

# Towards a unifying computational account of reference production and comprehension

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Feb 24, 2021

LingLangLunch, Brown University





# Reference comprehension and production

## Comprehension:

How do listeners predict the referent of (possibly ambiguous) referring expressions in real time?

## Production:

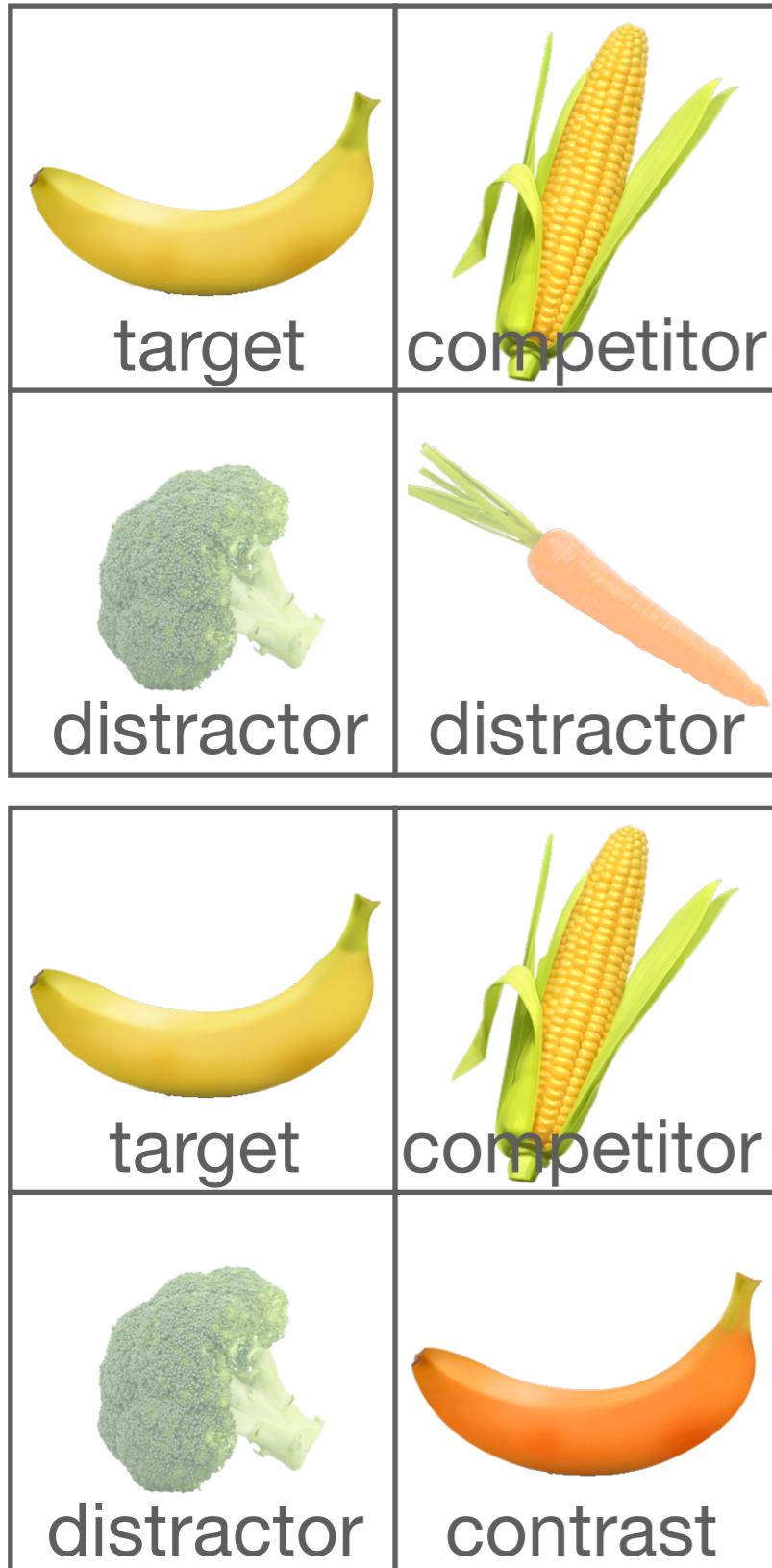
How do speakers decide which features of an object to include in a referring expression?

**Quantity-1:** Make your contribution as informative as required.

**Quantity-2:** Don't make your contribution more informative than necessary.

**Manner:** Be brief and orderly; avoid ambiguity and obscurity.

*“Click on the yellow...”*

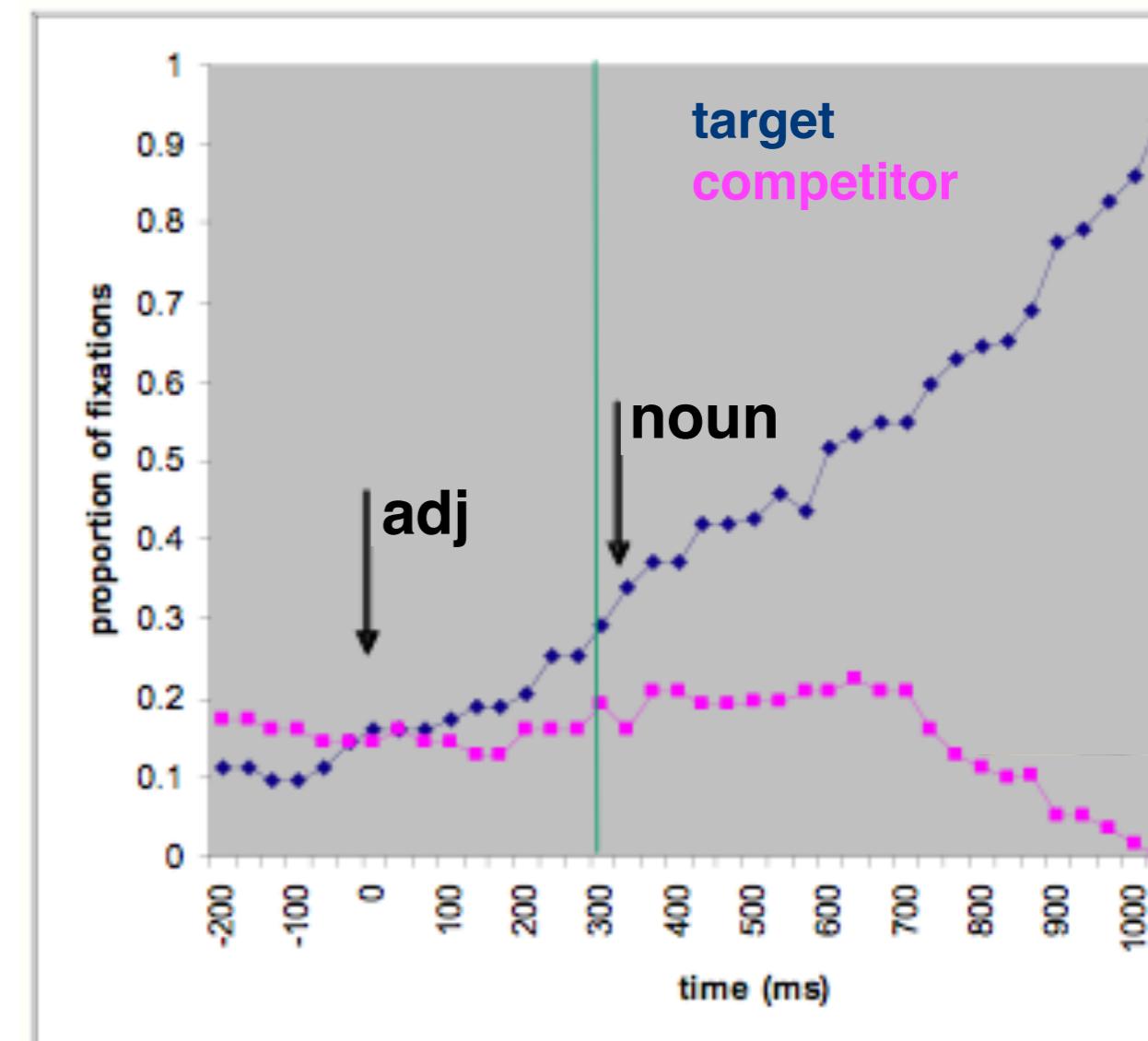


**no contrast**

Listeners  
expect  
speakers not  
to be over-  
informative.

**contrast**  
**Quantity-2**

# Comprehension: contrastive inferences



Sedivy et al 1999; Sedivy 2003; Grodner & Sedivy 2011; Heller et al 2008; Ryskin et al 2019; Rubio-Fernández & Jara-Ettinger 2018; Aparicio et al 2018; Alsop et al 2018

# Production: redundant referring expressions

**size sufficient**



*the small pin*

**75-80%**

**Quantity-2**

***the small blue pin***

**color sufficient**



*the blue pin*

**8-10%**

Speakers produce seemingly overinformative referring expressions.

Deutsch 1976; Pechmann 1989; Sedivy 2003; Gatt et al. 2011; Koolen et al 2013; Rubio-Fernández 2016; Westerbeek et al 2015; Davies & Katsos 2013; van Gompel et al 2019

# Reference comprehension and production

## Comprehension:

Listeners draw inferences based on the expectation that speakers not be over-informative.

## Production:

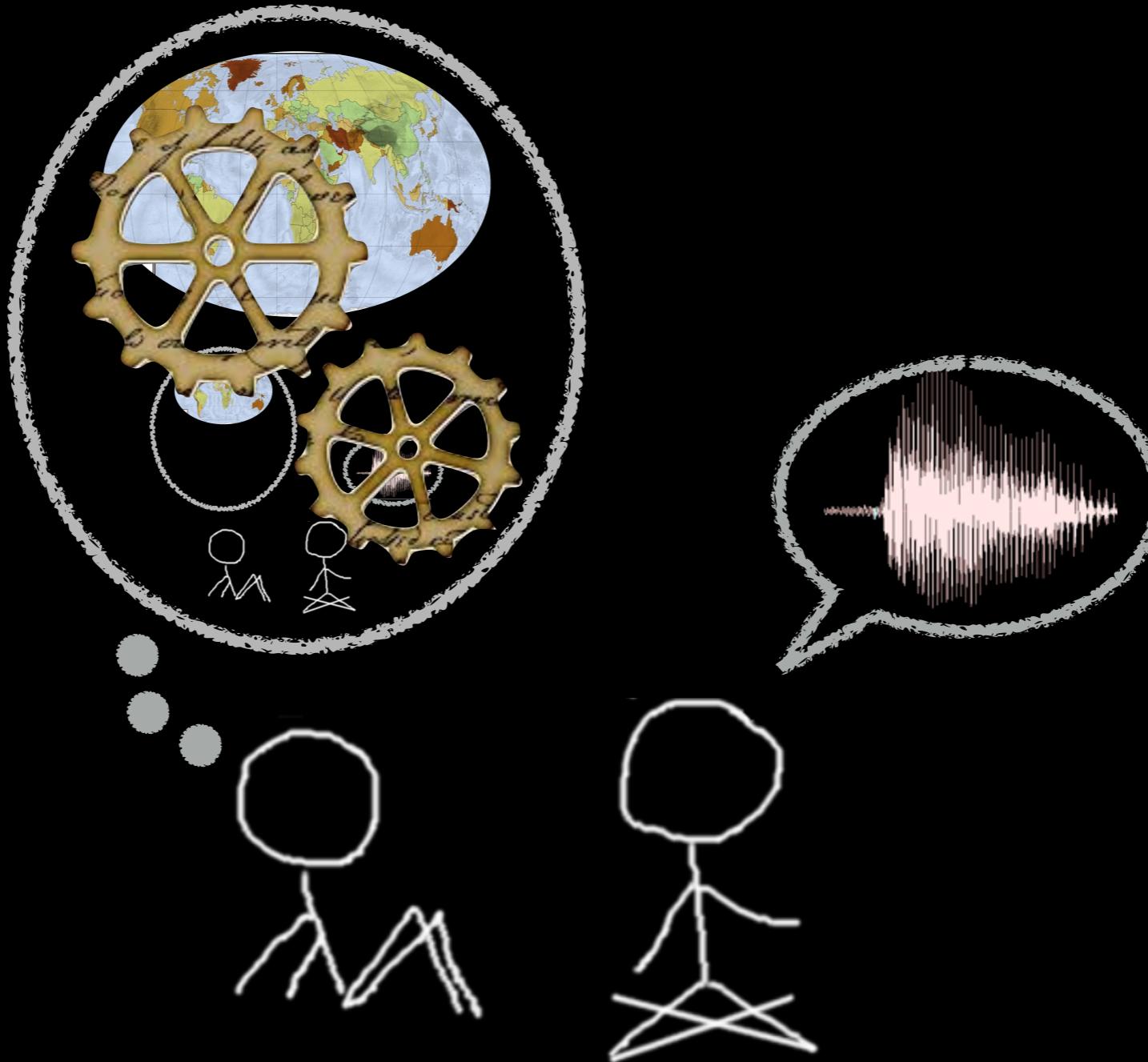
Speakers produce seemingly overinformative referring expressions.

Quantity-2

Qu~~a~~ntity-2

## HOW TO RESOLVE?

world  
knowledge  
reasoning  
context



linguistic  
signal

# PRAGMATICS

# Probabilistic pragmatics

Franke & Jäger, 2016; Goodman & Frank, 2016; Scontras, Tessler, & Franke 2018

## Reference

Frank & Goodman, 2012; Qing & Franke, 2015; Degen & Franke, 2012; Stiller et al., 2015; Franke & Degen, 2015; Degen et al, 2020

## Cost-based Quantity implicatures

Degen et al., 2013; Rohde et al., 2012

## Scalar implicatures

Goodman & Stuhlmüller, 2013; Degen et al., 2015

## Embedded implicatures

Potts et al., 2016; Bergen et al., 2016

## M-implicatures

Bergen et al., 2012

## Figurative meaning

Kao et al., 2013; 2014; 2015; Cohn-Gordon & Bergen, under review

## Gradable adjectives

Lassiter & Goodman, 2013; 2015; Qing & Franke, 2014

## Adjective ordering

Hahn et al 2018; Scontras et al 2019

## Other

plural predication Scontras & Goodman 2017

I-implicatures Poppels & Levy, 2016

generics Tessler & Goodman, 2019

modals Herbstritt & Franke, 2017

vague quantifiers Schöller & Franke, 2017

convention formation Hawkins et al 2018; 2019

questions Hawkins et al 2015

pragmatic adaptation Schuster & Degen, 2020

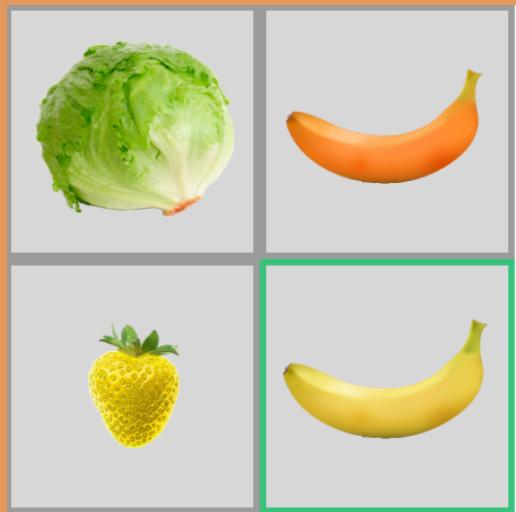
exhaustivity inferences Javangula & Degen in prep

atypicality inferences Kratvchenko & Demberg

social meaning Burnett 2017; 2019

# The Rational Speech Act framework (RSA)

**Comprehension:**  
contrastive inferences



“Click on the yellow...”

$$P_{L_1}(r|u) \propto P_{S_1}(u|r) \cdot P(r)$$

**Production:**  
redundant referring  
expressions



*the small blue pin*  
*la tachuela pequeña*

$$P_{S_1}(u|r) = e^{\alpha(\ln P_{L_0}(r|u) - C(u))}$$

$$P_{L_0}(r|u) \propto [[u]](r) \cdot P(r)$$



# PART I

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Elisa Kreiss

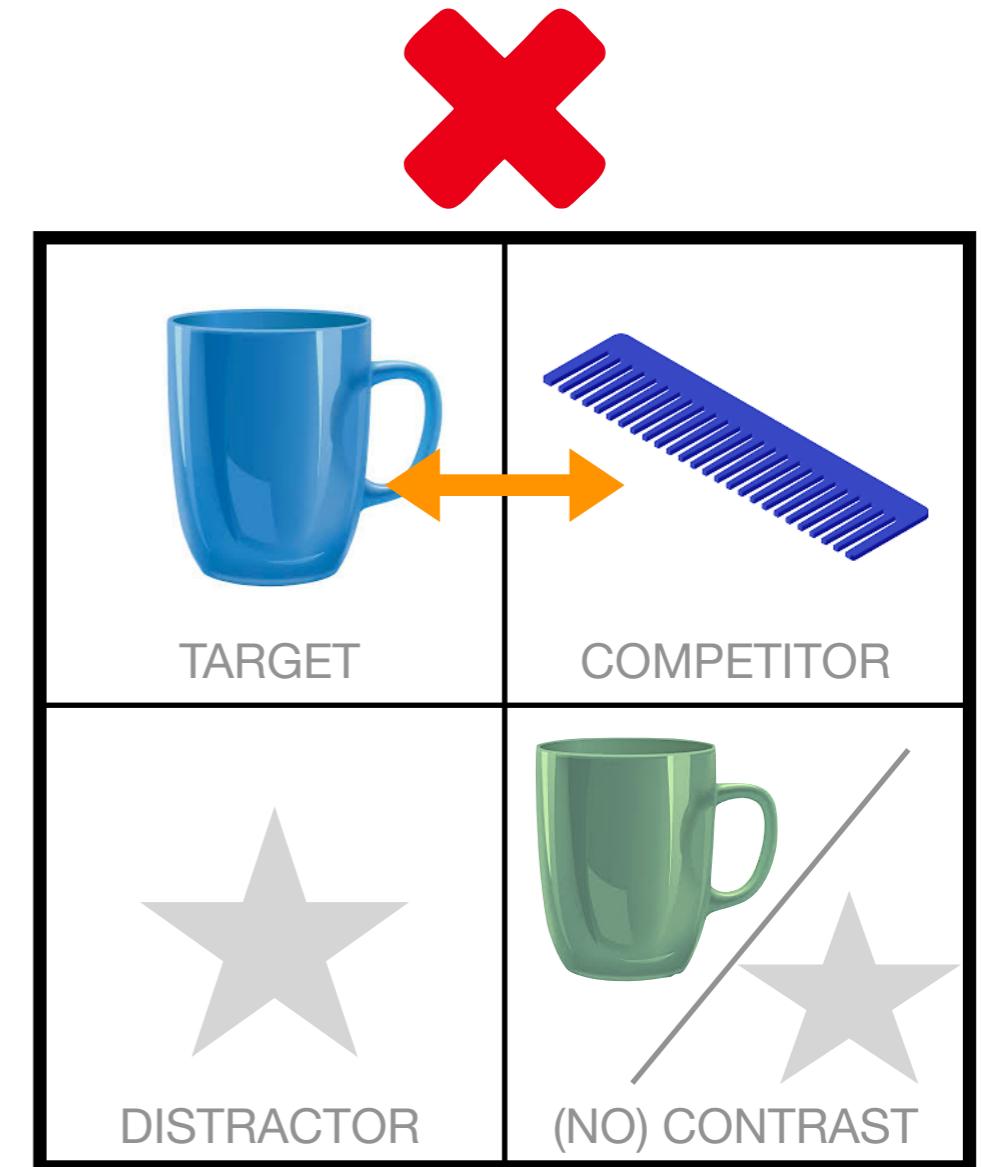
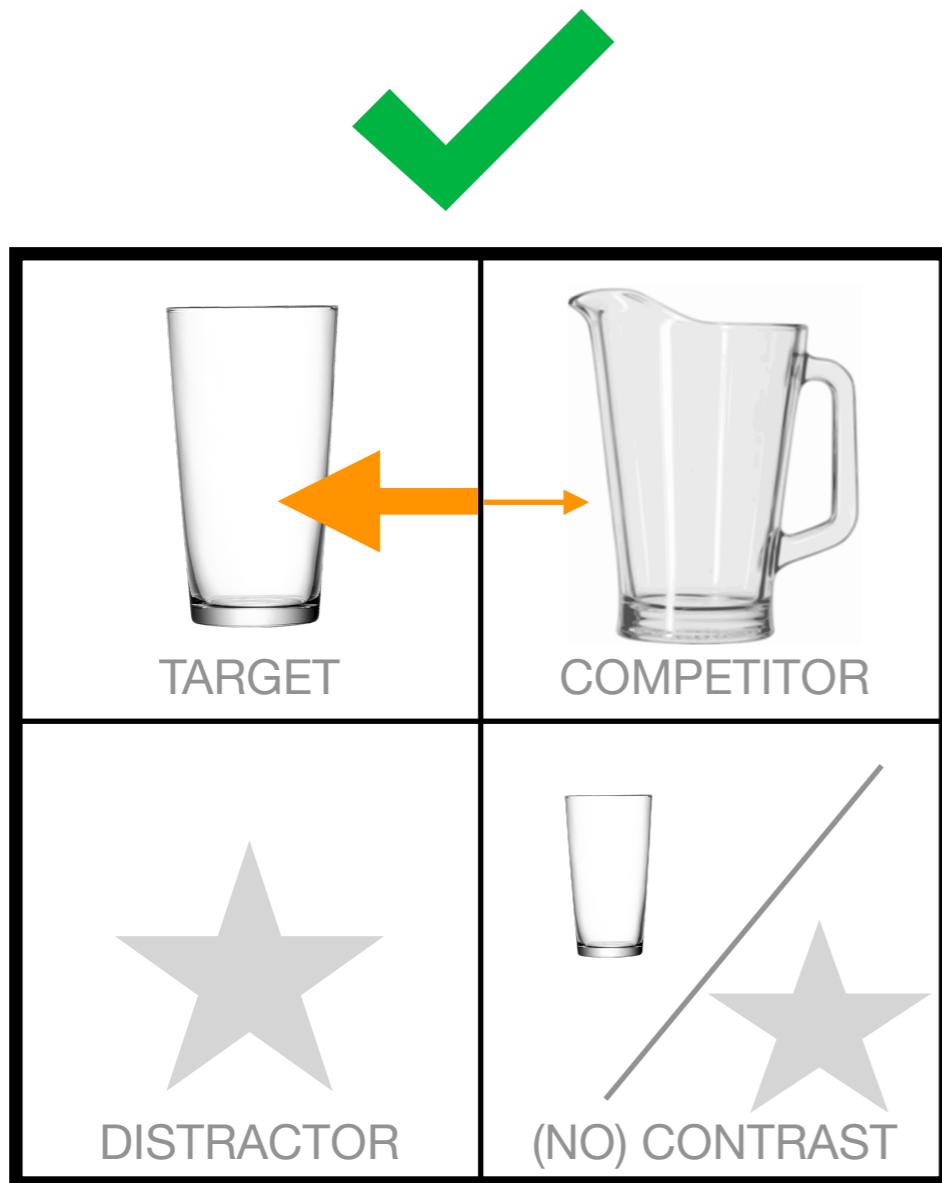
# Comprehension of referring expressions: contrastive inferences

Kreiss & Degen 2020, in prep

# Contrastive Inference (CI)

... is selected by the contrastive feature of a target object.

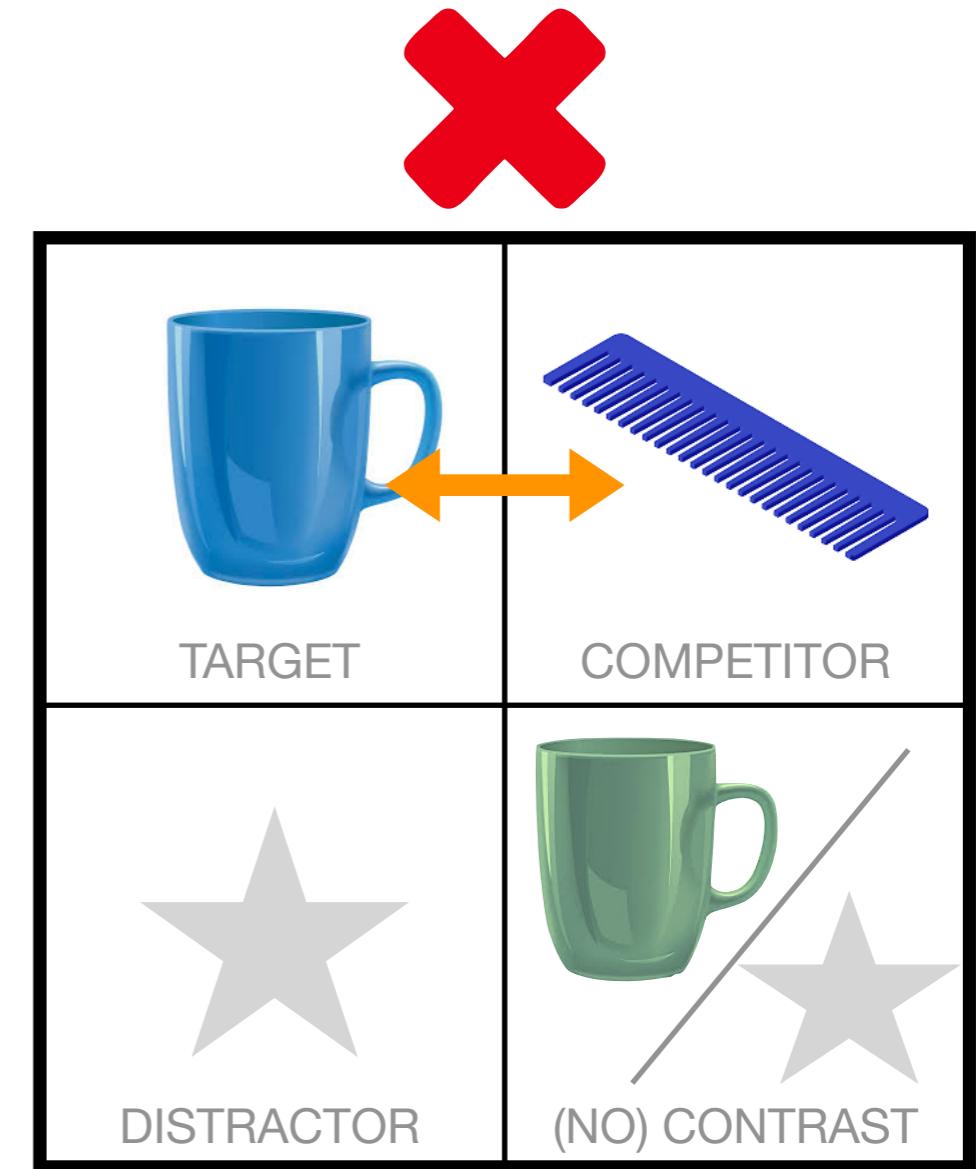
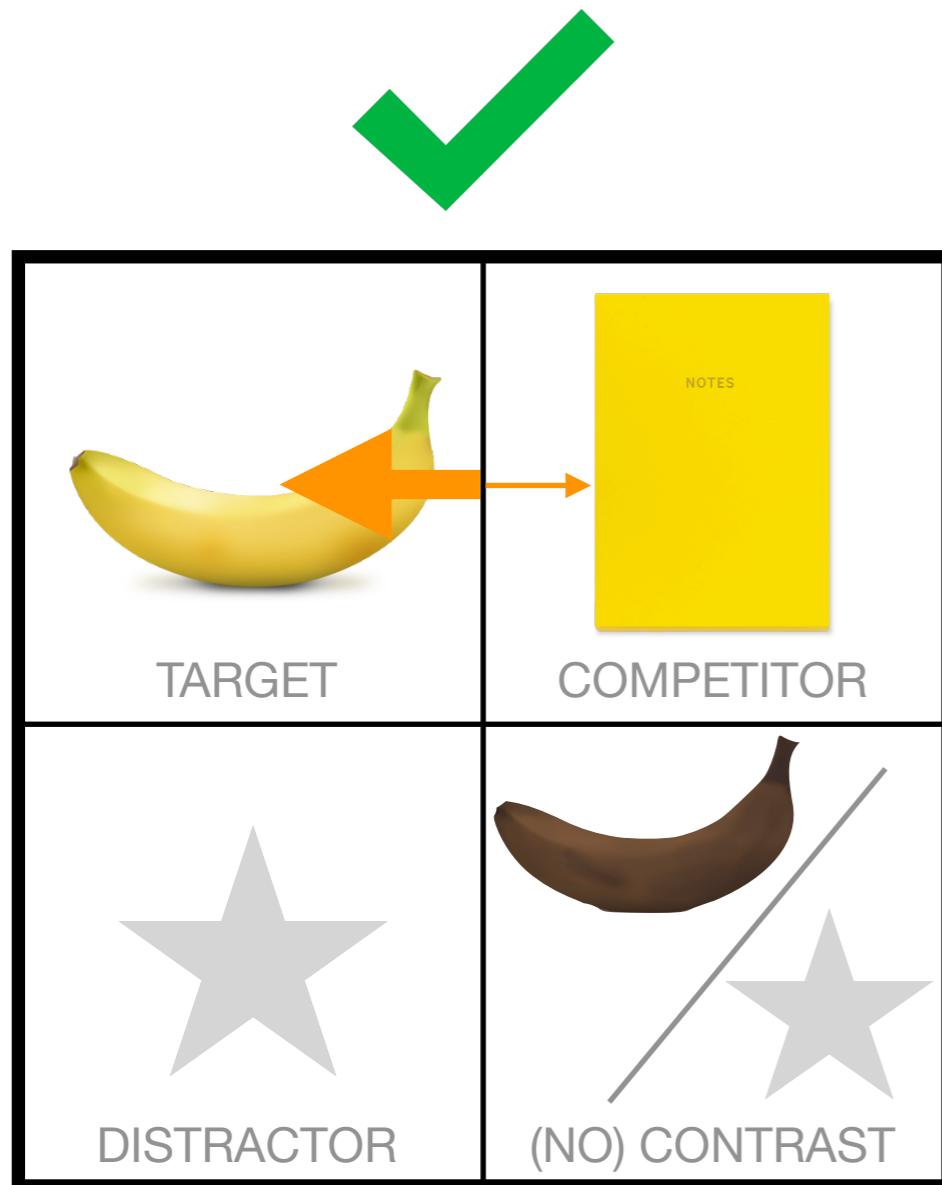
“Click on the (adj) ... !”



# Contrastive Inference (CI)

... is elicited by relative, but not (?) absolute adjectives.

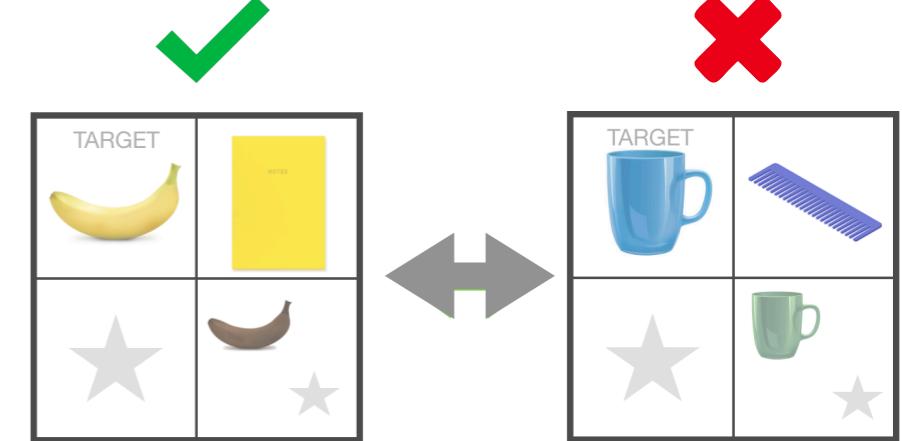
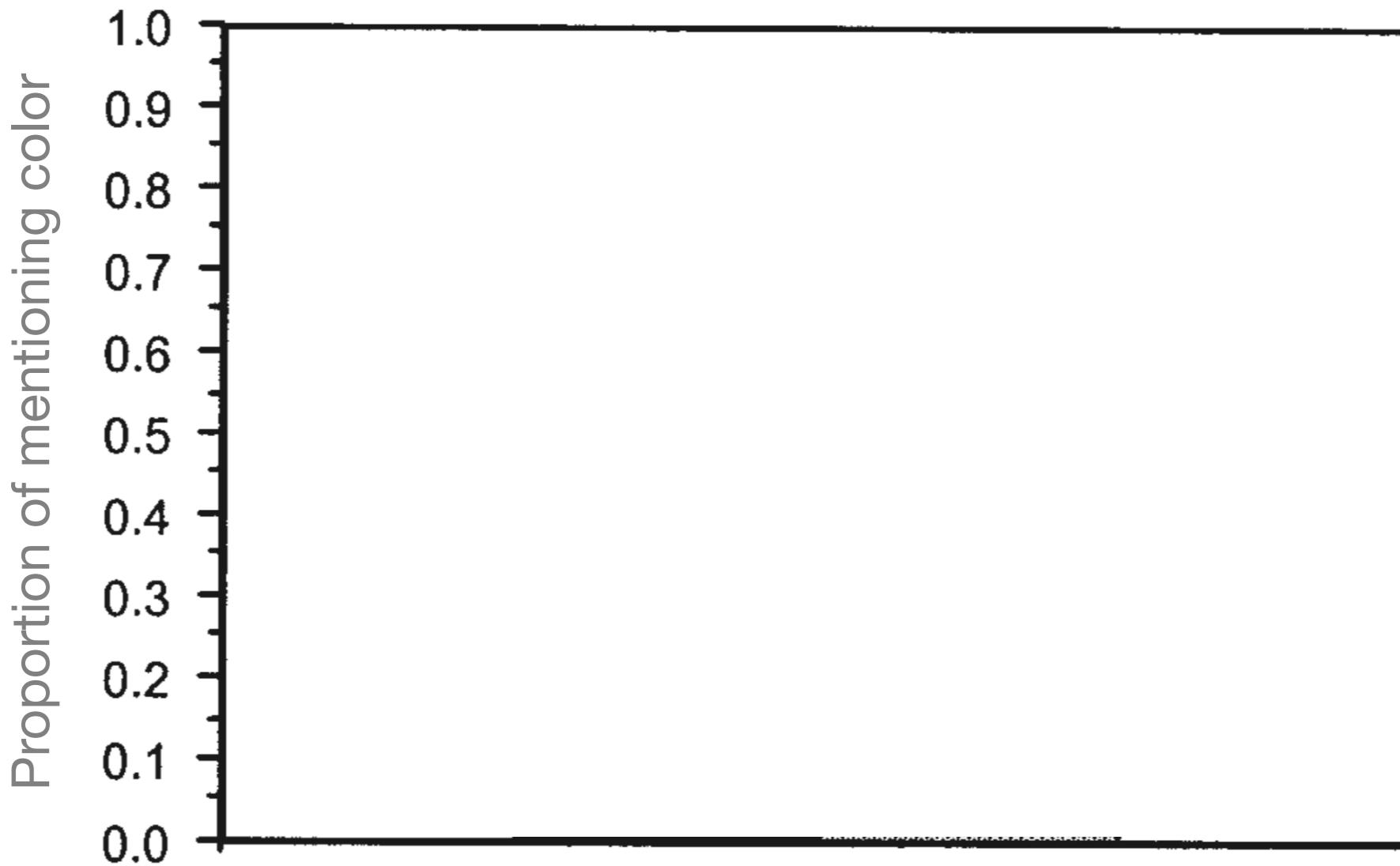
“Click on the (adj) ... !”



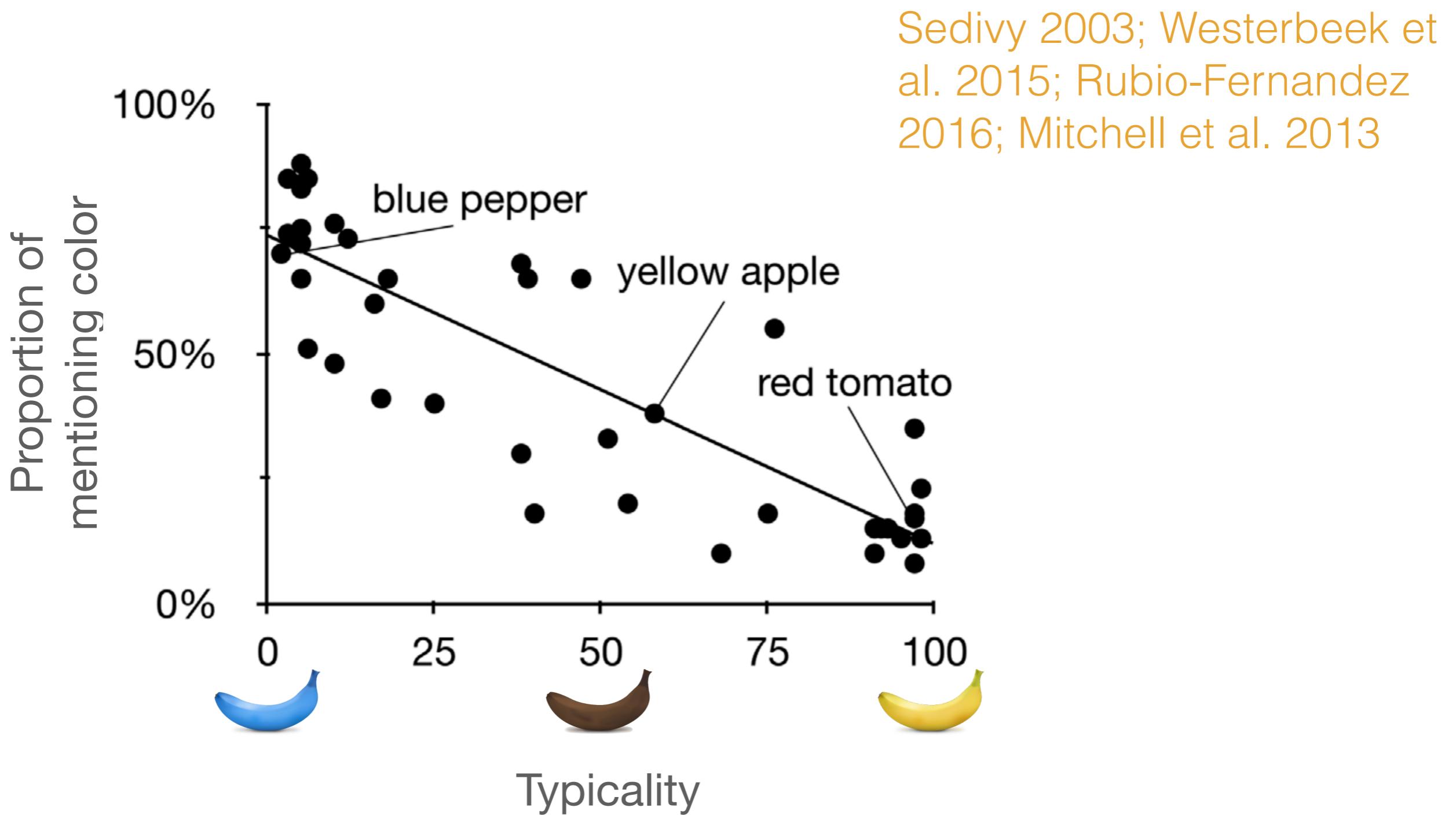
# Contrastive Inference (CI)

... is elicited by relative adjectives  
and absolute adjectives with a low production probability.

## Speech production



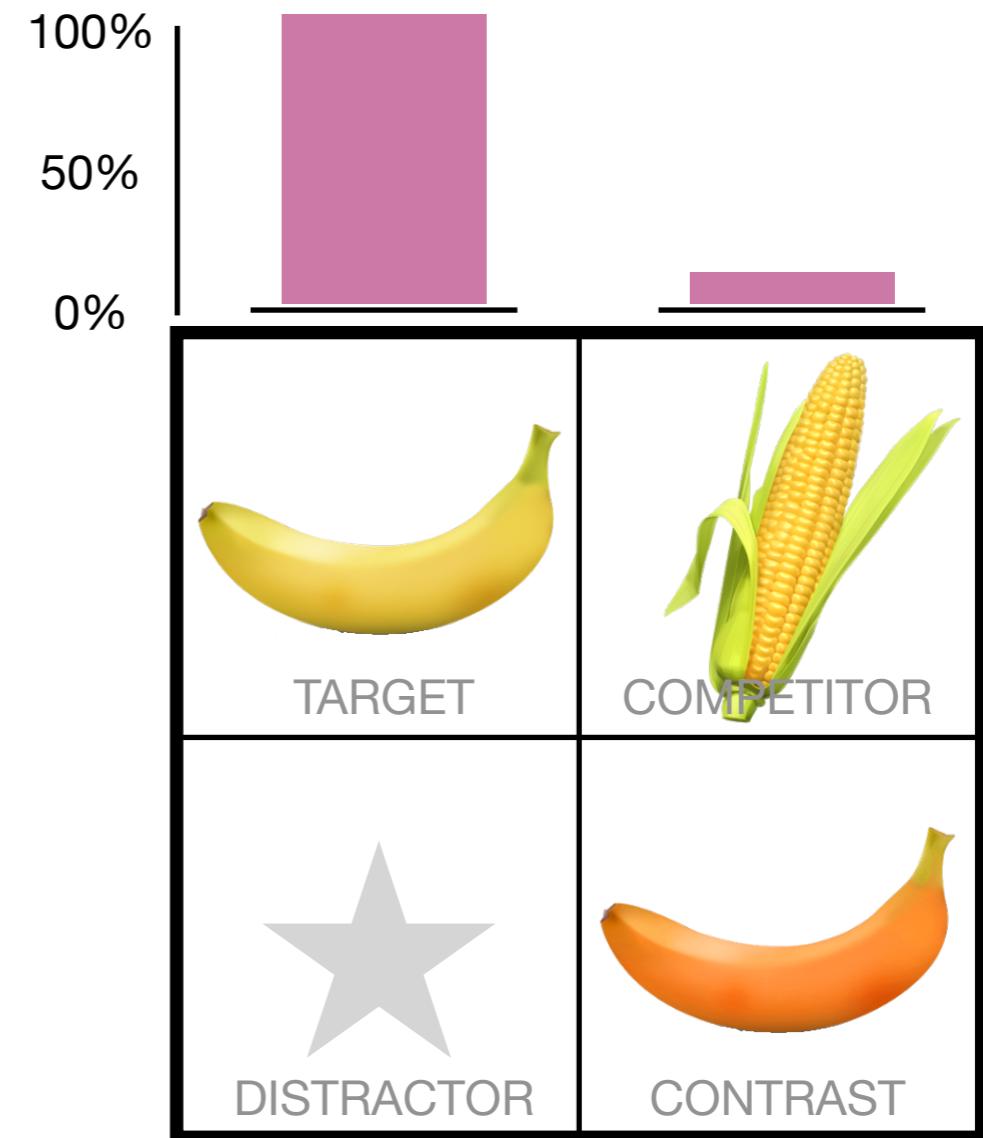
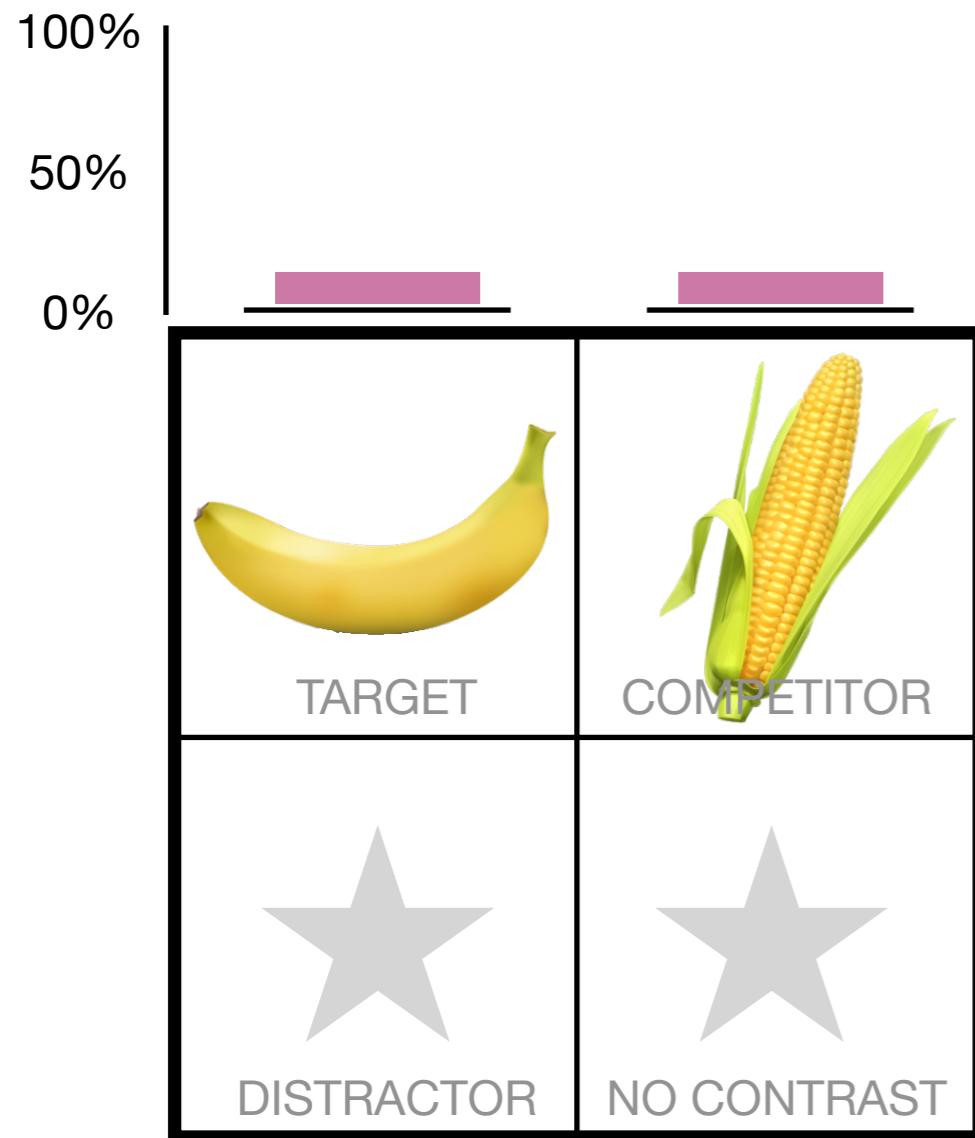
Sedivy et al (2003)



# Rational Speech Act Model

$$P_{L_1}(r \mid u) \propto P_{S_1}(u \mid r)^* P_{S_1}(r)$$

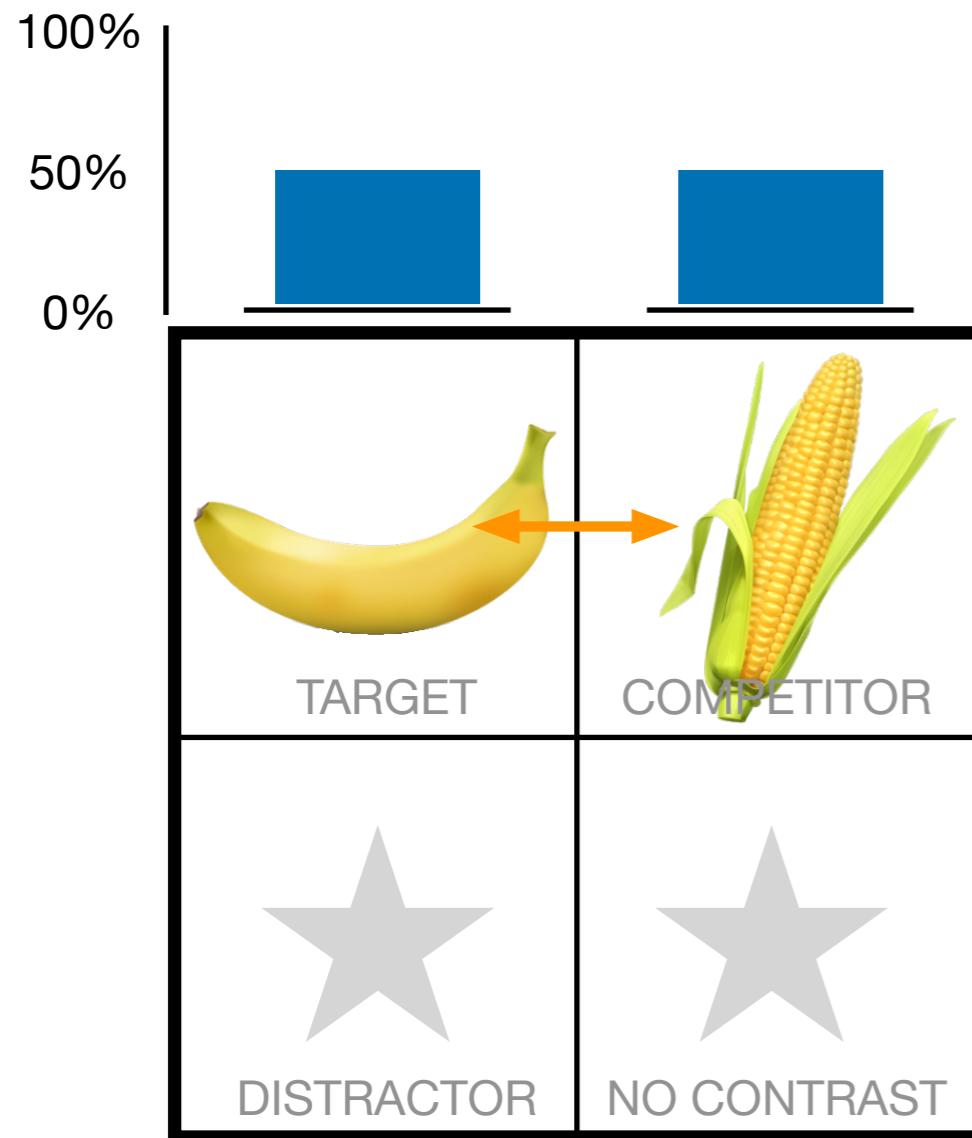
“Click on the yellow...”



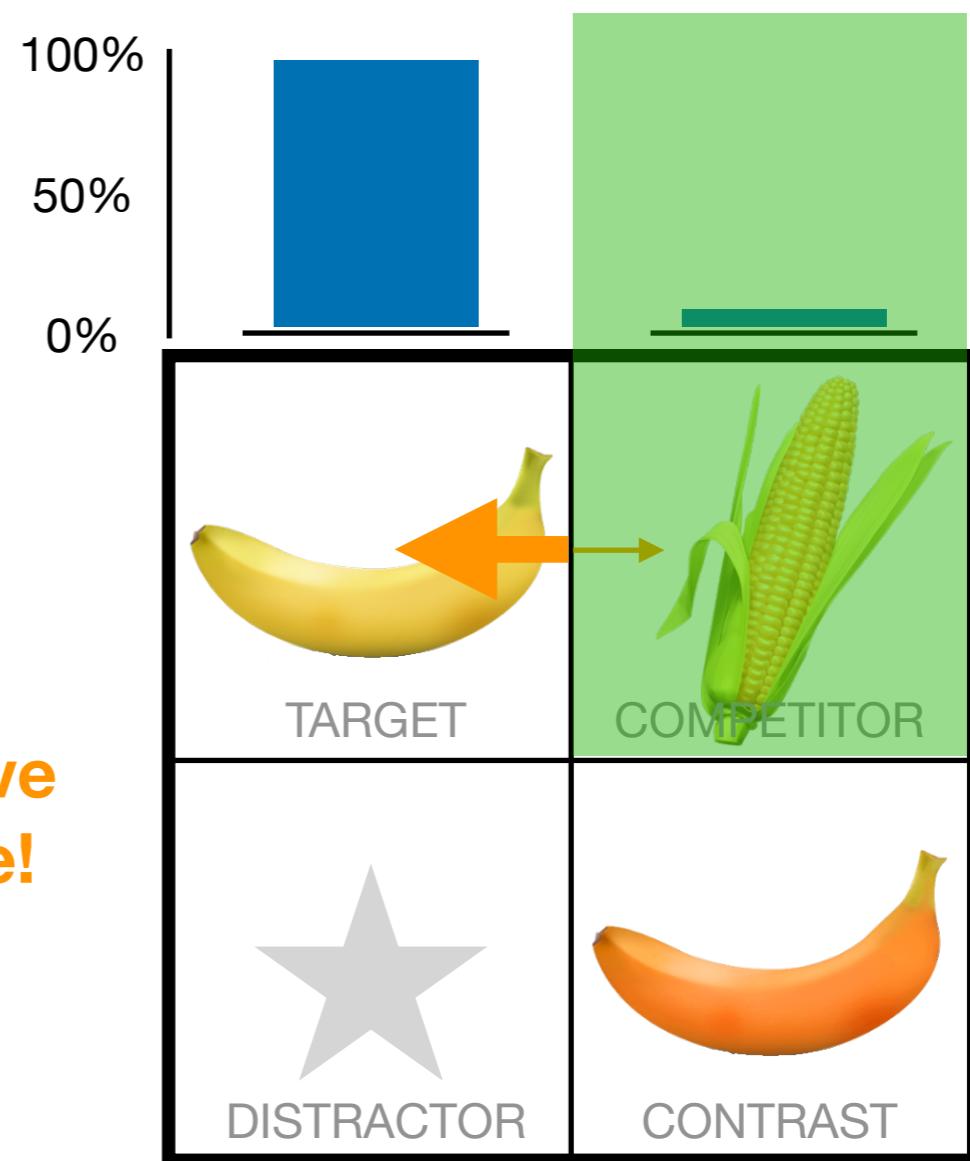
# Rational Speech Act Model

$$P_{L_1}(r | u) \propto P_{S_1}(u | r) * P_{S_1}(r)$$

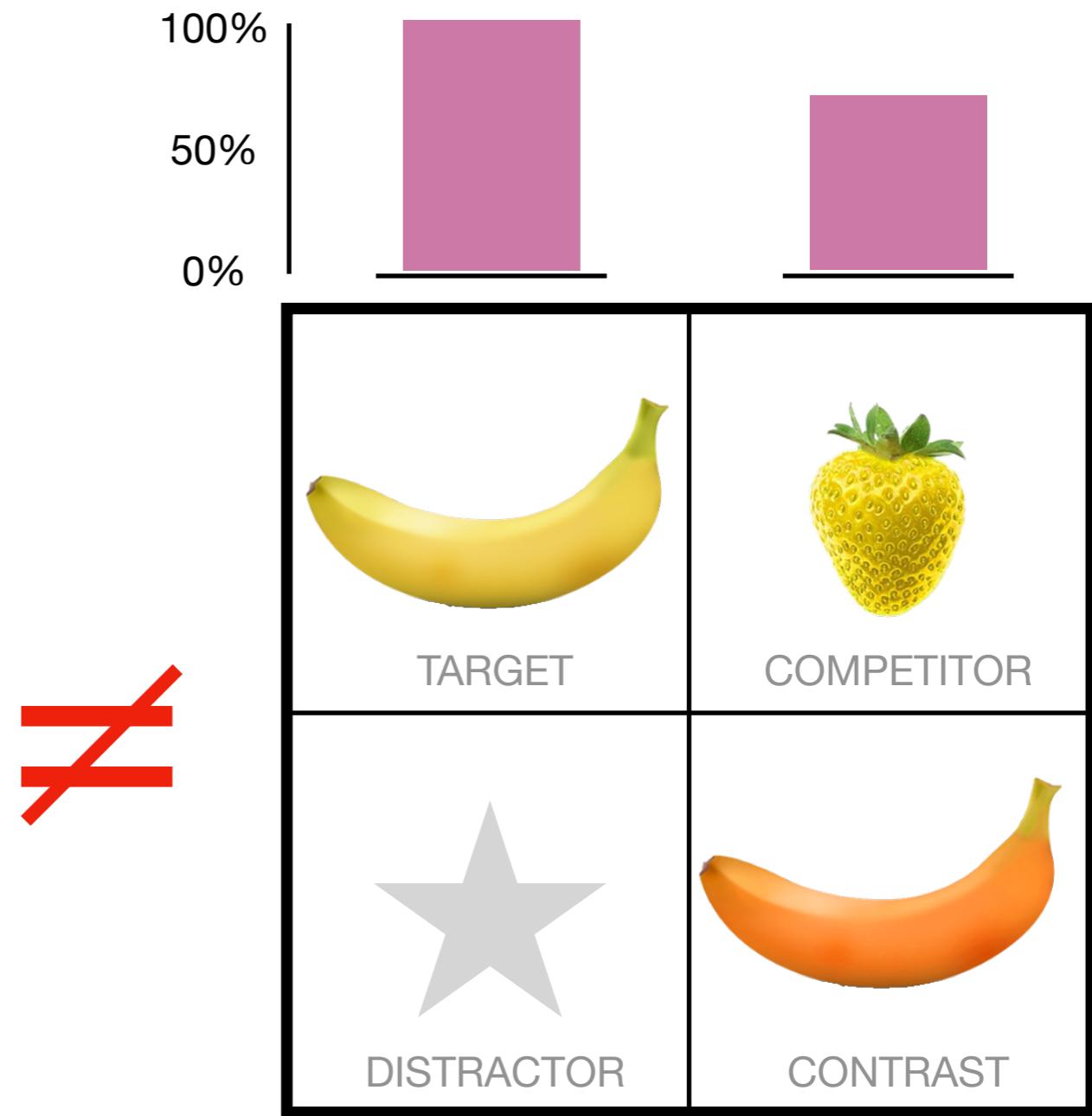
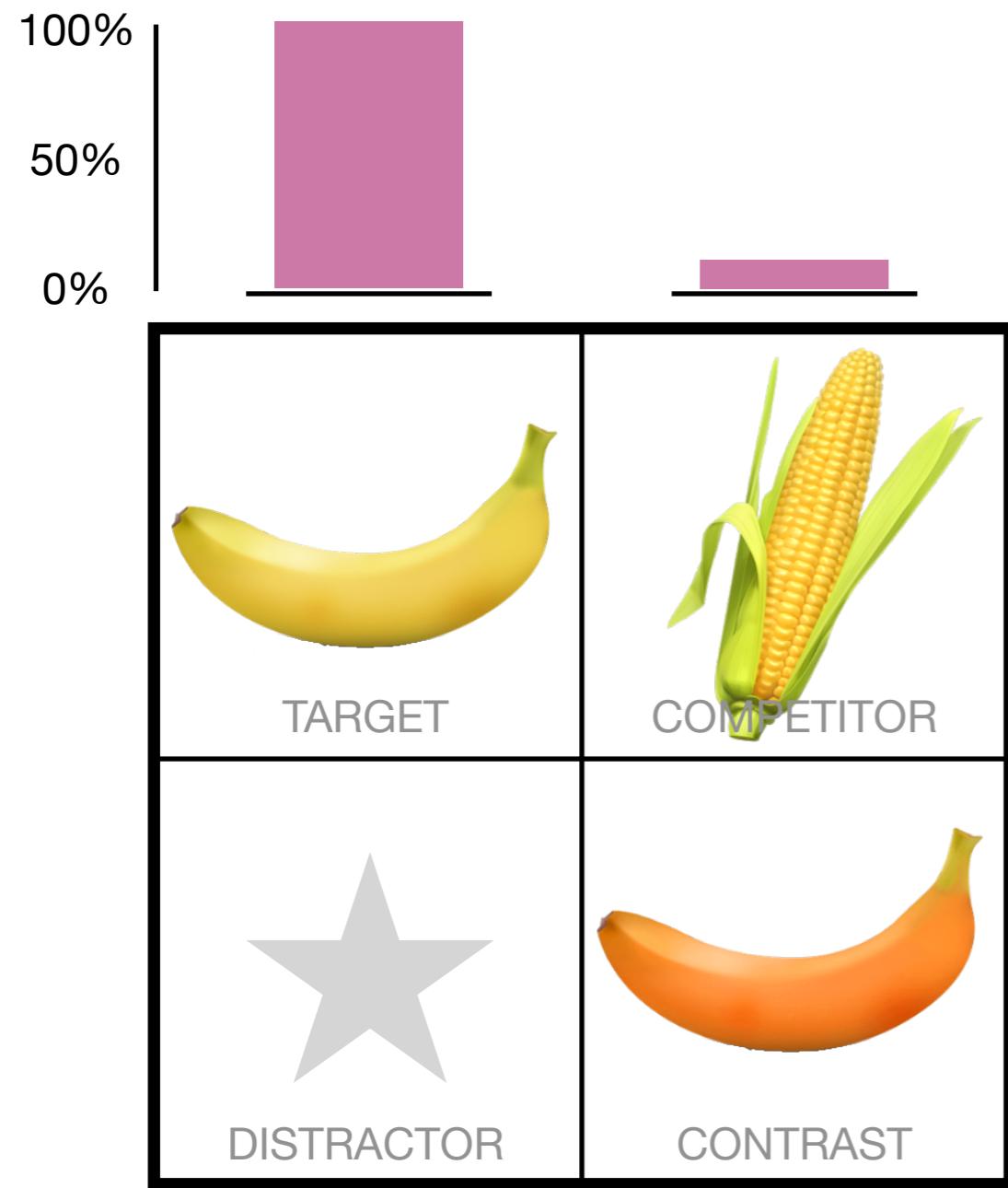
“Click on the yellow ... !”



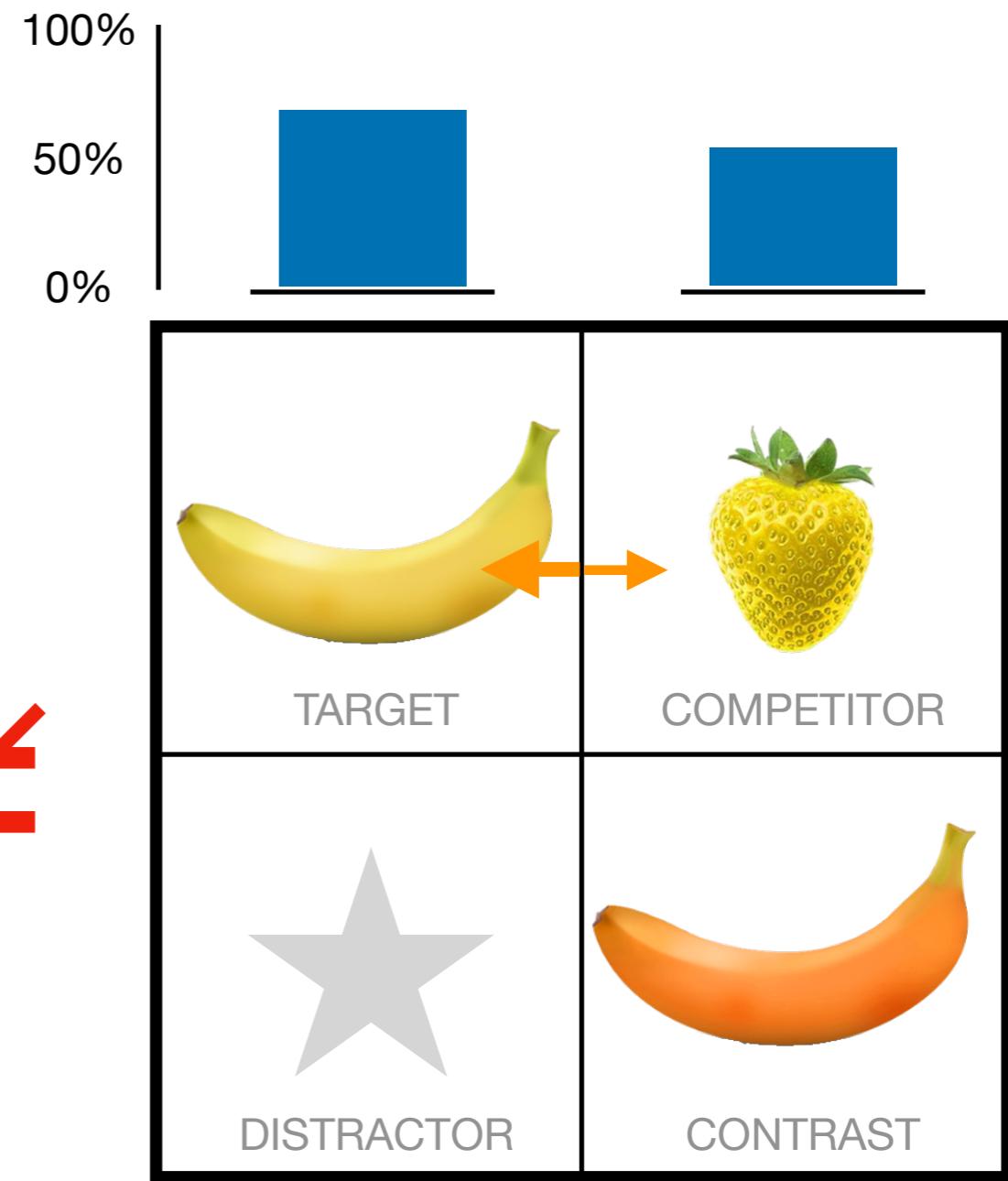
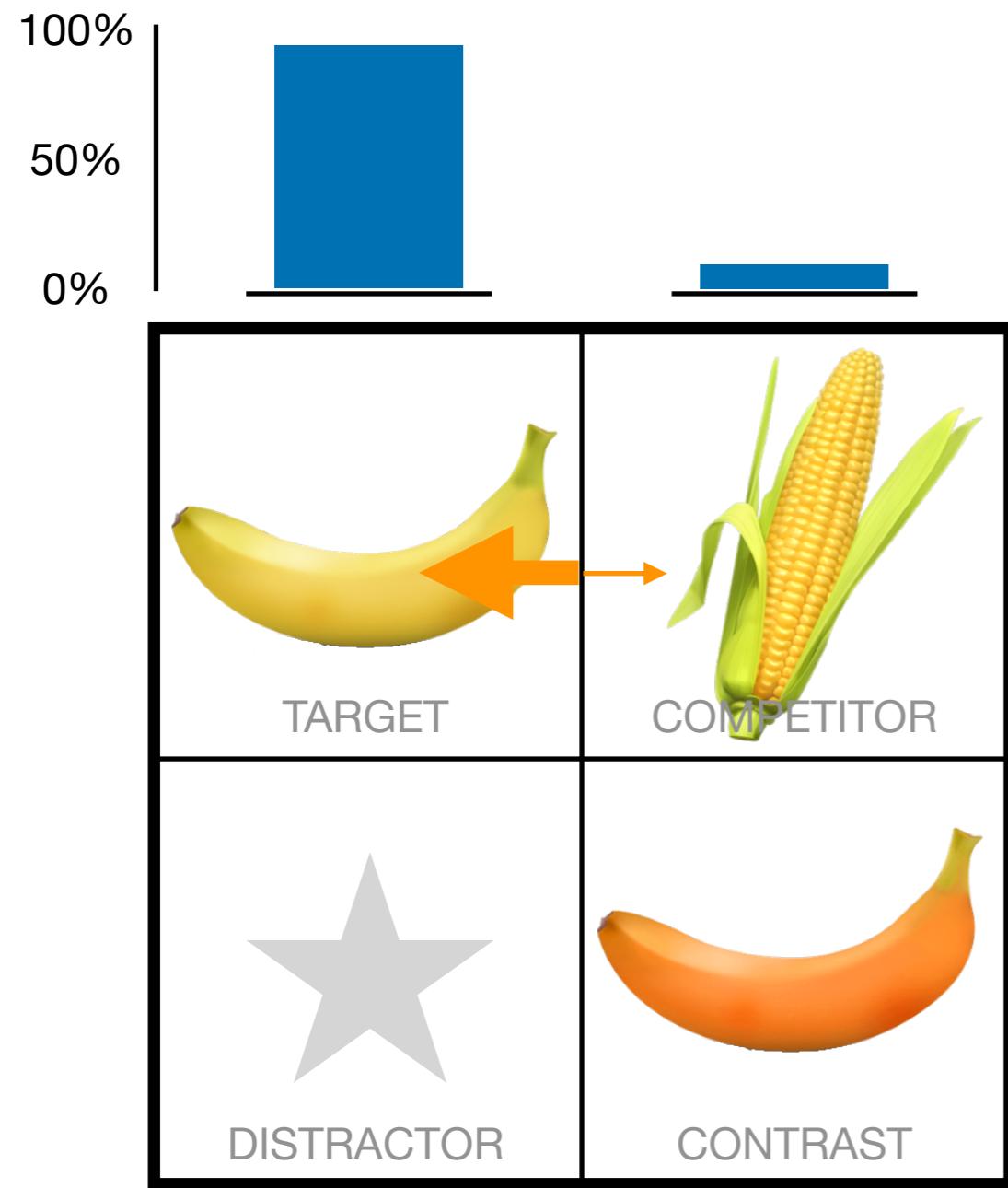
contrastive  
inference!



# Prediction



# Prediction



# Test RSA

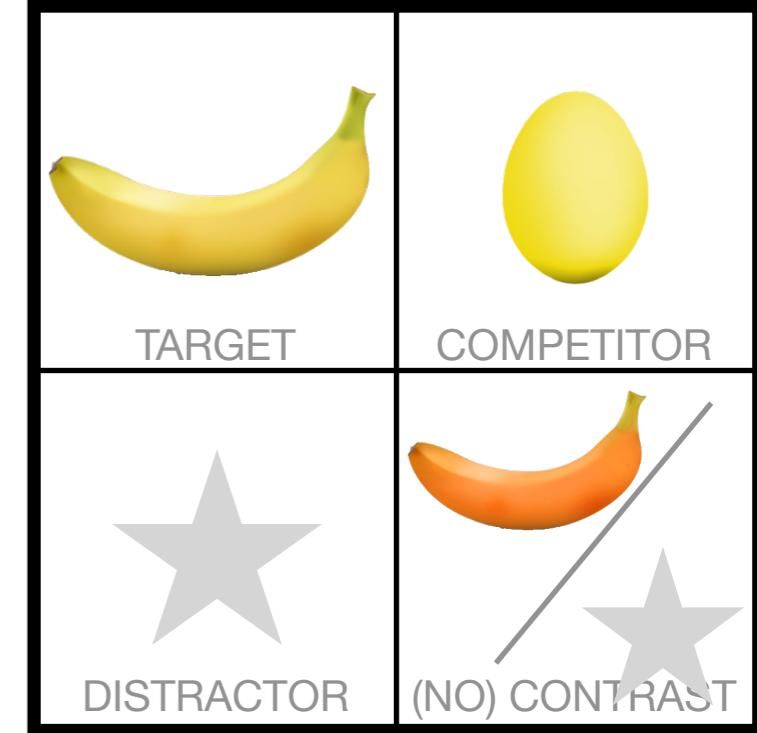
## 1. Production experiment

to obtain model  
predictions



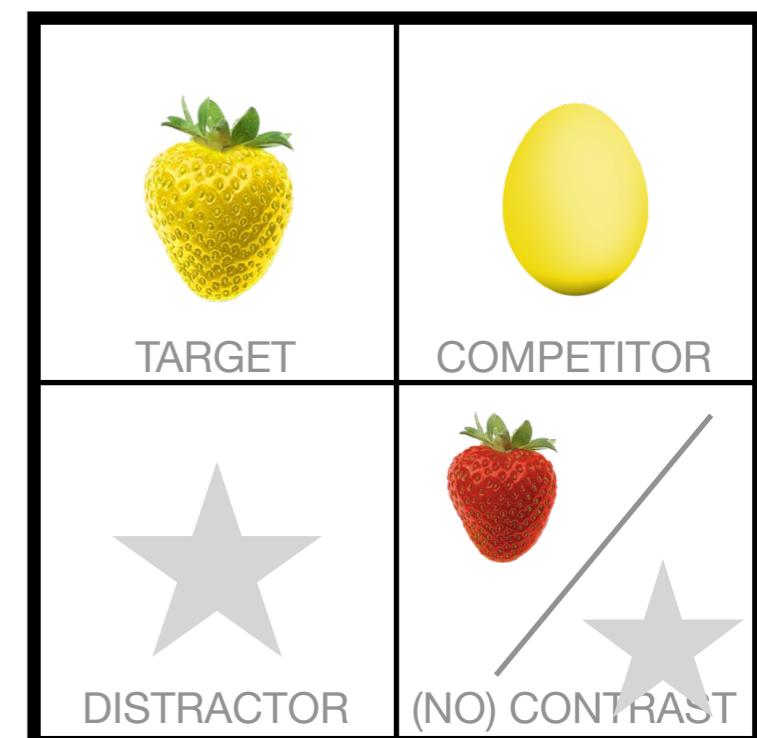
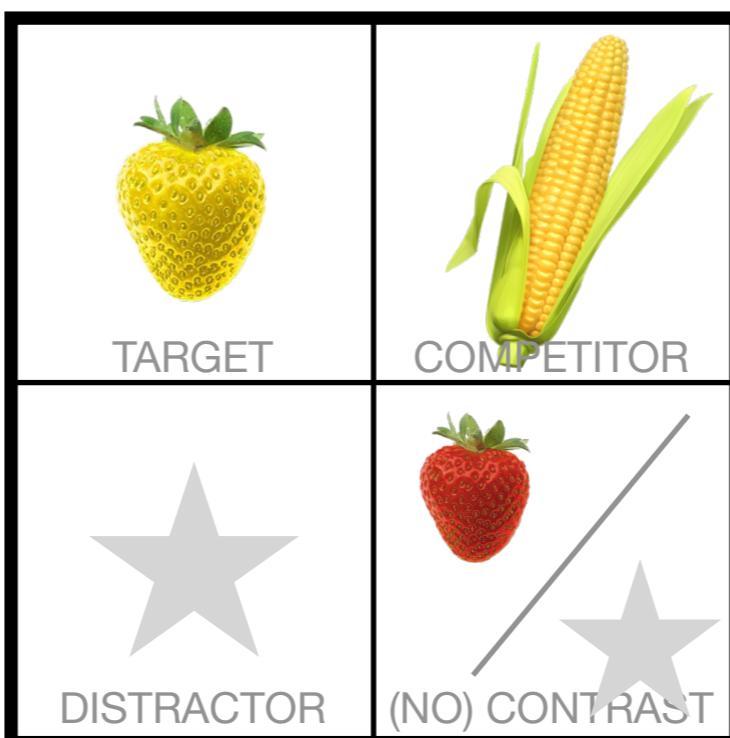
## 2. Model predictions

using production data



## 3. Comprehension experiment

to assess model  
predictions

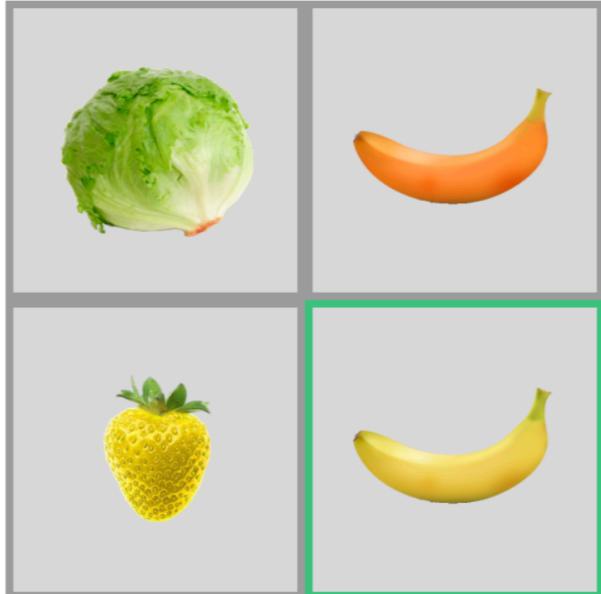


2 x 2 x 2 design:  
contrast presence, target  
typicality, competitor typicality

# Production experiment

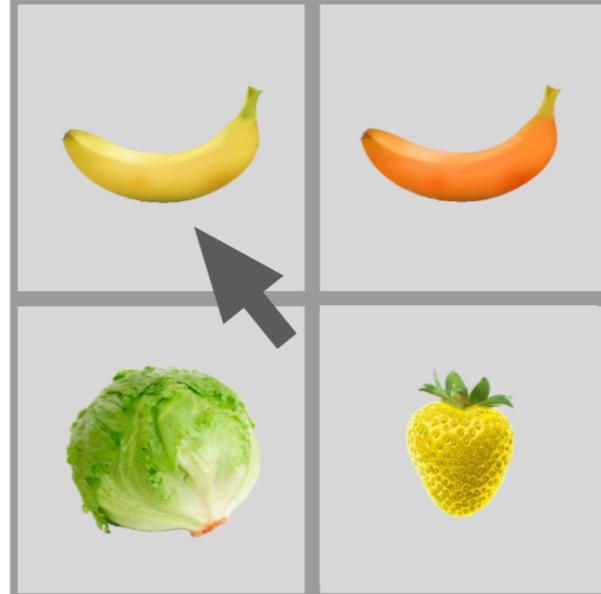
**You are the director**

the yellow banana|



**You are the matcher**

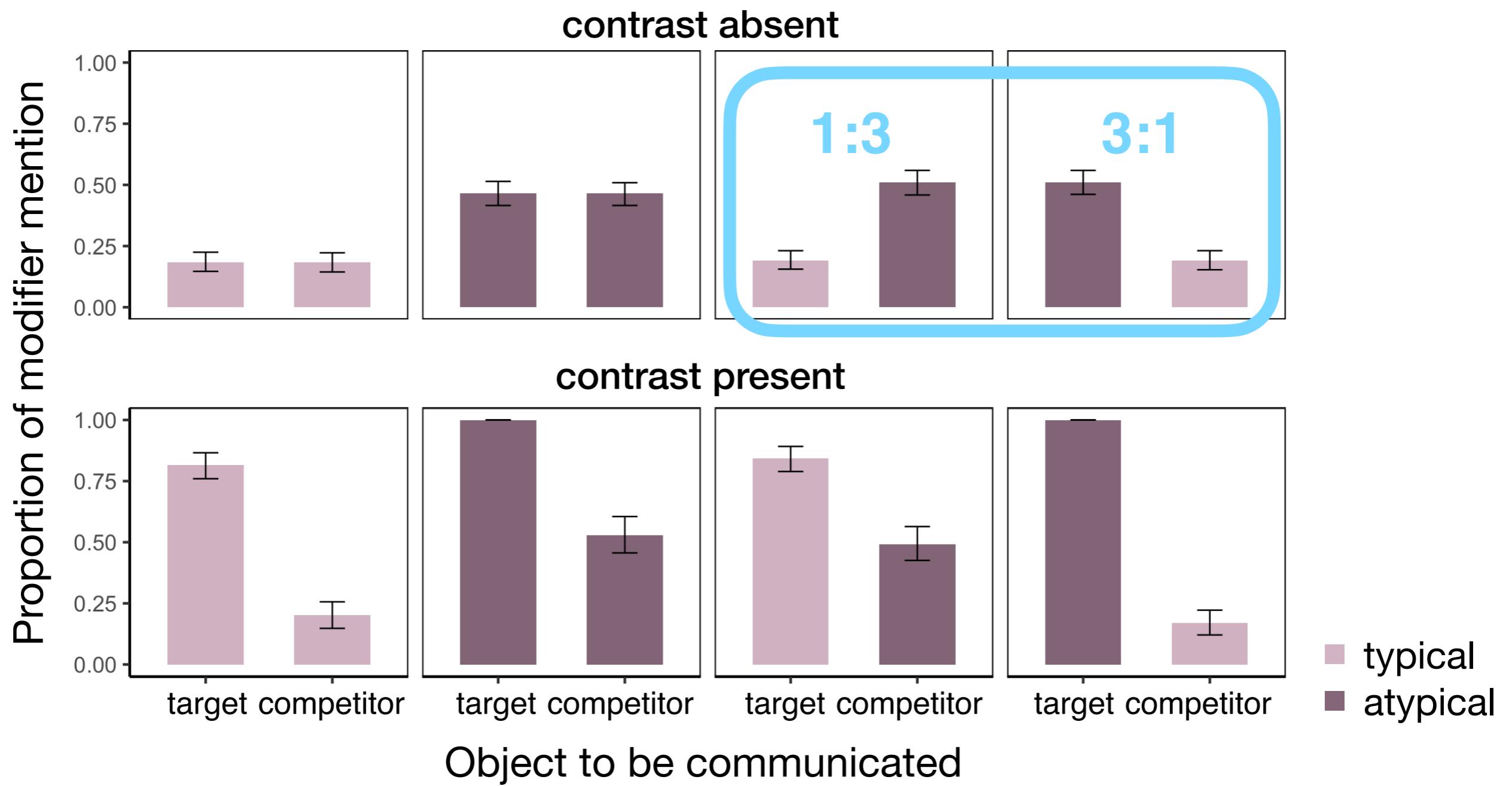
Director: the yellow banana



- ▶ Interactive reference game
- ▶ MTurk, n=141 participant pairs (112)
- ▶ 60 trials (32 critical; 28 fillers)

Clark & Wilkes-Gibbs (1986), Hawkins et al. (2015)

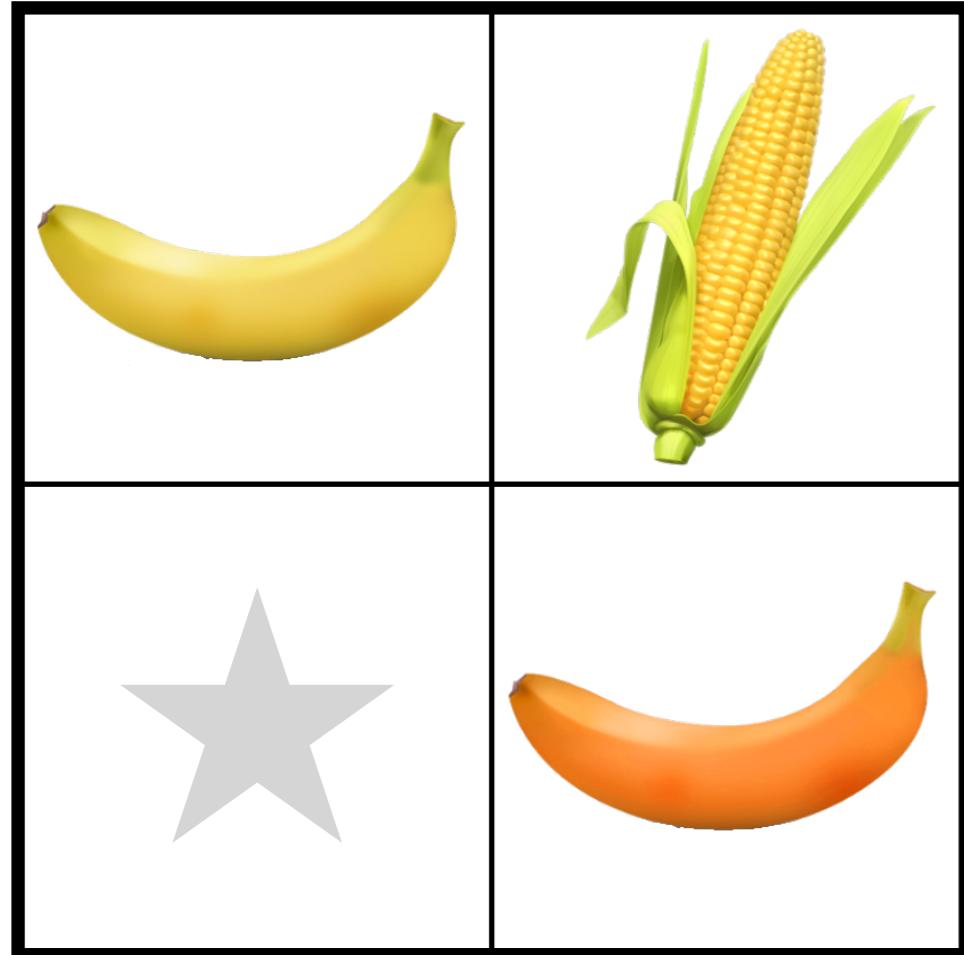
# Production results



$$P_{L_1}(r | u) \propto P_{S_1}(u | r) \cdot P(r) \quad \text{uniform}$$

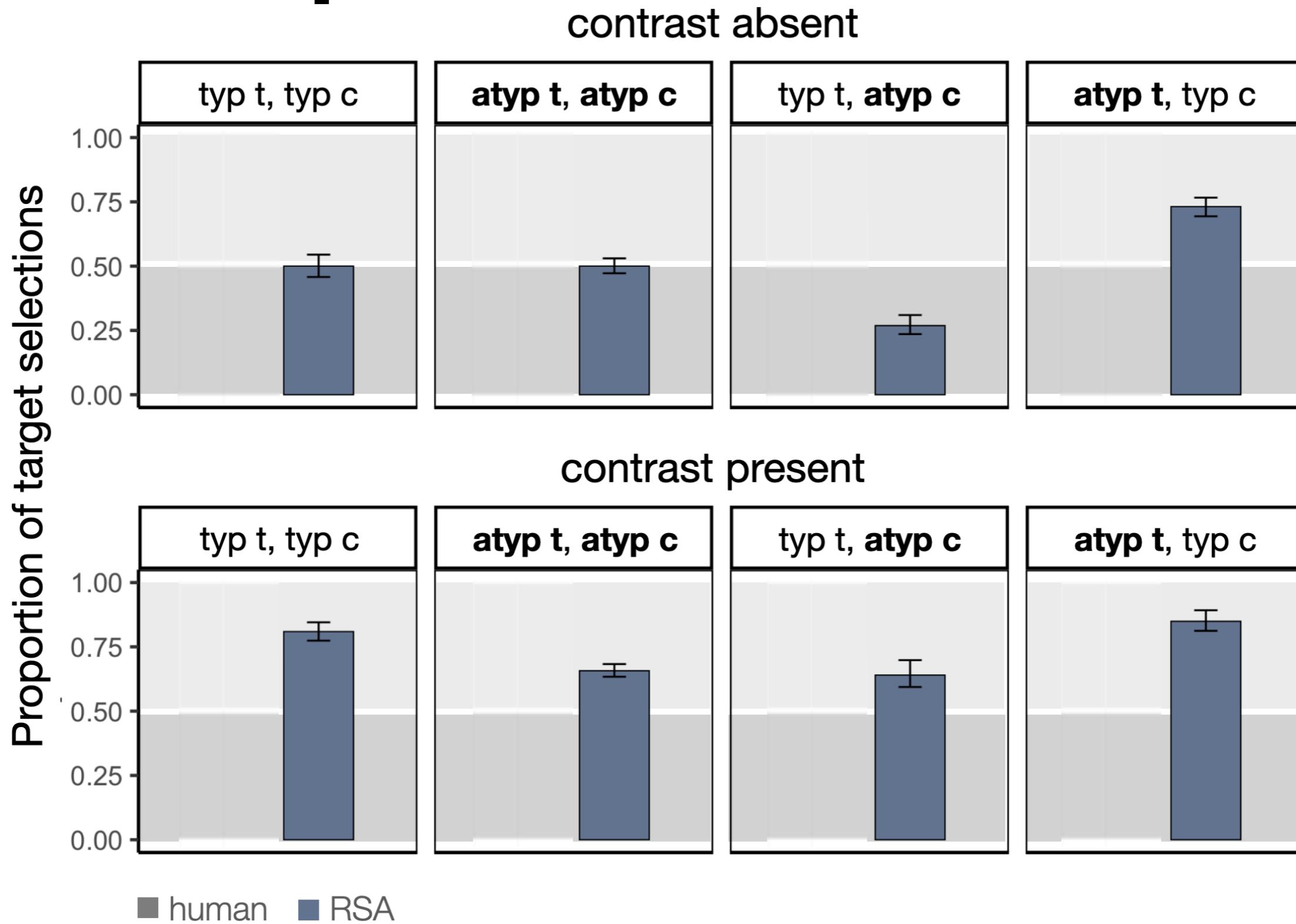
# Comprehension experiment

**Click on the yellow banana!**

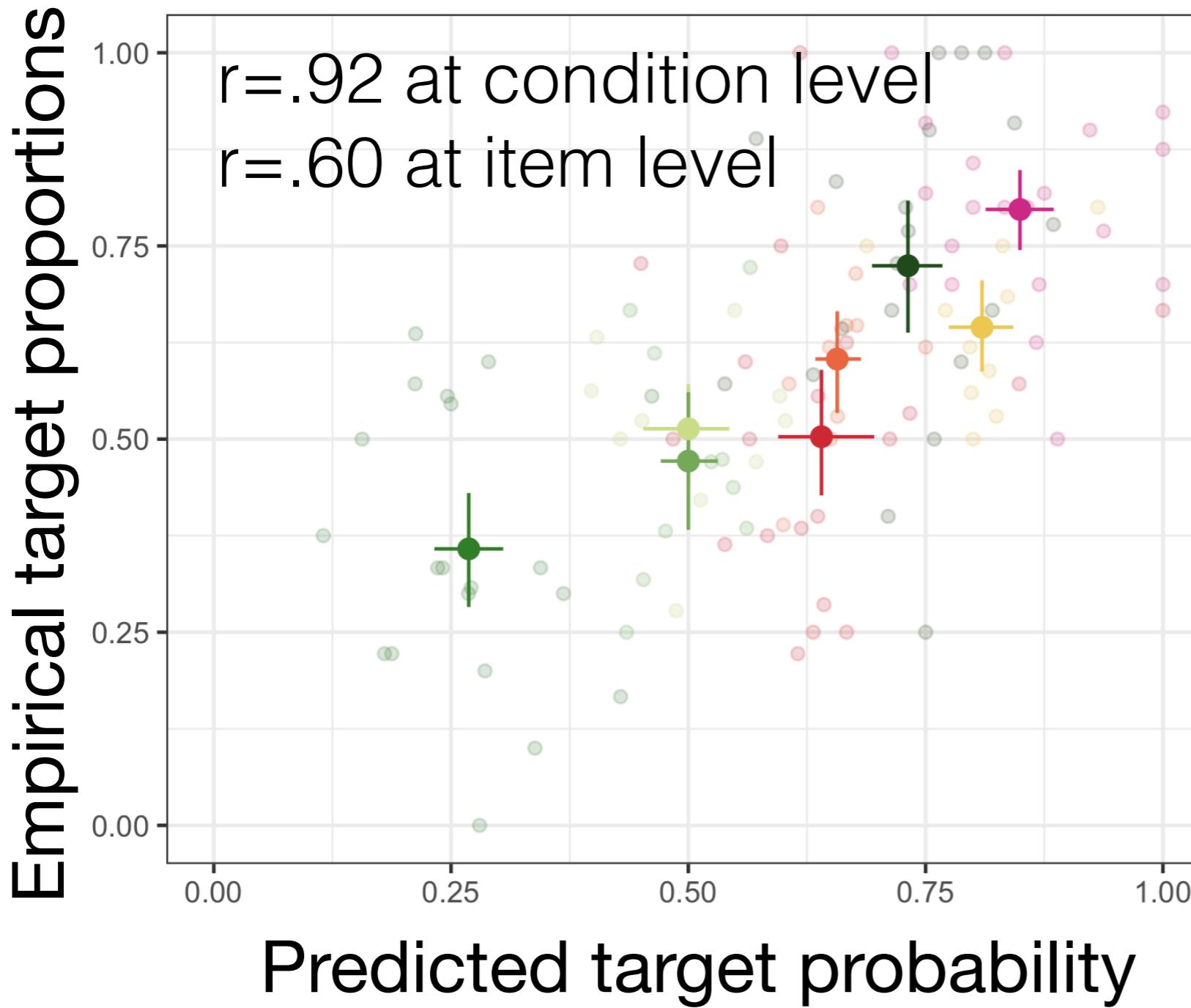


- ▶ incremental decision task rather than eye-tracking study
- ▶ competitor typicality manipulated between-subjects
- ▶ MTurk, n=79 (73)  
40 per competitor typicality condition
- ▶ 55 trials (20 critical; 35 fillers)

# Comprehension results



# Comparison of predicted and empirical target selections



Simple pragmatic RSA listener captures variability in contrastive inference strength by reasoning about (variability in) modifier production probabilities.

# Interim summary I

A simple pragmatic RSA listener captures variability in contrastive inference strength by reasoning about (variability in) modifier production probabilities.

Some consequences:

effects of adjective function or semantics only operative via their effect on listeners' production expectations

no need for “default descriptions”



Caroline  
Graf

Robert  
Hawkins

Leyla  
Kursat

Brandon  
Waldon

Noah  
Goodman

Elisa  
Kreiss

## PART II

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# Production of referring expressions: redundant modification

Degen et al 2020; Waldon & Degen 2021; Kursat & Degen to appear

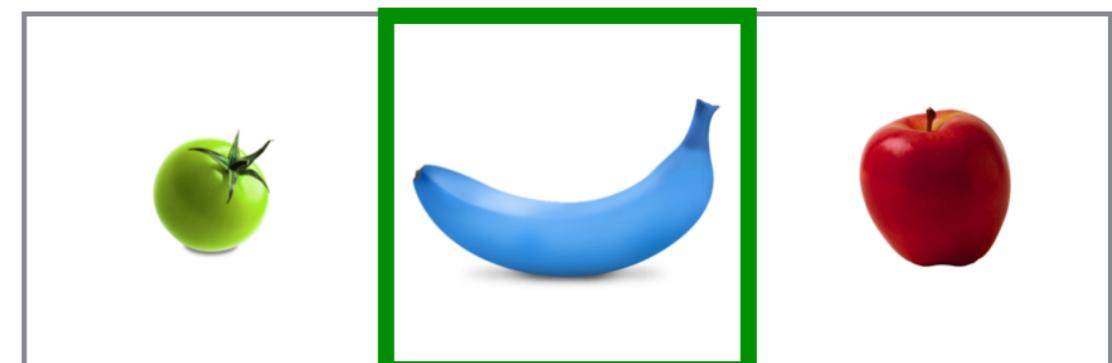
# 1. Redundant color and size modification

Degen et al 2020



# 2. Model extension: color typicality

Degen et al 2020



# 3. Model extension: cross-linguistic variability

Waldon & Degen 2021

*the small blue pin  
la tachuela pequeña*

# Production: redundant referring expressions

**size sufficient**



*the small pin*

**75-80%**

**color sufficient**



*the blue pin*

**8-10%**

Speakers produce seemingly overinformative referring expressions.

Deutsch 1976; Pechmann 1989; Sedivy 2003; Gatt et al. 2011; Koolen et al 2013; Rubio-Fernández 2016; Westerbeek et al 2015; Davies & Katsos 2013; van Gompel et al 2019

# The RSA framework

Frank & Goodman 2012

$$O = \{ \text{!}, \text{!} \text{ (red outline)}, \text{!} \}$$

$$U = \{\text{big, small, green, black}\}$$

big green, small green, small black}

obvious problem:  
no complex utterances

## Literal listener

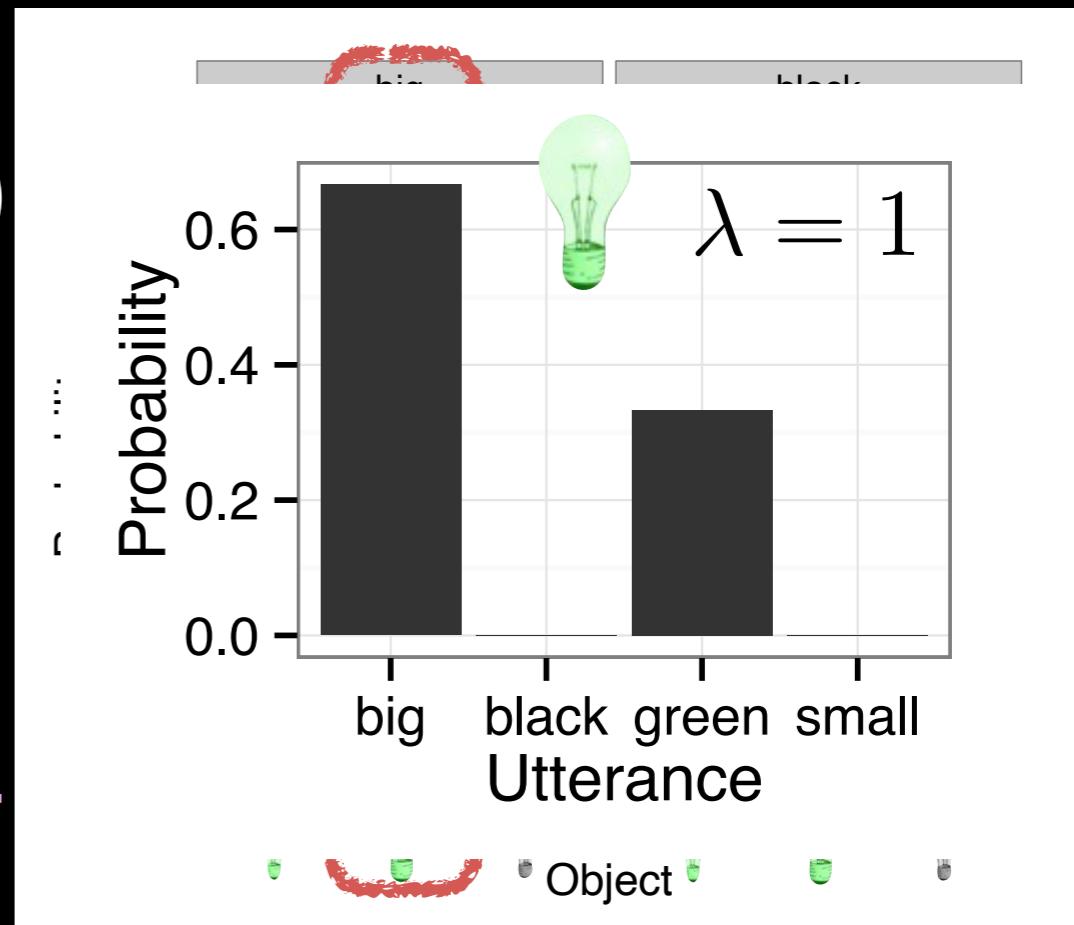
$$P_{L_0}(o|u) = \mathcal{U}(o|\{u \text{ is true of } o\})$$

$$[[u]] : O \rightarrow \{\text{true, false}\}$$

## Pragmatic speaker

$$P_{S_1}(u|o) \propto e^{\lambda \cdot (\ln P_{L_0}(o|u) - C(u))}$$

Quantity Manner



# Utterance semantics & cost

## Intersective semantics

$$[[u]] = [[u_1]] \wedge [[u_2]]$$

$$[[\text{big green}]] = [[\text{big}]] \wedge [[\text{green}]]$$

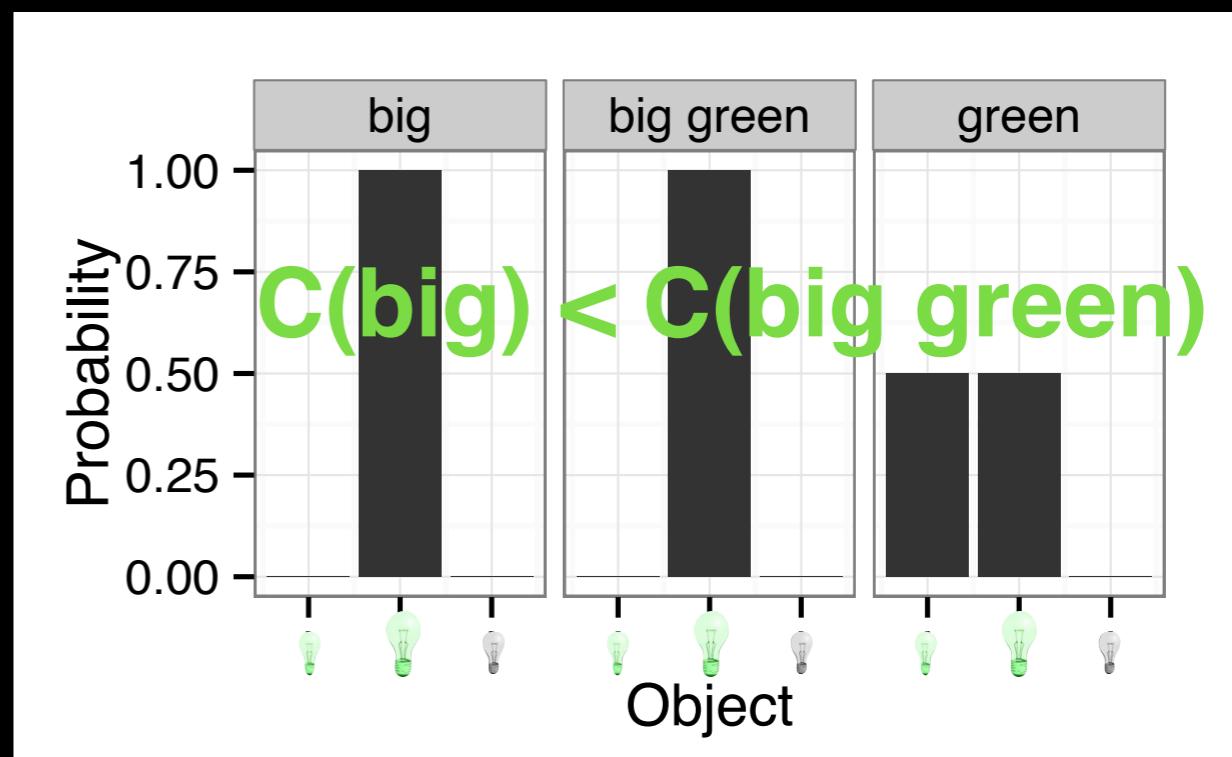
## Cost

$$C(u) = C(u_1) + C(u_2)$$

RSA does not produce overinformative REs...

Gatt et al 2013; Westerbeek et al 2015

...with deterministic Boolean semantics



# Motivation for relaxed semantics?

Modifiers differ:

size adjectives are more vague and context-dependent than color adjectives

color is more salient than size  
Arts et al 2011; Gatt et al 2013

size adjectives are judged to be more subjective than color adjectives  
Scontras, Degen, & Goodman 2017

# Non-deterministic semantics

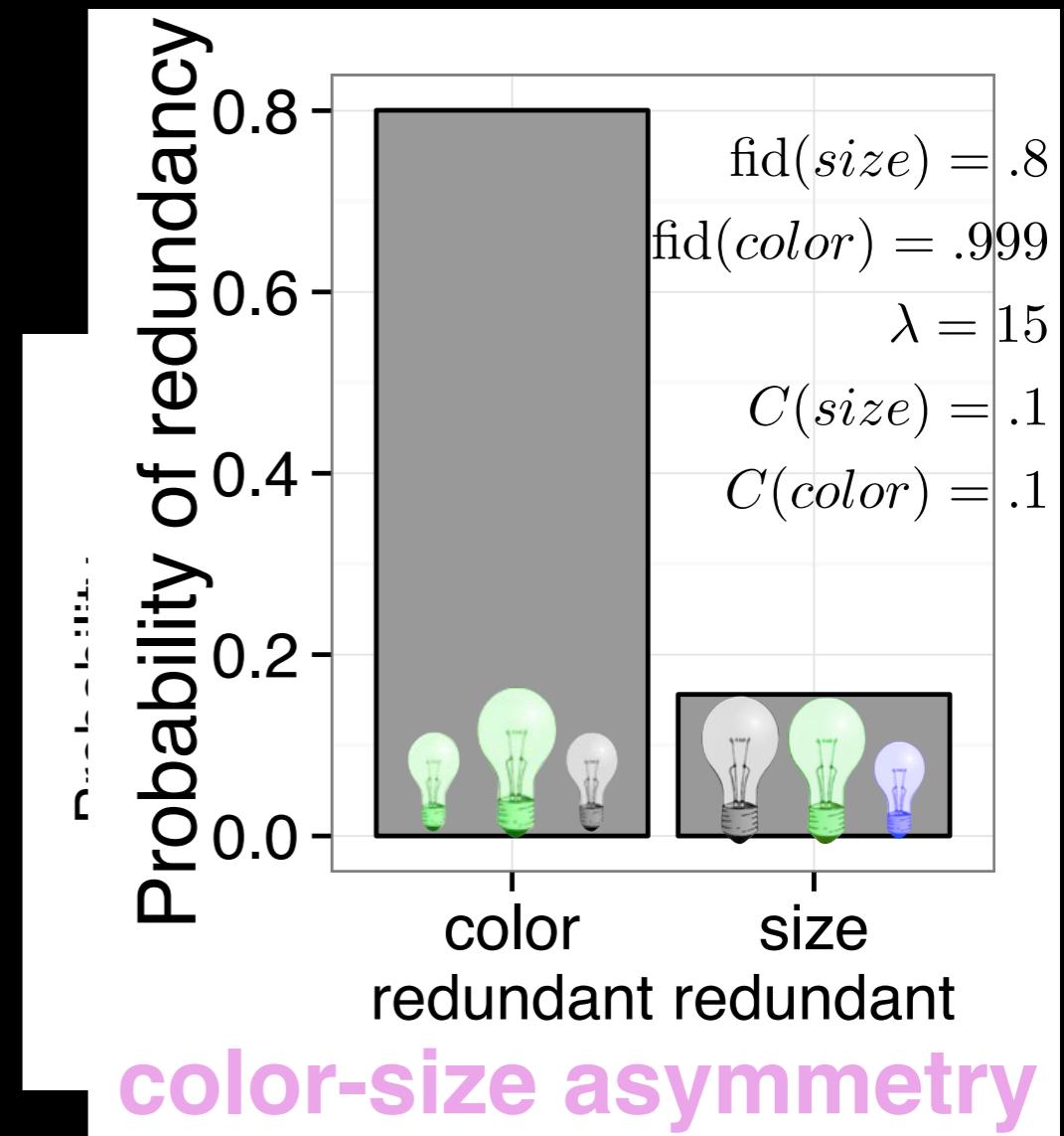
**Literal listener**

$$P_{L_0}(o|u) \propto \begin{cases} 1 - \epsilon & [[u]](o) = \text{true} \\ \epsilon & \text{otherwise} \end{cases}$$

**Pragmatic speaker**

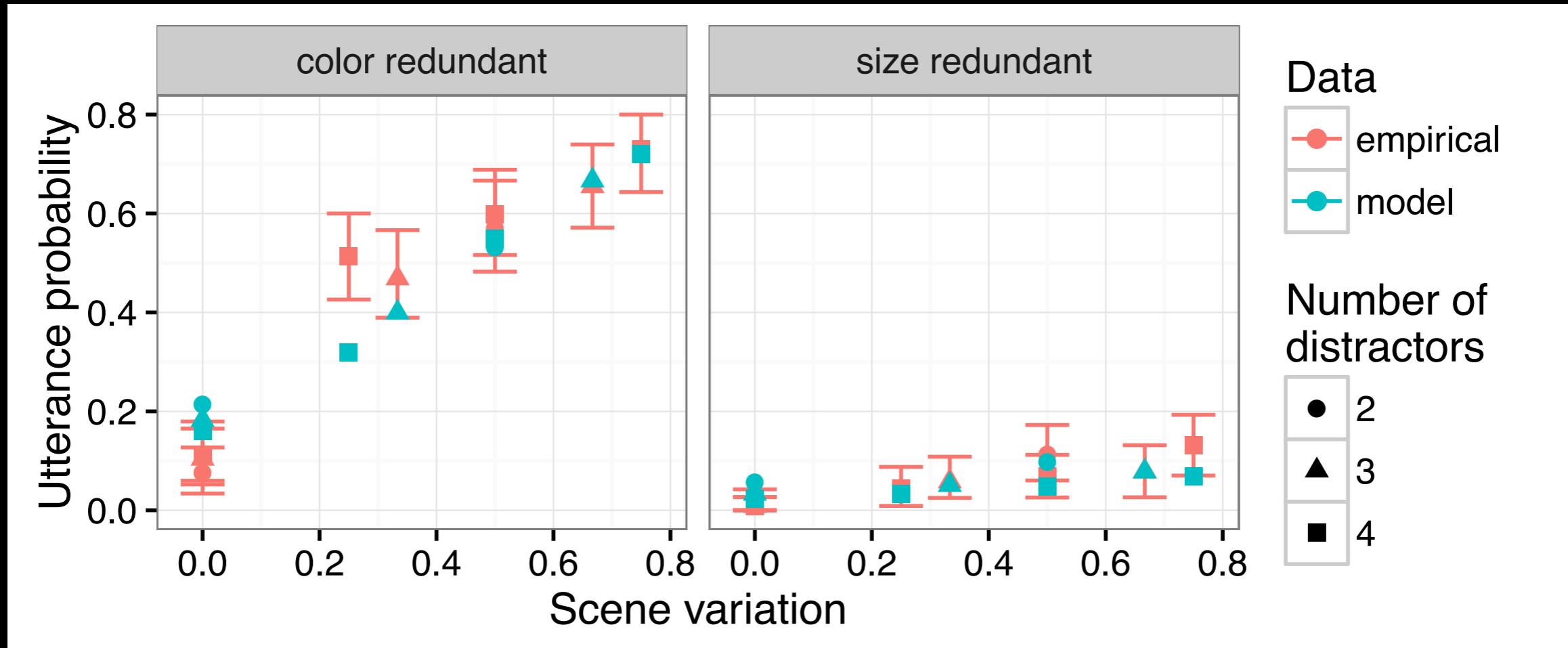
$$P_{S_1}(u|o) \propto e^{\lambda \cdot (\ln P_{L_0}(o|u) - C(u))}$$

**fidelity**

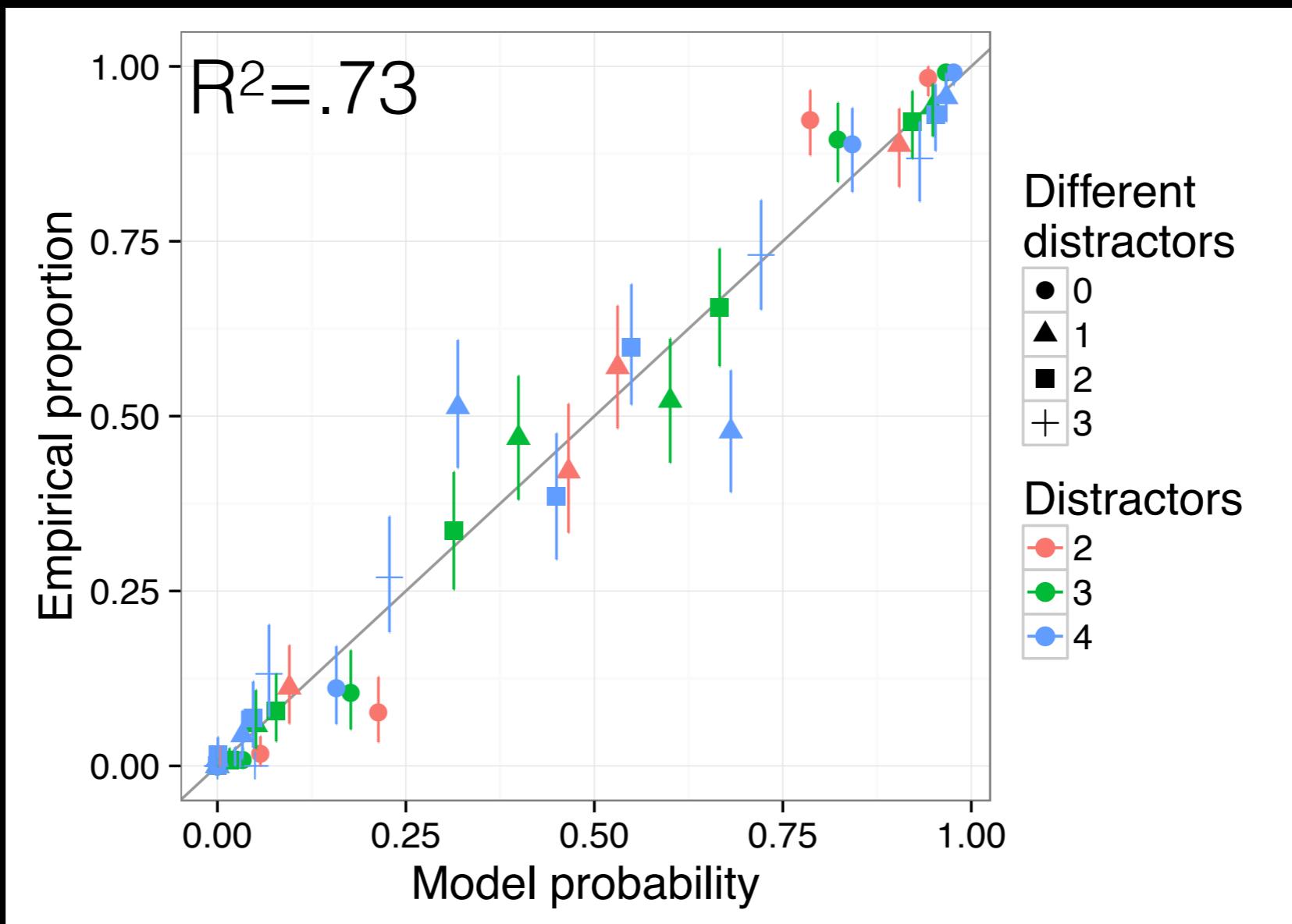


If modifiers don't “work perfectly”,  
**adding modifiers adds information**

# Interactive reference game results



# Model fit



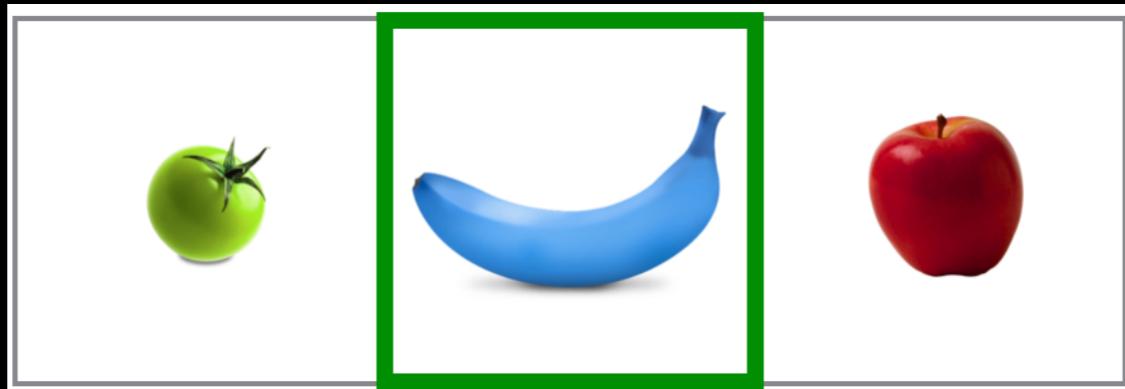
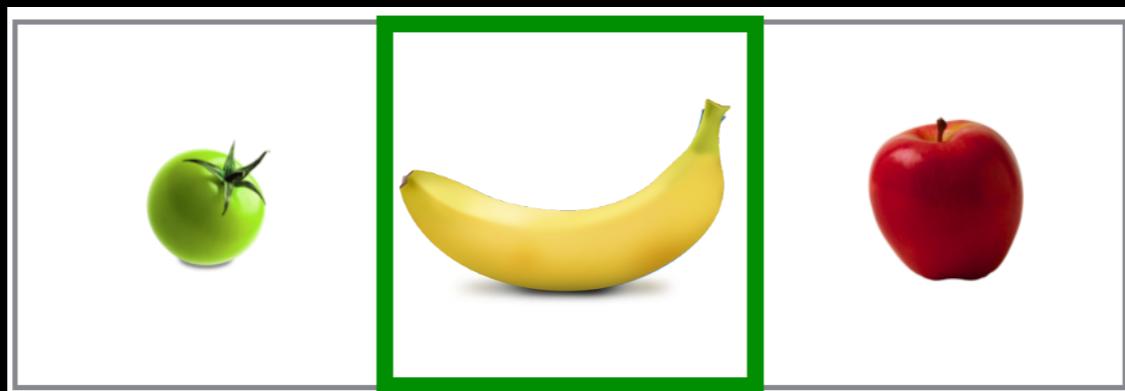
# Interim summary II

A continuous-semantics RSA speaker captures variability in overmodification by reasoning about a continuous semantics literal listener: overmodification is more likely, the less inferable the intended referent is from the simply modified description.

A consequence:

“overinformative” —> “usefully redundant”

# Extending the model to within-color variability



# Extending the continuous semantics

## Literal listener

$$P_{L_0}(o|u) \propto [[u]](o)$$

$$[[u]](o) = \text{typicality}(u, o)$$

## Pragmatic speaker

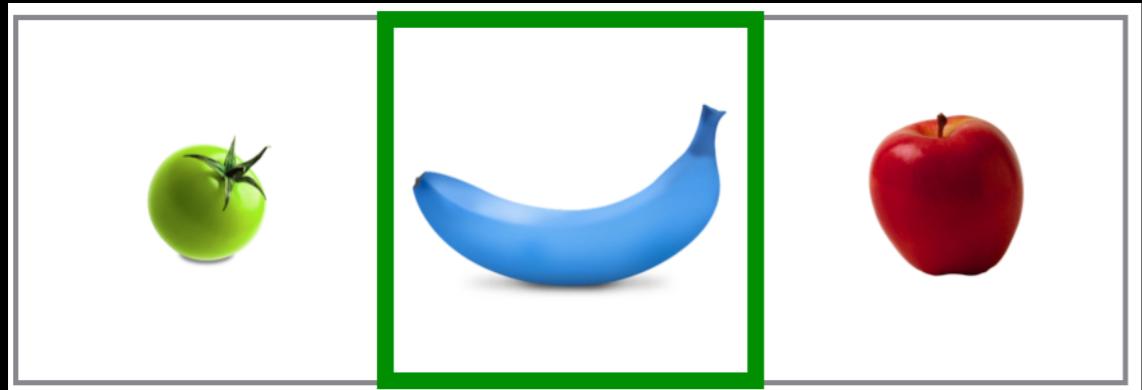
$$P_{S_1}(u|o) \propto e^{\lambda \ln P_{L_0}(o|u) - \text{cost}(u)}$$

How typical is  $o$  for  $u$ ?



- “banana”
- “yellow banana”
- “yellow”
- “brown banana”
- “brown”
- ...

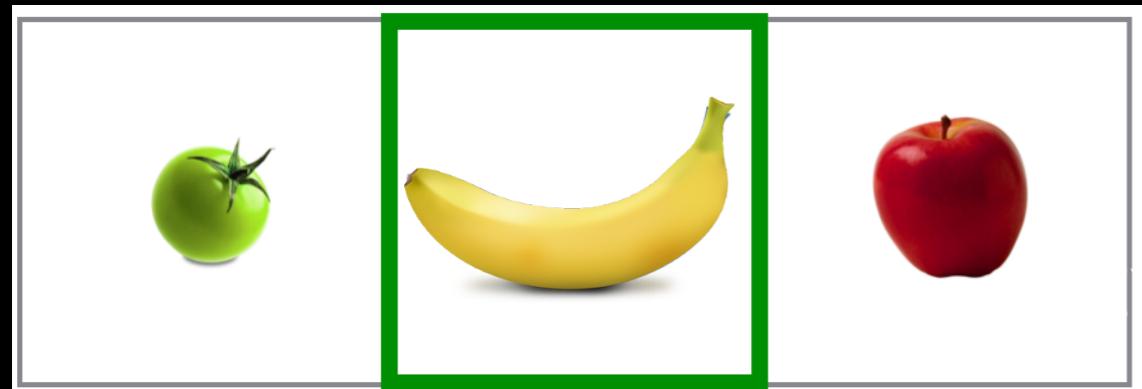
# RSA predictions with continuous semantics



$\text{typicality}(\text{"banana"}, \text{blue banana}) = .4$

$\text{typicality}(\text{"blue banana"}, \text{blue banana}) = .98$

$\text{typicality}(\text{"banana"}, \text{red apple}) = .01$

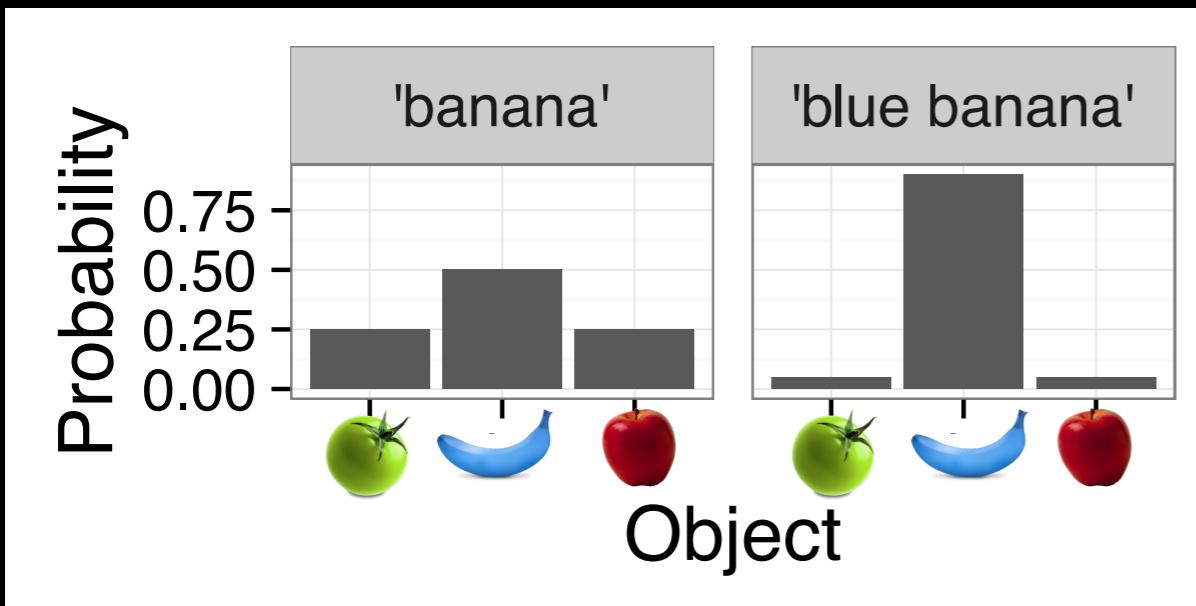


$\text{typicality}(\text{"banana"}, \text{yellow banana}) = .98$

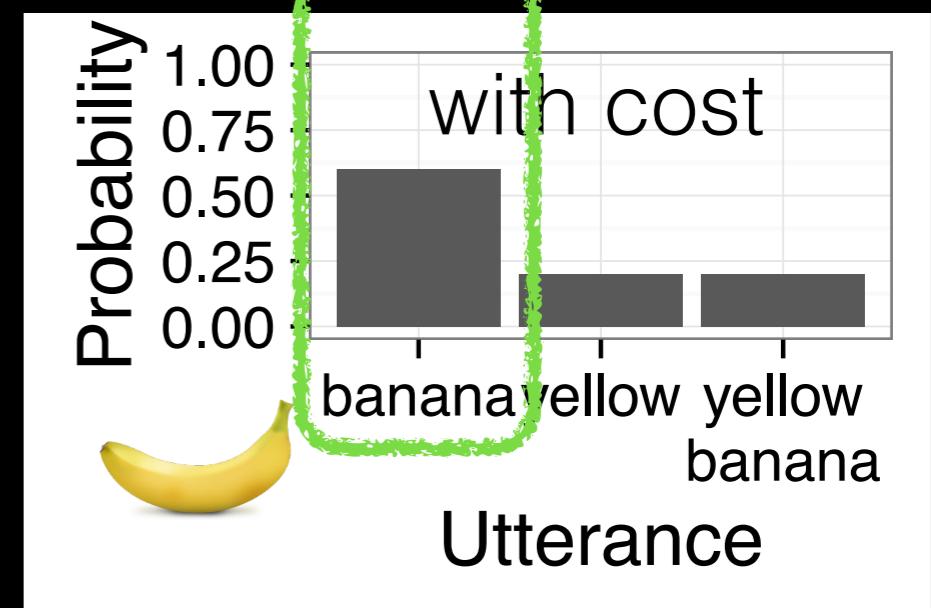
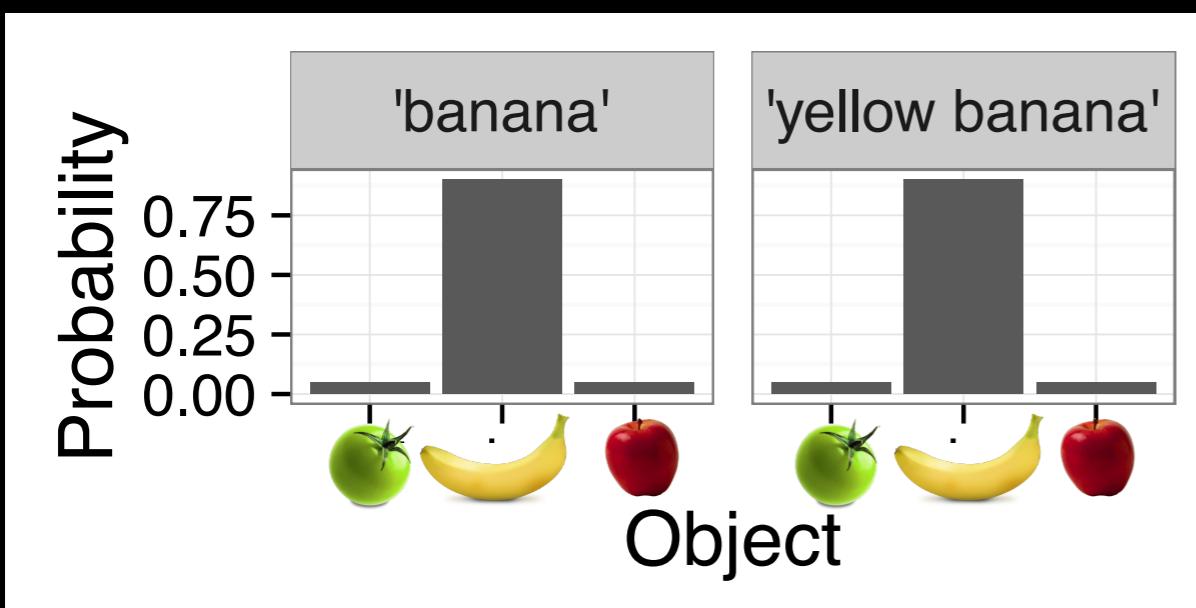
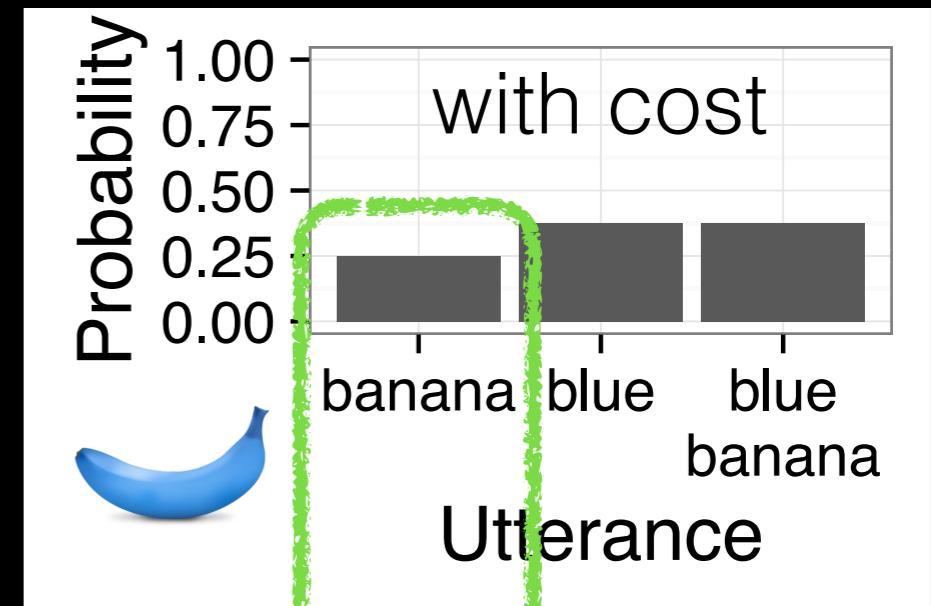
$\text{typicality}(\text{"yellow banana"}, \text{yellow banana}) = .98$

# Predictions

Literal listener



Pragmatic speaker



Redundancy more likely when probability of confusion is high

# Independent empirical evidence for RSA with continuous semantics?

## Literal listener

$$P_{L_0}(o|u) \propto [[u]](o)$$

$$[[u]](o) = \text{typicality}(u, o)$$

## Pragmatic speaker

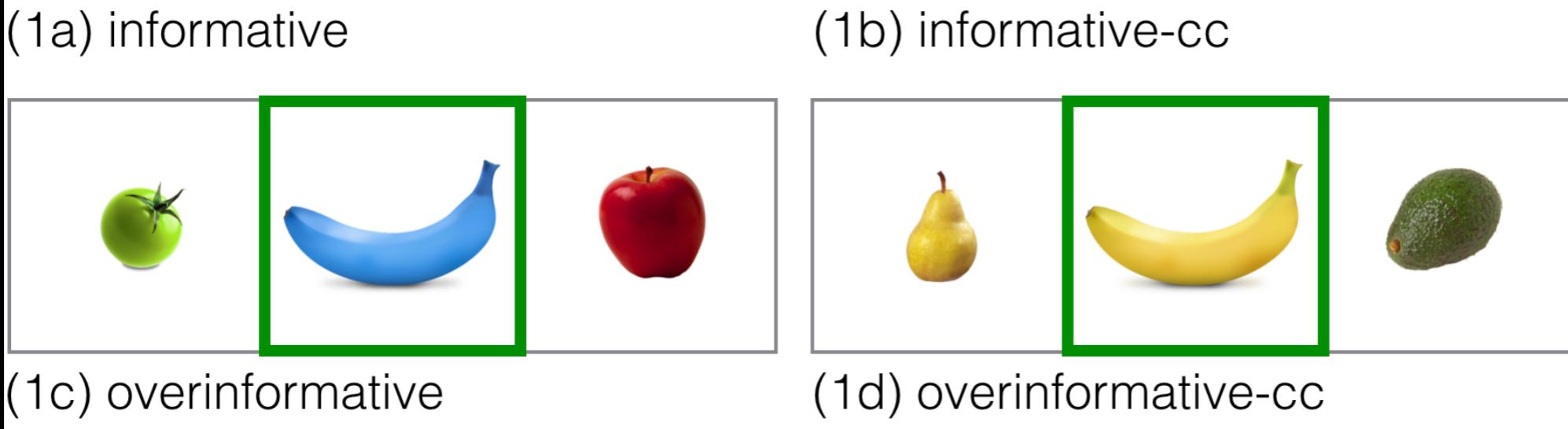
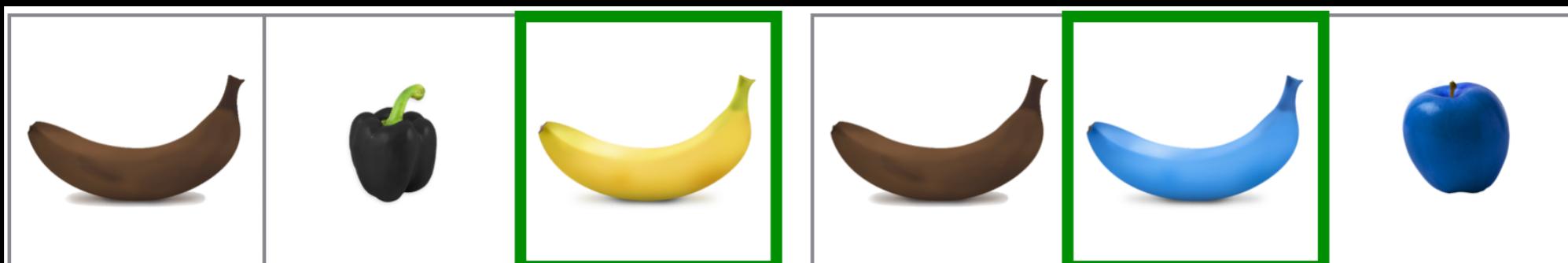
$$P_{S_1}(u|o) \propto e^{\lambda \ln P_{L_0}(o|u) - \text{cost}(u)}$$

1. Typicality norming
2. Production study
3. Model evaluation

Production study: interactive  
reference game experiment

# Production study

- 60 pairs of participants on Mechanical Turk
- random assignment to speaker/listener role
- 42 trials
- varied contextual informativeness of utterances:



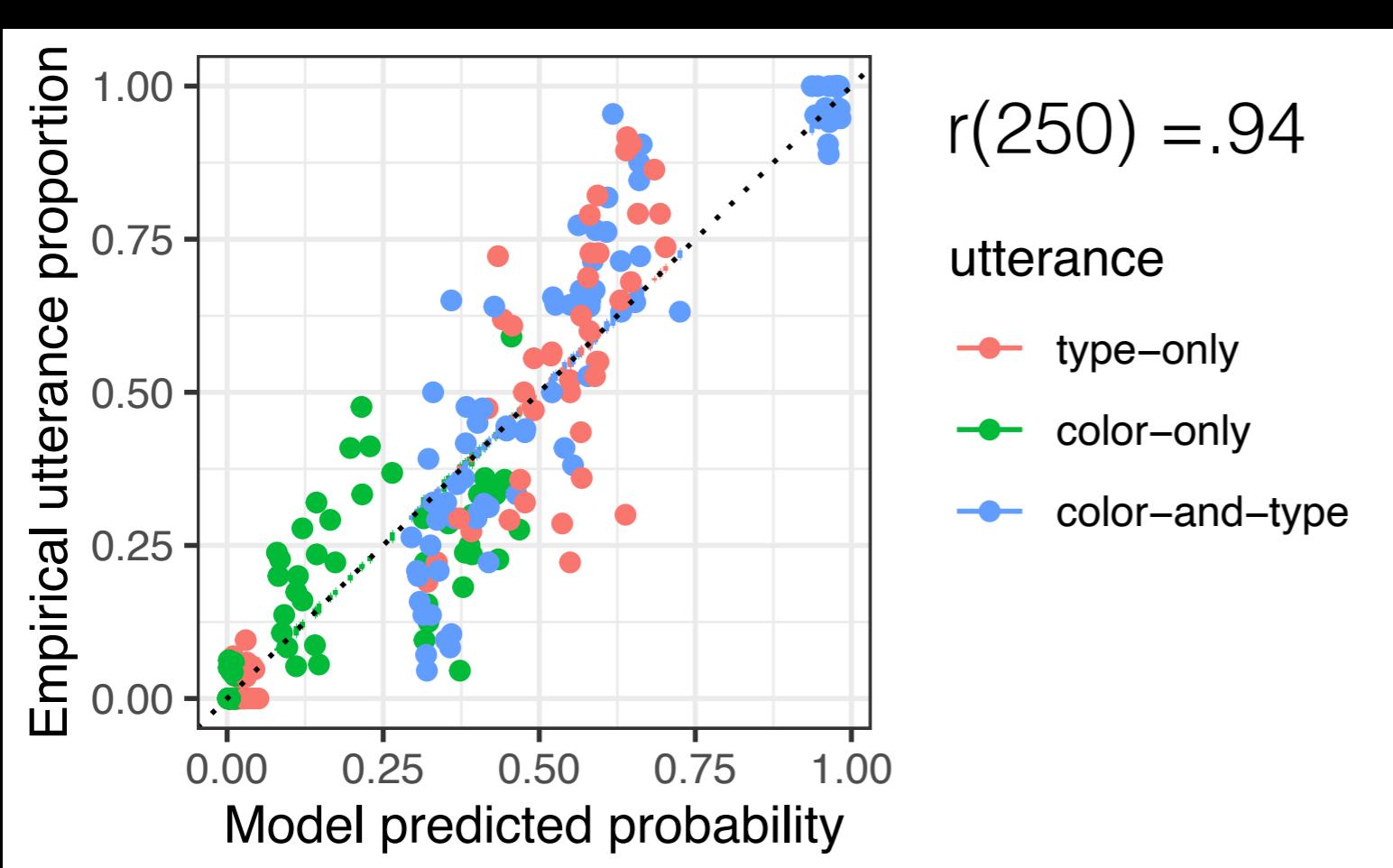
presence of same type

x

presence of color competitor

# Model evaluation

		Semantics	
		<i>empirical</i>	<i>fixed plus empirical</i>
Cost	<i>empirical</i>	-1474.6 (4)	-1354.4 (7)
	<i>fixed</i>	-1434.8 (4)	-1321.9 (7)
	<i>none</i>	-1372.9 (2)	<b>-1209.8 (5)</b>



A continuous-semantics RSA speaker captures variability in color modification by reasoning about a continuous semantics literal listener: the less inferable the intended referent is from the unmodified noun, the more likely modification is.

# Final extension: cross-linguistic variability

Color overmodification less likely in Spanish (with post-nominal adjectives) than in English. [Rubio-Fernández 2016](#)

Strong argument for the role of incrementality.

Utterances	Size-sufficient (SS) scene			Color-sufficient (CS) scene		
	$O_{\text{big\_blue}}$	$O_{\text{big\_red}}$	$O_{\text{small\_blue}}$	$O_{\text{small\_red}}$	$O_{\text{big\_red}}$	$O_{\text{small\_blue}}$
English	<i>blue pin, red pin, big pin, small pin, big blue pin, big red pin, small blue pin</i>				<i>blue pin, red pin, big pin, small pin, small red pin, big red pin, small blue pin</i>	
Spanish -postnom.	<i>pin blue, pin red, pin big, pin small, pin blue big, pin red big, pin blue small</i>				<i>pin blue, pin red, pin big, pin small, pin red small, pin red big, pin blue small</i>	

# Incremental RSA

Cohn-Gordon, Goodman, & Potts 2018

$$L_0^{INCR}(r|c, i) \propto \mathcal{X}^D(c, i, r) \cdot P(r)$$

$$\mathcal{X}^D(c, i, r) = \frac{|u: [[u]]^D(r) = 1 \wedge u \text{ is a continuation of } c+i|}{|u: u \text{ is a continuation of } c+i|}$$

$$S_1^{INCR}(i|c, r) \propto e^{\alpha(L_0^{INCR}(r|c, i) - C(i))}$$

$$S_1(u|r) = \prod_{j=1}^n S_1^{INCR}(i_j | c = [i_1 \dots i_{j-1}], r)$$

proportion of  
applicable  
continuations

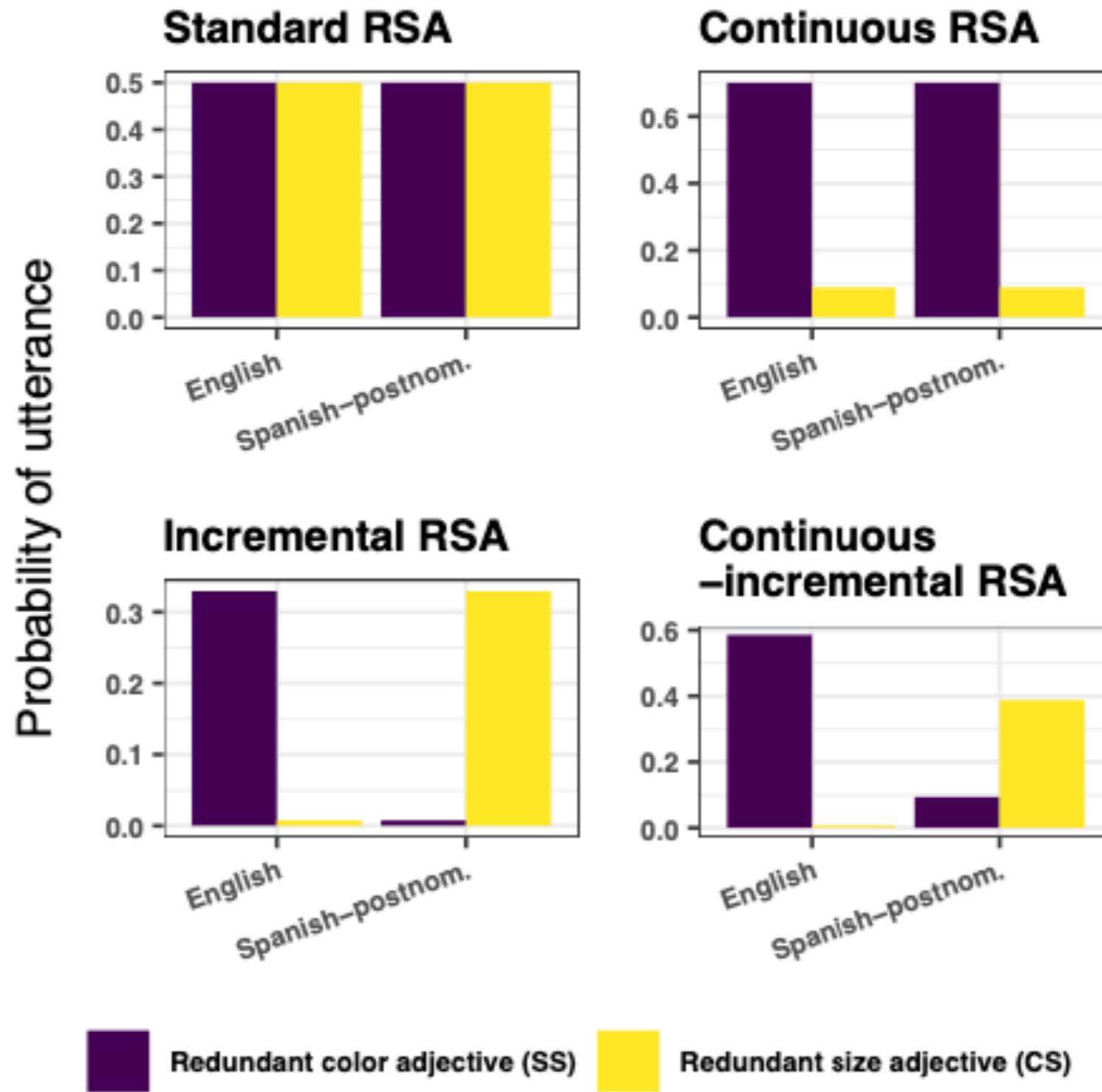
# Continuous-Incremental RSA

Waldon & Degen 2021

$$\mathcal{X}^C(c, i, r) = \frac{\sum [[u]]^C(r): u \text{ is a continuation of } c+i}{|u: u \text{ is a continuation of } c+i|}$$

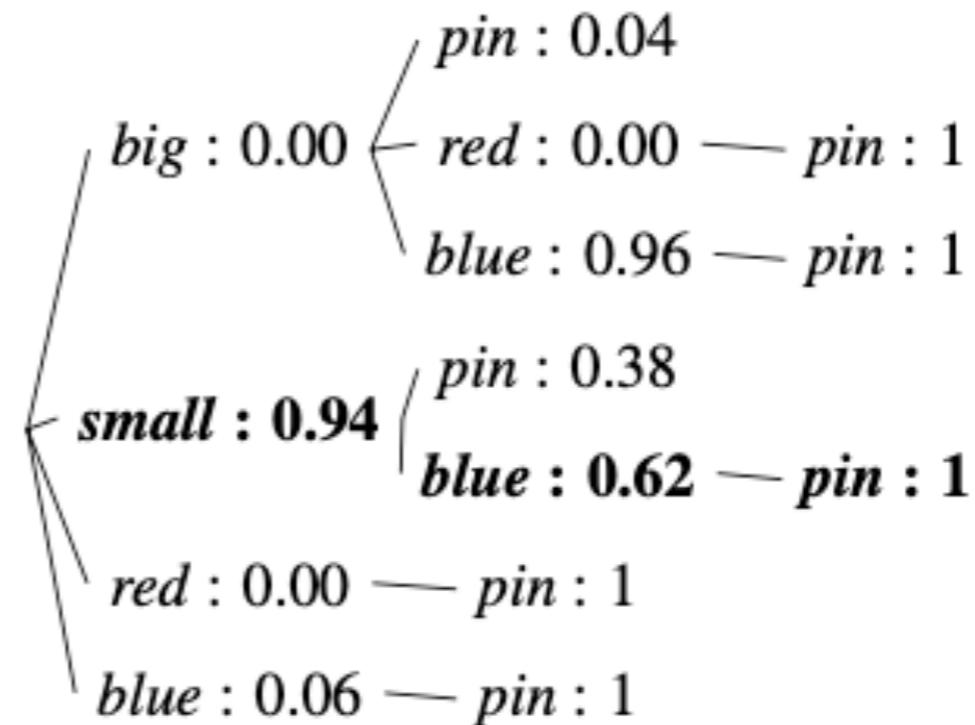
sum of semantic  
values over number  
of continuations

# Model predictions



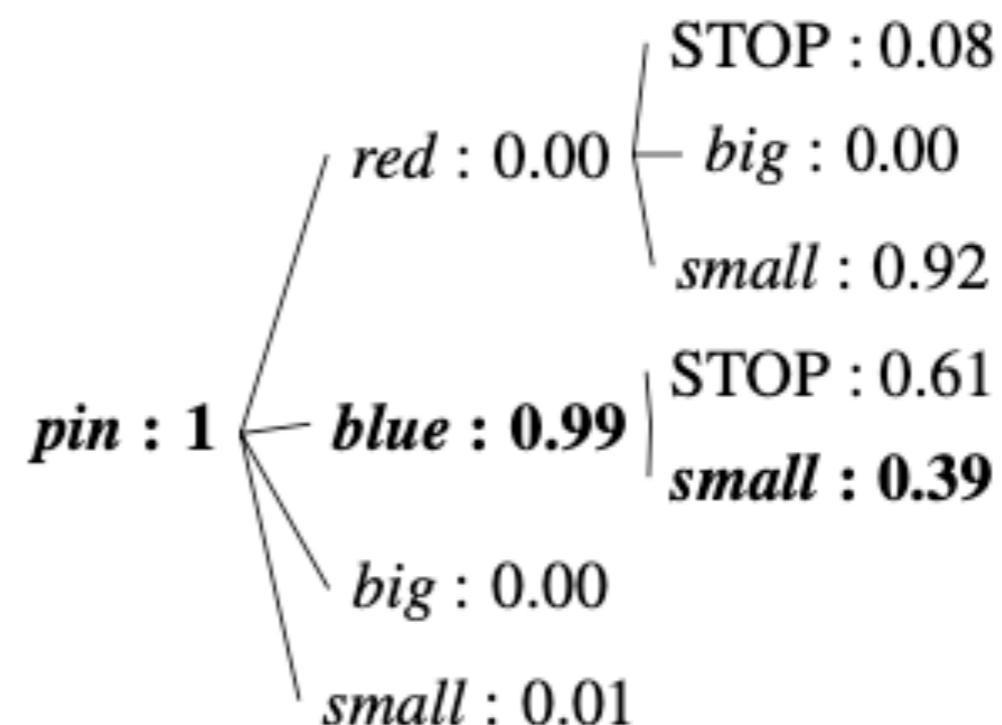
# Continuous-Incremental RSA

## English size-sufficient



Analogous contexts (symmetric in Incremental RSA)

## Spanish color-sufficient



# Continuous-Incremental RSA

Combining incremental and continuous RSA

- provides some support for Rubio-Fernández's claim that modification is generally less useful post-nominally
- makes interesting novel prediction for flipped color/size overmodification asymmetry in post-nominal adjective languages

**Much more empirical work needed!**

# Reference comprehension and production

## Comprehension:

Listeners draw inferences based on the expectation that speakers not be over-informative.

## Production:

Speakers produce seemingly overinformative referring expressions.

Quantity-2

Qu~~a~~ntity-2

## HOW TO RESOLVE?

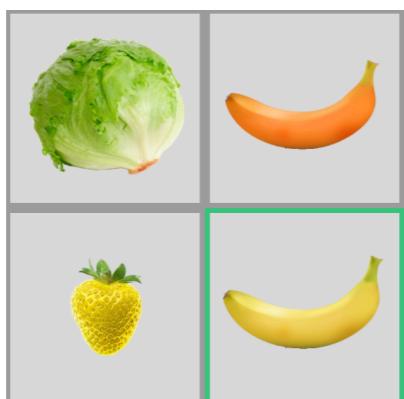
# Reference comprehension and production

## Comprehension:

Listeners draw inferences based on the expectation that speakers be **sufficiently contextually informative.**

## Production:

Speakers produce **usefully redundant** referring expressions.



RSA: useful modeling framework to formalize the link between production and comprehension via probabilistic inference.

## Probabilistic language understanding

### An introduction to the Rational Speech Act framework

By Gregory Scontras, Michael Henry Tessler, and Michael Franke

The present course serves as a practical introduction to the Rational Speech Act modeling framework. Little is presupposed beyond a willingness to explore recent progress in formal, implementable models of language understanding.

#### Main content

##### I. [Introducing the Rational Speech Act framework](#)

*An introduction to language understanding as Bayesian inference*

##### II. [Modeling pragmatic inference](#)

*Enriching the literal interpretations*

##### III. [Inferring the Question-Under-Discussion](#)

*Non-literal language*

##### IV. [Combining RSA and compositional semantics](#)

*Jointly inferring parameters and interpretations*

##### V. [Fixing free parameters](#)

*Vagueness*

##### VI. [Expanding our ontology](#)

*Plural predication*

##### VII. [Extending our models of predication](#)

*Generic language*

##### VIII. [Modeling semantic inference](#)

*Lexical uncertainty*

##### IX. [Social reasoning about social reasoning](#)

*Politeness*

The literal listener rule can be written as follows:

```
// set of states (here: objects of reference)
// we represent objects as JavaScript objects to demarcate them from utterances
// internally we treat objects as strings nonetheless
var objects = [{color: "blue", shape: "square", string: "blue square"}, 
               {color: "blue", shape: "circle", string: "blue circle"}, 
               {color: "green", shape: "square", string: "green square"}]

// set of utterances
var utterances = ["blue", "green", "square", "circle"]

// prior over world states
var objectPrior = function() {
  var obj = uniformDraw(objects)
  return obj.string
}

// meaning function to interpret the utterances
var meaning = function(utterance, obj){
  _.includes(obj, utterance)
}

// literal listener
var literalListener = function(utterance){
  Infer({model: function(){
    var obj = objectPrior();
    var uttTruthVal = meaning(utterance, obj);
    condition(uttTruthVal == true)
    return obj
  }})
}

viz.table(literalListener("blue"))
```

run

(state)	probability
blue circle	0.5
blue square	0.5

#### Exercises:

- In the model above, `objectPrior()` returns a sample from a `uniformDraw` over the possible objects of reference. What happens when the listener's beliefs are not uniform over the

# Scontras, Tessler, & Franke

[forestdb.org/models/overinf.html](http://forestdb.org/models/overinf.html)

Thank you!