

# The Rational Speech Act framework: an integrative theory of the interaction between literal meaning, world knowledge, and context

Judith Degen

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XPrag 2019, Edinburgh



# Early modern XPrag

focus on implicature cost question

Bott & Noveck 2004; Breheny et al 2006

Default theory

Levinson 2000

Relevance theory

Sperber & Wilson 1995;  
Carston 1998

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Constraint-based account

Degen & Tanenhaus 2015

# Informational privilege

Default theory

Levinson 2000

extreme

informational

privilege

Literal-first hypothesis

Huang & Snedeker 2009

certain information

- **processed earlier**

- **weighted more**

**heavily** in resulting

interpretation

Relevance theory

Sperber & Wilson 1995;

Carston 1998

extreme  
parallelism

Constraint-based account

Degen & Tanenhaus 2015

all information

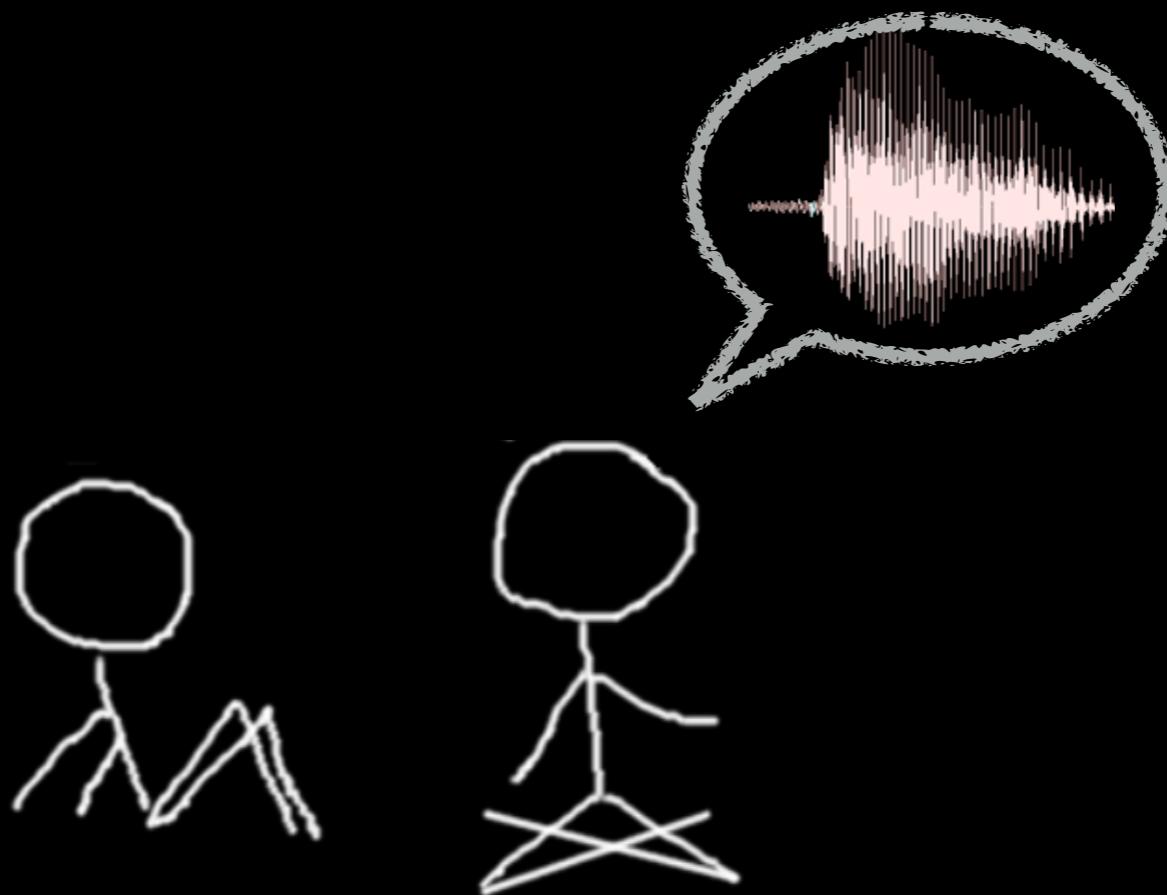
- **processed in parallel**

- **weighted equally** in

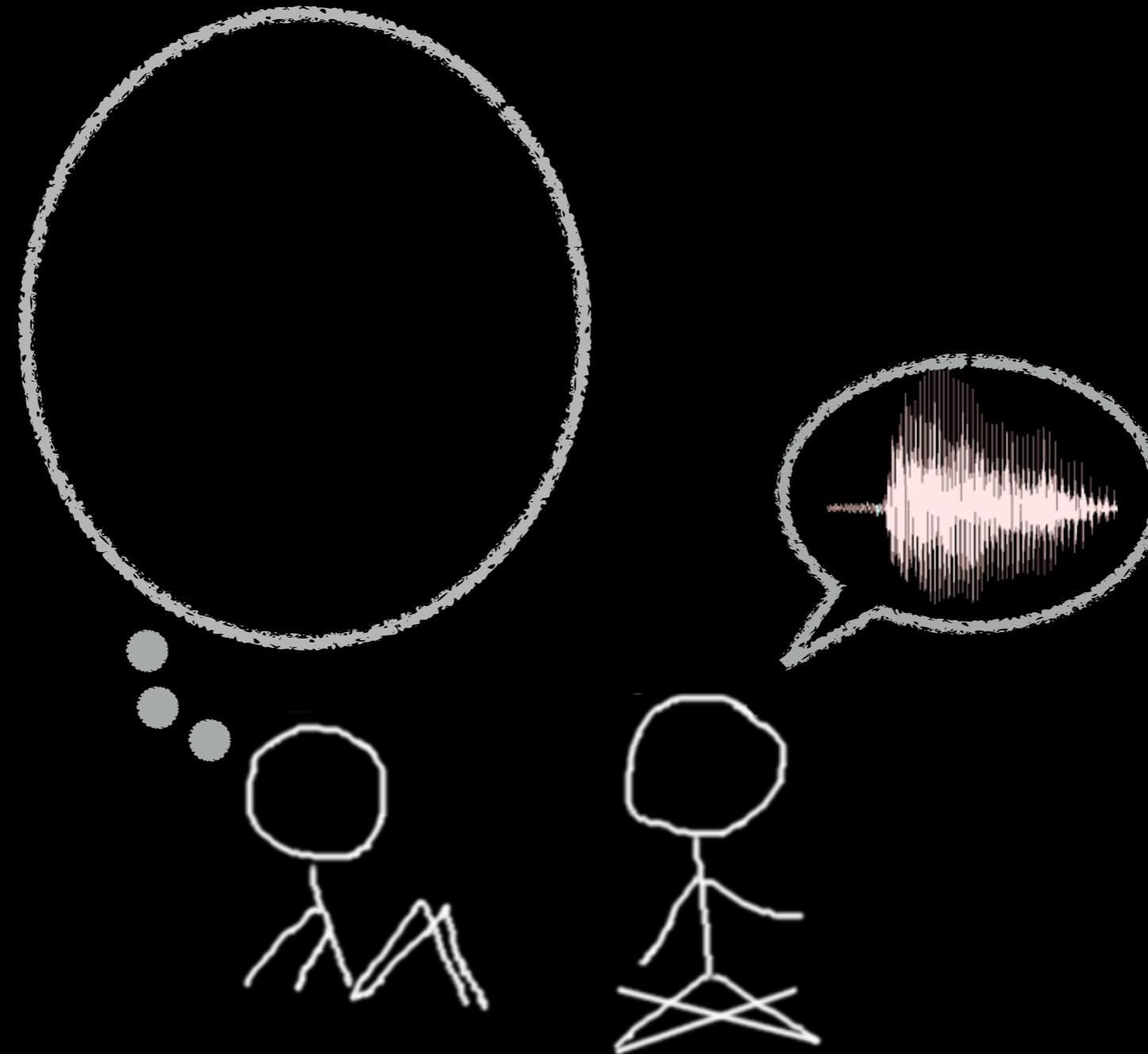
resulting interpretation

Degen & Tanenhaus 2019



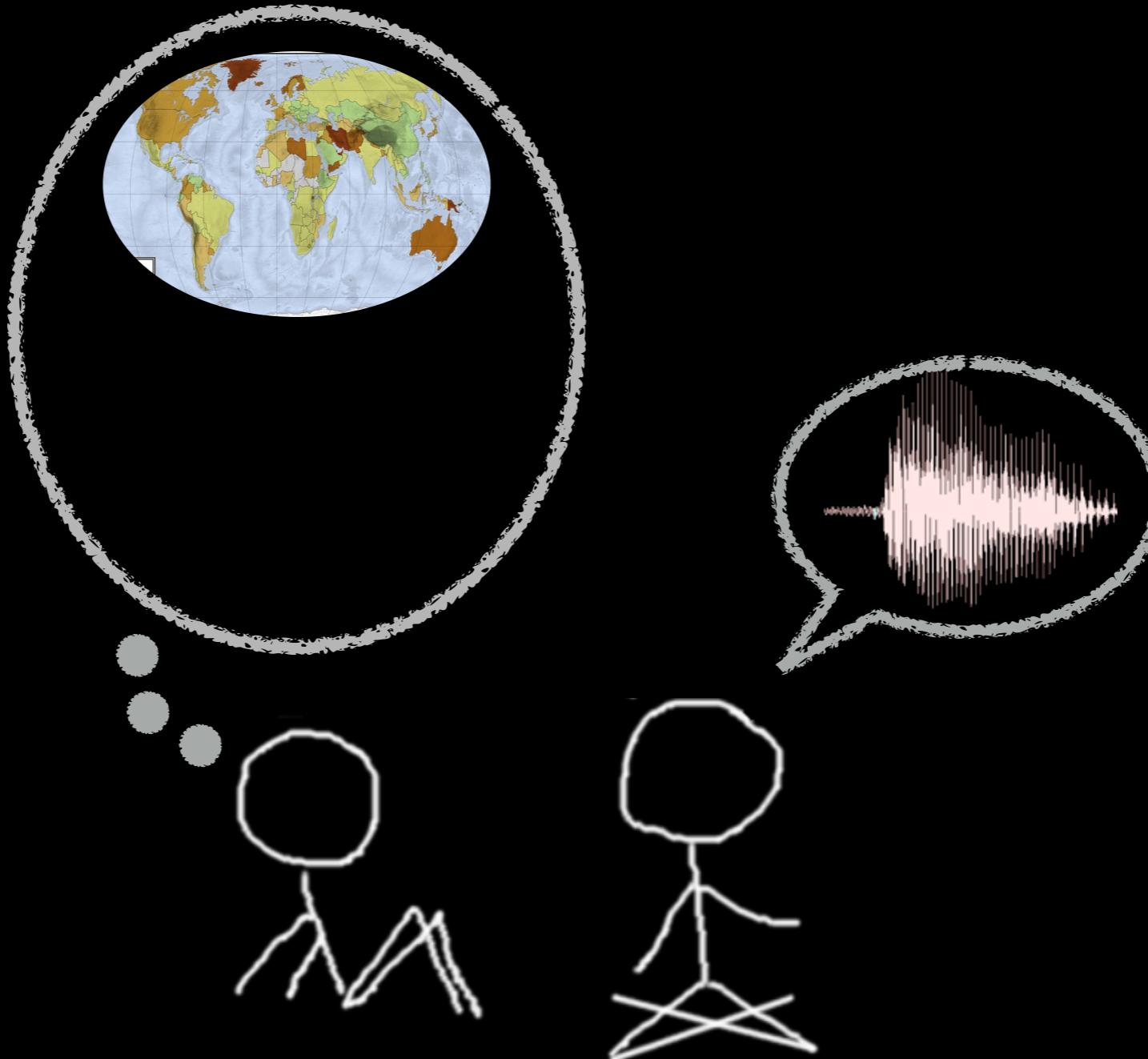


linguistic  
signal



linguistic  
signal

world  
knowledge

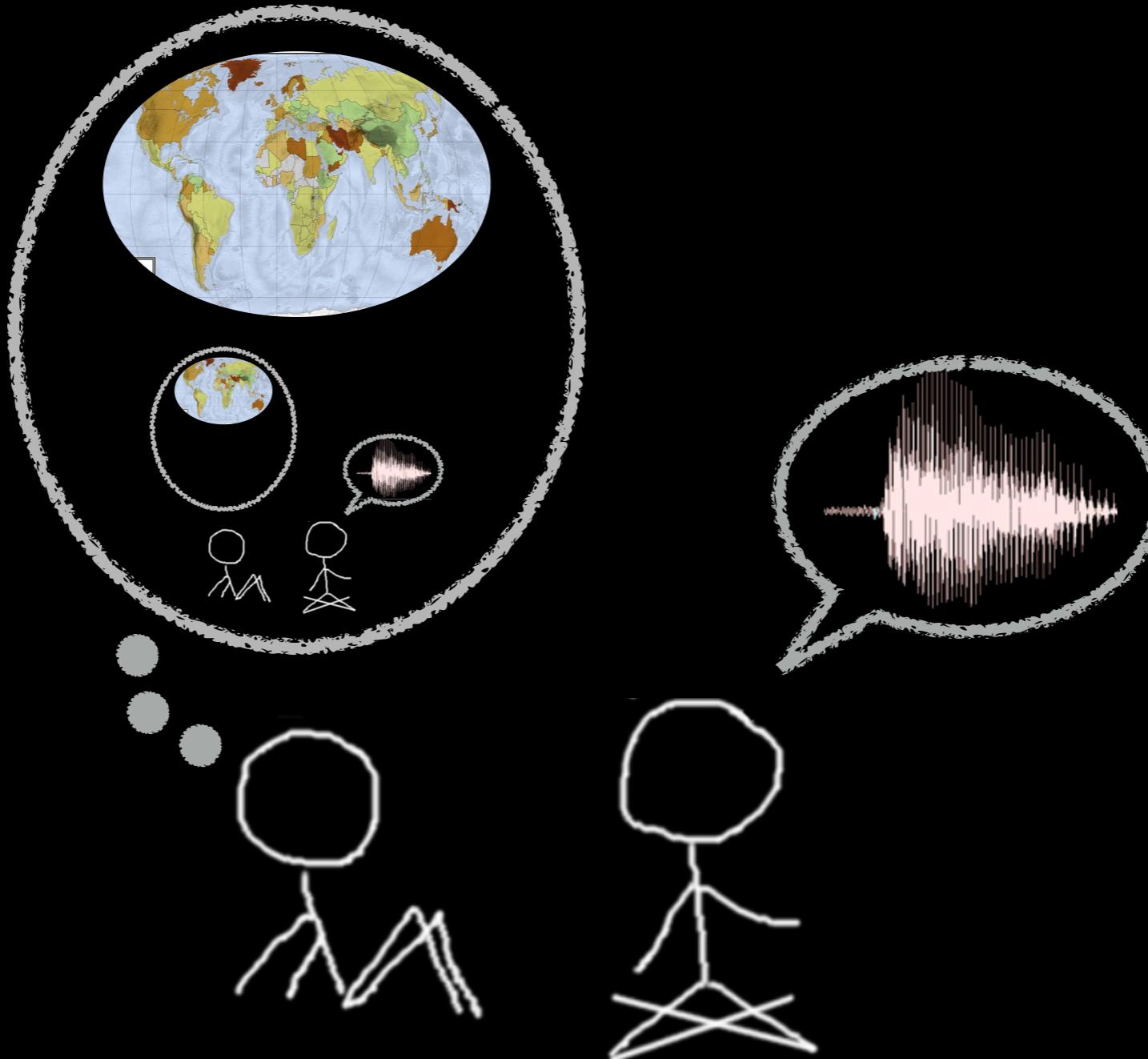


linguistic  
signal

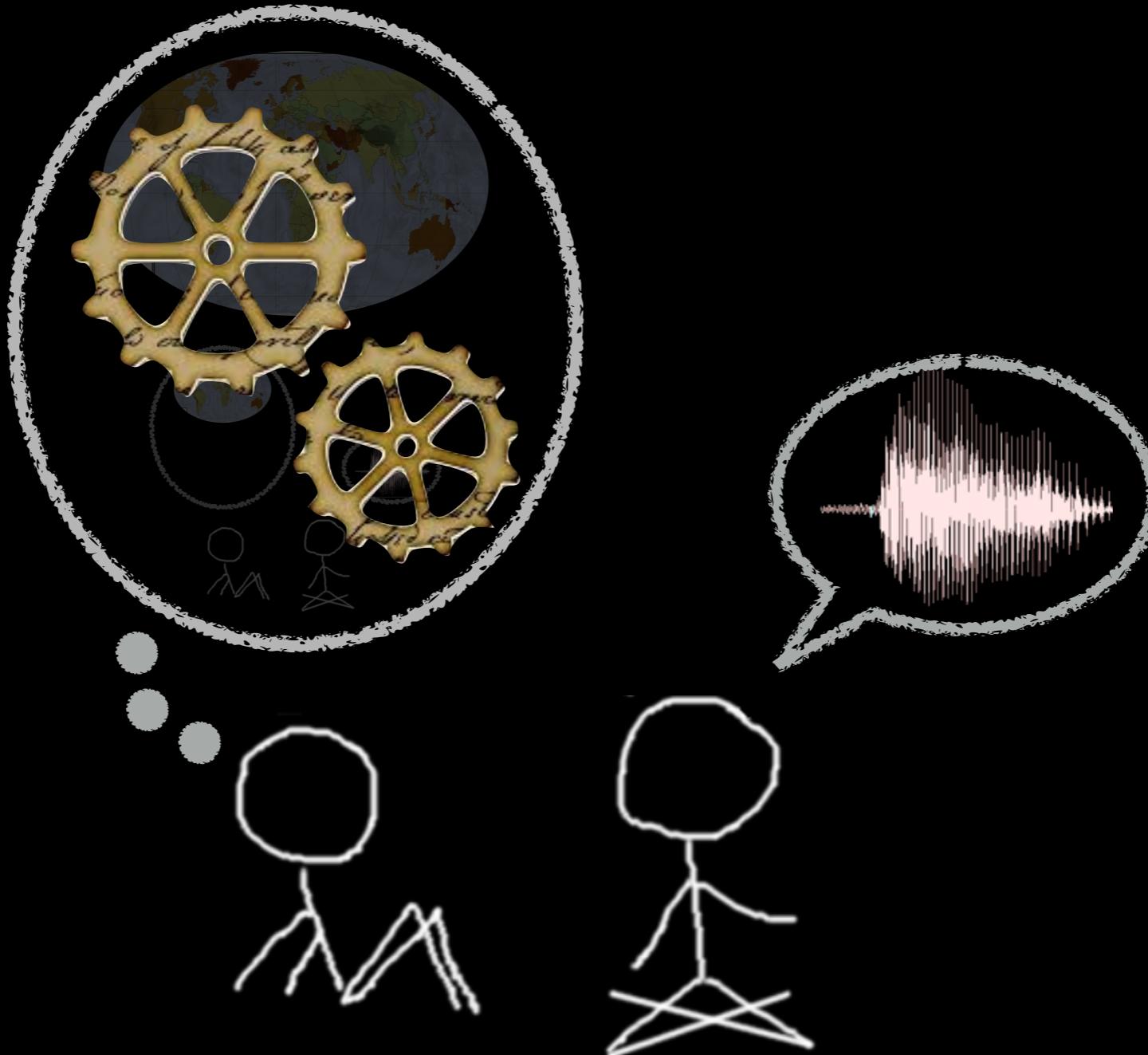
world  
knowledge

context

linguistic  
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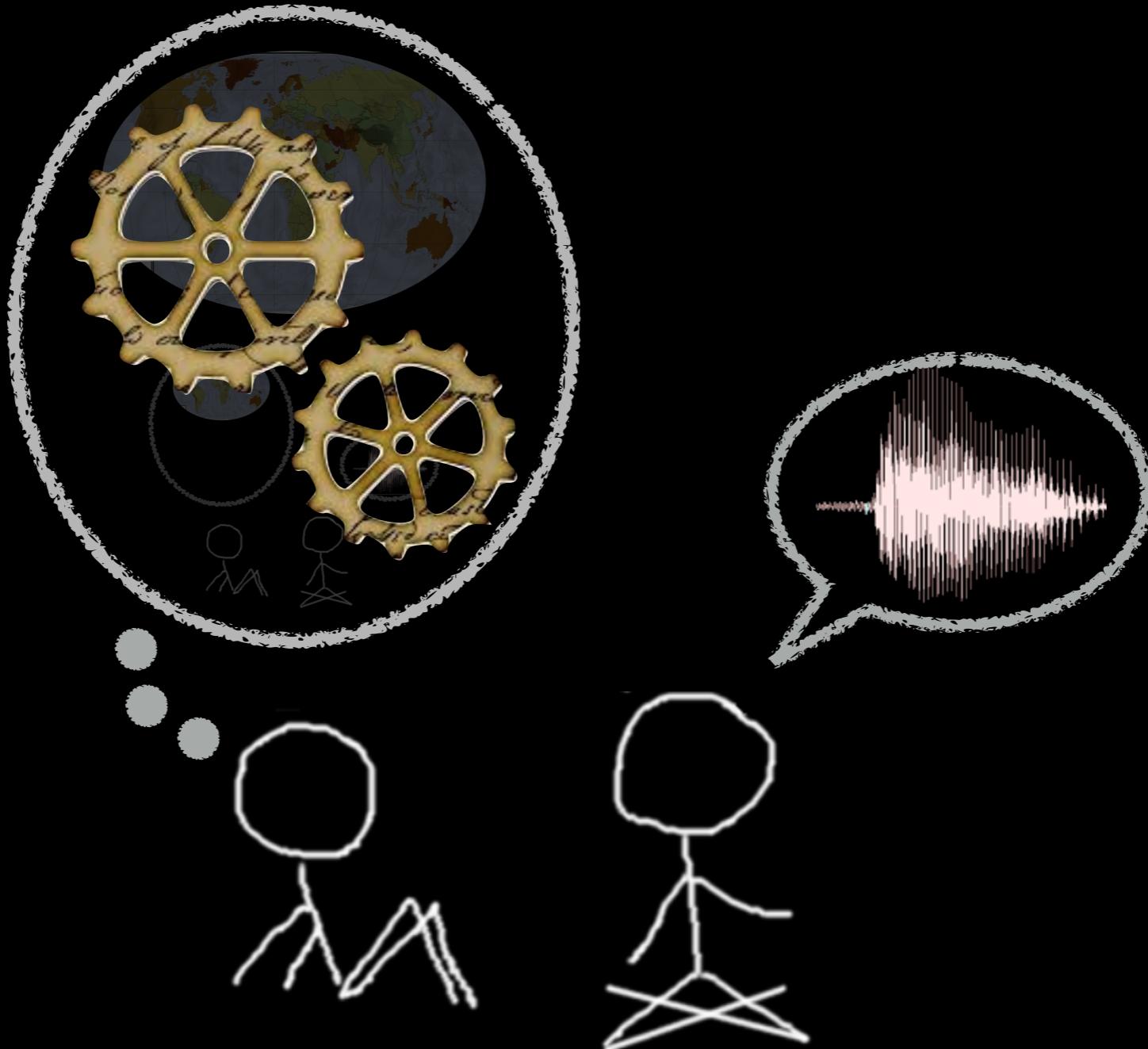


world  
knowledge  
reasoning  
context



linguistic  
signal

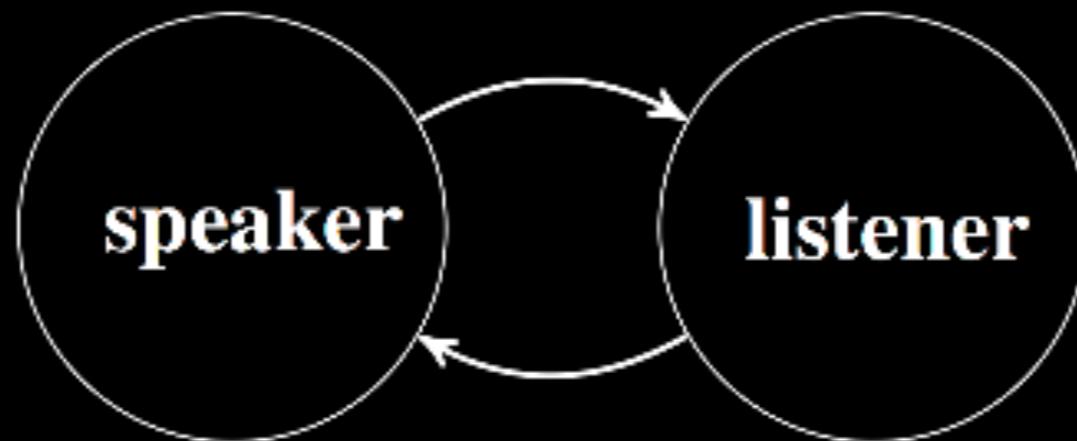
world  
knowledge  
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context



# PRAGMATICS

linguistic  
signal

# The Rational Speech Act Framework



# RSA

# Probabilistic pragmatics

Franke & Jäger, 2016; Goodman & Frank, 2016; Scontras, Tessler, & Franke 2018

## Reference

Frank & Goodman, 2012; Qing & Franke, 2015; Degen & Franke, 2012; Stiller et al., 2015; Franke & Degen, 2015; Degen et al, under review

## Cost-based Quantity implicatures

Degen et al., 2013; Rohde et al., 2012

## Scalar implicatures

Goodman & Stuhlmüller, 2013; Degen et al., 2015

## Embedded implicatures

Potts et al., 2016; Bergen et al., 2016

## M-implicatures

Bergen et al., 2012

## Figurative meaning

Kao et al., 2013; 2014; 2015; Cohn-Gordon & Bergen, under review

## Gradable adjectives

Lassiter & Goodman, 2013; 2015; Qing & Franke, 2014

## Adjective ordering

Hahn et al 2018; Scontras et al 2019

## Other

plural predication Scontras & Goodman 2017

I-implicatures Poppels & Levy, 2016

generics Tessler & Goodman, 2019

modals Herbstritt & Franke, 2017

vague quantifiers Schöller & Franke, 2017

convention formation Hawkins et al 2018; 2019

questions Hawkins et al 2015

pragmatic adaptation Schuster & Degen, in prep

exhaustivity inferences Javangula & Degen in prep

atypicality inferences Kratvchenko & Demberg

social meaning Burnett 2017; 2019

# Bayesian models in other areas

RSA

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**language processing:**

- speech perception
- syntactic adaptation
- reading (surprisal theory)

RSA

# Bayesian models in other areas

**higher-level cognition:**

- reasoning
  - categorization
  - social reasoning
  - intuitive physics
- 
- language processing:**
- speech perception
  - syntactic adaptation
  - reading (surprisal theory)

RSA

# Bayesian models in other areas

**cognitive science more broadly:**

- visual perception
- auditory perception
- multi-modal integration

**higher-level cognition:**

- reasoning
- categorization
- social reasoning
- intuitive physics

**language processing:**

- speech perception
- syntactic adaptation
- reading (surprisal theory)

RSA

# Outline

- I. “**Overinformativeness**” in production
  - why do we do it?
- II. “**Underinformativeness**” in production
  - how do we deal with it in comprehension?

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- I. “**Overinformativeness**” in production
  - why do we do it?
- II. “**Underinformativeness**” in production
  - how do we deal with it in comprehension?

```
var runModel = function(speakerMode) {
  var speakerERP = speakerMode;
  return Enumerate(function() {
    var utt = sample(speakerERP);
    factor(params.speakeroptim);
    return utt;
  });
};
```

models



corpora



experiments

# Part I

---

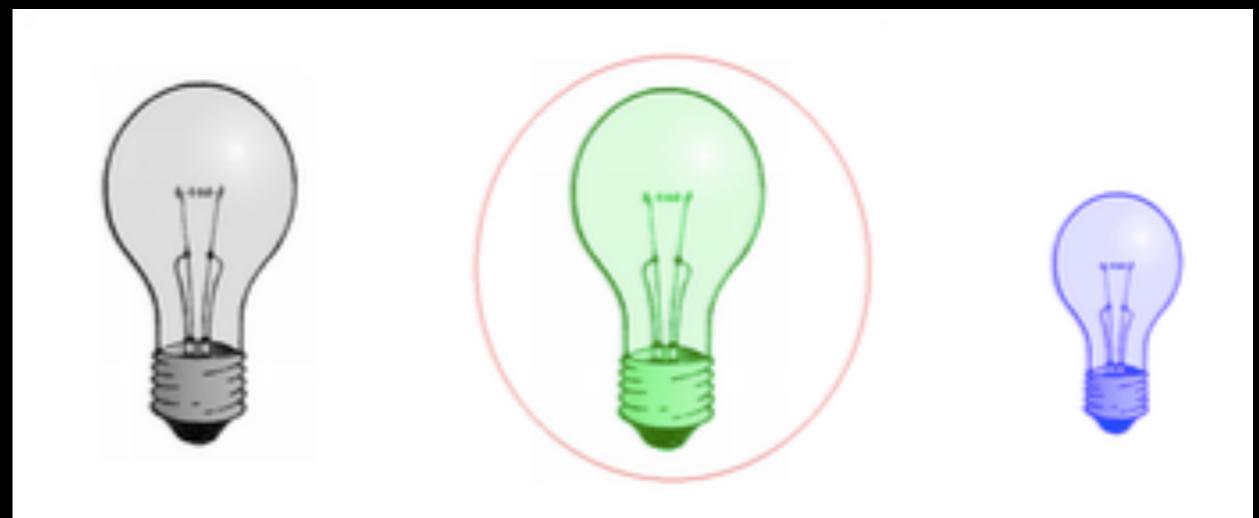
## Production of referring expressions

# CONTENT SELECTION

Which features of an object should/do speakers mention?

# Overinformative referring expressions — color/size asymmetry

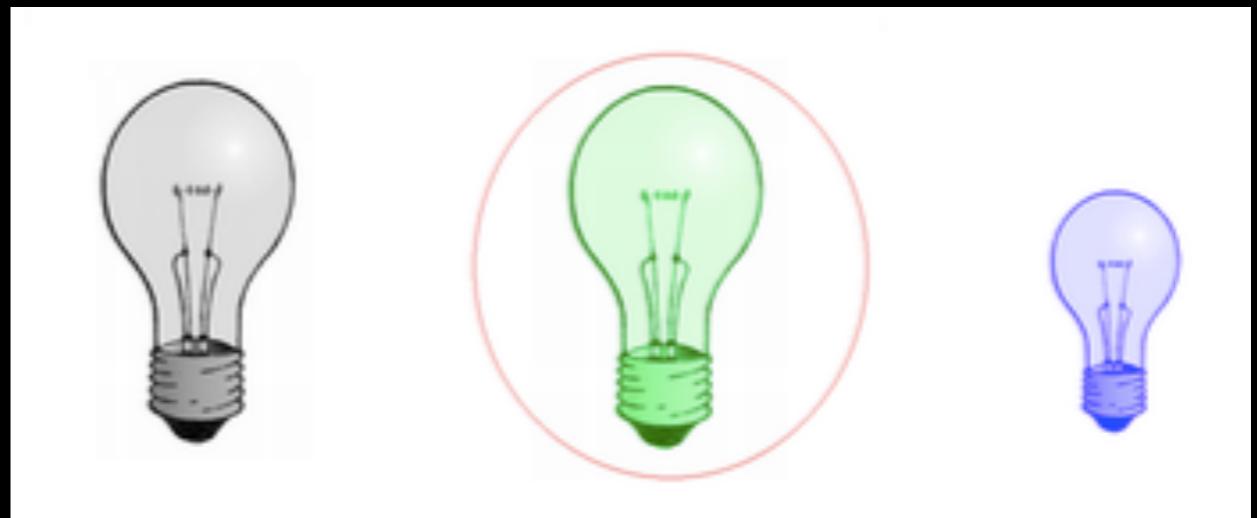
**color sufficient**



*the green lightbulb*

# Overinformative referring expressions — color/size asymmetry

**color sufficient**



*the green lightbulb*

***the big green lightbulb*** 8-10%

# Overinformative referring expressions — color/size asymmetry

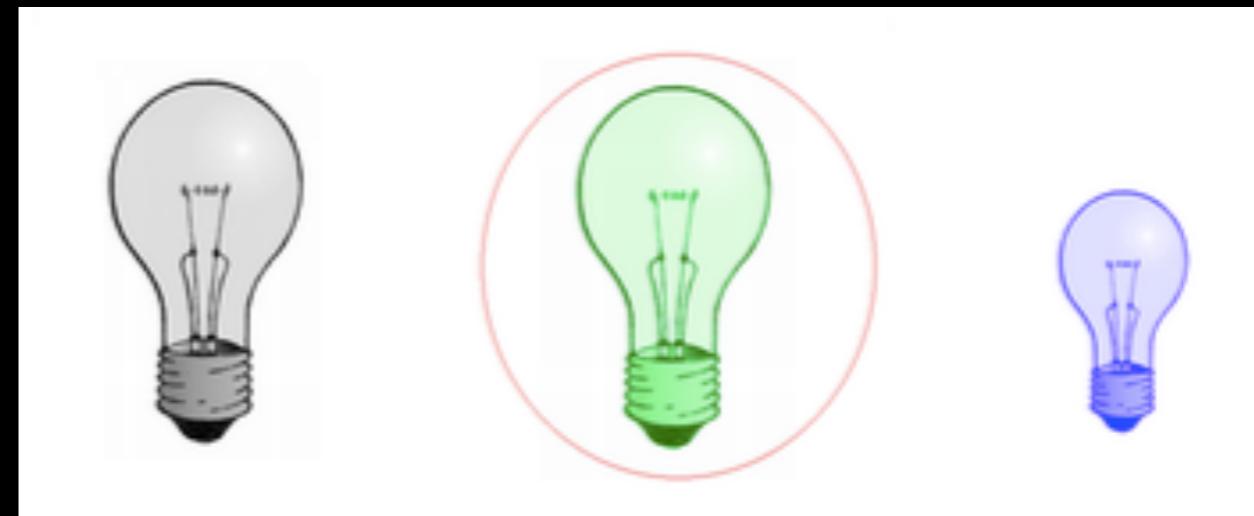
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*the big lightbulb*

**75-80%**    ***the big green lightbulb***    **8-10%**

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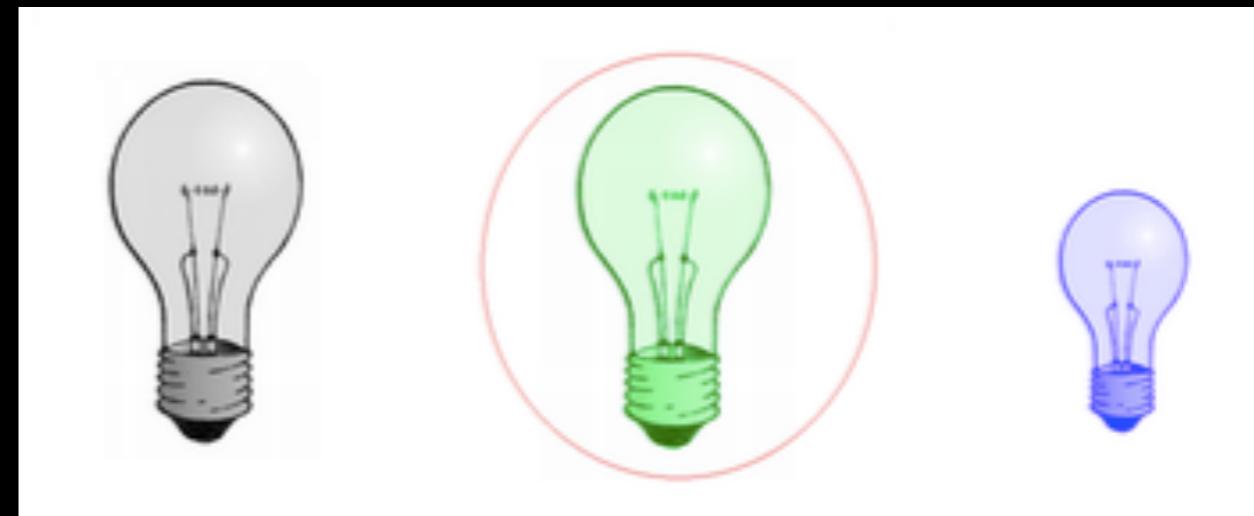
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**color sufficient**



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1. speakers produce overinformative referring expressions
2. more overinformative color than size mentions

# Overinformative referring expressions — color/size asymmetry

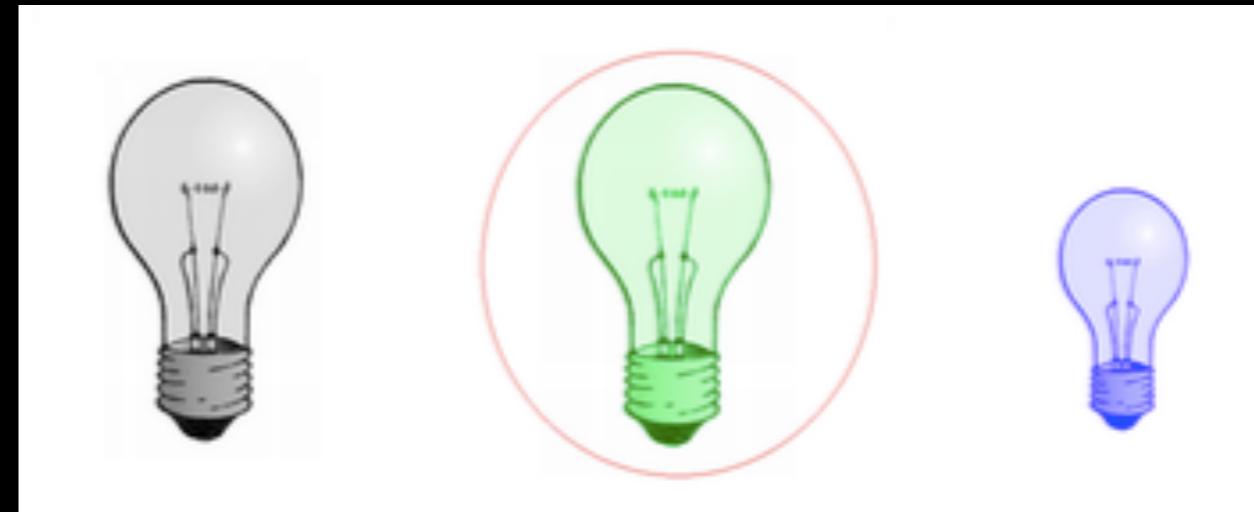
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1. speakers produce overinformative referring expressions  
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**“OVERINFORMATIVENESS”**

Deutsch 1976; Pechmann 1989; Sedivy 2003; Gatt et al. 2011; many others

# Computational models of REs

- Greedy Algorithm  
Dale 1989
- Incremental Algorithm  
Dale & Reiter 1995
- PRO  
Gatt et al 2013; van Gompel et al 2019

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- Greedy Algorithm  
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- Informativeness

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Preferences

- PRO  
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Probabilities

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Frank & Goodman 2012

# The RSA framework

Frank & Goodman 2012

$$O = \{ \text{!}, \text{!}, \text{!} \}$$

$$U = \{\text{big}, \text{small}, \text{green}, \text{black}\}$$

# The RSA framework

Frank & Goodman 2012

$$O = \{ \text{!}, \text{!}, \text{!} \}$$

$$U = \{\text{big}, \text{small}, \text{green}, \text{black}\}$$

## Literal listener

$$P_{L_0}(o|u) = \mathcal{U}(o|\{u \text{ is true of } o\})$$

$$[[u]] : O \rightarrow \{\text{true}, \text{false}\}$$

# The RSA framework

Frank & Goodman 2012

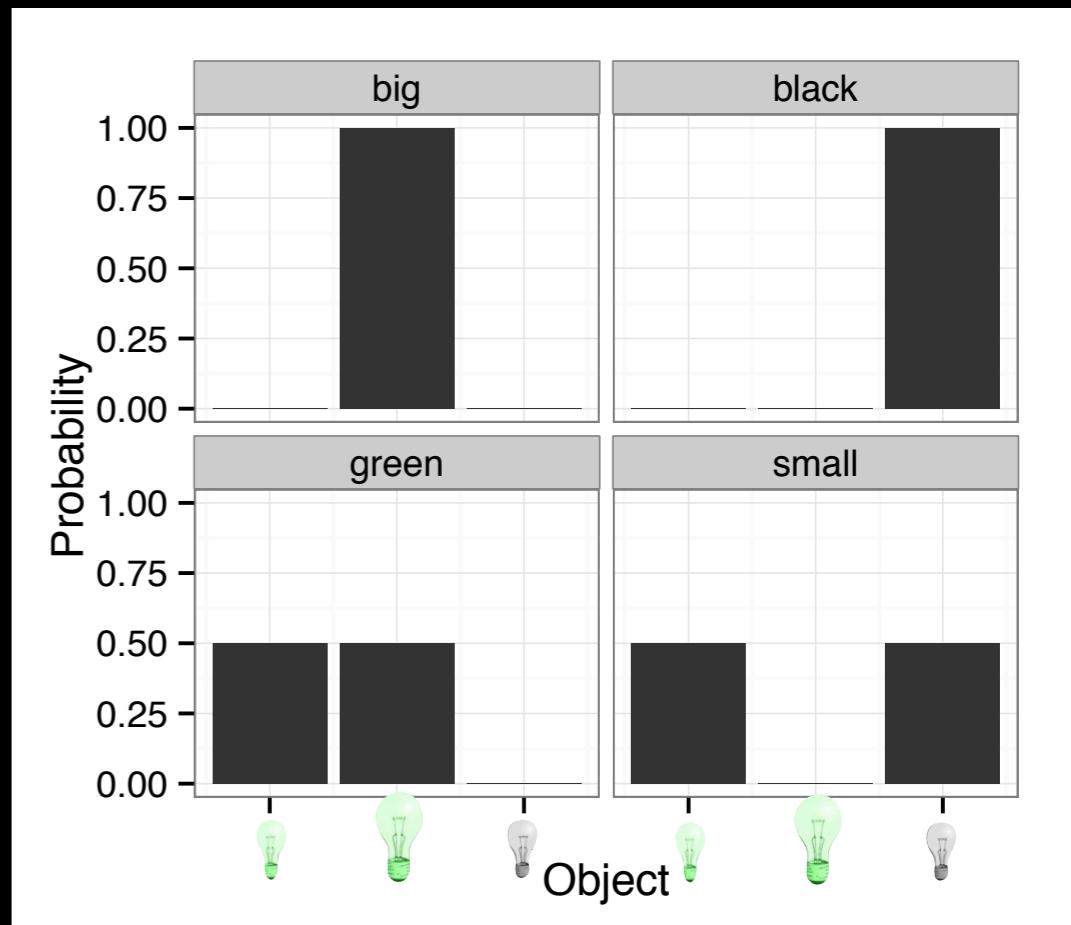
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# The RSA framework

Frank & Goodman 2012

$$O = \{ \text{!}, \text{bulb}, \text{?} \}$$

$$U = \{\text{big}, \text{small}, \text{green}, \text{black}\}$$

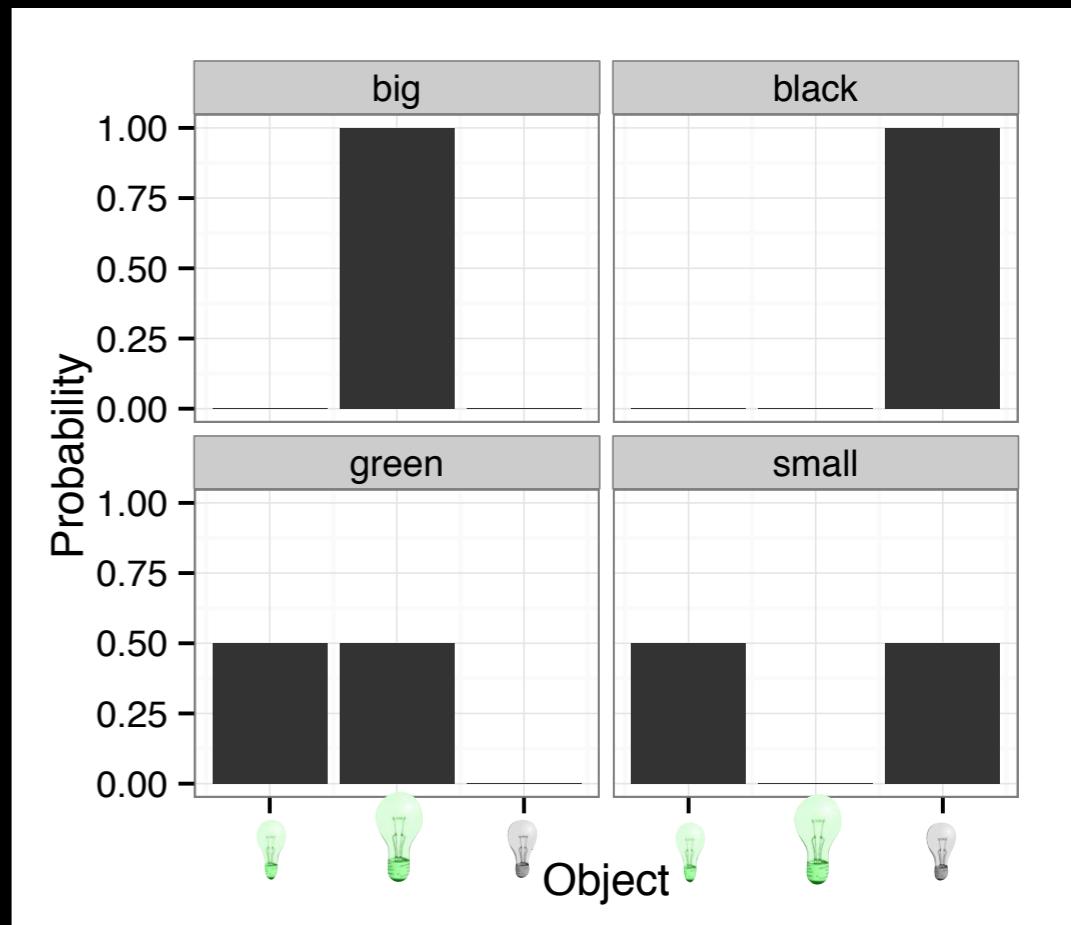
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## Pragmatic speaker

$$P_{S_1}(u|o) \propto e^{\lambda \cdot (\ln P_{L_0}(o|u) - C(u))}$$



# The RSA framework

Frank & Goodman 2012

$$O = \{ \text{!}, \text{!} \text{ (red outline)}, \text{!} \}$$

$$U = \{\text{big}, \text{small}, \text{green}, \text{black}\}$$

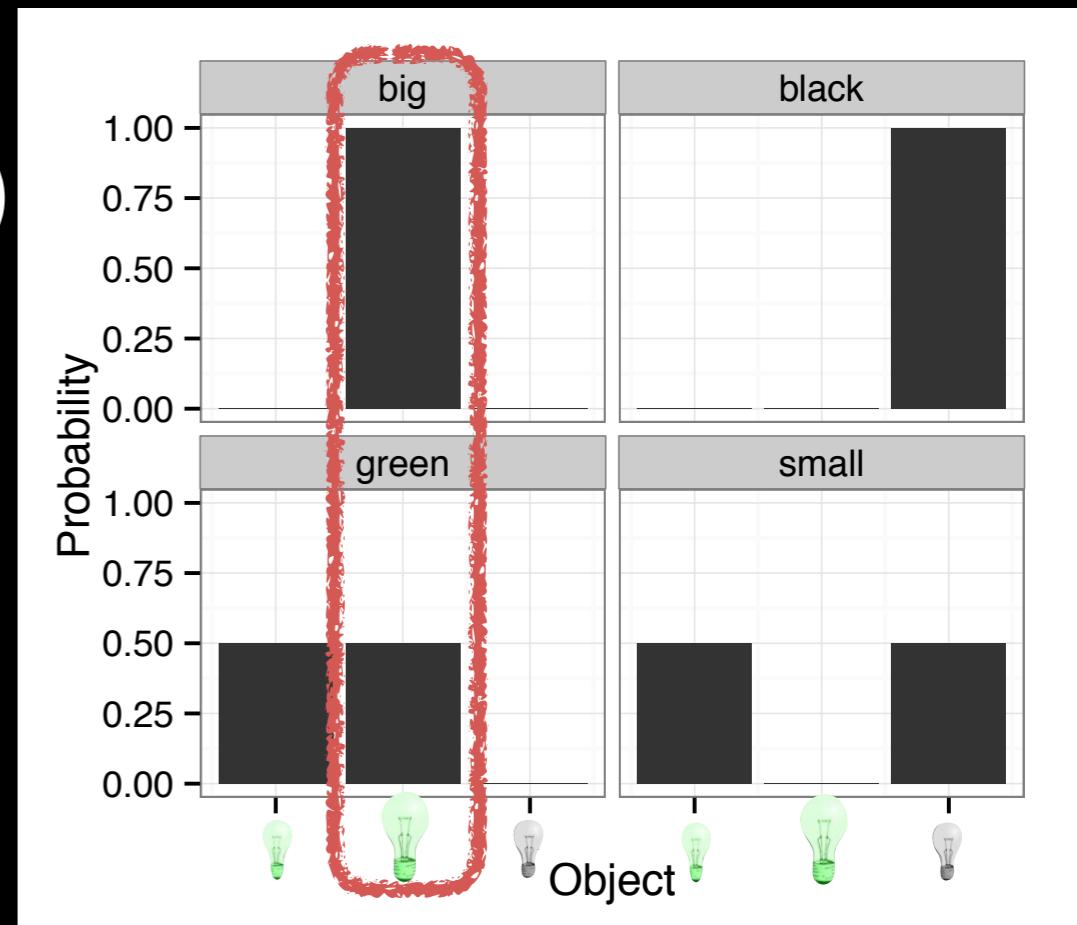
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$$O = \{ \text{!}, \text{💡}, \text{💡} \}$$

$$U = \{\text{big}, \text{small}, \text{green}, \text{black}\}$$

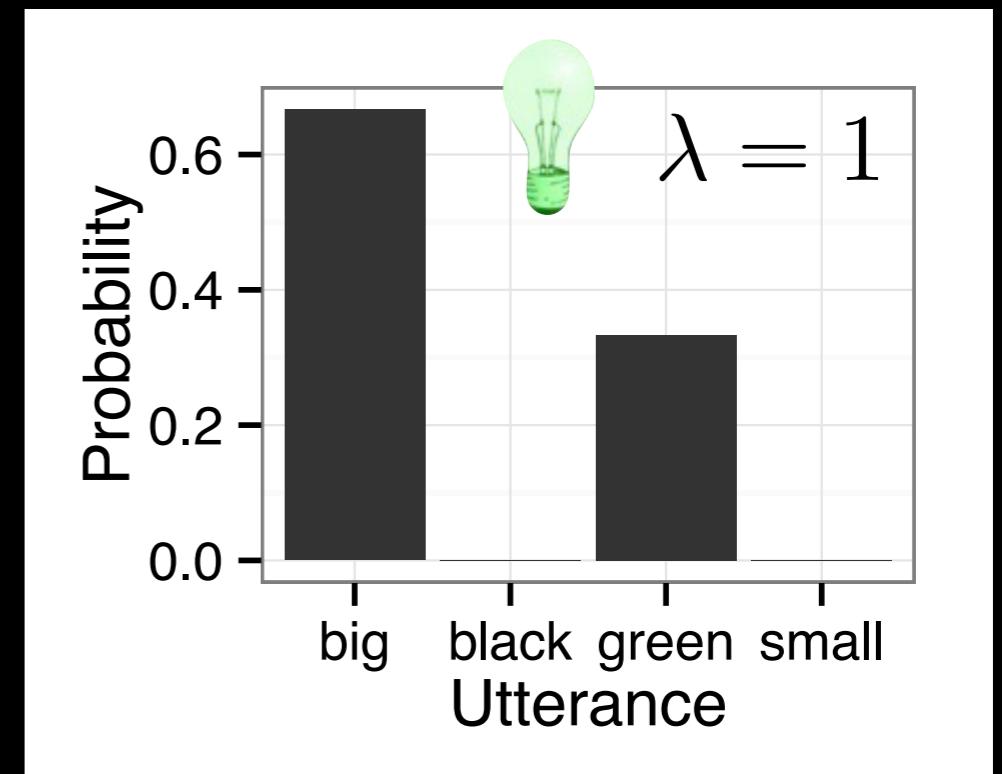
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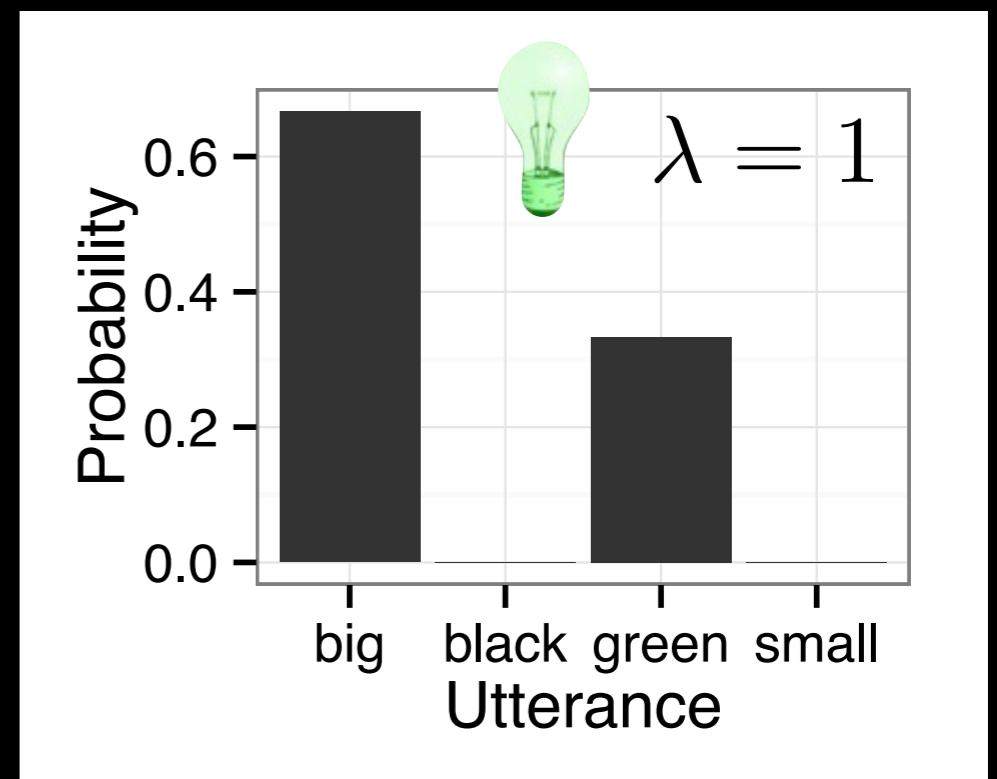
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Quantity



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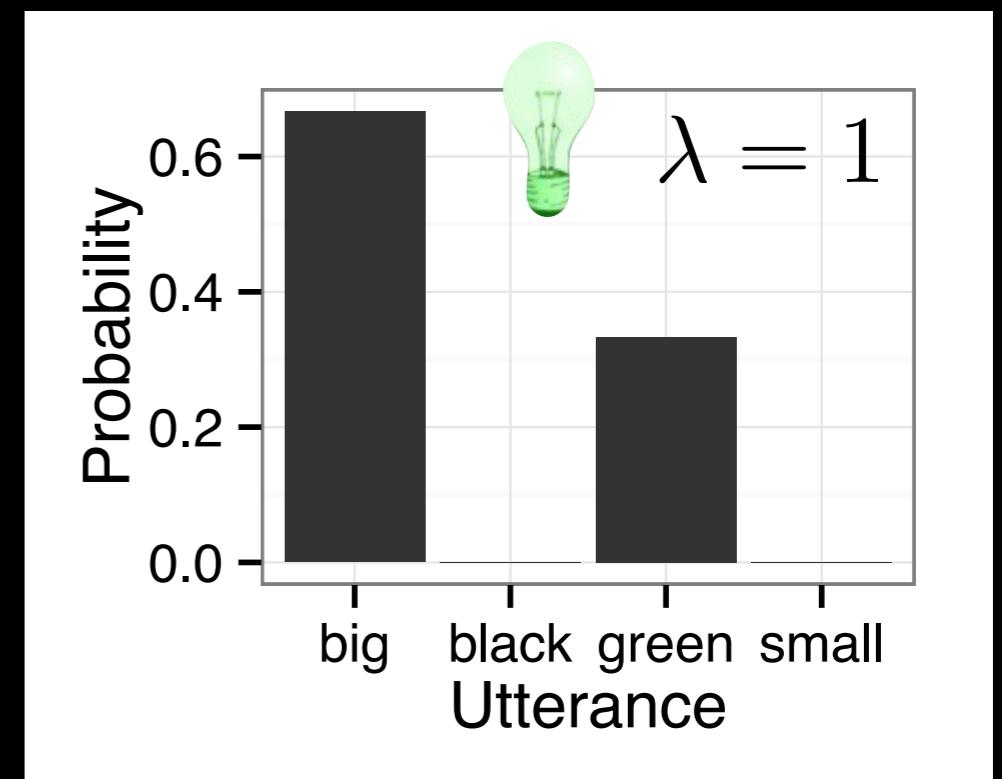
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$$[[u]] : O \rightarrow \{\text{true}, \text{false}\}$$

## Pragmatic speaker

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Manner



# The RSA framework

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$$O = \{ \text{!}, \text{bulb}, \text{?} \}$$

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obvious problem:  
no complex utterances

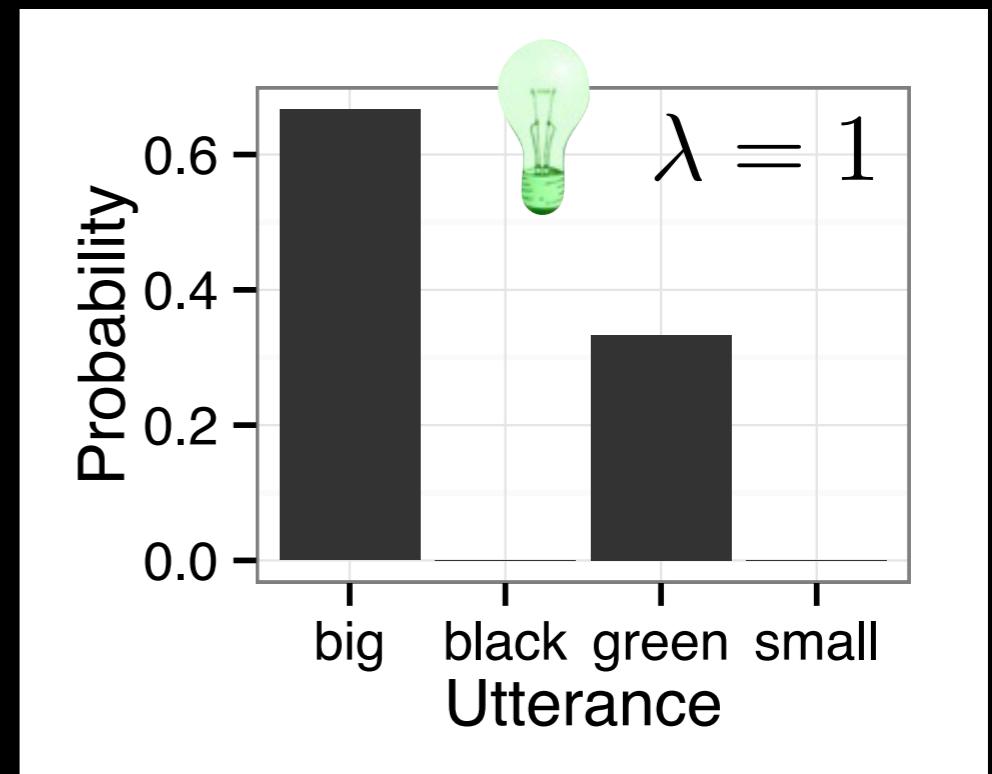
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Frank & Goodman 2012

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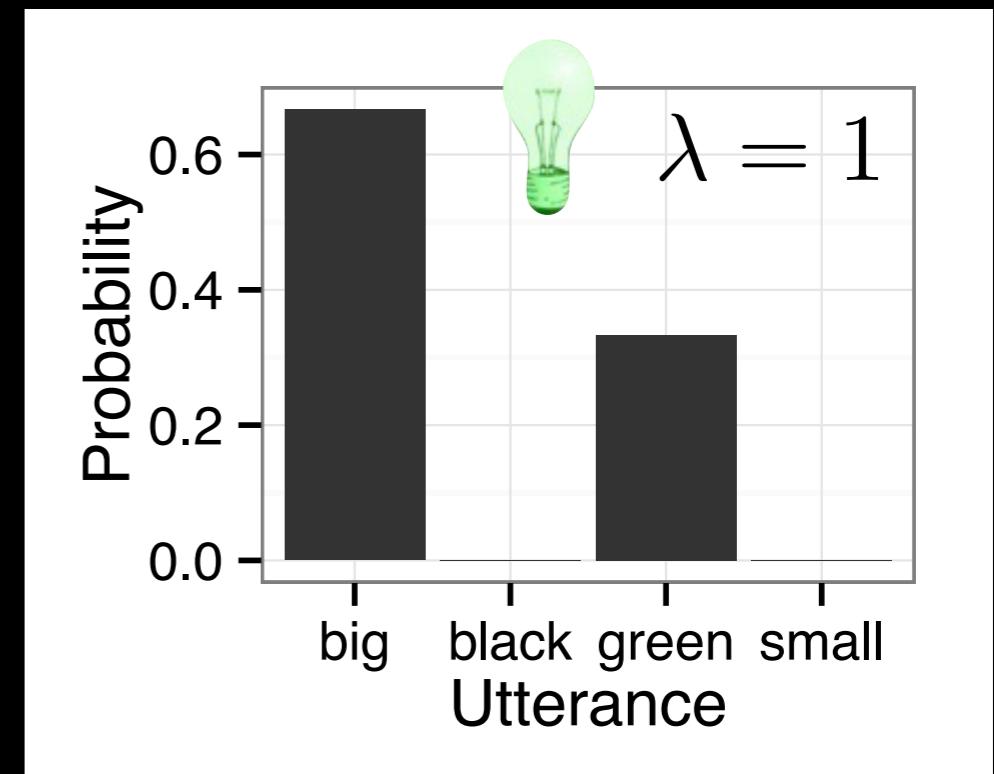
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# Utterance semantics & cost

## Intersective semantics

$$[[u]] = [[u_1]] \wedge [[u_2]]$$

$$[[\text{big green}]] = [[\text{big}]] \wedge [[\text{green}]]$$

## Cost

$$C(u) = C(u_1) + C(u_2)$$

# Utterance semantics & cost

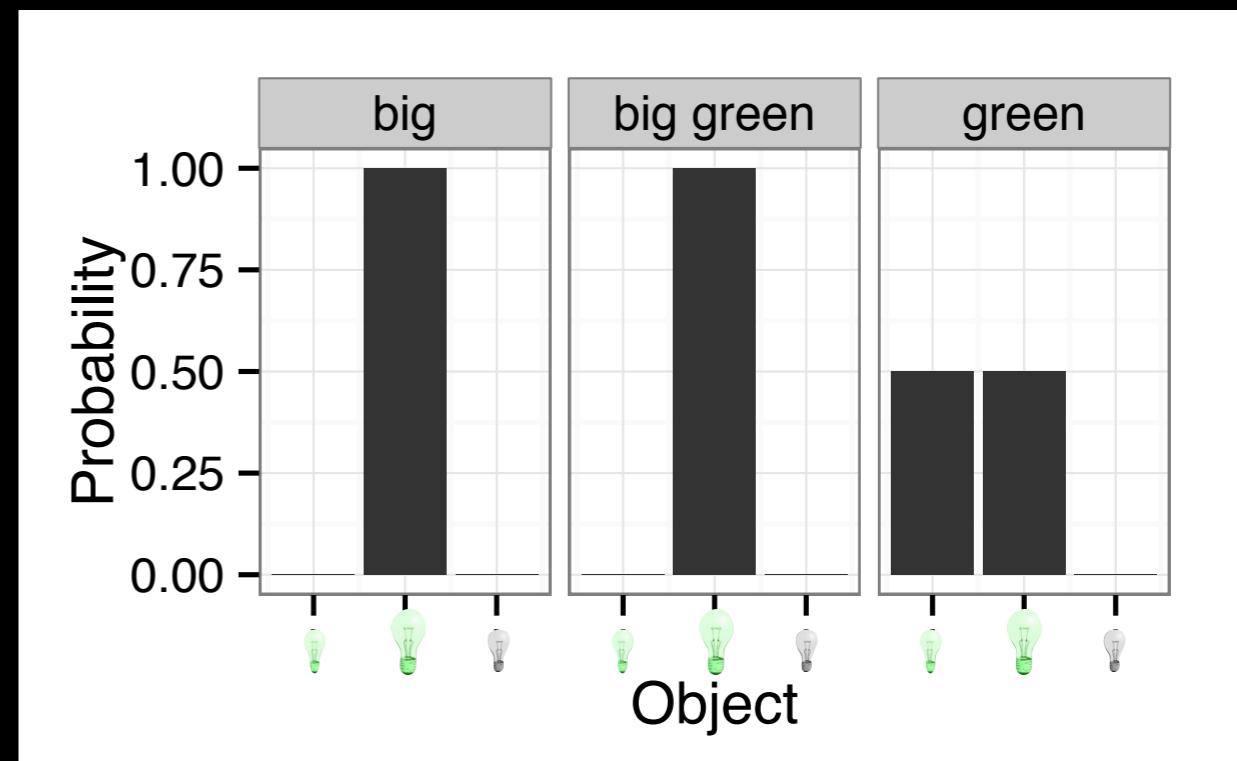
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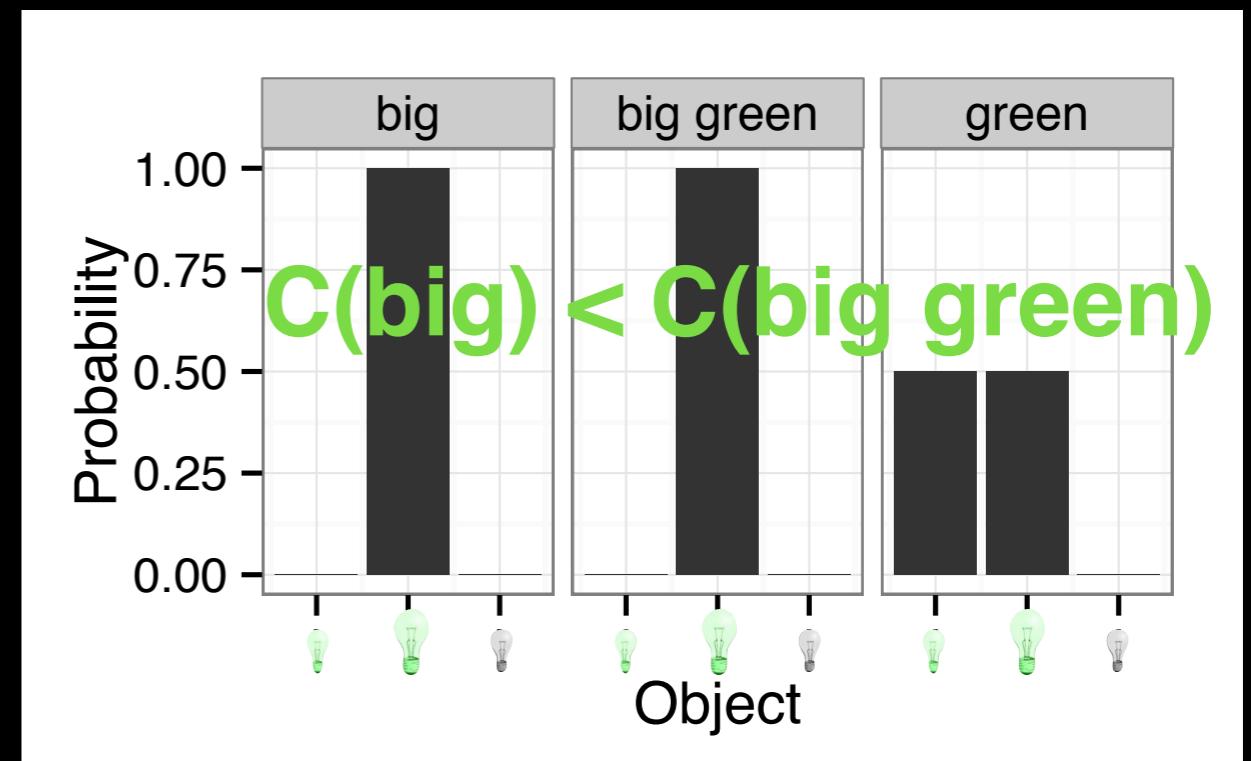
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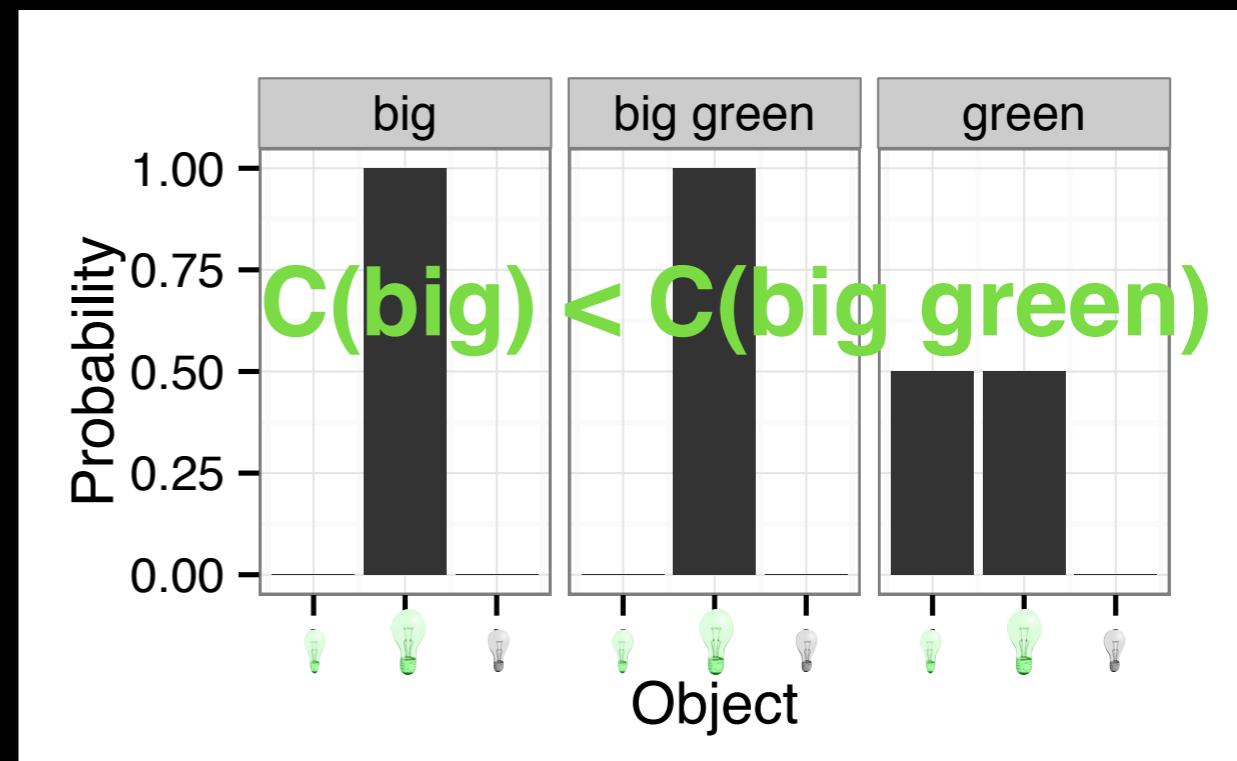
$$[[\text{big green}]] = [[\text{big}]] \wedge [[\text{green}]]$$

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RSA does not produce overinformative REs...

Gatt et al 2013; Westerbeek et al 2015



# Utterance semantics & cost

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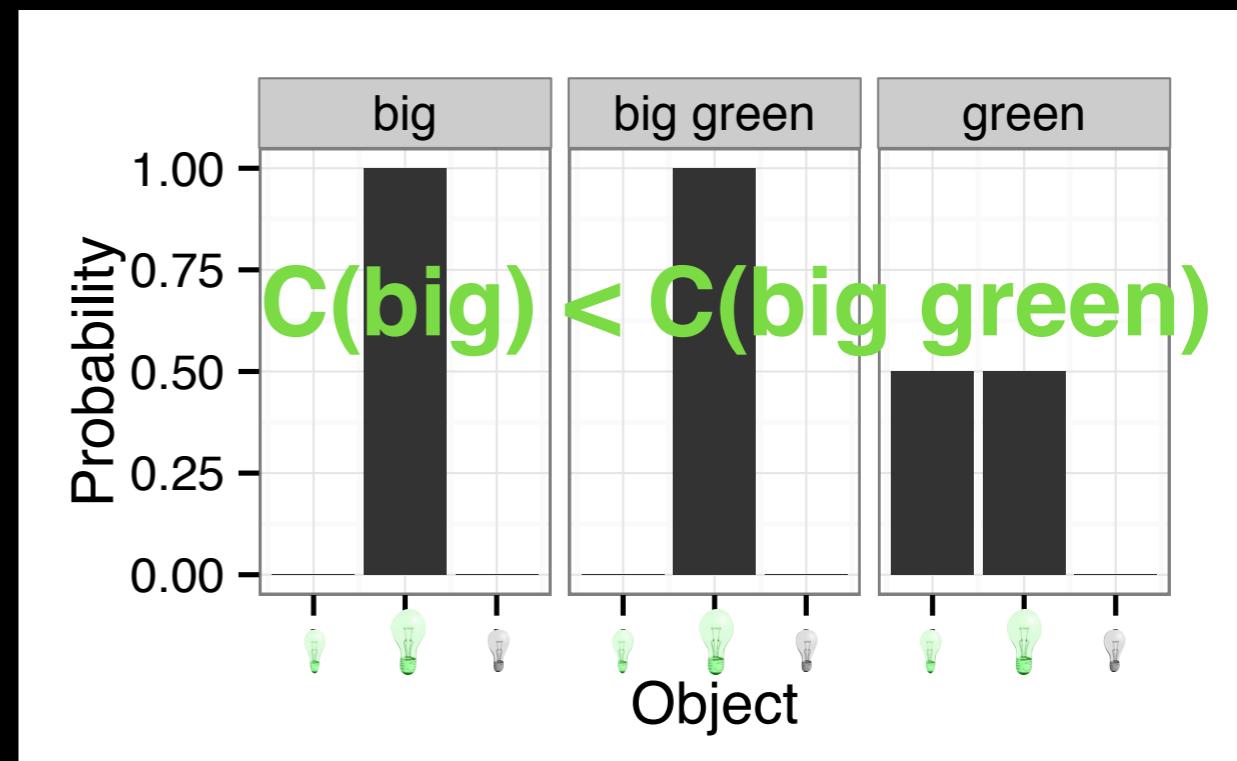
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$$C(u) = C(u_1) + C(u_2)$$

RSA does not produce overinformative REs...

Gatt et al 2013; Westerbeek et al 2015

...with deterministic semantics



# Motivation for non-deterministic semantics?

Modifiers differ:

size adjectives are vague and context-dependent  
in a way that color adjectives are not

Kennedy & McNally 2005

color is intrinsically salient in a way that size is not

Arts et al 2011; Gatt et al 2013

size adjectives are judged to be more subjective  
than color adjectives

Scontras, Degen, & Goodman 2017

# Non-deterministic semantics

## Literal listener

$$P_{L_0}(o|u) \propto \begin{cases} 1 - \epsilon & [[u]](o) = \text{true} \\ \epsilon & \text{otherwise} \end{cases}$$

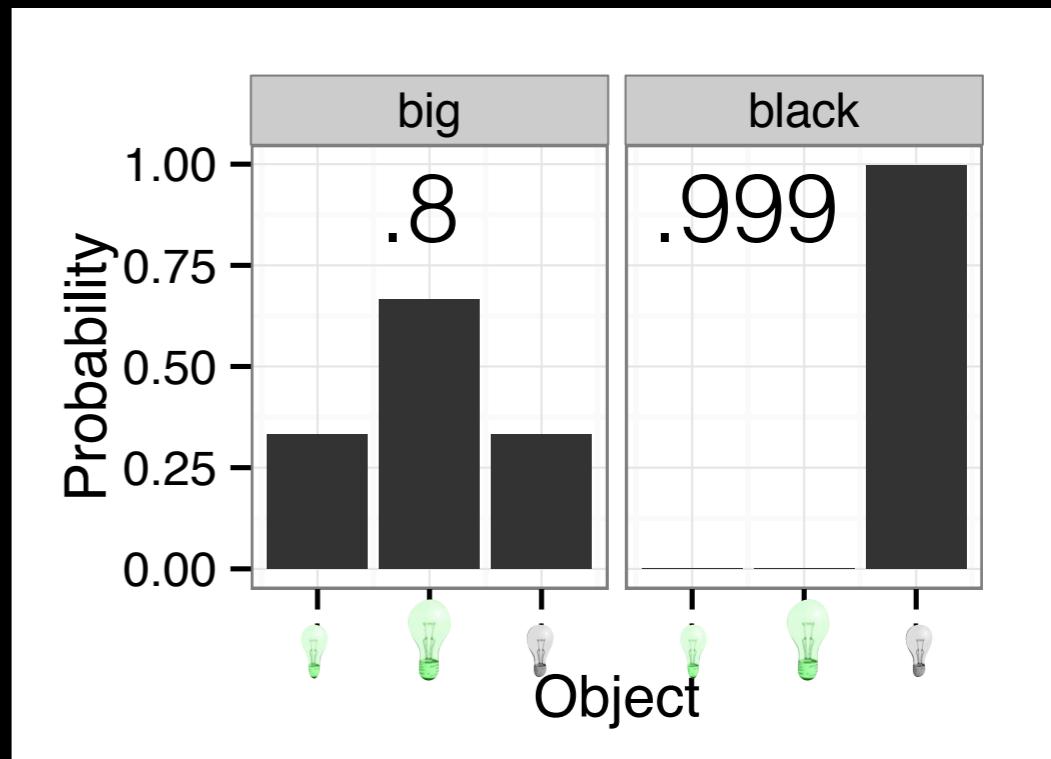
# Non-deterministic semantics

**Literal listener**  **fidelity**

$$P_{L_0}(o|u) \propto \begin{cases} 1 - \epsilon & [[u]](o) = \text{true} \\ \epsilon & \text{otherwise} \end{cases}$$

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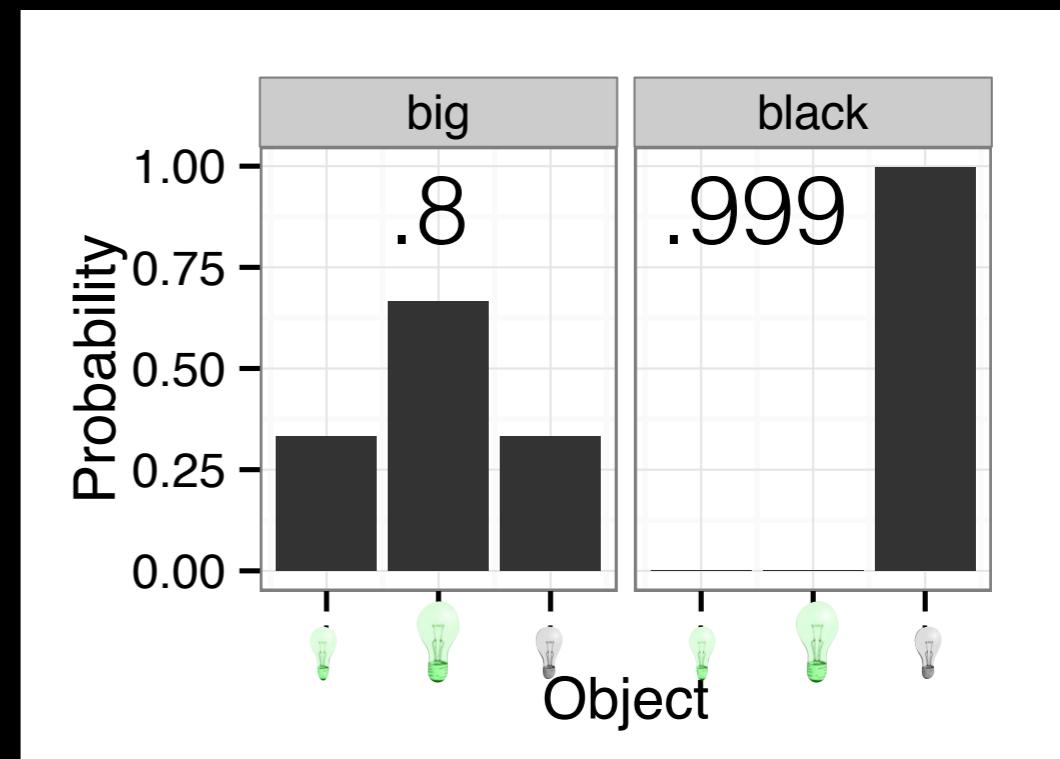
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# Non-deterministic semantics

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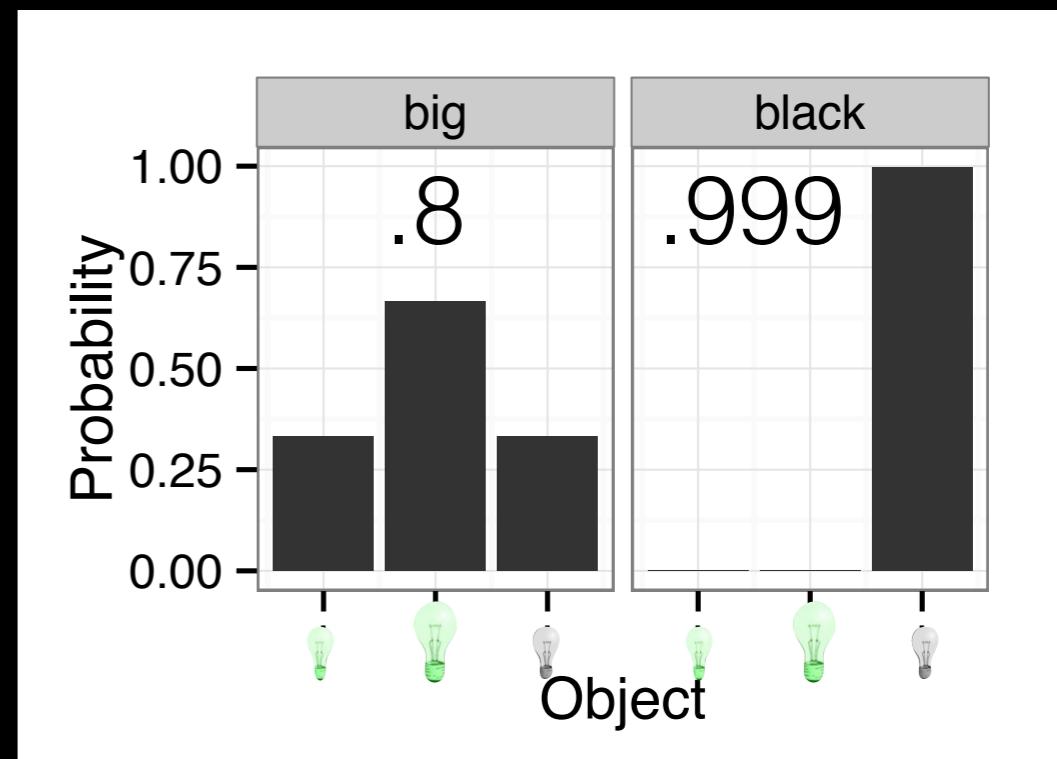
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Two free fidelity parameters:

$\text{fid}(\text{size})$   $\text{fid}(\text{color})$



# Non-deterministic semantics

**Literal listener** 

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**Pragmatic speaker**

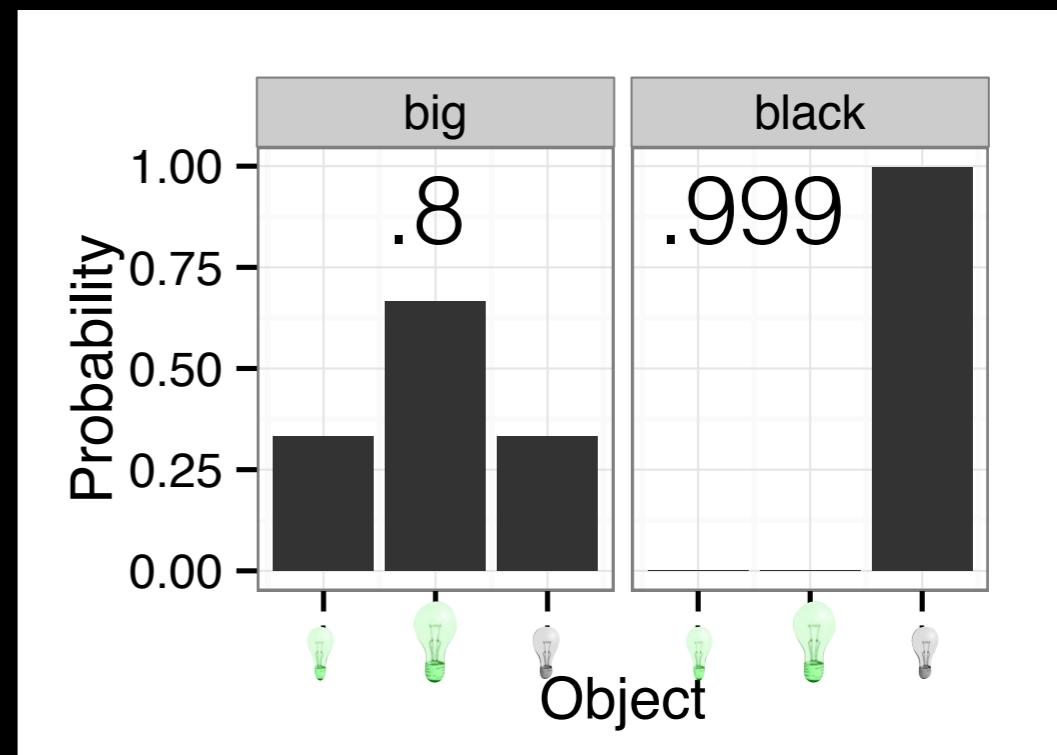
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Two free cost parameters:

$C(\text{size})$   $C(\text{color})$



# Non-deterministic semantics

**Literal listener**

fidelity

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**Pragmatic speaker**

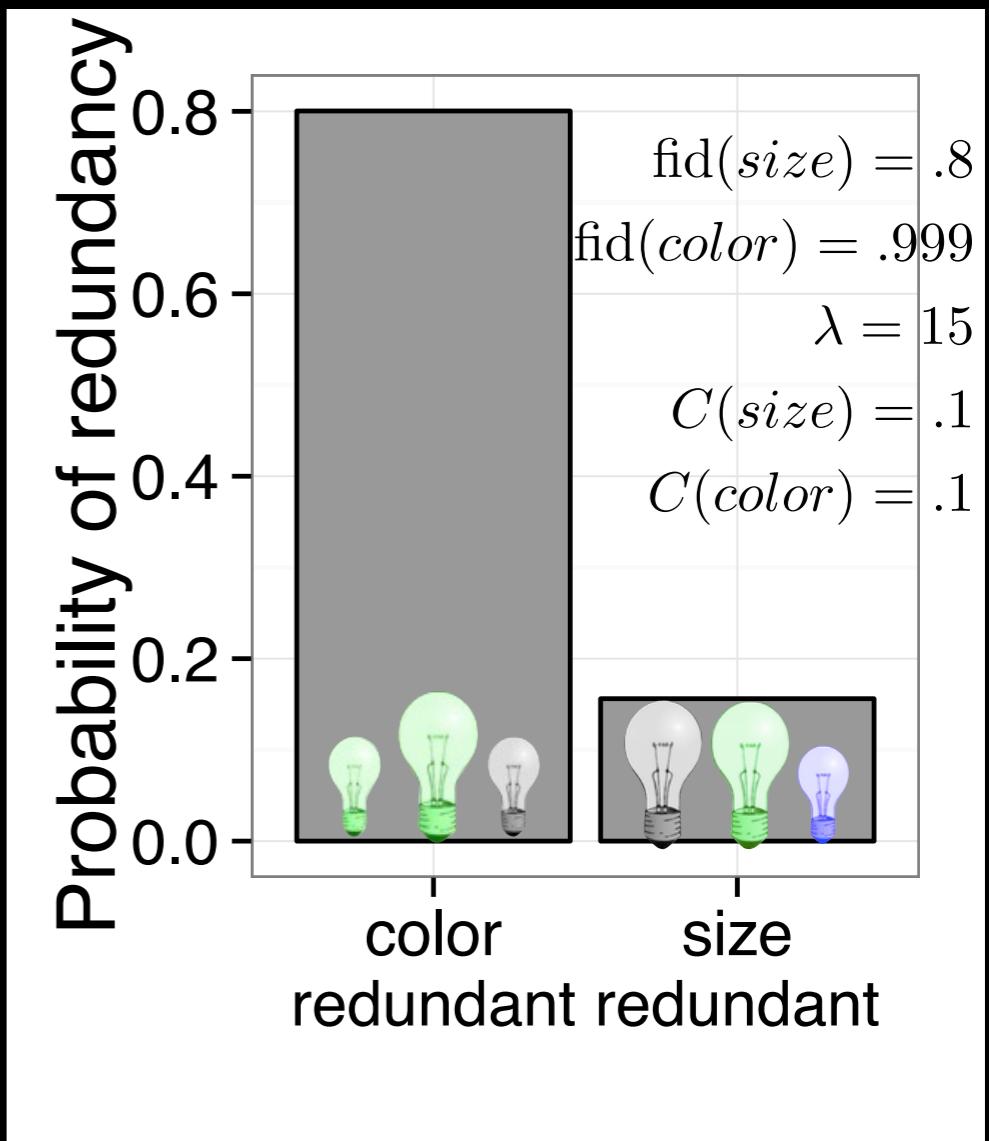
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fidelity

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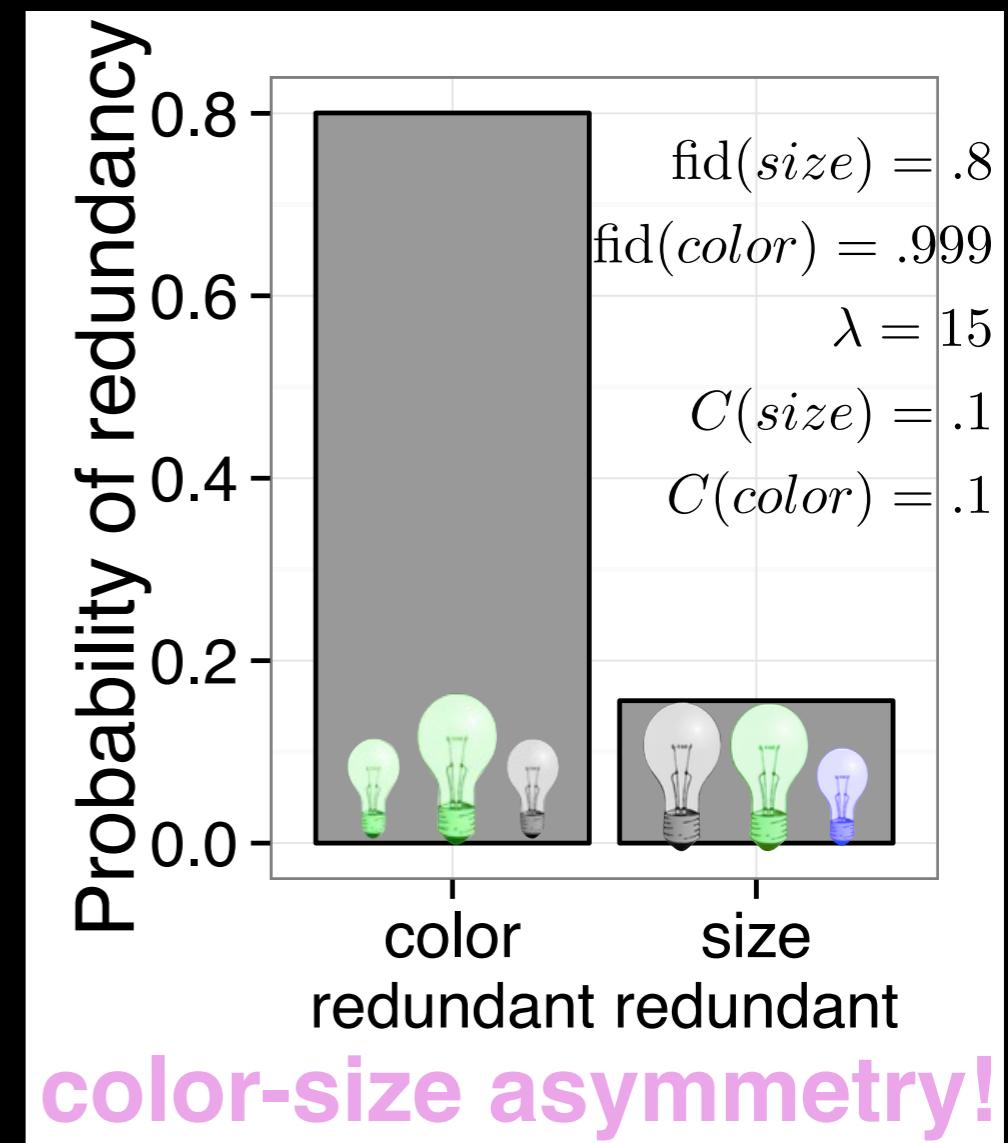
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fidelity

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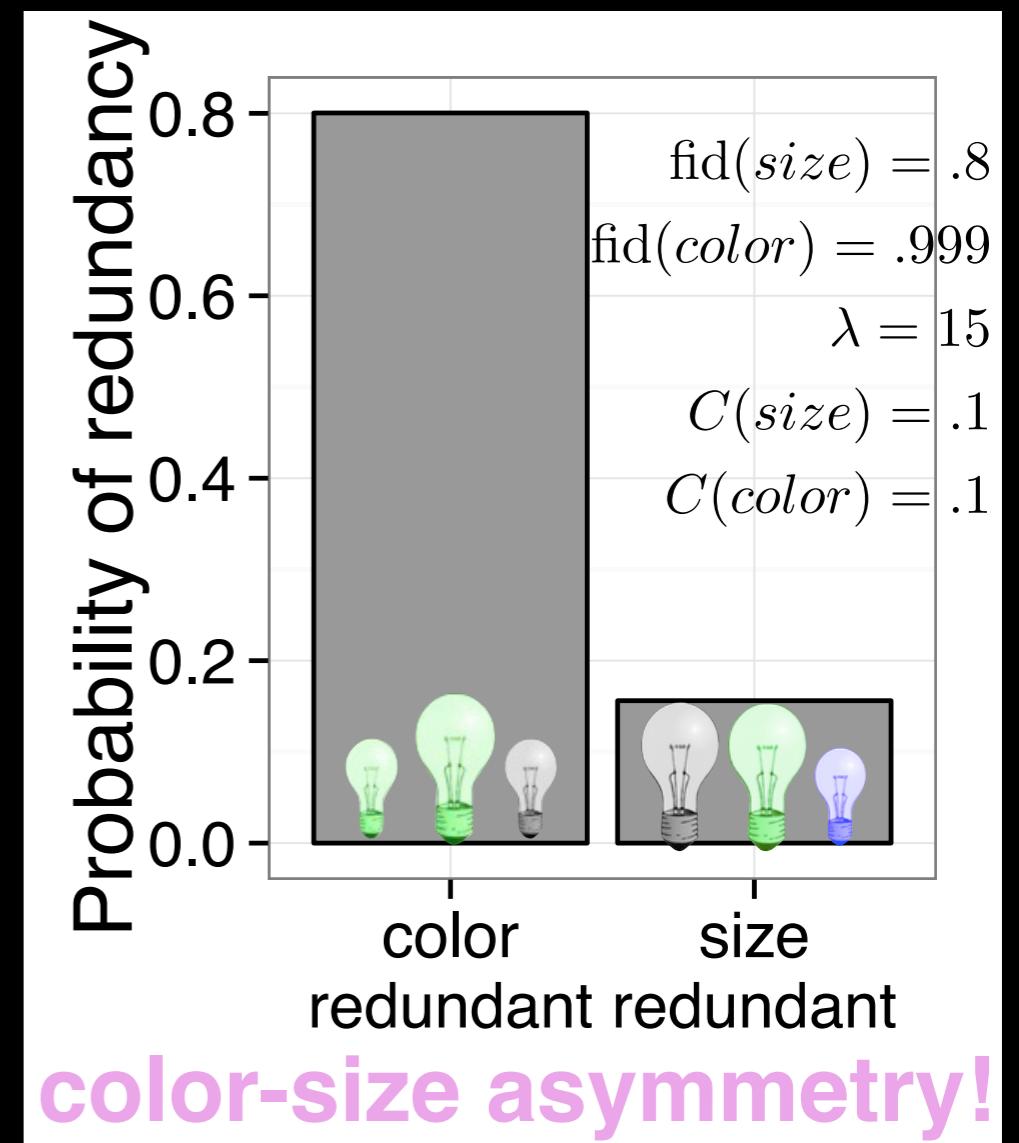
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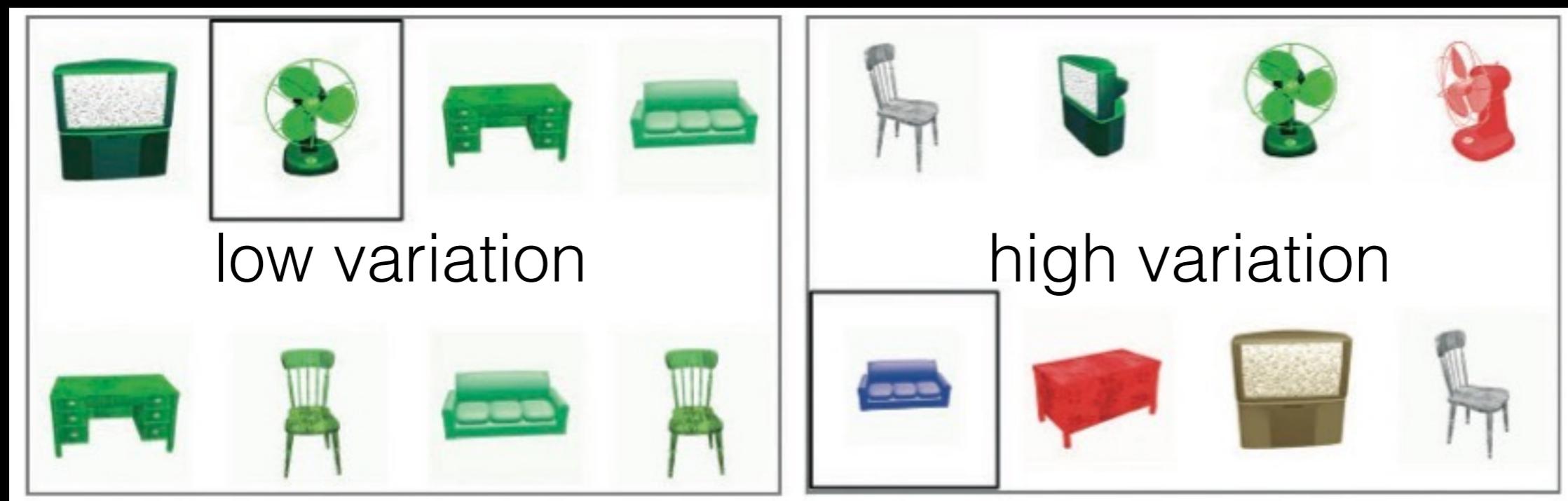
$C(\text{size})$   $C(\text{color})$

If modifiers don't "work perfectly",  
**adding modifiers adds information**



Independent empirical  
evidence for RSA with non-  
deterministic semantics?

# Scene variation



Koolen et al 2013, Davies & Katsos 2013

# Scene variation



more redundant color use in high-variation scenes

Koolen et al 2013, Davies & Katsos 2013

# Scene variation



more redundant color use in high-variation scenes

Koolen et al 2013, Davies & Katsos 2013

non-deterministic RSA predicts this result

Independent  
**quantitative** evidence  
for non-deterministic  
RSA?

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scene variation increases probability of redundancy

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$$\frac{n_{\text{diff}}}{n_{\text{total}}}$$

proportion of total distractors that don't share target value on insufficient dimension



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proportion of total distractors that don't share target value on insufficient dimension



sufficient dimension: size

insufficient dimension: color

$$\frac{n_{\text{red}}}{n_{\text{total}}} = \frac{2}{4} = .5$$

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scene variation increases probability of redundancy

$$\frac{n_{\text{diff}}}{n_{\text{total}}}$$

proportion of total distractors that don't share target value on insufficient dimension



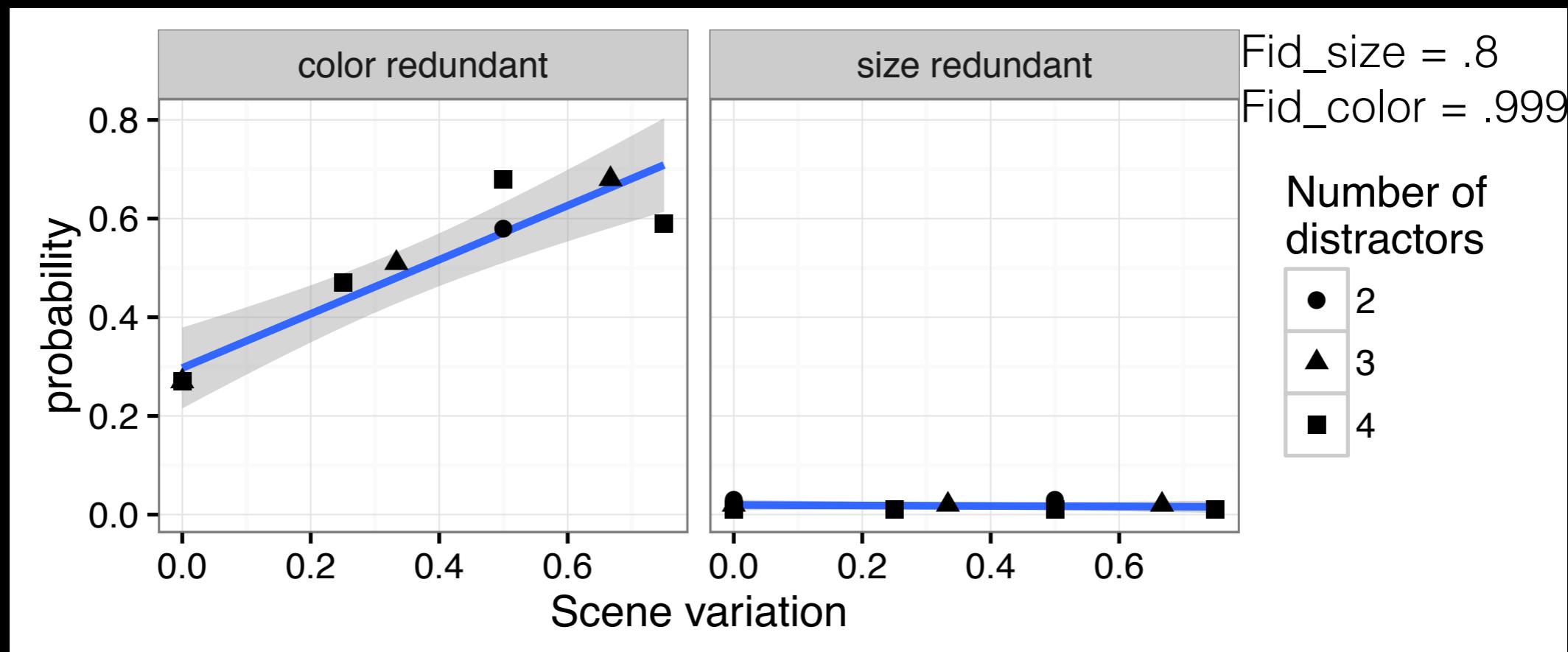
sufficient dimension: size

insufficient dimension: color

$$\frac{n_{\text{red}}}{n_{\text{total}}} = \frac{2}{4} = .5$$

greater proportion = more variation

# Model predictions



Prediction: increase in redundant adjective use with increasing scene variation for color but not size

# Interactive reference game experiment

- 58 pairs of participants on Mechanical Turk
- random assignment to speaker/listener role
- 72 trials (half targets, half fillers)
- 36 object types
- on all target trials, one of size or color was sufficient
- **scene variation manipulation:**
  - total number of distractors (2, 3, 4)
  - number of distractors that shared the insufficient feature value with target

# Speaker's perspective

You: the stapler

listener: which one??

You: big purple

Round 1 of  
72

|

Send



# Listener's perspective

speaker: the stapler

You: which one??

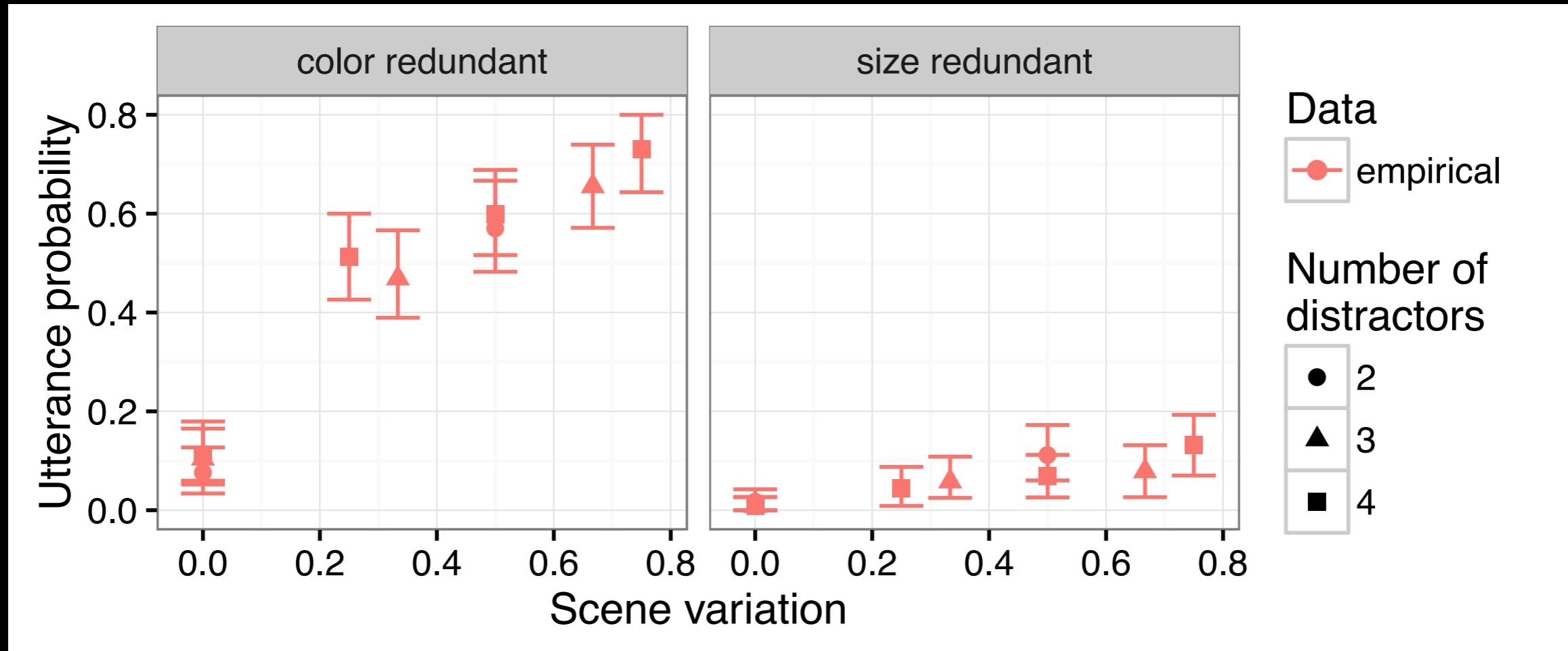
speaker: big purple

Round 1 of  
72

Send

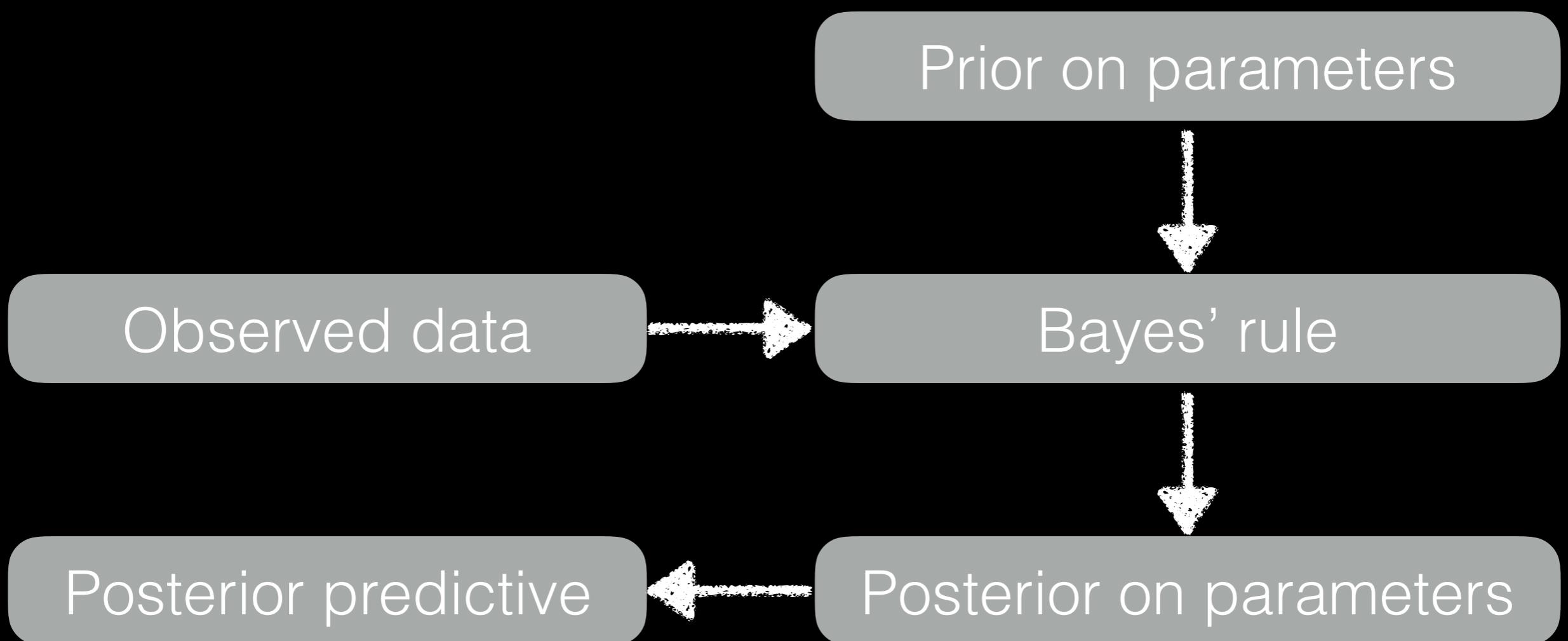


# Results

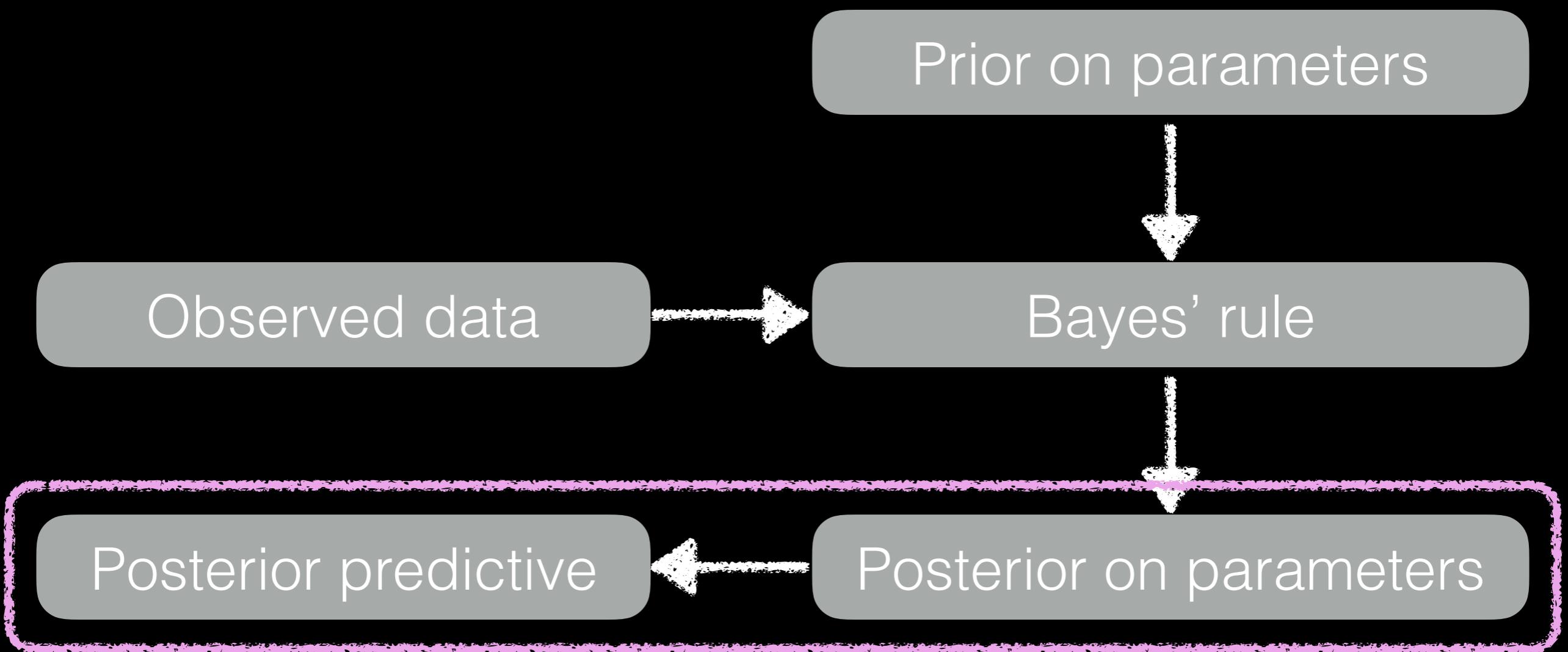


1. more redundant adjective use with greater scene variation
2. greater effect of scene variation for color than size

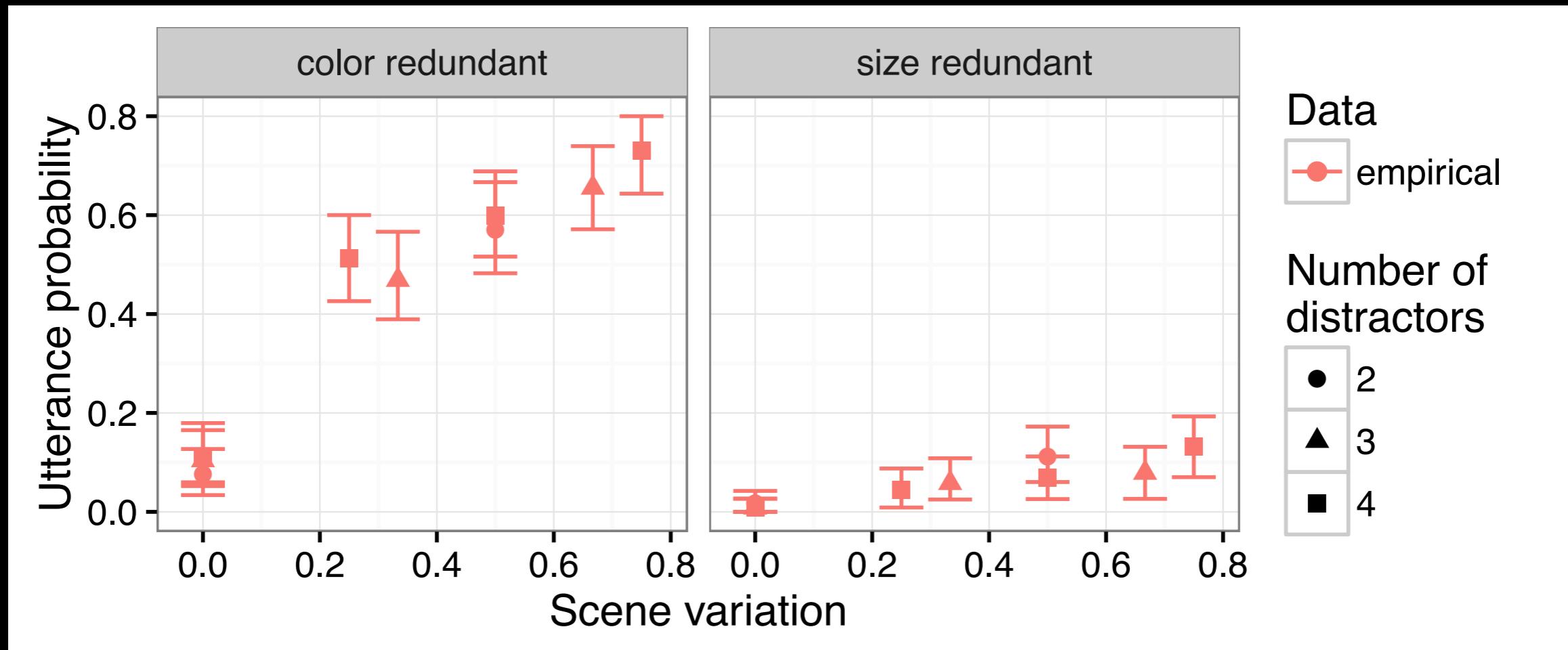
# Bayesian data analysis



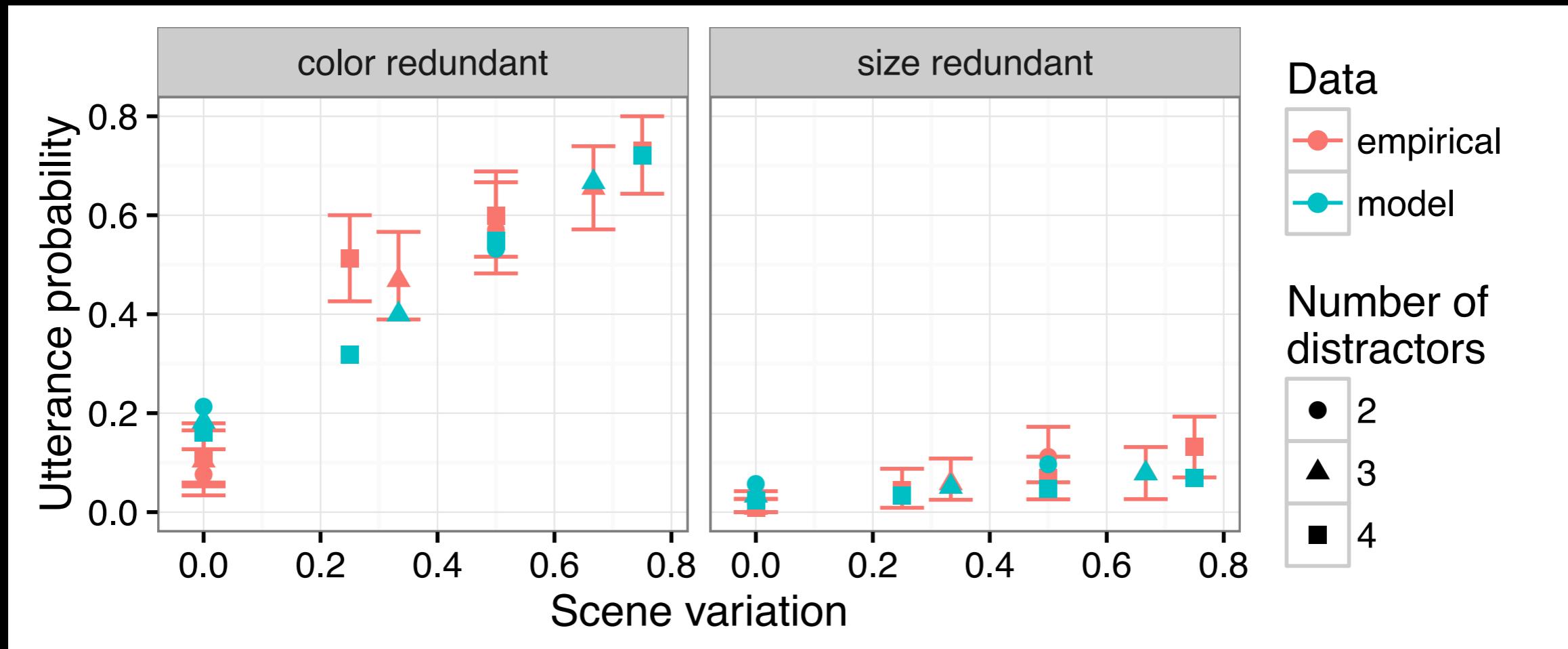
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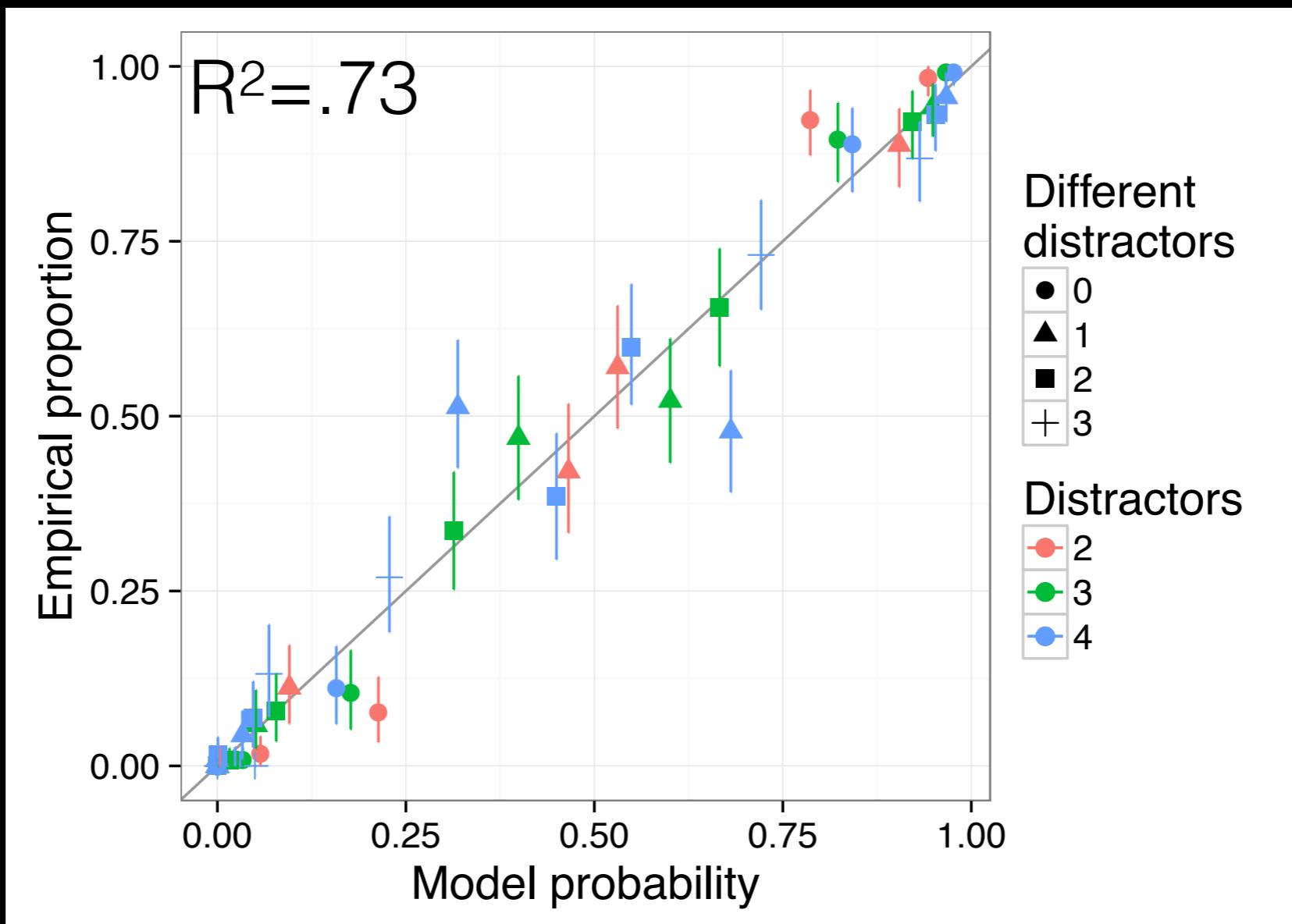
# Results



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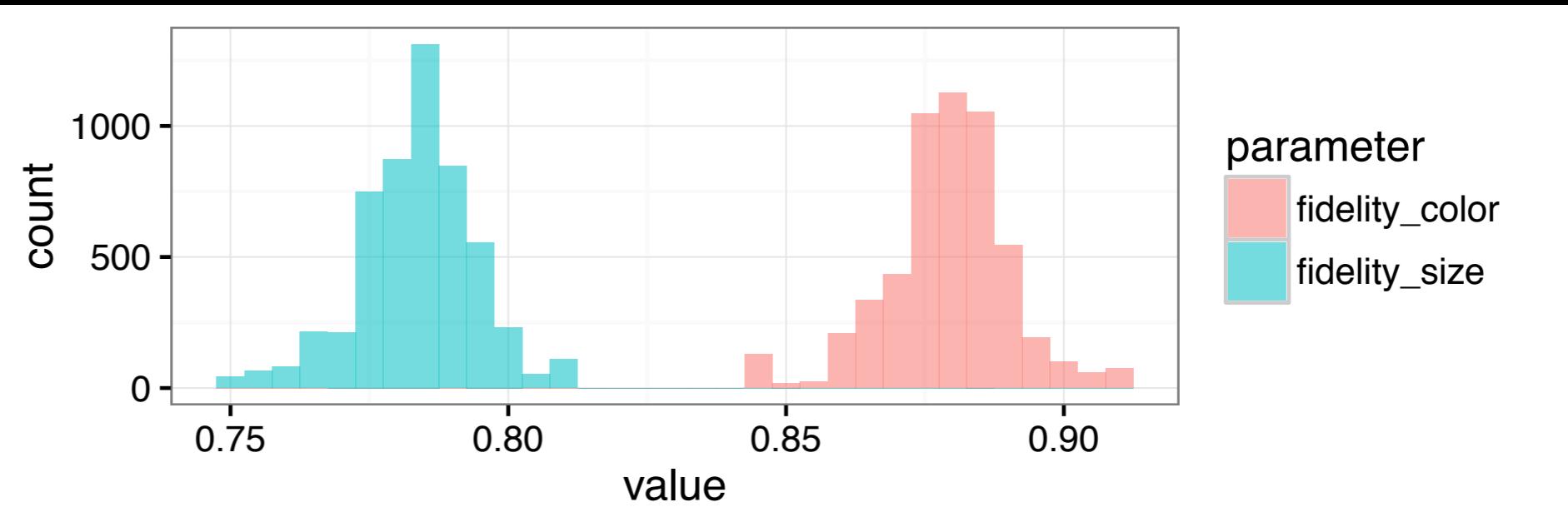


# Model fit

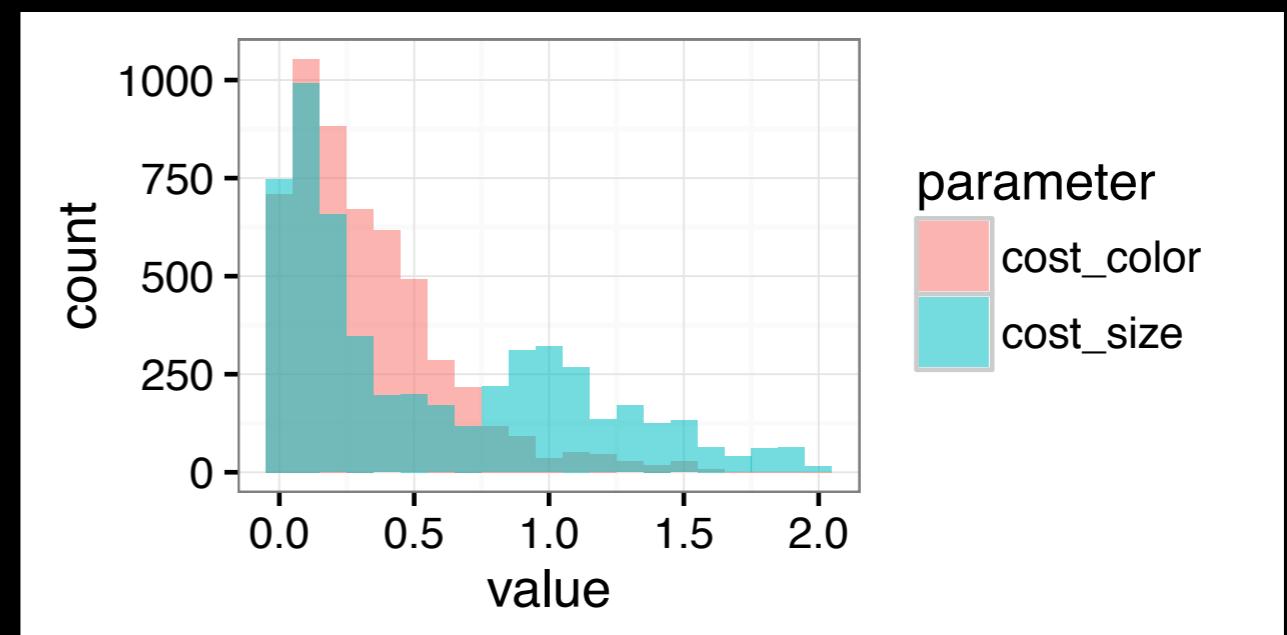


# Posteriors over parameters

**Fidelity:**  
inferred size  
fidelity lower  
than inferred  
color fidelity



**Cost:**  
inferred size and  
color costs similar  
(with tendency  
towards costlier size)



# Interim summary

if modifiers are noisy, adding modifiers adds utility

RSA with noisy truth functions captures this:

overinformative referring expressions

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**rationally redundant referring expressions**

level of reference



Graf et al 2016; Degen et al under review

typicality effects



Degen et al under review

# Part II

---

Comprehension of scalar  
expressions

# Scalar implicature

(1) John: Why is Ann happy?

Mary: She found some of her marbles.

**Inference:** Ann found **some**, but not **all** her marbles.

**Generalization** Grice 1975; Horn 1972, 2004

By uttering the **weaker** alternative from a scale of a **weaker** and a **stronger** alternative, the speaker implicates the negation of the **stronger** alternative.

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**Pragmatic interpretation**

...some, but not all...

**Literal interpretation**

...some, and possibly all...

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**"UNDERINFORMATIVENESS"**

# RSA for scalar implicature

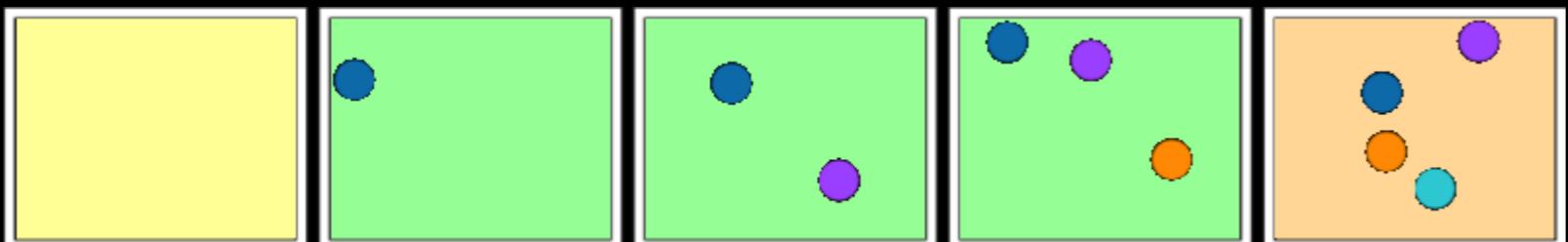
$$M = \{m_{\neg \exists}, m_{\exists \neg \forall}, m_{\forall}\}$$

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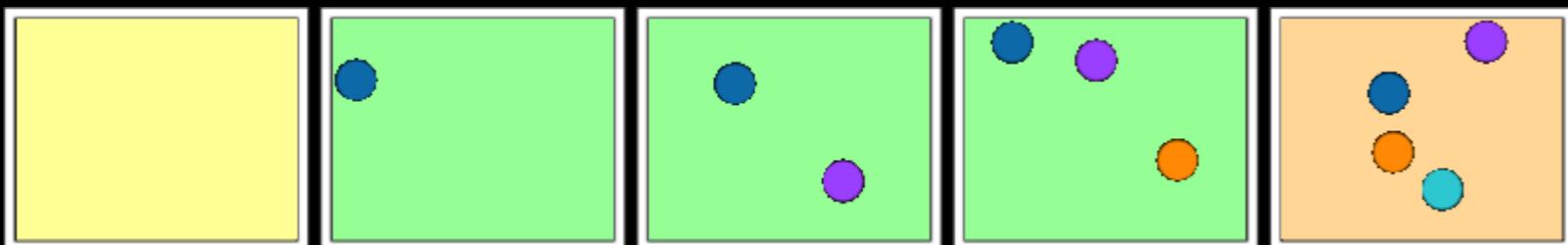


*Ann found some of her marbles*

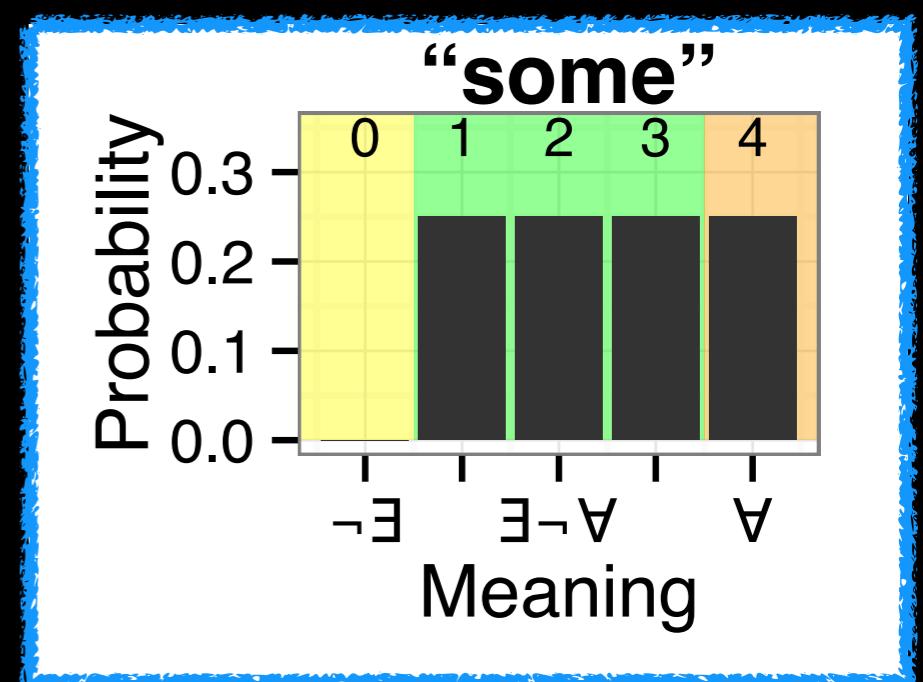
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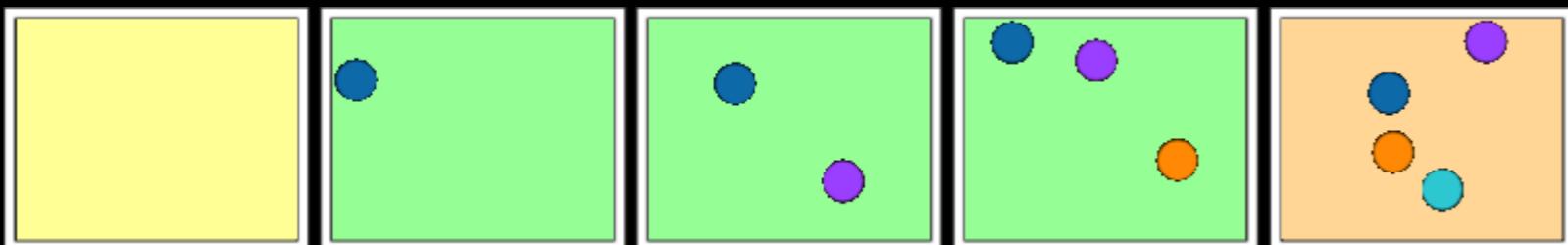


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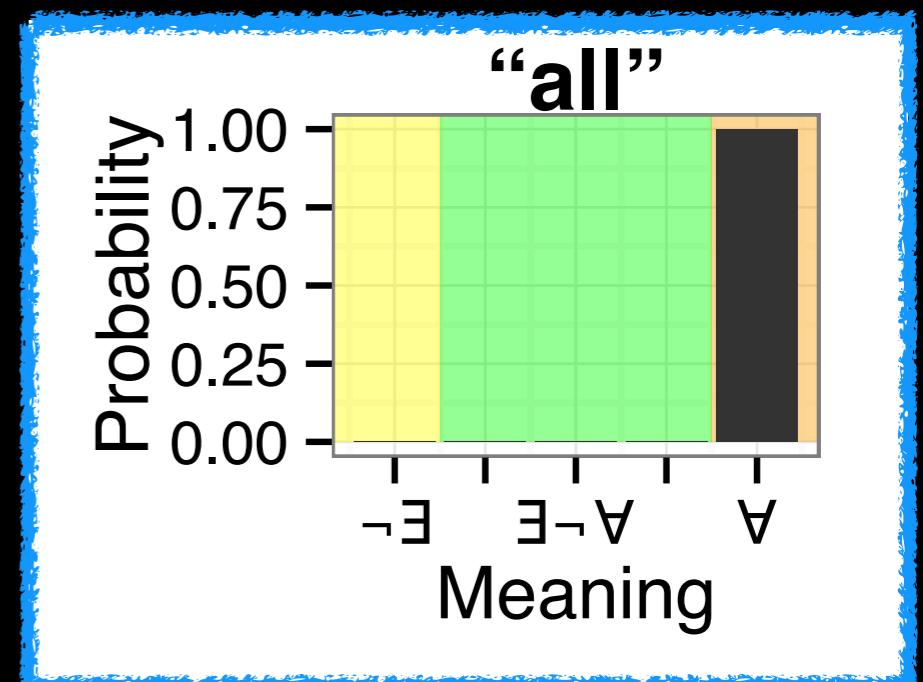
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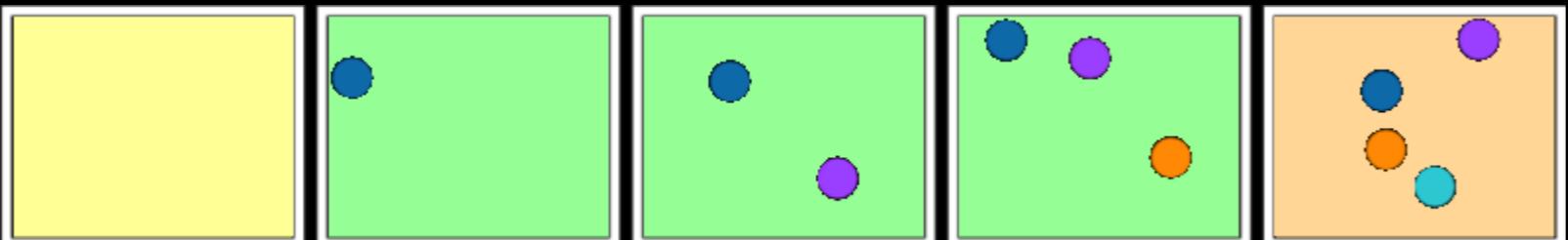
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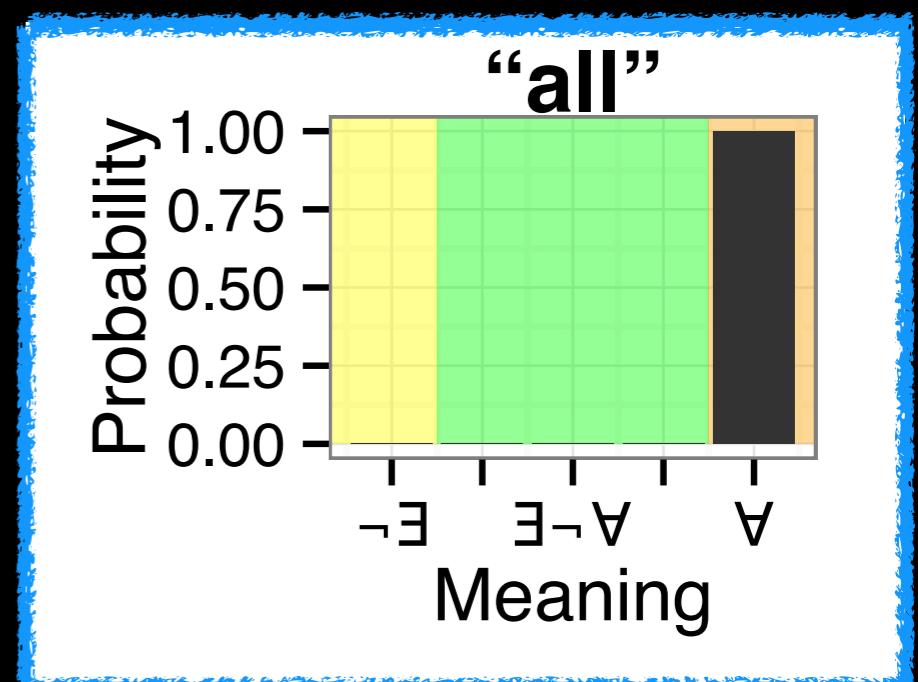
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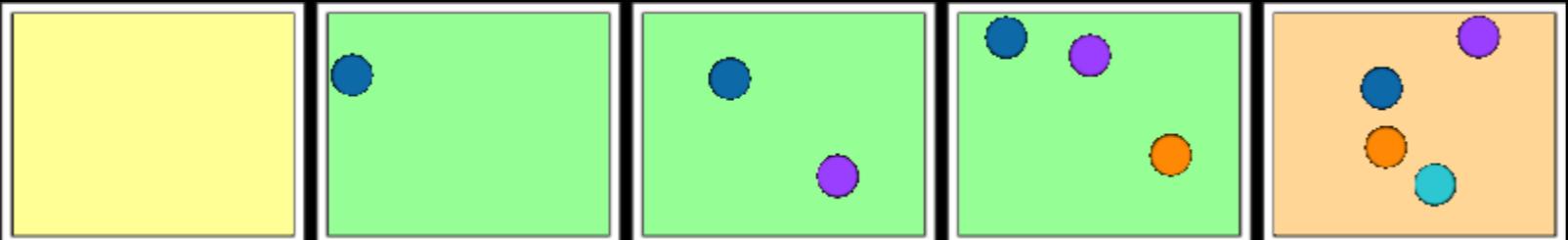
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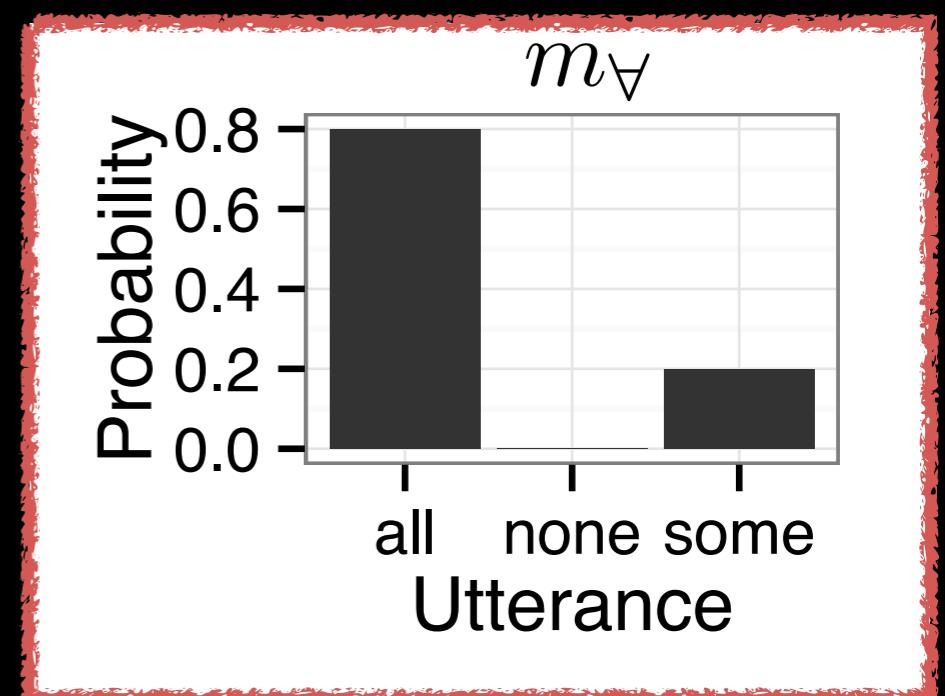
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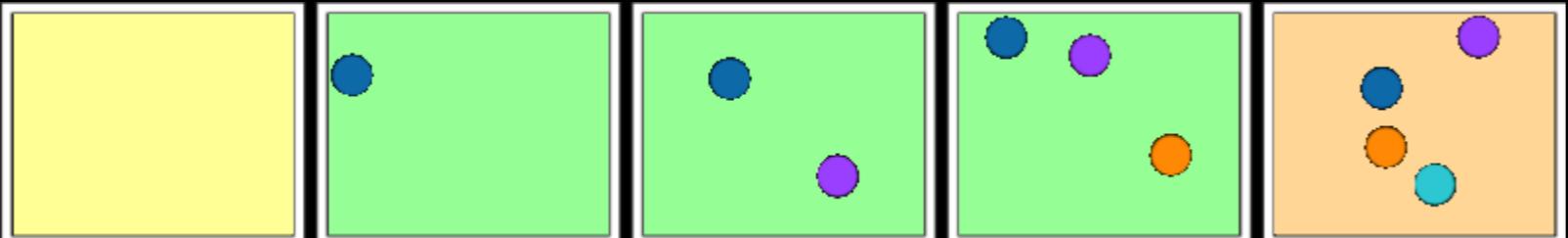
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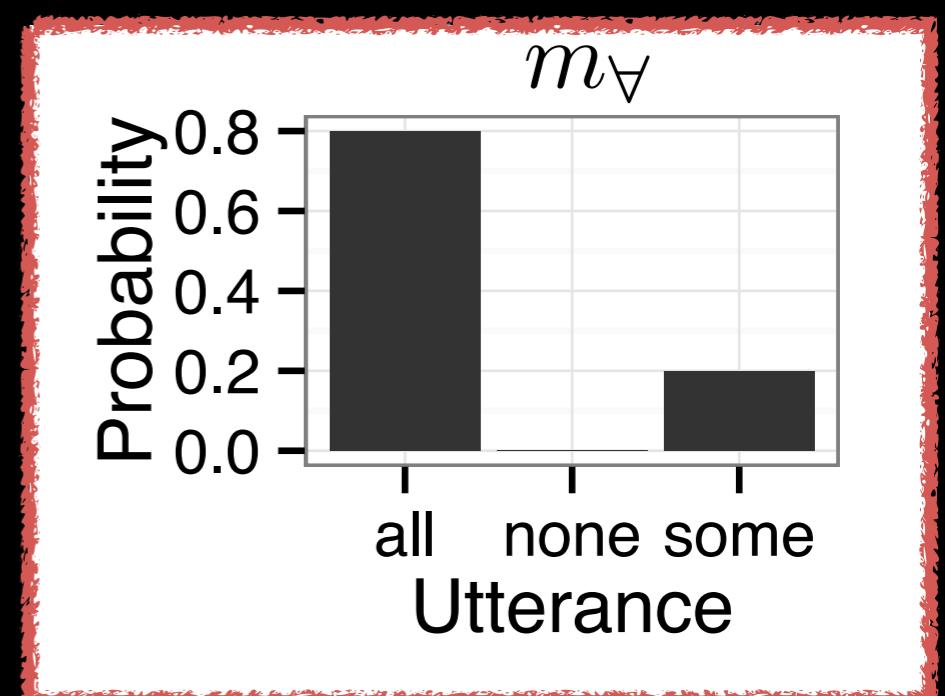
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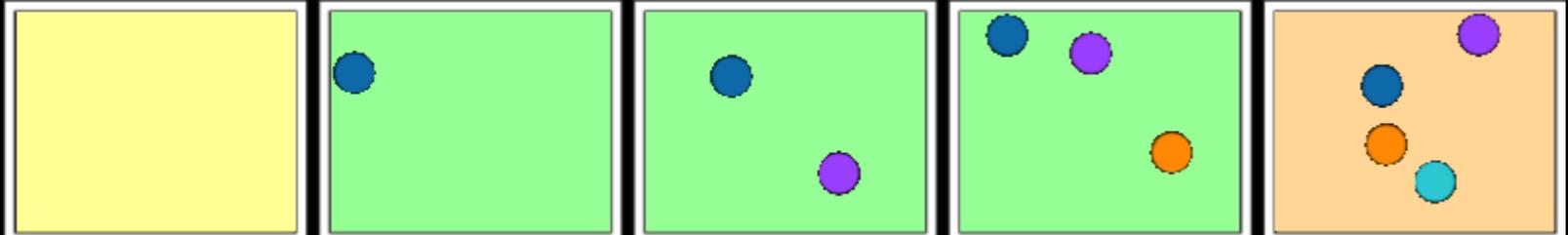
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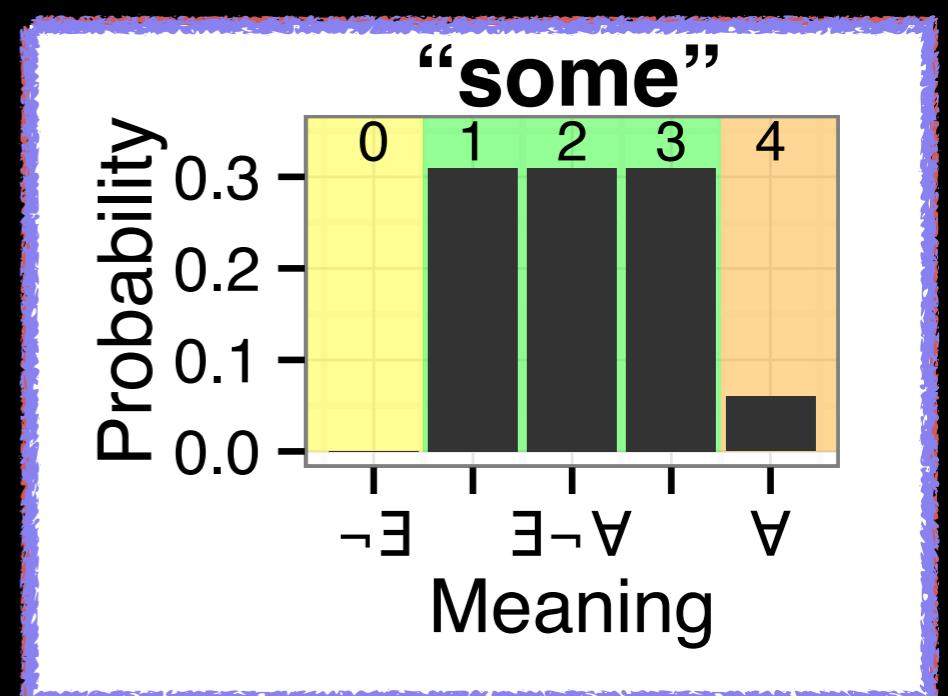
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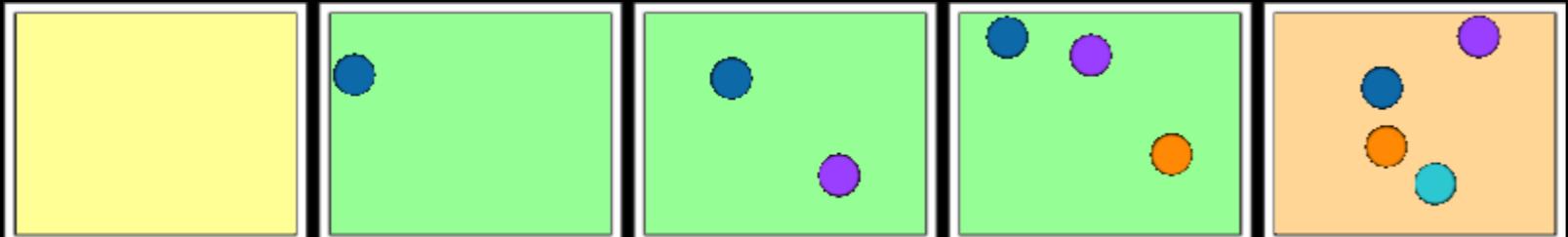
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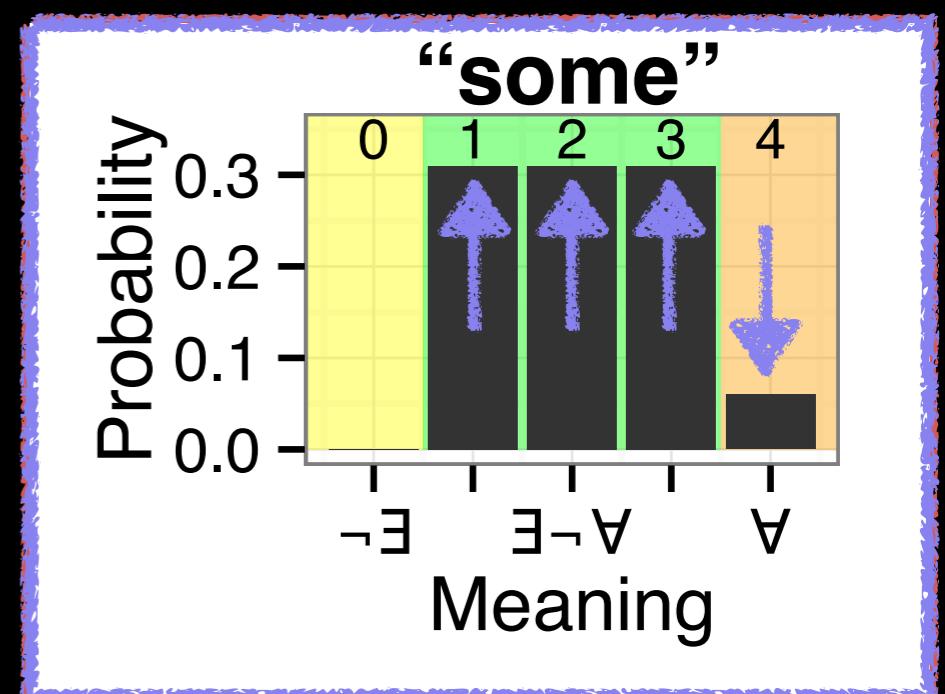
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# Context in scalar implicature

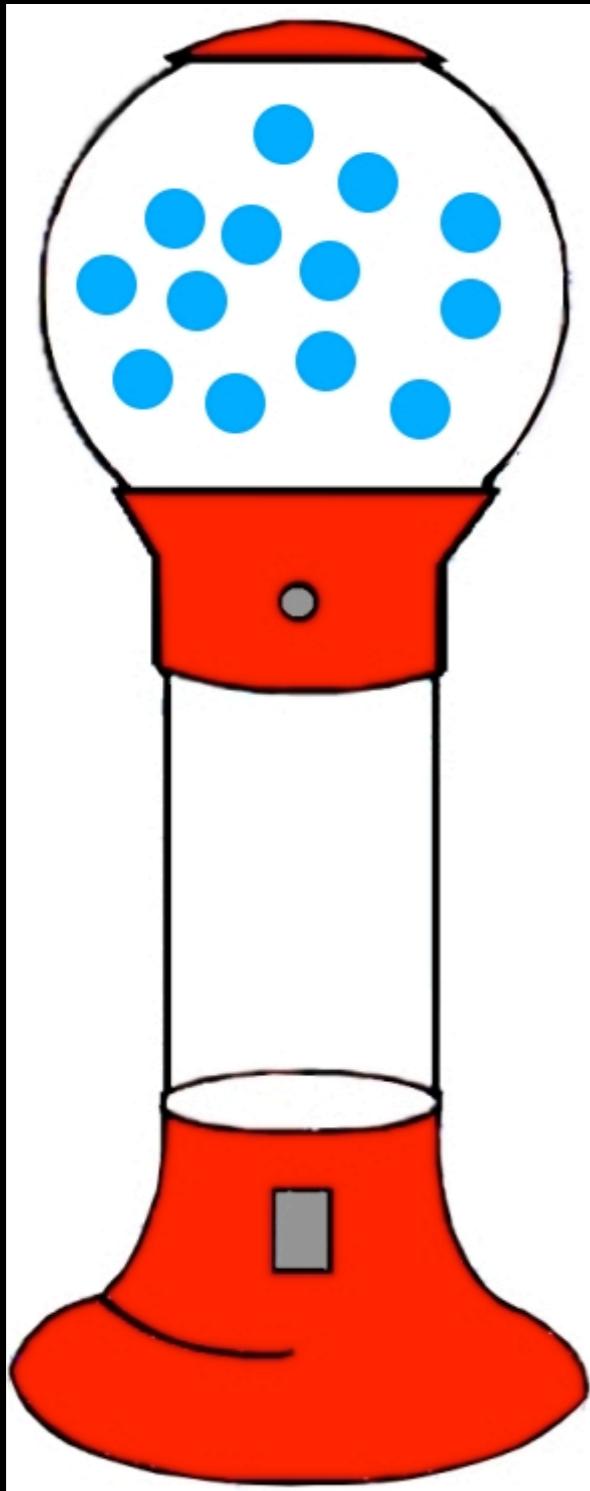
- pragmatic factors:
  - world knowledge/prior beliefs Degen et al 2015; Javangula & Degen in prep
  - speaker knowledge Bergen & Grodner 2012; Goodman & Stuhlmüller 2013; Breheny et al 2013
  - utterance alternatives Degen & Tanenhaus 2015; 2016; Rees & Bott 2018; Bott & Chemla 2016
  - conversational goal / Question Under Discussion (QUD) Zondervan 2010; Degen 2013; Degen & Goodman 2014
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# Number alternatives in processing “some”

Degen & Tanenhaus 2015

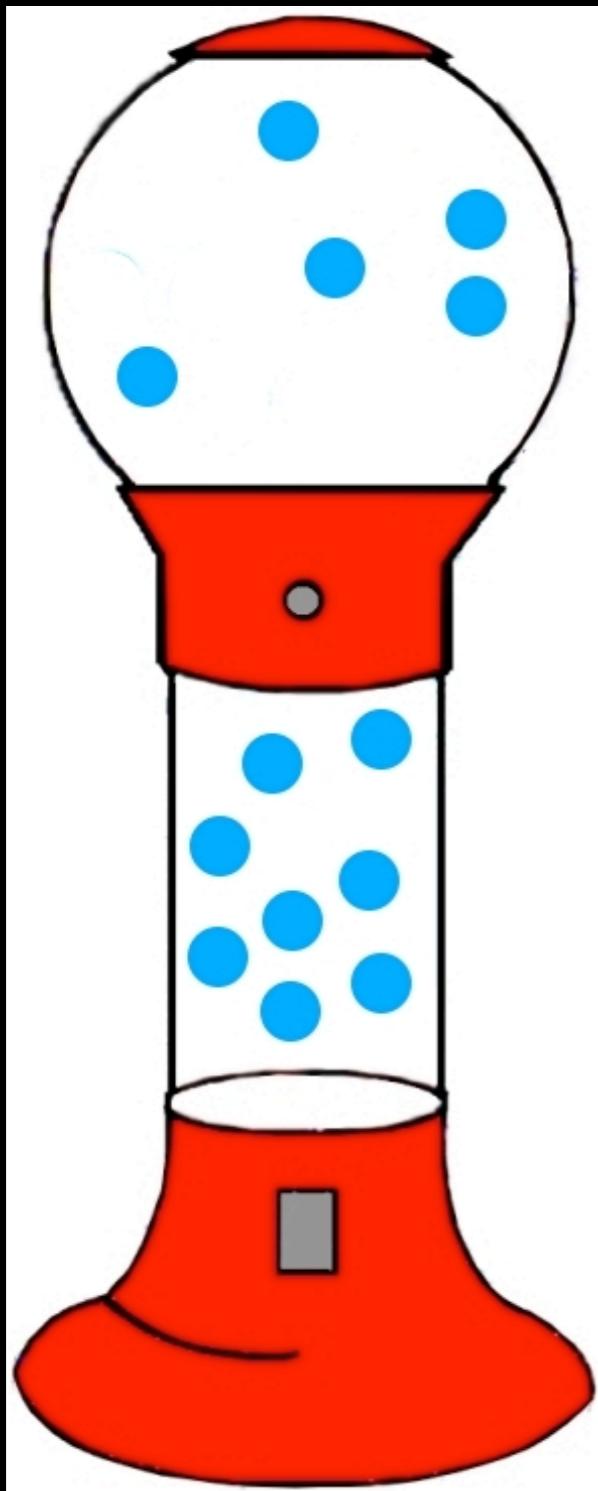


## Naturalness ratings

- Do listeners have **expectations** about use of *some*?  $P(\text{some} | M)$
- Do expectations depend on the contextual availability of **number alternatives**?  $P(\text{some} | M, C)$

# Number alternatives in processing “some”

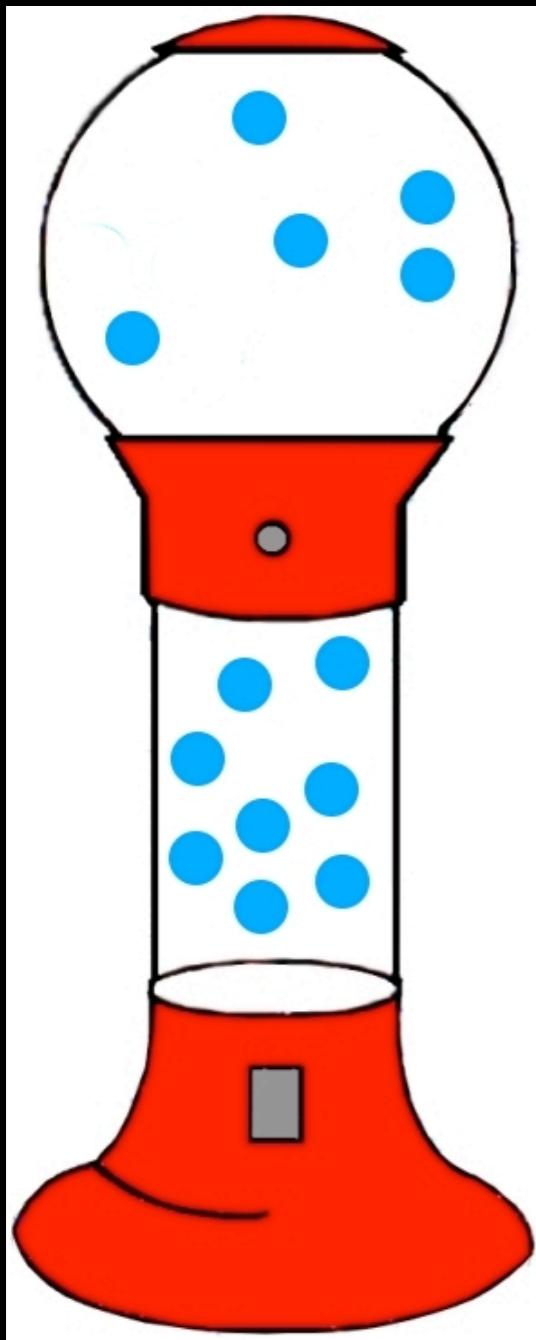
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# The gumball paradigm



*You got some of the gumballs*

How natural was the statement as a description of the scene?

Very unnatural      Very natural

1      2      3      4      5      6      7

**FALSE**

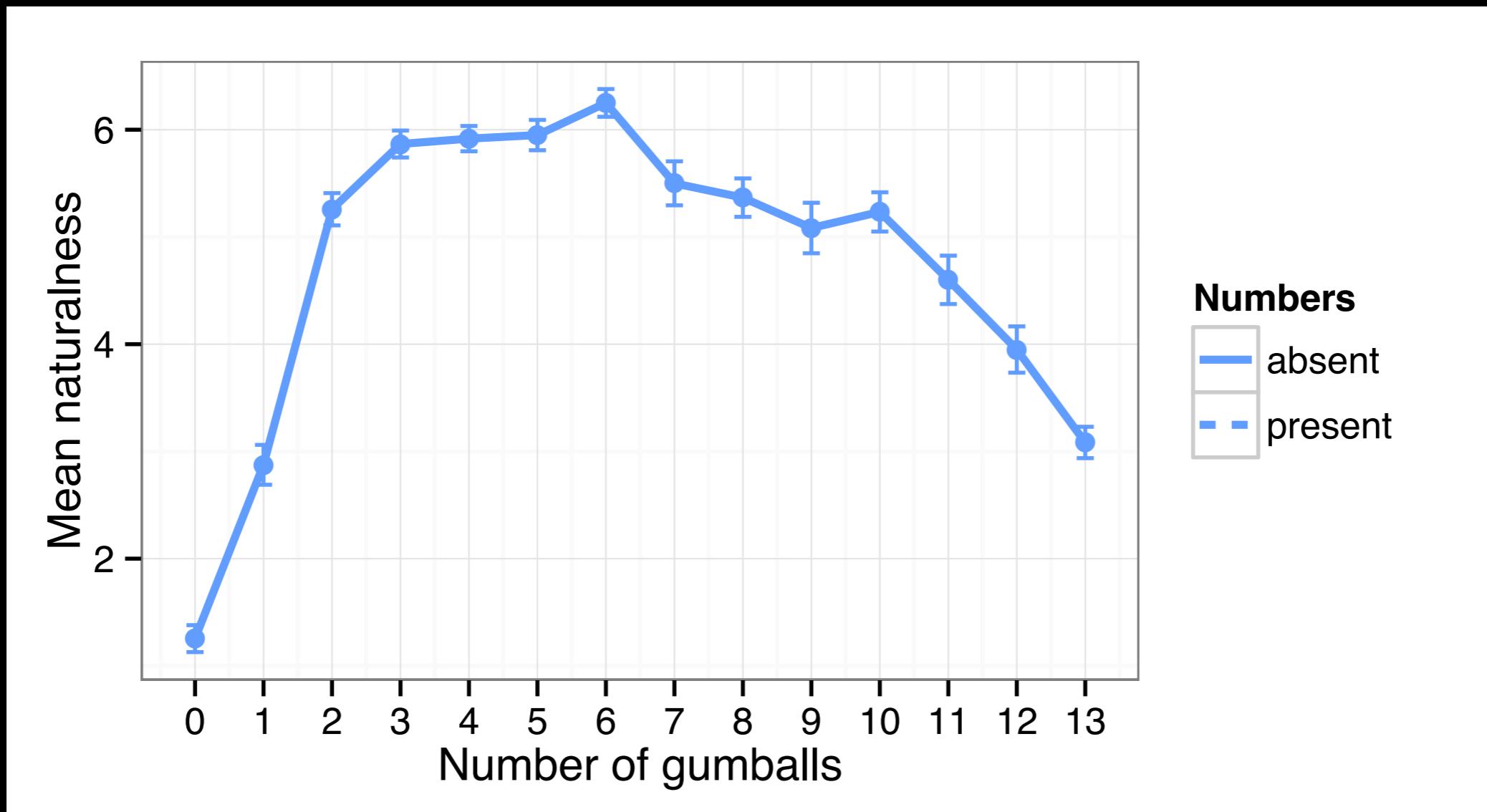
360 participants on MTurk

Independent variables:

- set size in lower chamber: 0 - 13
- quantifier: *some*, *all*, *none*, (*one*, *two*, ...)
- presence of number terms

# Expectations of use for *some*

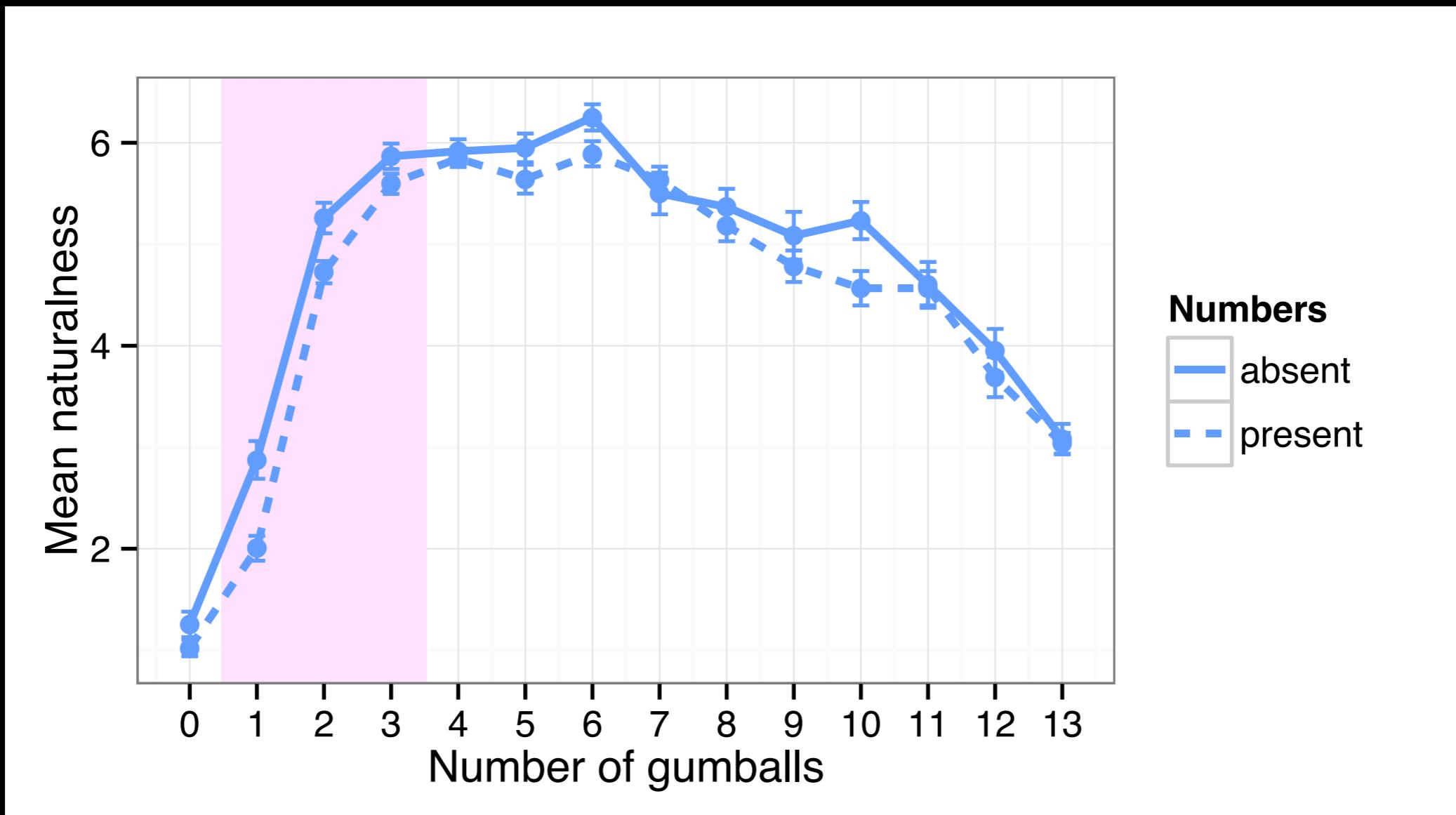
cf van Tiel 2014



*some* is a dispreferred alternative for small sets ( $p < .0001$ )

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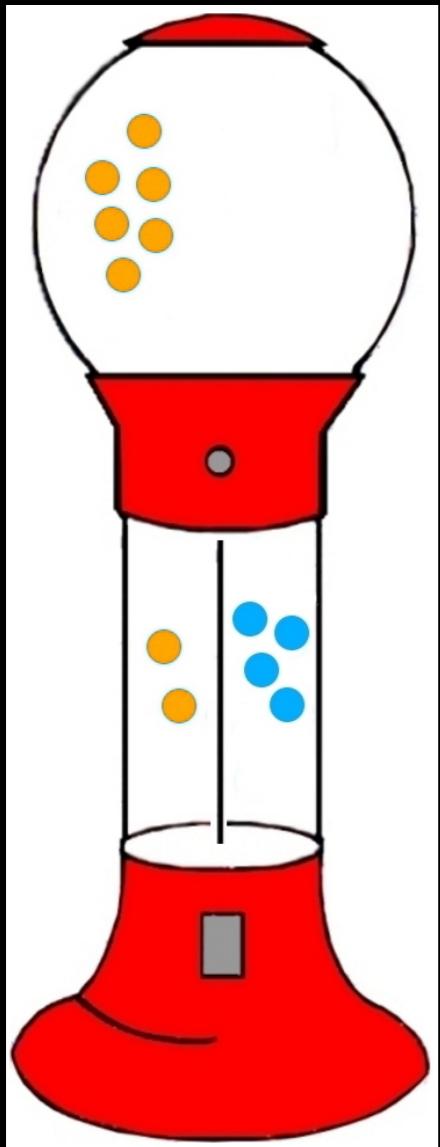
cf van Tiel 2014



*some* is a dispreferred alternative for small sets ( $p < .0001$ )  
especially when numbers are available alternatives ( $p < .01$ )

# Processing alternatives online

Degen & Tanenhaus 2016



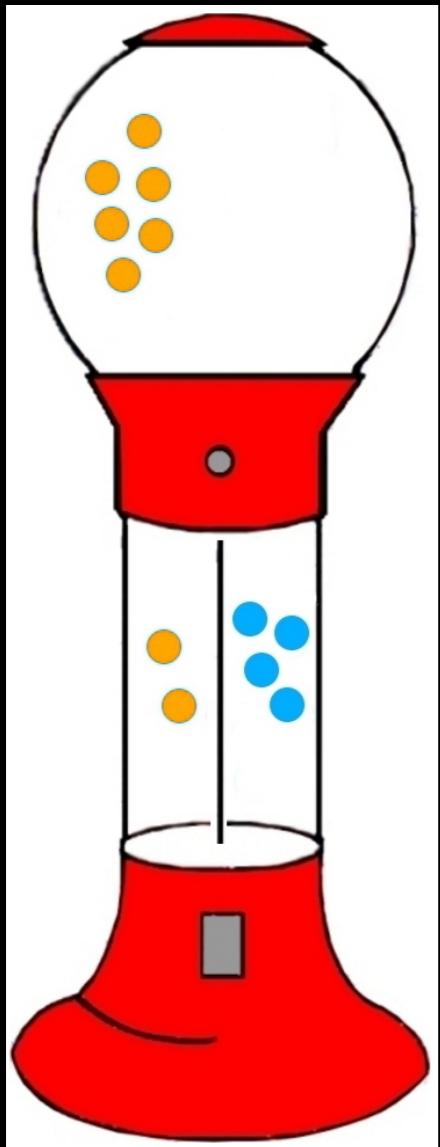
You got some of the orange gumballs

# Processing alternatives online

Degen & Tanenhaus 2016

**absent:** *some/all*

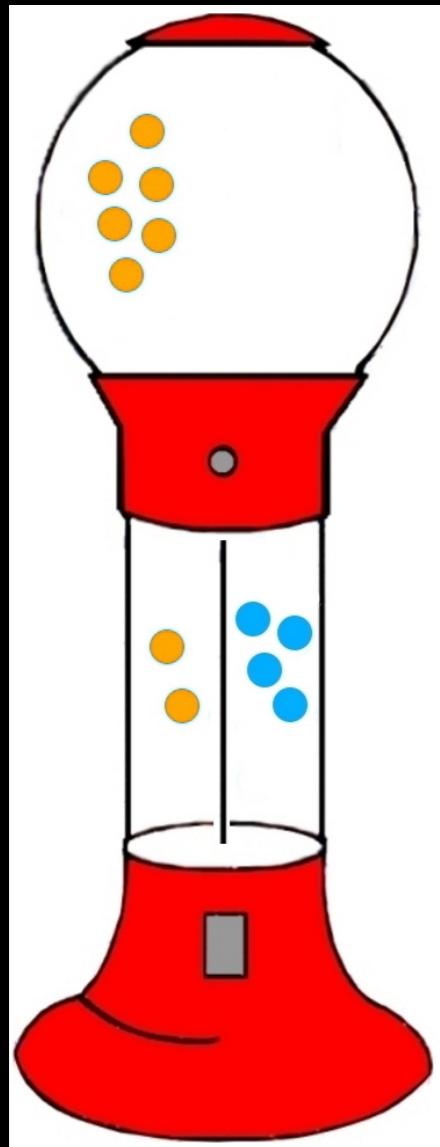
**present:** *some/all/two/three/four/five*



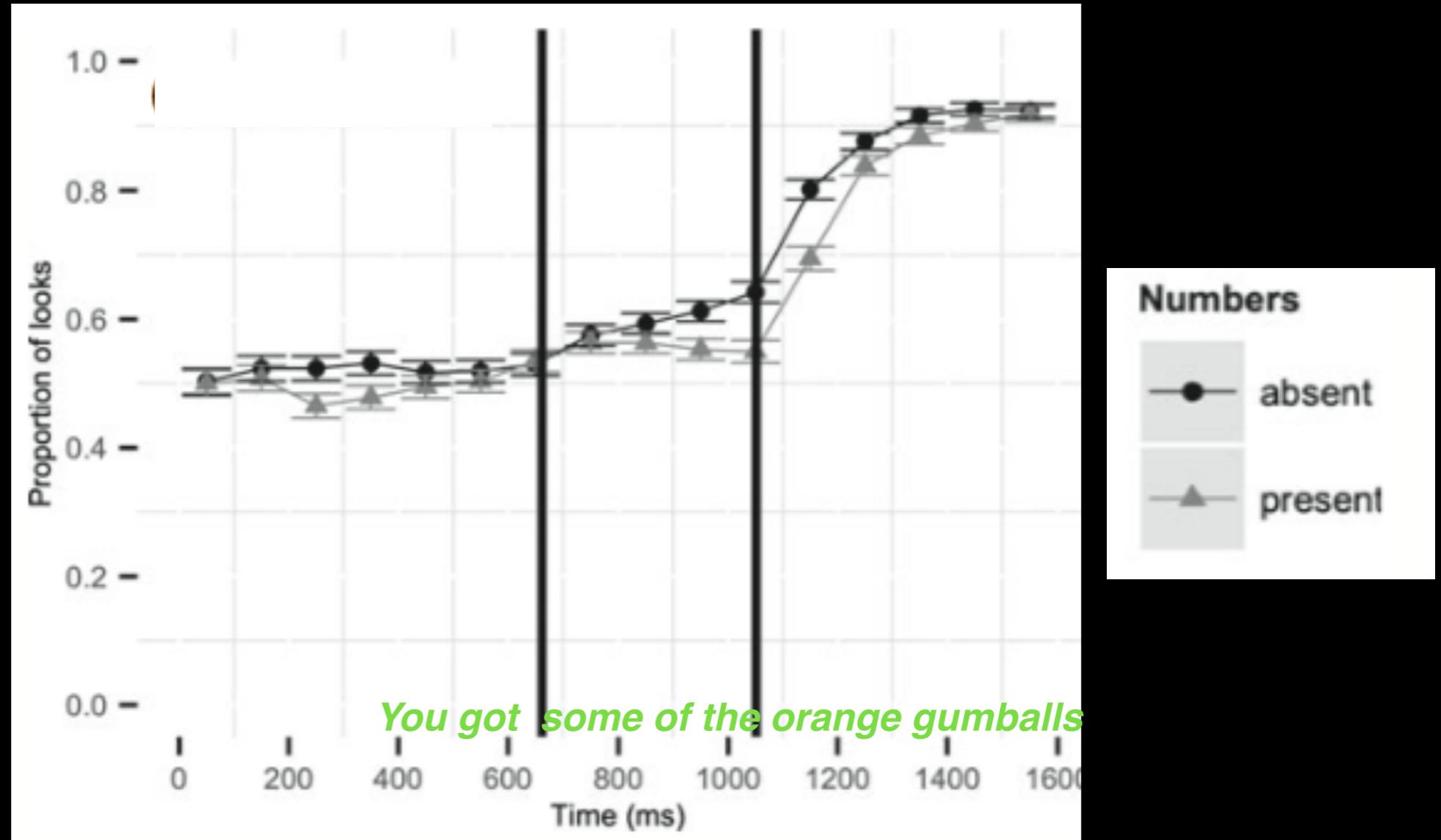
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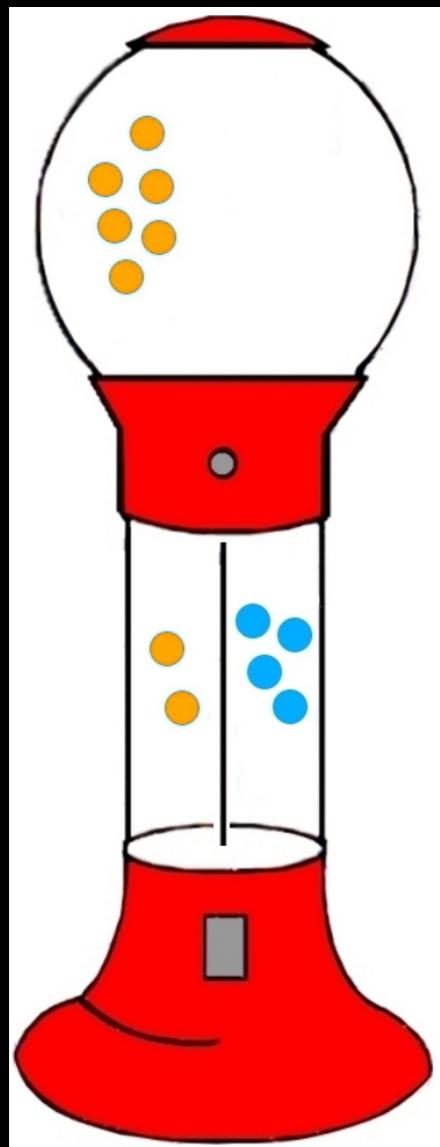
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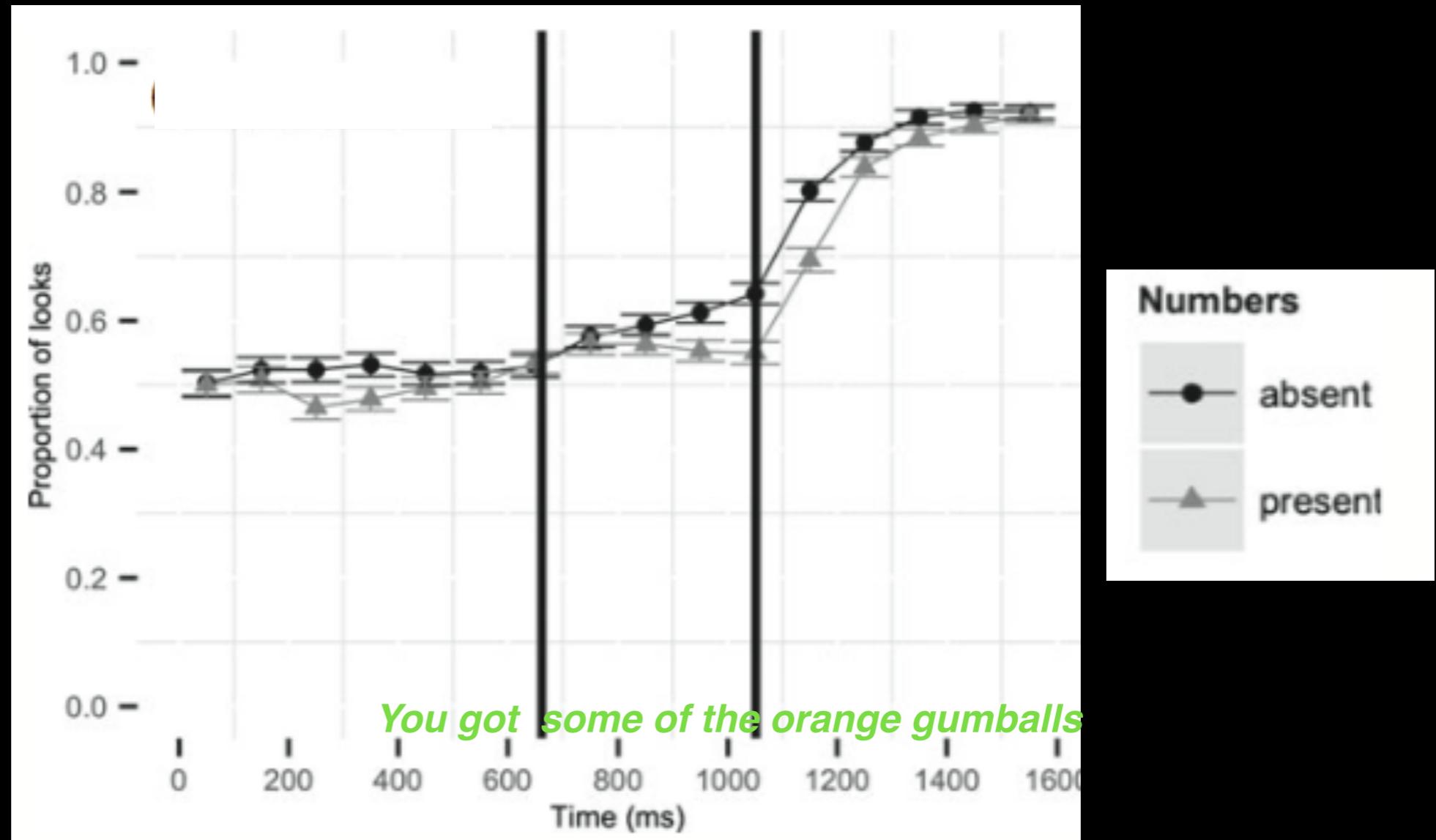
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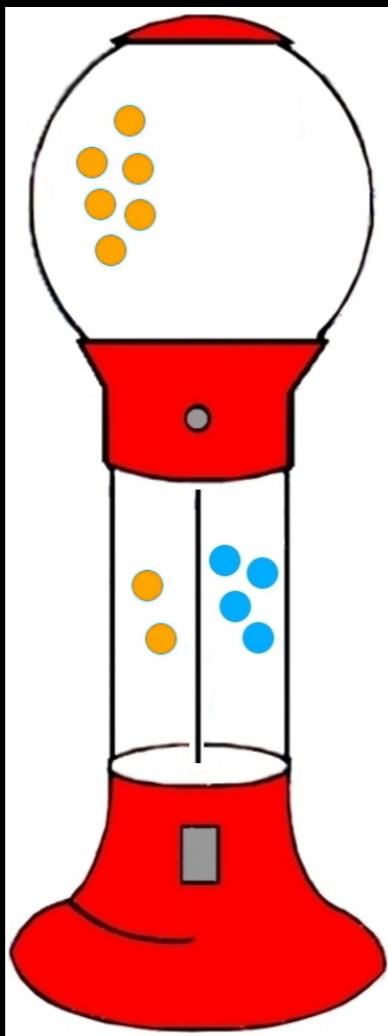


implicatures are slower to process when number alternatives are contextually available

# Context in RSA: alternatives

Absent:  $U = \{\text{none, some, all}\}$

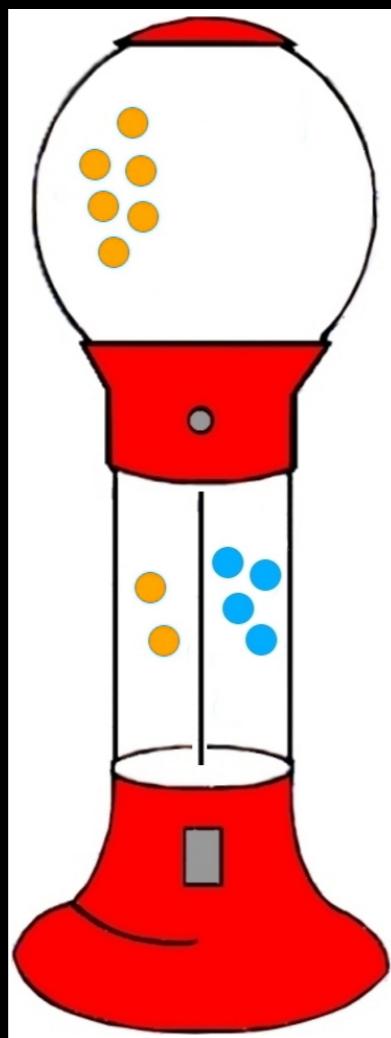
Present:  $U = \{\text{none, some, all, one, two, three, four}\}$



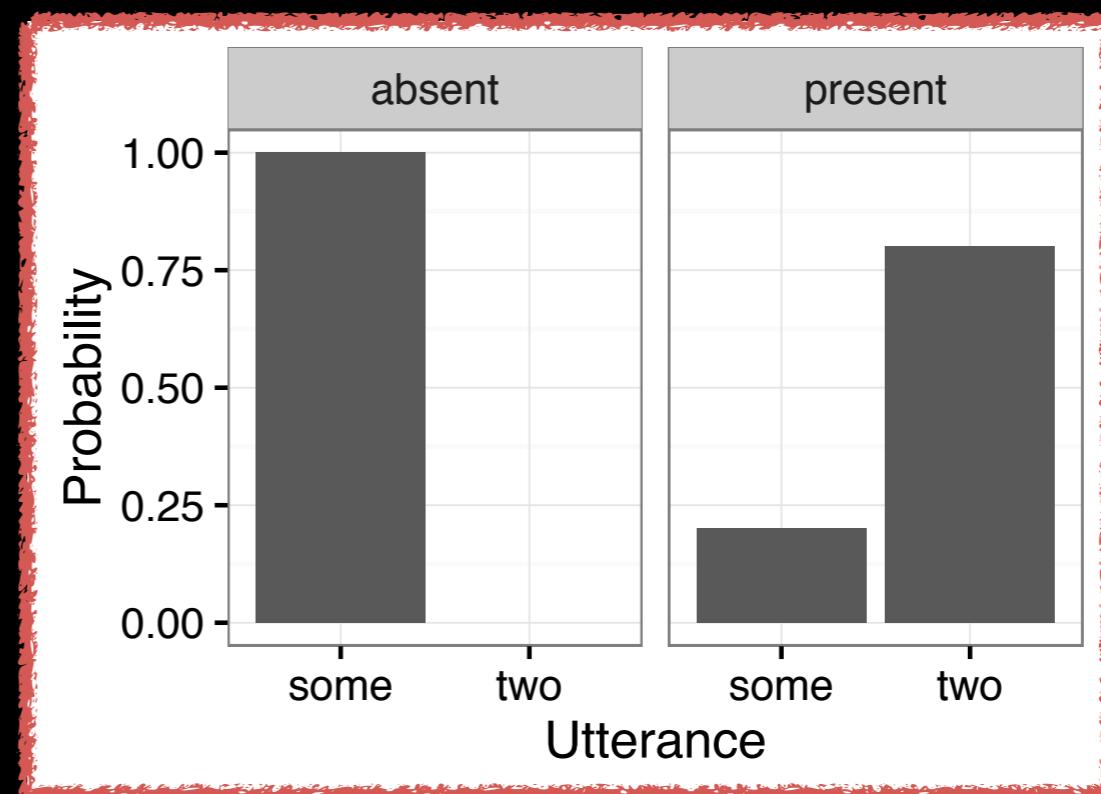
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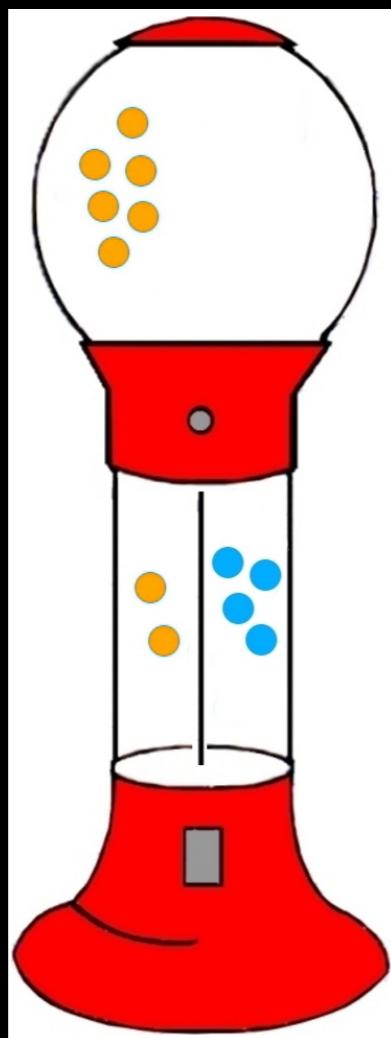
**Pragmatic speaker  
state = 2**



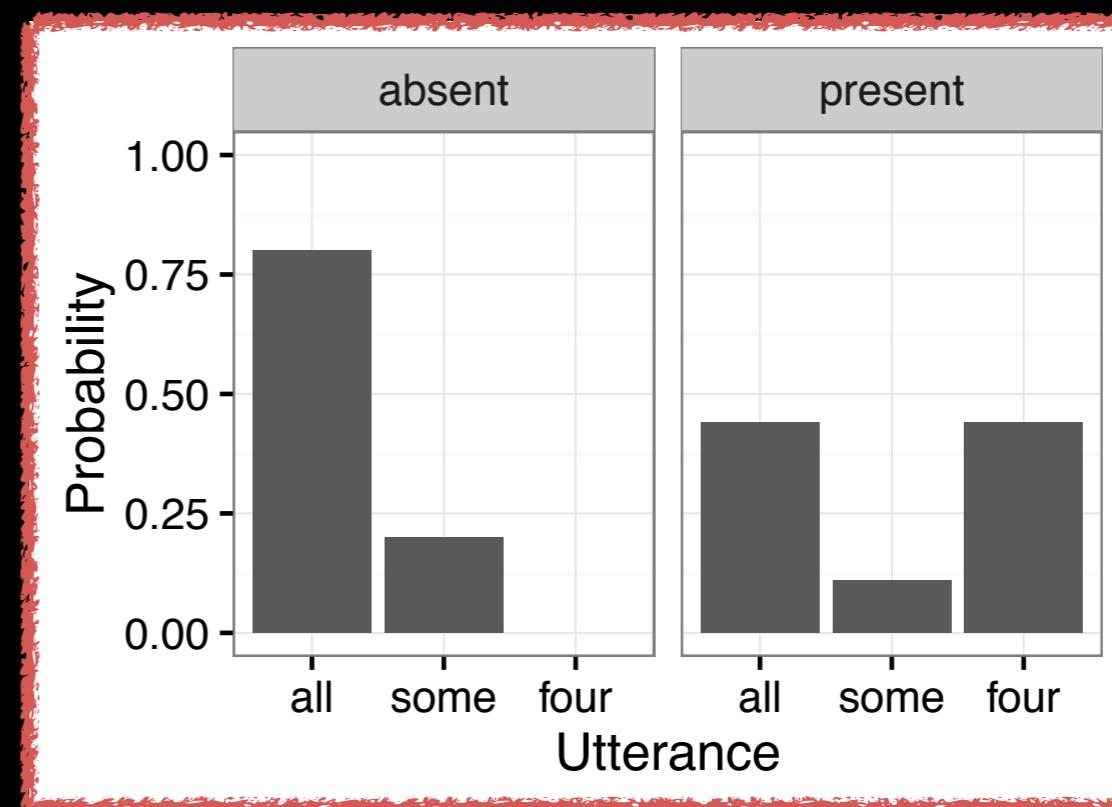
# Context in RSA: alternatives

Absent:  $U = \{\text{none, some, all}\}$

Present:  $U = \{\text{none, some, all, one, two, three, four}\}$



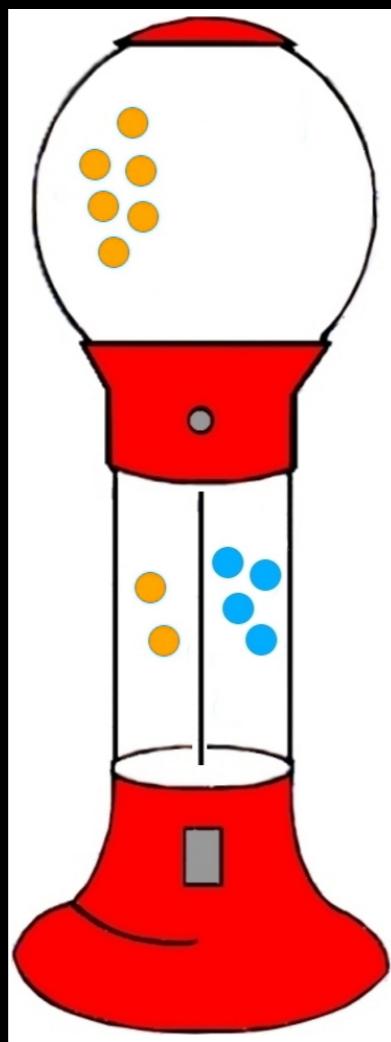
**Pragmatic speaker  
state = 4**



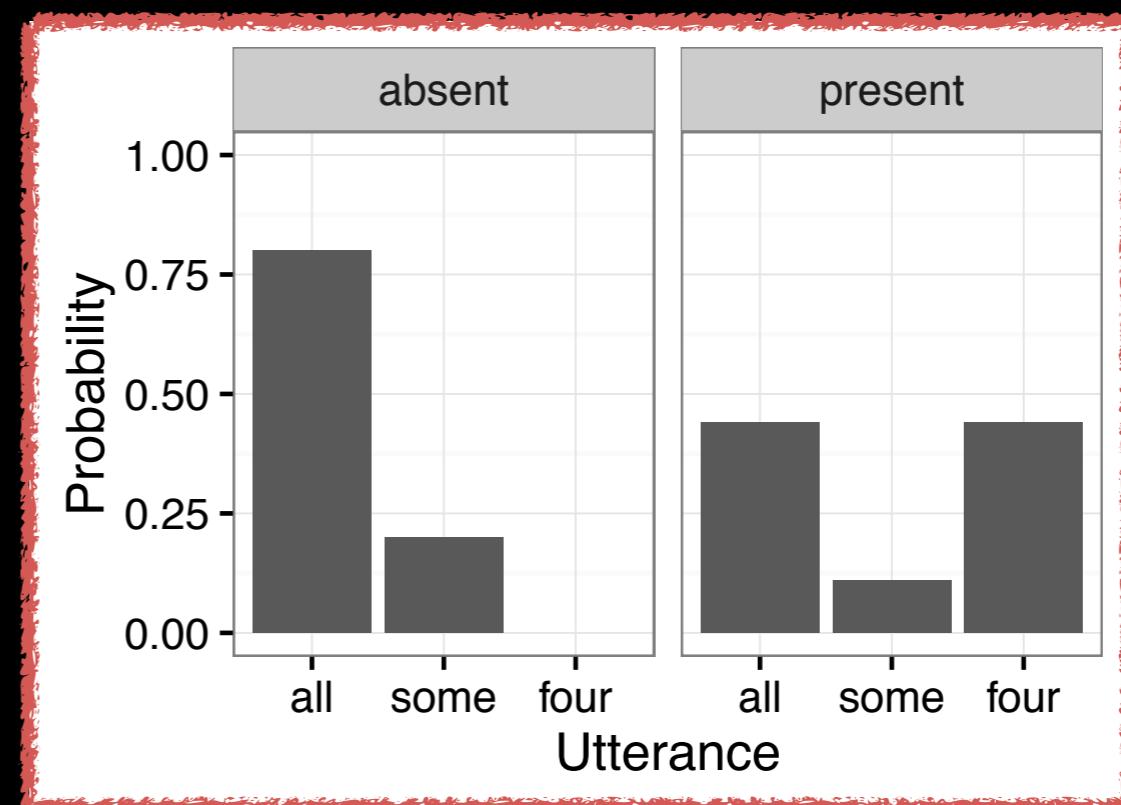
# Context in RSA: alternatives

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Present:  $U = \{\text{none, some, all, one, two, three, four}\}$



**Pragmatic speaker  
state = 4**

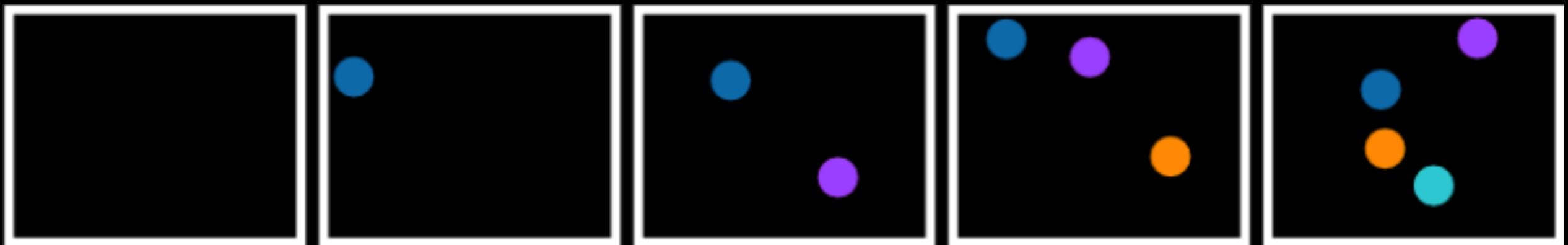


both “some” and “all” less expected when numbers are present

# QUD effects on scalar implicature

Degen & Goodman 2014

Does the QUD modulate scalar implicature strength?

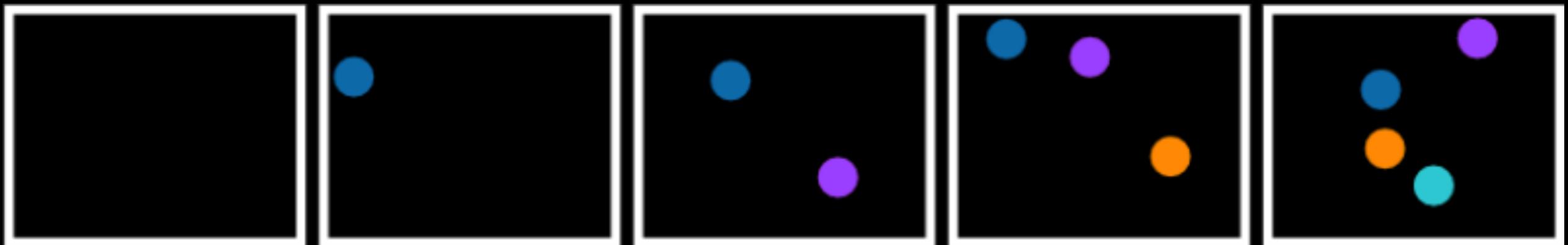


**Implicit QUD**

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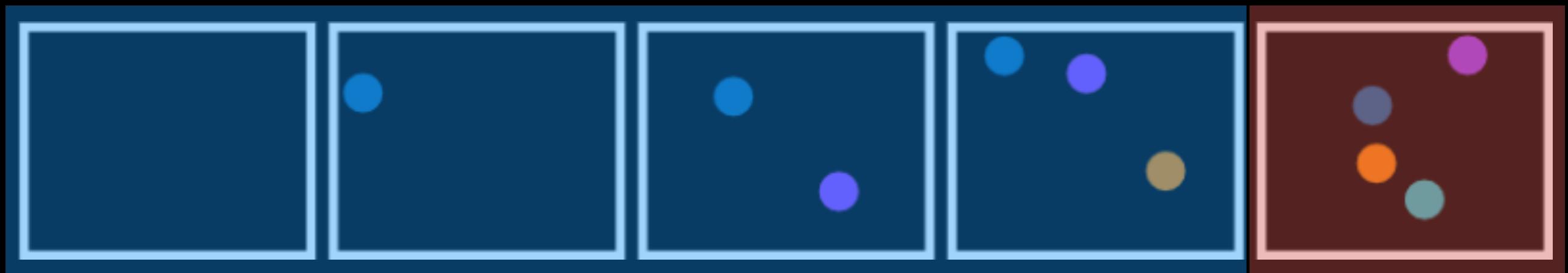
## Implicit QUD

**all?** Did the speaker find all of the marbles?

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**Implicit QUD**

**all?** Did the speaker find all of the marbles?

# QUD effects on scalar implicature

Degen & Goodman 2014

Does the QUD modulate scalar implicature strength?



## Implicit QUD

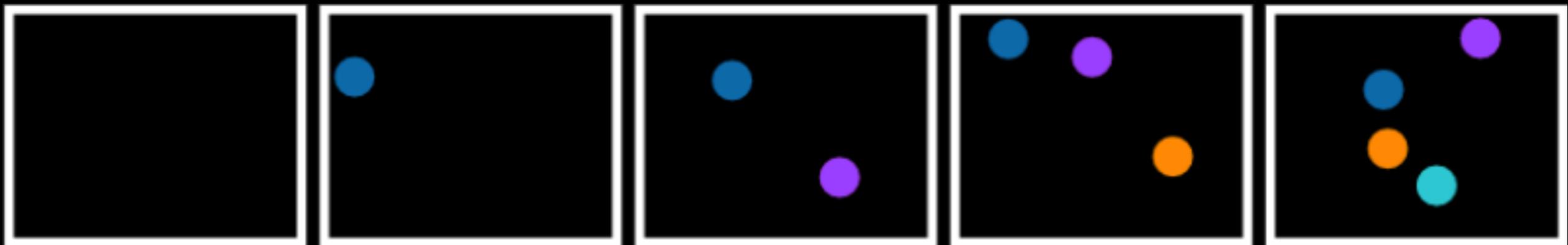
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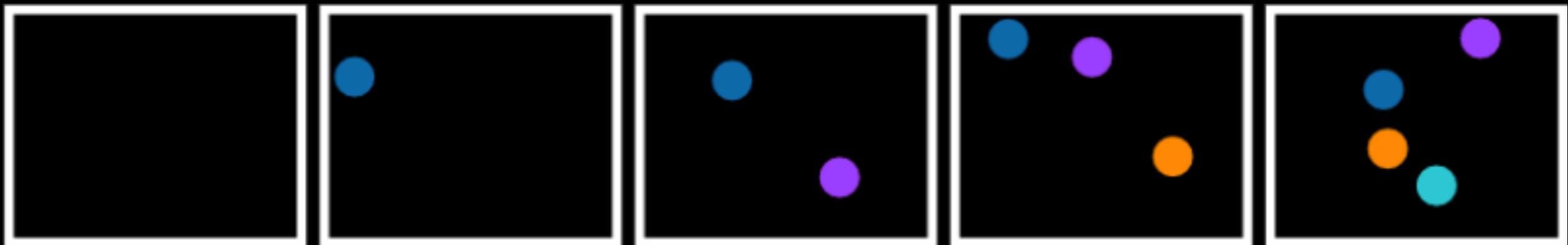
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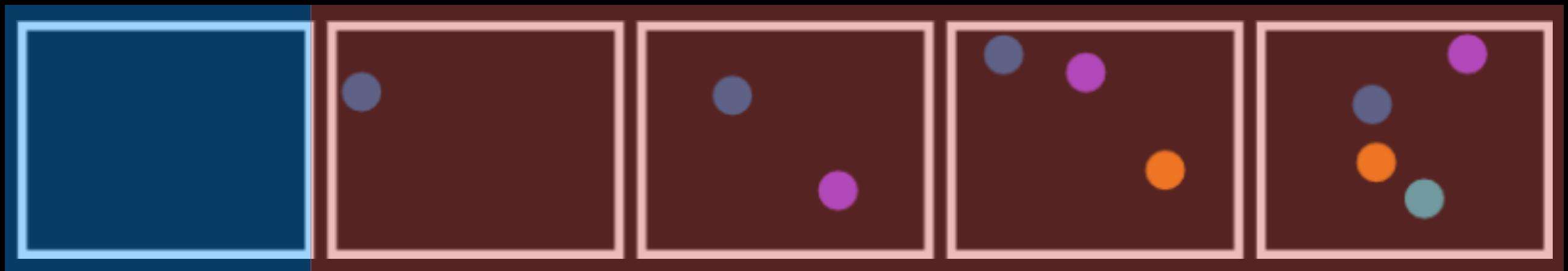
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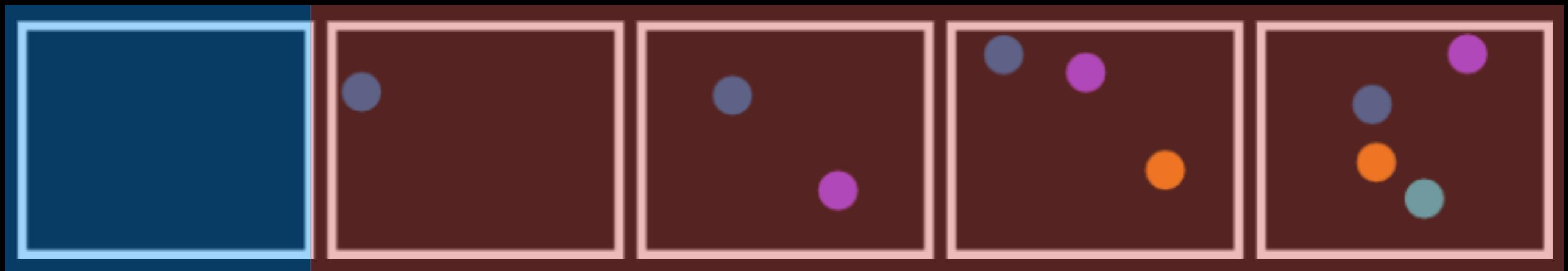
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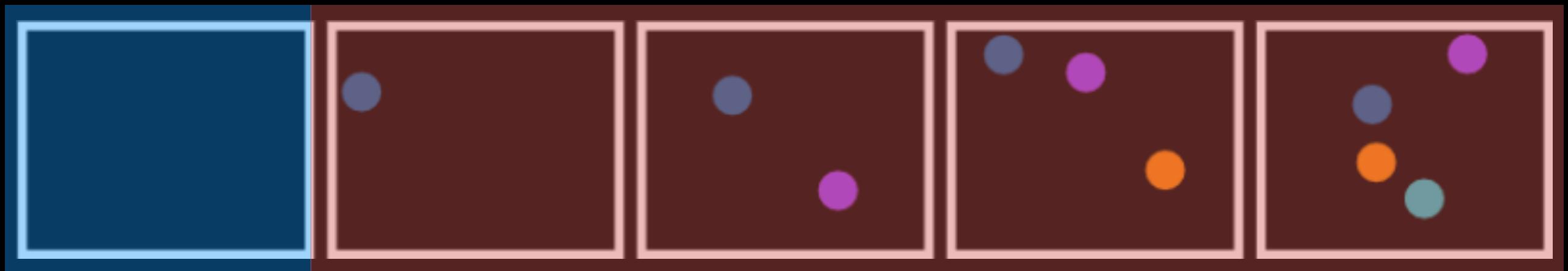
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**Implicit QUD** → manipulated via cover stories

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I found **all** / **some** of the marbles.

# Task and results

Ann found this box:



She called out to her husband:

**'I found some of the marbles!'**

Is Ann's statement true?

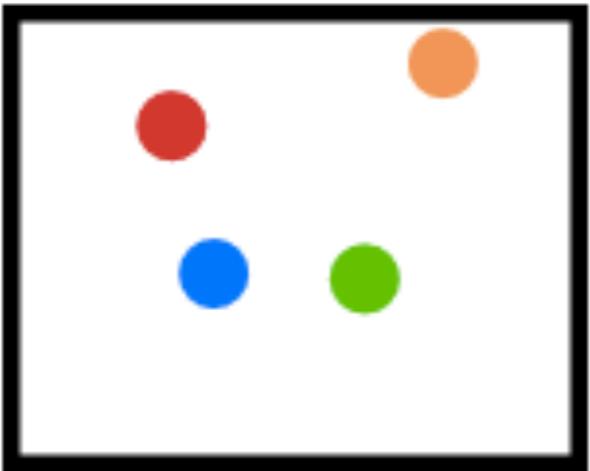
Yes

No

48 participants on  
Mechanical Turk

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Ann found this box:



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Is Ann's statement true?

literal      pragmatic

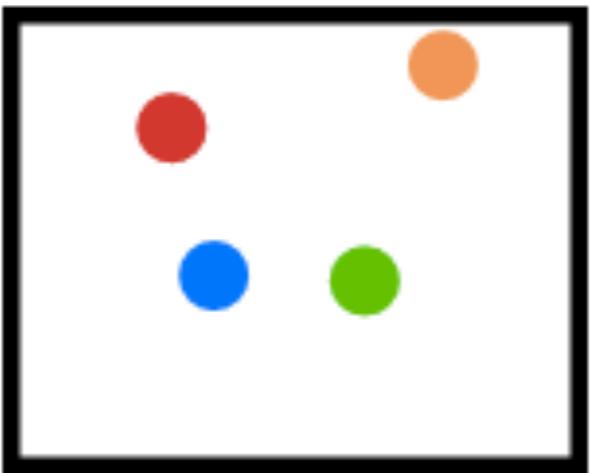
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No

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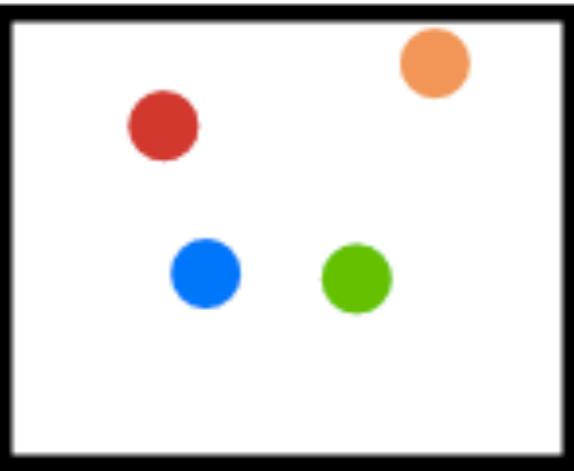
Yes

No

48 participants on  
Mechanical Turk

# Task and results

Ann found this box:

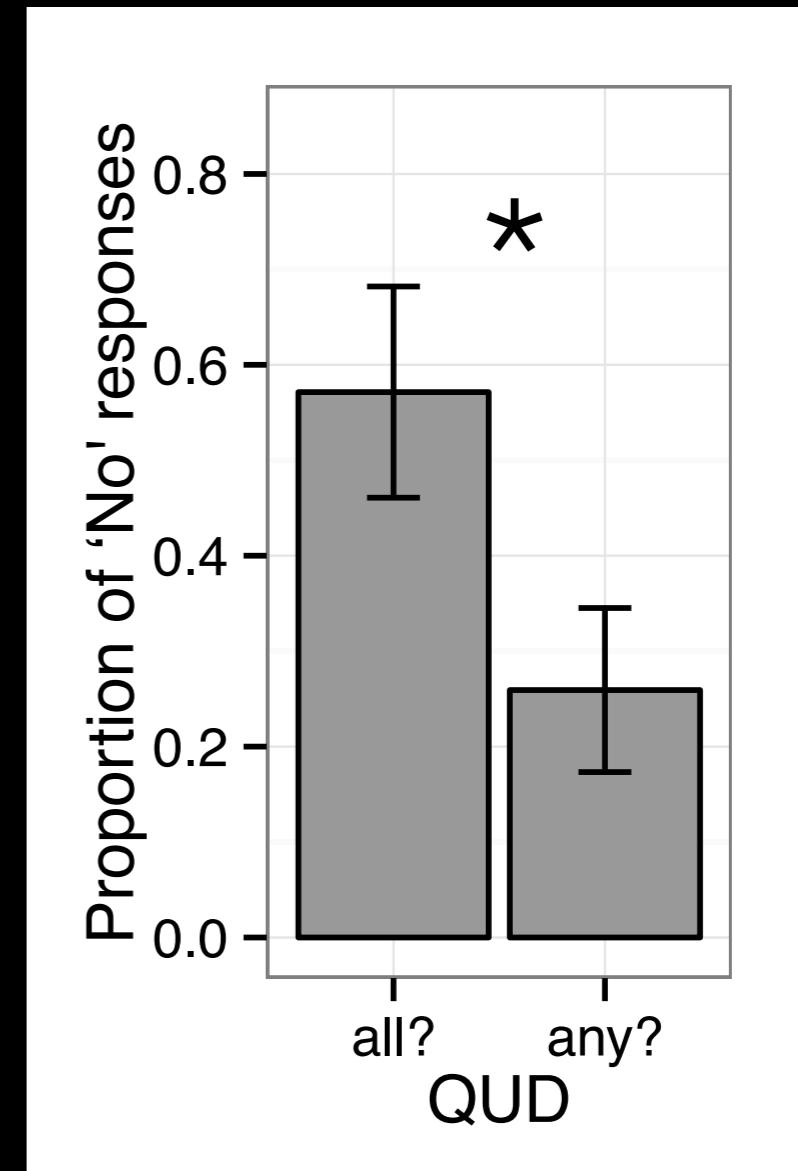


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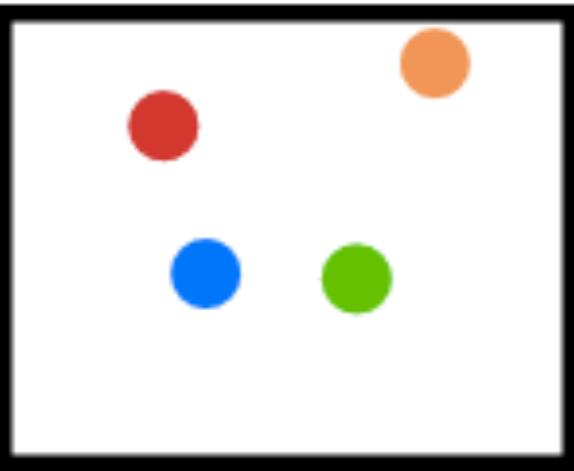
Yes       No



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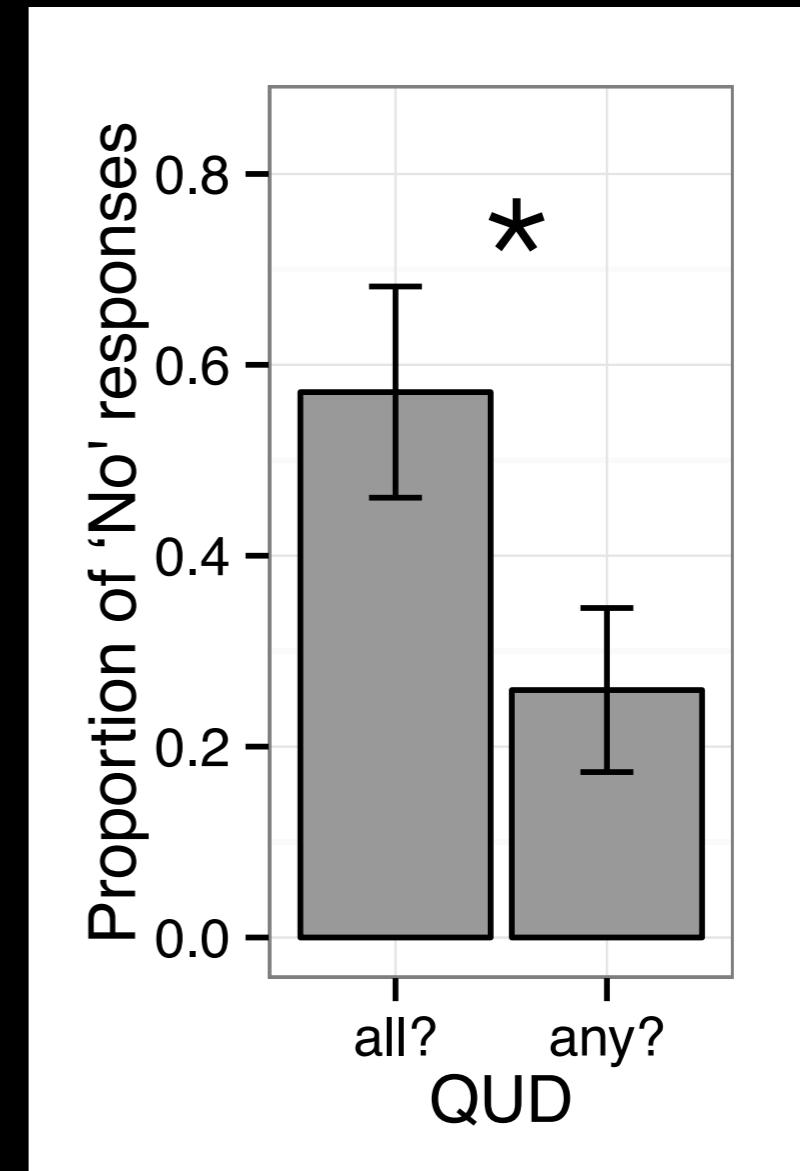


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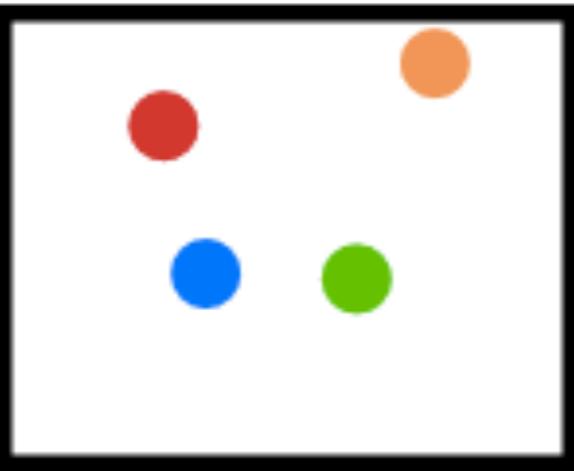


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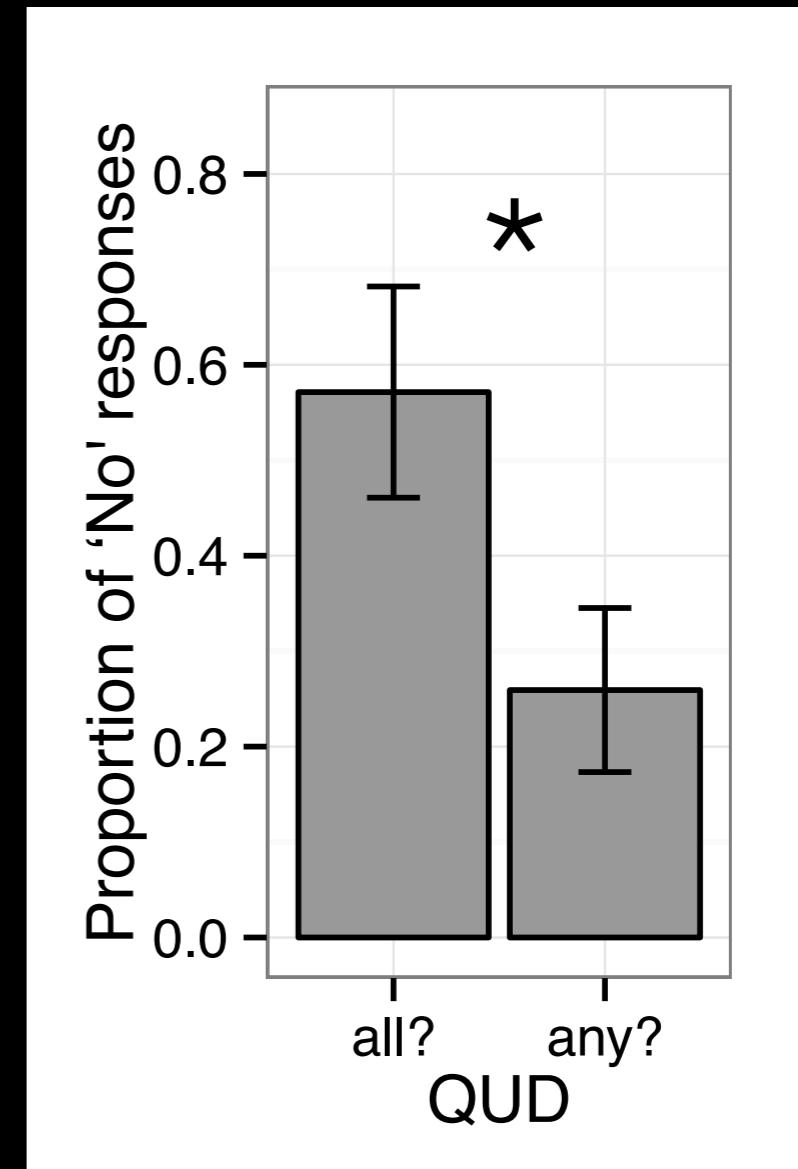


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see also Degen 2013

# Context in RSA: QUD

Degen & Goodman 2014

$$Q = \{q_{\text{all?}}, q_{\text{any?}}\}$$

$$P_{L_1}(m|u, \mathbf{\bar{q}}) \propto P_{S_1}(u|m, \mathbf{\bar{q}}) \cdot P(m)$$

(assuming uniform prior on QUDs and independence of QUD and actual state of the world)

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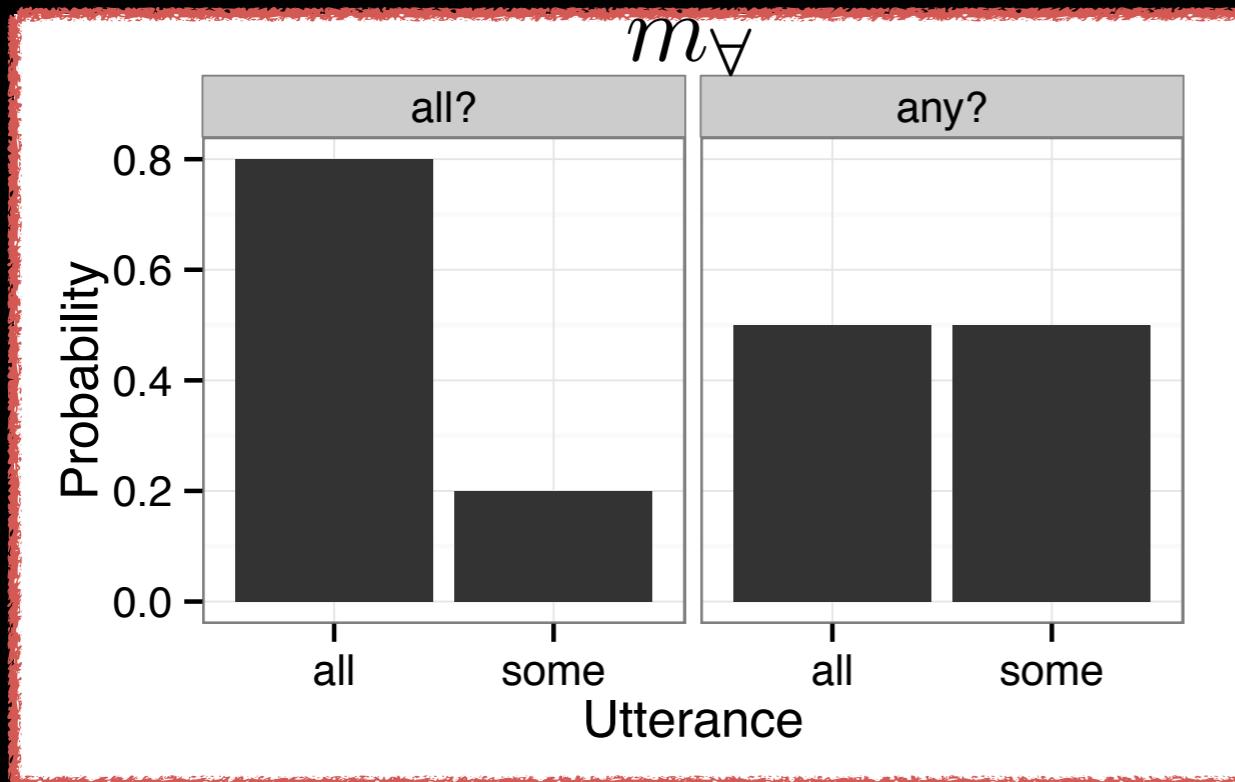
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# Context in RSA: QUD

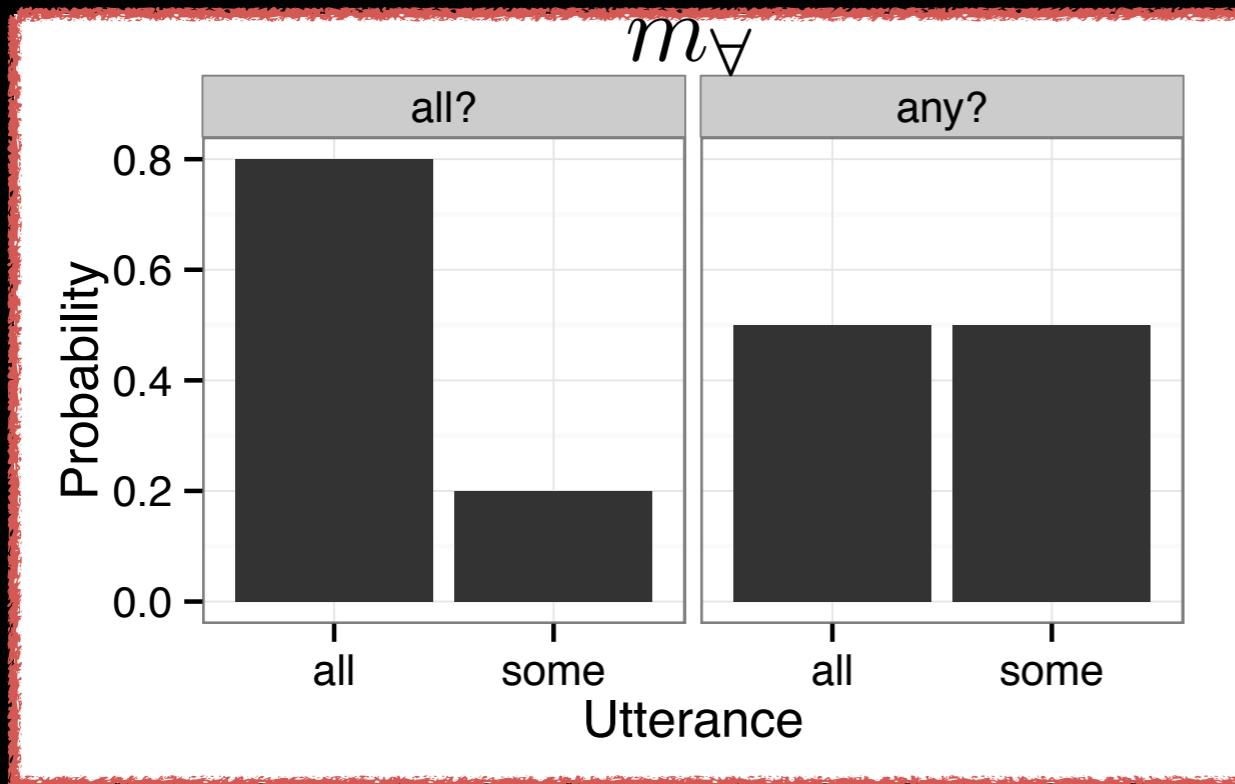
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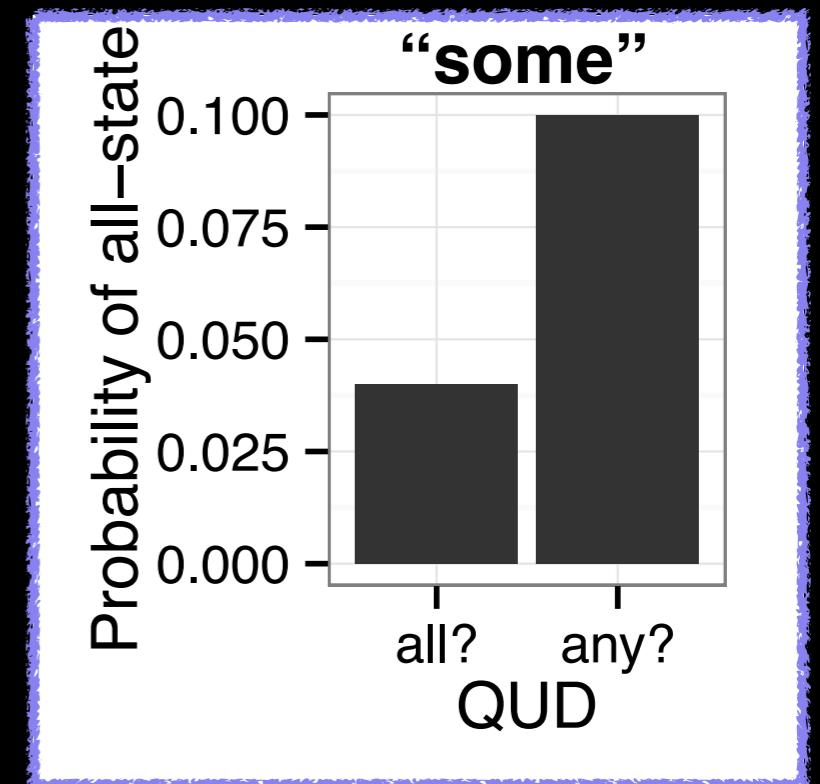
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**Pragmatic listener**



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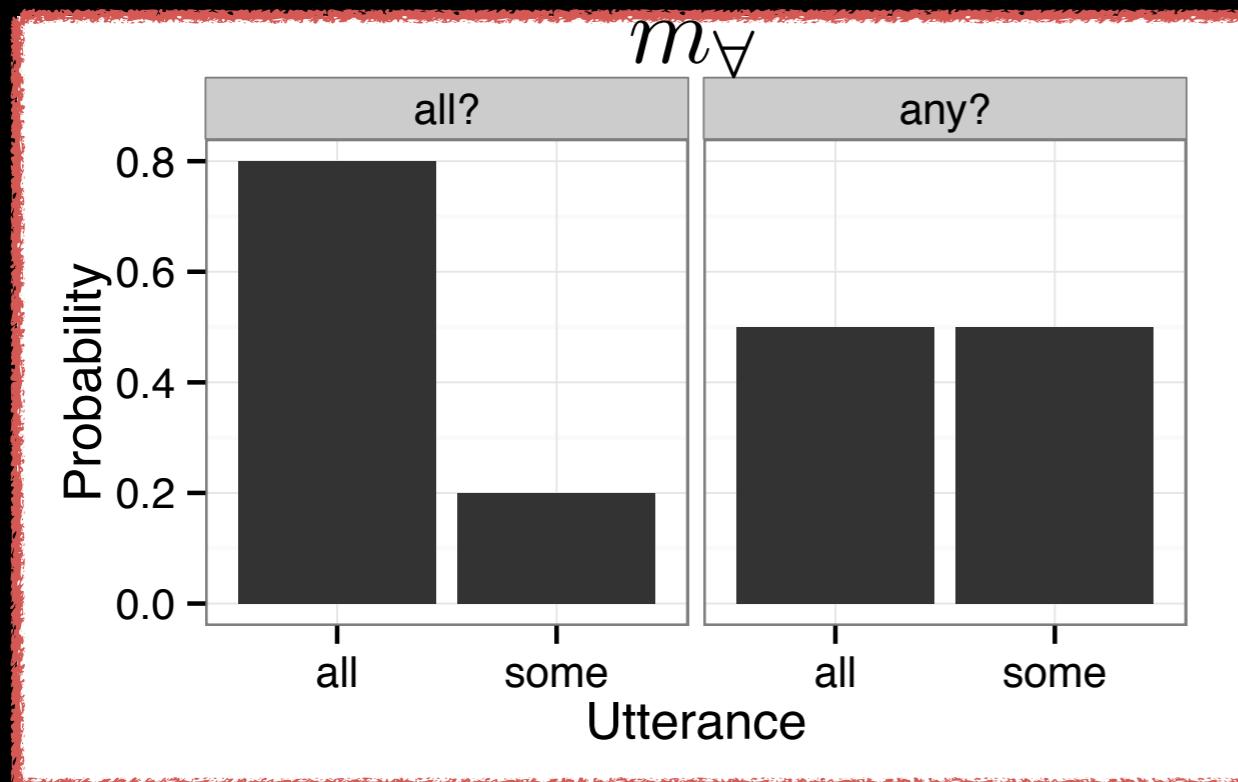
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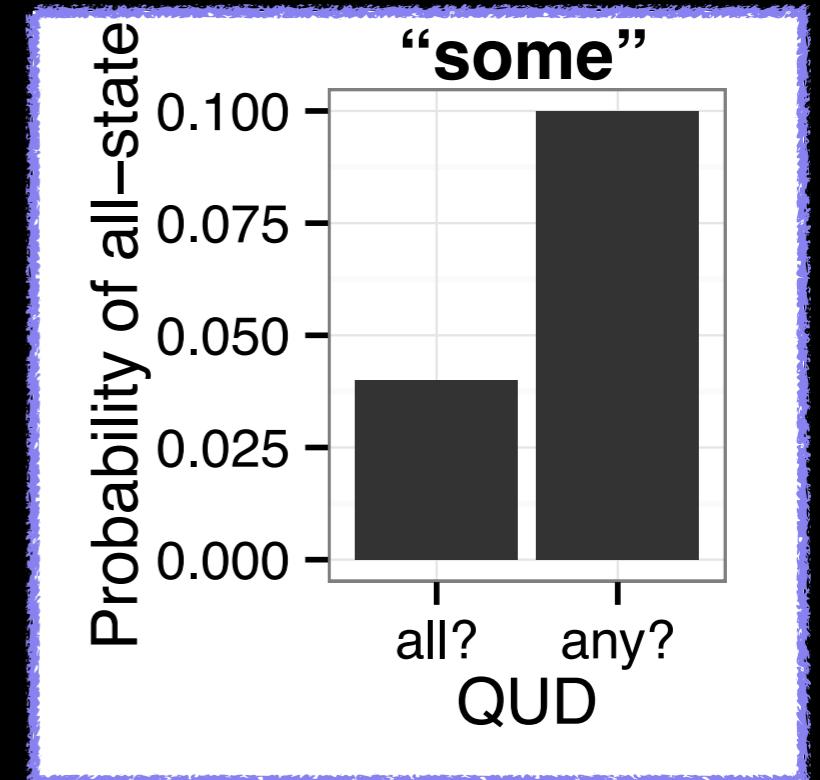
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**Pragmatic listener**



RSA captures QUD effects in scalar implicature

# Summary

## I. **Overinformativeness** in production

redundant referring expressions are rational when  
modifiers are noisy

## II. **Underinformativeness** in production

listeners make efficient use of context in drawing scalar  
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RSA as the most promising current framework

# RSA?

Default theory

Levinson 2000

extreme  
informational  
privilege

Literal-first hypothesis

Huang & Snedeker 2009

Relevance theory

Sperber & Wilson 1995;  
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# Challenges / limitations / future directions

- online processing Tessler & Levy 2019; Cohn-Gordon et al 2019; Augurzky et al 2019
- resource limitations Franke & Degen 2016
- beyond one-shot utterances Hawkins et al 2015
- more interesting structure
- adaptation Schuster & Degen 2019; in prep
- linking functions Augurzky et al 2019; Qing et al 2018; Waldon & Degen in prep

## Probabilistic language understanding An introduction to the Rational Speech Act framework

By Gregory Scontras, Michael Henry Tessler, and Michael Franke

The present course serves as a practical introduction to the Rational Speech Act modeling framework. Little is presupposed beyond a willingness to explore recent progress in formal, implementable models of language understanding.

### Main content

#### I. [Introducing the Rational Speech Act framework](#)

*An introduction to language understanding as Bayesian inference*

#### II. [Modeling pragmatic inference](#)

*Enriching the literal interpretations*

#### III. [Inferring the Question-Under-Discussion](#)

*Non-literal language*

#### IV. [Combining RSA and compositional semantics](#)

*Jointly inferring parameters and interpretations*

#### V. [Fixing free parameters](#)

*Vagueness*

#### VI. [Expanding our ontology](#)

*Plural predication*

#### VII. [Extending our models of predication](#)

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#### IX. [Social reasoning about social reasoning](#)

*Politeness*

The literal listener rule can be written as follows:

```
// set of states (here: objects of reference)
// we represent objects as JavaScript objects to demarcate them from utterances
// internally we treat objects as strings nonetheless
var objects = [{color: "blue", shape: "square", string: "blue square"}, 
               {color: "blue", shape: "circle", string: "blue circle"}, 
               {color: "green", shape: "square", string: "green square"}]

// set of utterances
var utterances = ["blue", "green", "square", "circle"]

// prior over world states
var objectPrior = function() {
  var obj = uniformDraw(objects)
  return obj.string
}

// meaning function to interpret the utterances
var meaning = function(utterance, obj){
  _.includes(obj, utterance)
}

// literal listener
var literalListener = function(utterance){
  Infer({model: function(){
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    condition(uttTruthVal == true)
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}

viz.table(literalListener("blue"))
```

run

(state)	probability
blue circle	0.5
blue square	0.5

### Exercises:

- I. In the model above, `objectPrior()` returns a sample from a `uniformDraw` over the possible objects of reference. What happens when the listener's beliefs are not uniform over the

# Scontras, Tessler, & Franke

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Scontras, Tessler, & Franke  
 XPrag.de summer school:  
 “Probabilistic pragmatics”

# Thank you

## Collaborators

Elisa Kreiss

Noah Goodman

Caroline Graf

Robert Hawkins

Mike Tanenhaus

Michael Franke

Greg Scontras

Michael Henry Tessler

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- NIH grant HD27206 to MT