a 602 distribution over possible threshold values – with mass centered around N. Whenever an 603 individual encounters a single trial of our truth value judgment task experiment, a threshold 604 value is sampled from this distribution. By allowing values of θ to vary stochastically in this 605 way, we can capture that $S_1(\mathbf{u} \mid \mathbf{s})$ can fall both above and below θ for a given participant. 606

The model in its present form already captures an interesting asymmetry in inferred 607 implicature rates between exhaustive and scalar trials of the experiment: note specifically 608 (c.f. Figure 8) that inferred implicature rates are greater in the binary and ternary 609 conditions for scalar trials over exhaustive trials. This is expected given the model's inferred 610 speaker probabilities: the speaker probability of producing "There is a cat on the card" in 611 the context of there being a cat and dog on the card (an exhaustive implicature-inducing 612 trial) is greater than the speaker probability of producing "There is a cat or a dog on the card" in that same context (a scalar implicature-inducing trial). Assuming noisy θ values centered around N, participants are expected to respond 'Right' more frequently on 615 exhaustive than on scalar trials, which is precisely what is observed. Recall that these 616 probabilities were derived via the simplifying assumption of uniform cost on utterances; in 617 fact, adding cost to relatively complex disjunctive sentences over simple declarative sentences 618

only predicts a more pronounced asymmetry in the experimentally-observed direction.

As suggested above, the quantitative predictions of our model will depend crucially on 620 the values assigned to its free parameters - including (but not limited to) the probability 621 thresholds and speaker costs of possible utterances. However, the values of these parameters 622 can be estimated in a principled and informed manner through Bayesian statistical analysis 623 of our experimental data. Samples from prior distributions over possible parameter values 624 yield predicted patterns of response, which are then compared against empirically-observed 625 response patterns in order to determine the a posteriori probability that these values are in 626 fact the 'real' latent parameter values. The resulting posterior distributions are sampled 627 from in turn, in order to parameterize the model and assess overall quantitative fit given the 628 data. Though we leave a quantitative assessment of our model to future work (Waldon et al., 629 in prep), we sketch the general procedure here to emphasize that the model is amenable to 630 rigorous and data-driven evaluation. 631

One empirical problem is the pattern of responses we observed for "cat and dog" on 632 trials where there was only a cat on the card. Because this utterance is strictly false in this 633 world state, it is surprising – on both the traditional view as well as on the account 634 developed here – that participants assigned this utterance ratings above "wrong" with any 635 systematicity. However, this is what we observed, particularly in the quaternary and quinary conditions of the experiment, where a sizeable minority of participants considered this utterance "kinda right". As Figure 9 demonstrates, the conditional speaker probability of this utterance in this world state is 0; thus, there is no conceivable threshold value that 639 would allow this utterance to ever be rated above "wrong" (on the reasonable assumption 640 that the thresholds in our responder model R should be nonzero). Any linking hypothesis 641 will have to engage with this data point, and we leave to future work an analysis which 642 captures participants' behavior in this condition. 643

For the time being, however, we present the above analysis as a proof of concept for the following idea: by relaxing the assumptions of the traditional view of scalar

implicature—namely, that scalar implicatures either are or are not calculated, and that behavior on sentence verification tasks directly reflects this binary interpretation process—we 647 can propose quantitative models of the variation in behavior that is observed in experimental 648 settings. We note that the linking hypothesis proposed here is just one in the space of 649 possible hypotheses. For example, one might reject this threshold-based analysis in favor of 650 one whereby responses are the outcomes of sampling on the (pragmatic speaker or pragmatic 651 listener) probability distributions provided by an RSA model. We leave this systematic, 652 quantitative investigation to future work. For now we emphasize that explicit computational 653 modeling of behavioral responses is a tool that is available to researchers in experimental 654 pragmatics. While using the RSA framework as the modeling tool requires revising 655 traditional assumptions about the nature of scalar implicature by relaxing the crisp notion of 656 scalar implicature as something that is or is not "calculated" in interpretation, it provides new flexibility to explicitly discuss behavior in experimental settings. One need not adopt the RSA framework as the tool for hypothesizing and testing the link between theoretical constructs and behavior in pragmatic experiments. However, the empirical findings we have 660 reported here—that the inferences researchers draw about "implicature rate" are volatile and 661 depend on various features of the paradigm and the linking hypothesis employed—strongly 662 suggest that experimental pragmatics as a field must engage more seriously with the 663 foundational questions of what we are measuring in the experiments we run. 664

Concluding, we have shown in this paper that inferred "implicature rate" – a ubiquitous notion in theoretical and experimental pragmatics – as estimated in truth value judgment tasks, depends on both the number of responses participants are provided with as well as on the linking hypothesis from proportion of behavioral responses to "implicature rate". We further sketched an alternate linking hypothesis that treats behavioral responses as the result of probabilistic reasoning about speakers' likely productions. While a thorough model comparison is still outstanding, this kind of linking hypothesis opens a door towards more systematic and rigorous formulation and testing of linking hypotheses between theoretical notions of interest in pragmatics and behavioral responses in experimental paradigms.

Author Responsibilities

All authors contributed to the conception and design of the study. MJ conducted the online survey studies; reported the results and performed the statistical analysis; BW conducted the modeling and wrote the discussion section; JD wrote the theoretical introduction, and contributed to the experimental section and the discussion section and the modeling sections. All authors contributed to manuscript revision, read and approved the submitted version.

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Table 1

Model parameter estimates and their credible intervals. Rows marked with an asterisk in the evidence column do not contain 0 in the credible interval, thereby providing evidence for an effect.

Predictors	Estimate	2.5%	97.5%	Evidence
Intercept	-8.60	-13.98	-4.53	*
Link = Weak	-0.15	-4.86	4.77	
Task = Quaternary	-1.83	-8.08	4.20	
Task = Quinary	-4.05	-10.90	2.38	
Task = Ternary	-1.45	-7.31	4.56	
Implicature = Scalar	6.09	1.00	12.29	*
Link = Weak : Task = Quaternary	14.03	7.24	21.88	*
Link = Weak : Task = Quinary	17.28	10.64	25.80	*
Link = Weak : Task = Ternary	3.81	-1.49	9.22	
Link = Weak : Implicature = Scalar	0.90	-4.01	6.43	
Task = Quaternary : Implicature = Scalar	-5.67	-13.66	1.54	
Task = Quinary : Implicature = Scalar	-2.31	-9.30	4.61	
Task = Ternary : Implicature = Scalar	-1.31	-7.70	4.65	
Link=Weak : Task=Quaternary : Implicature=Scalar	-3.29	-12.07	4.55	
Link=Weak : Task=Quinary : Implicature=Scalar	-7.74	-16.59	-0.16	*
Link=Weak : Task=Ternary : Implicature=Scalar	-1.44	-7.00	4.22	

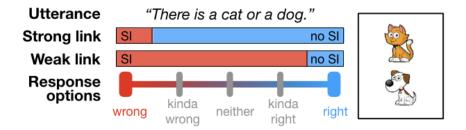


Figure 1. Strong and Weak link from response options to researcher inference about scalar implicature rate, exemplified for the disjunctive utterance when the conjunction is true.

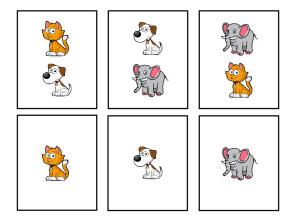


Figure 2. Cards used in the connective guessing game.

elephant	cat	cat and dog	cat or dog	
control:	control:	control:	control:	
unambiguously	unambiguously	unambiguously	unambiguously	
false	true	false	true	
control:	critical:	control:	critical:	
unambiguously	exhaustivity	unambiguously	scalar	
false	implicature	true	implicature	

Figure 3. Trial types (critical and control). Headers indicate utterance types. Rows indicate card types. Critical trials are marked in bold.

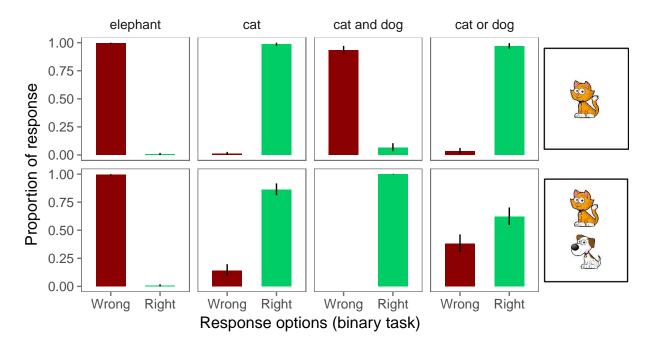


Figure 4. Proportion of responses for the binary forced choice judgments. Error bars indicate 95% bootstrapped confidence intervals.

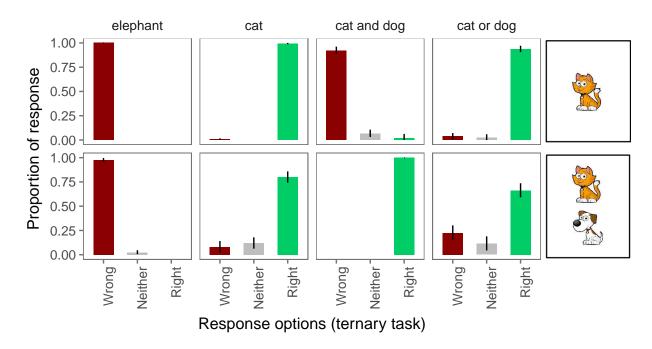


Figure 5. Proportion of responses for the ternary forced choice judgments. Error bars indicate 95% bootstrapped confidence intervals.

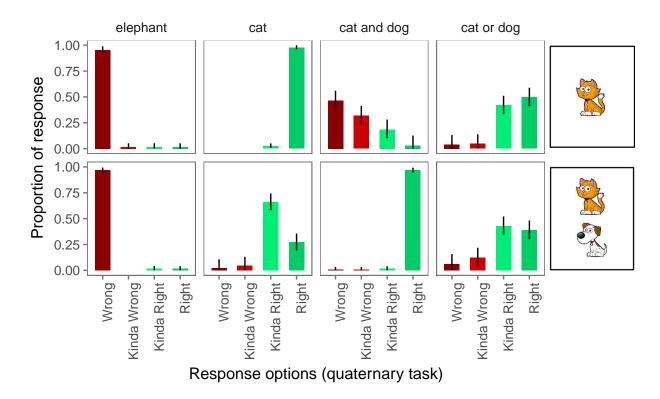


Figure 6. Proportion of responses for the quaternary forced choice judgments. Error bars indicate 95% bootstrapped confidence intervals.

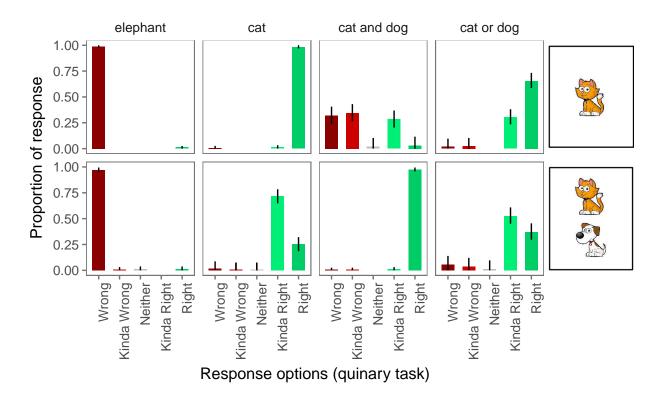


Figure 7. Proportion of responses for the quinary forced choice judgments. Error bars indicate 95% bootstrapped confidence intervals.

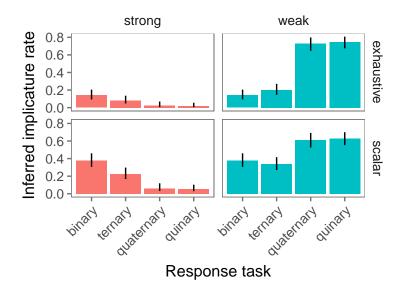


Figure 8. Inferred implicature rates on exhaustive and scalar trials as obtained with the binary, ternary, quaternary, and quinary response task. Columns indicate link from response to implicature rate (strong: proportion of "wrong judgments; weak: proportion of non-'right" judgments).

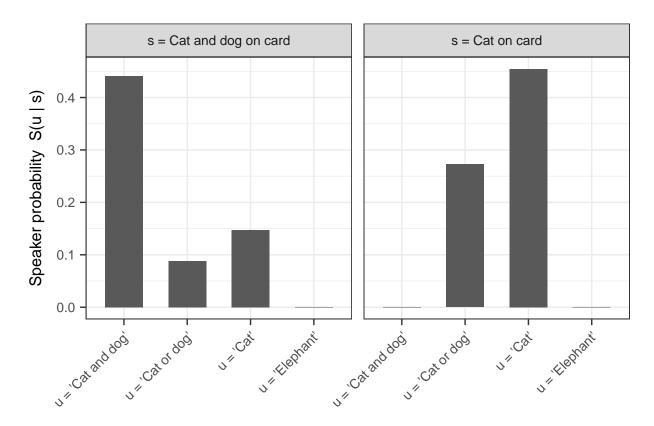


Figure 9. Speaker probabilities of utterances on the exhaustive and scalar trials, as obtained using the model described in this section.