

Algorithm Design & Problem Solving: **Starting Searching**



Contents



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Introducing Searching

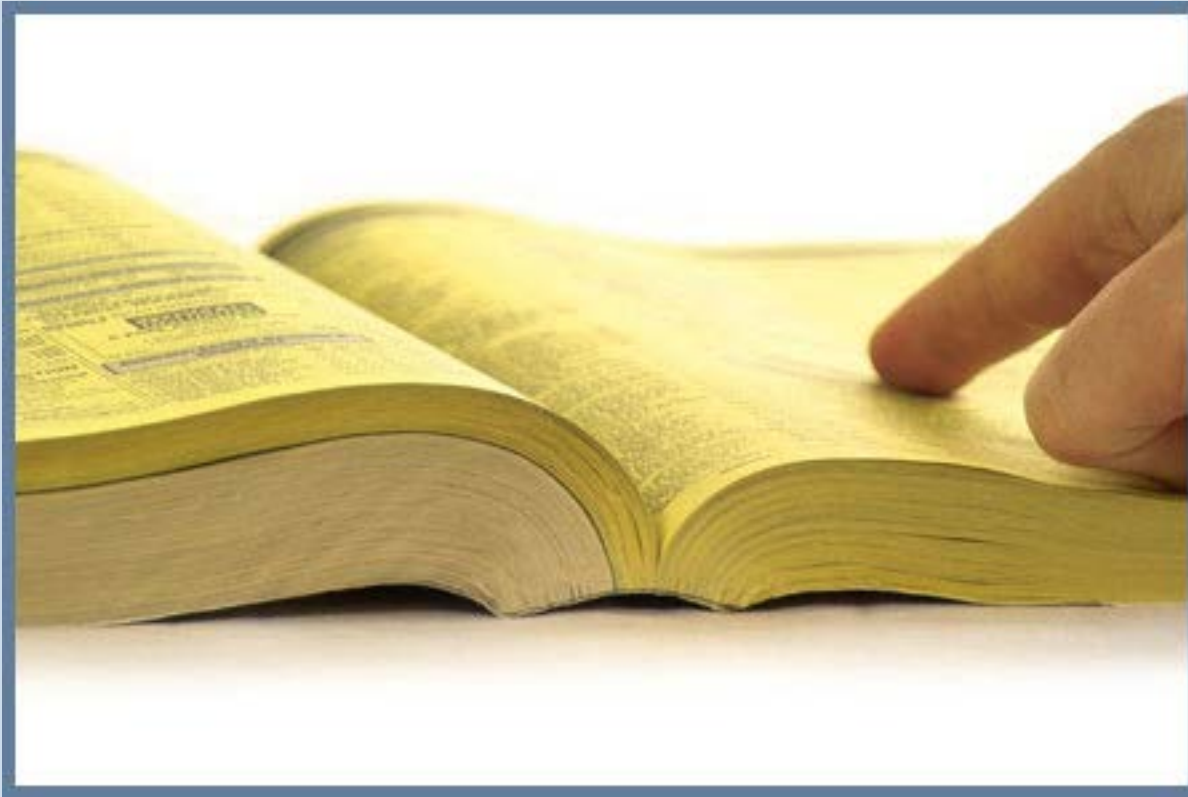
2

Linear Search

3

Binary Search

**How did you find a name in a
phonebook?**



How did you find this card?



Linear Search



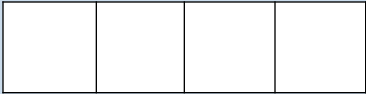

I need to find the student whose
name is

Linear Search



- ❖ Most basic of search algorithms
- ❖ Moves **sequentially** through the array looking for a matching value

Linear Search

LINEAR SEARCH		
Best	Average	Worst
$O(1)$	$O(n)$	$O(n)$
 Array		 Brute-force

Linear Search

❖ When is it best used?

- Small problem set
- Unsorted problem set

Binary Search



1. Everybody stand up

2. Pair off with somebody standing;
stay standing if taller, if shorter sit
down.

3. If still standing, go to step 2

**Divide &
Conquer**

Binary Search



- ❖ Relies on a **divide and conquer** strategy to find a value within an already-sorted collection

Binary Search



BINARY SEARCH

Best

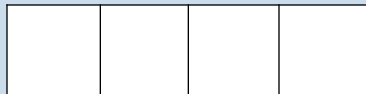
Average

Worst

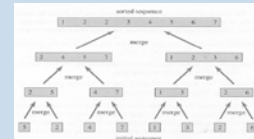
$O(1)$

$O(\log n)$

$O(\log n)$



Array



Divide & Conquer

Do you remember logarithms?



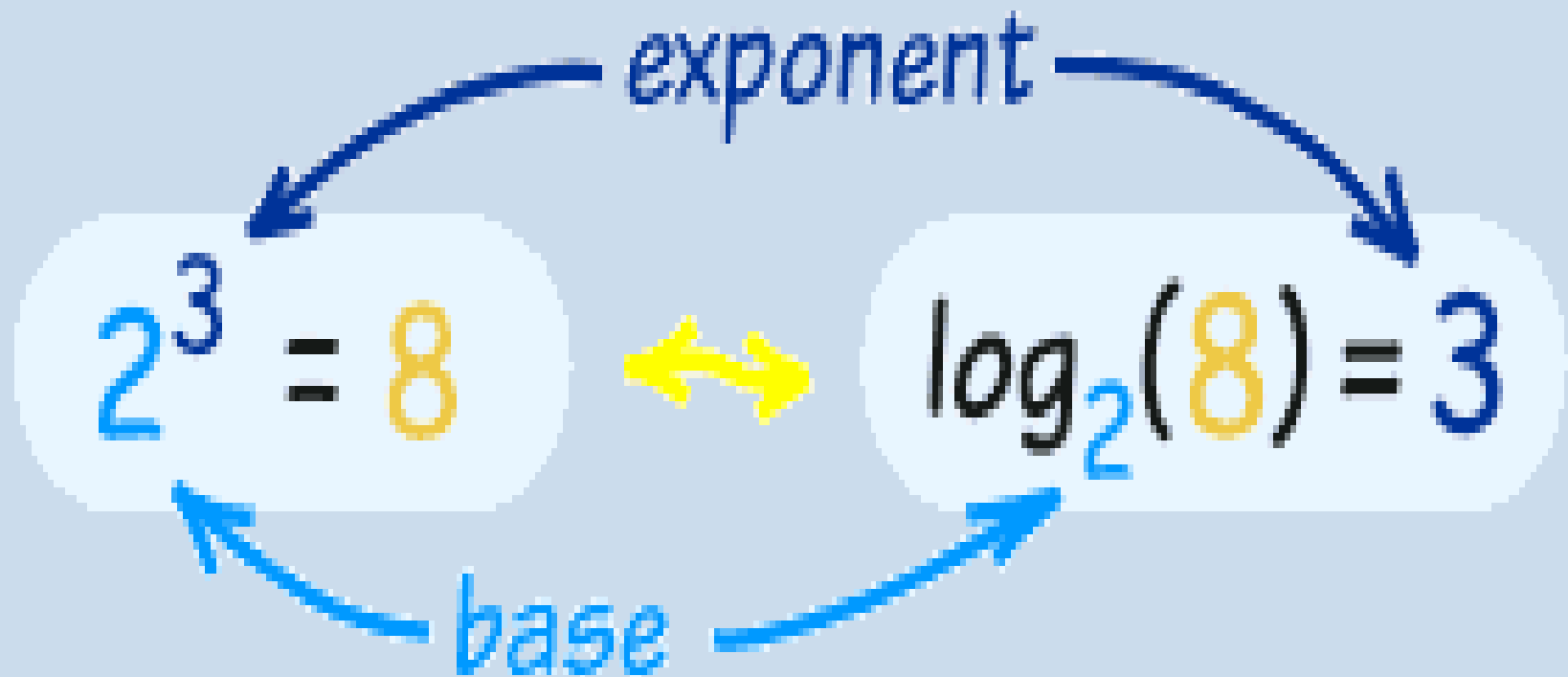
❖ In its simplest form:

- How many of one number do we multiply to get another number?

$$\underbrace{2 \times 2 \times 2}_3 = 8 \quad \leftrightarrow \quad \log_2(8) = 3$$

←
base

Do you remember logarithms?



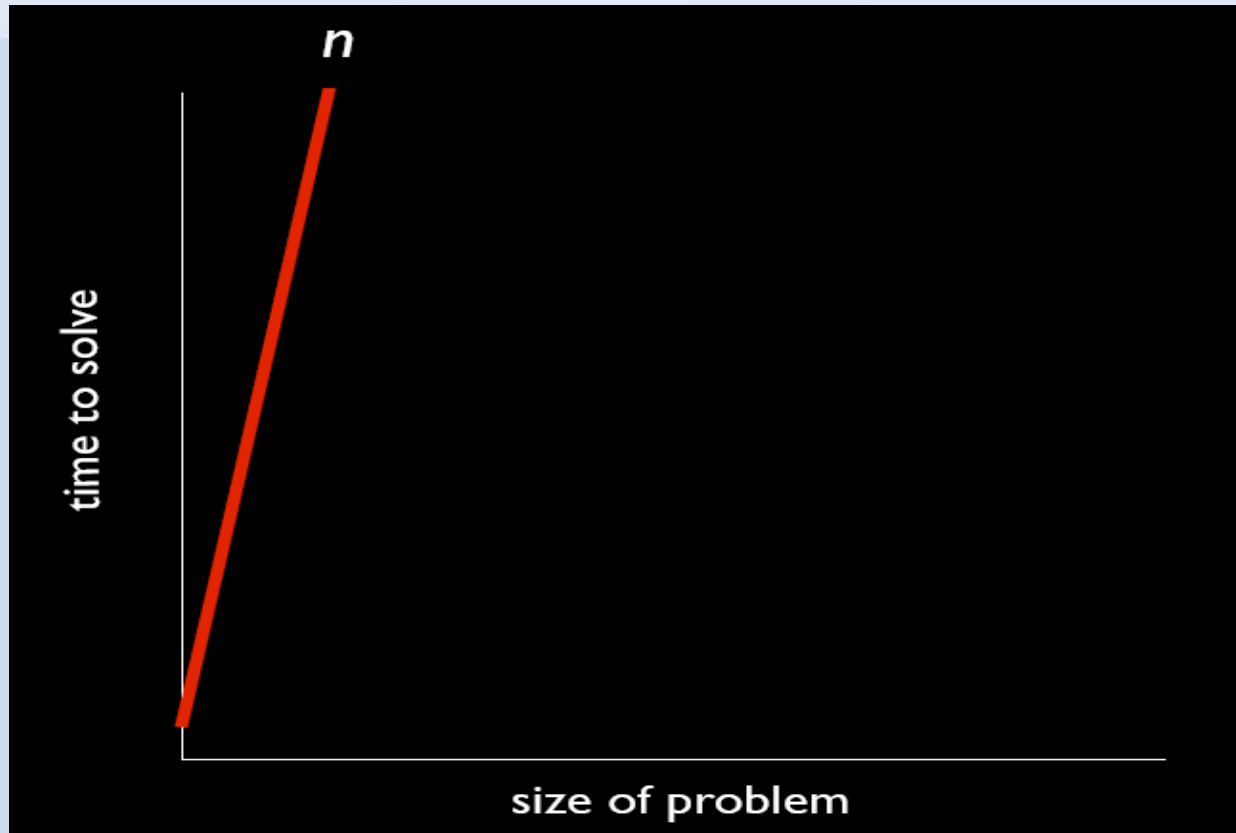
Binary Search



❖ When is it best used?

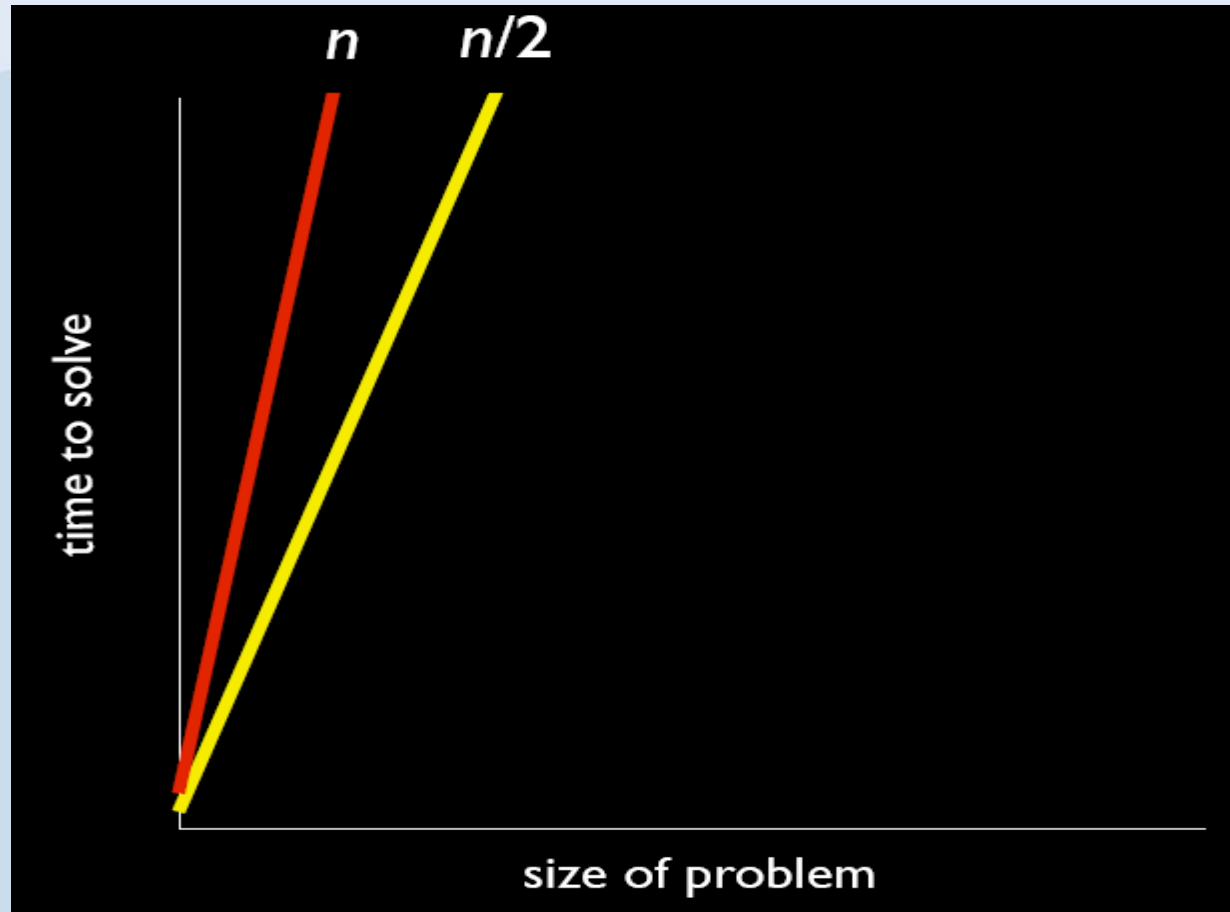
- On a large problem set
- Sorted problem set

$O(n)$ 




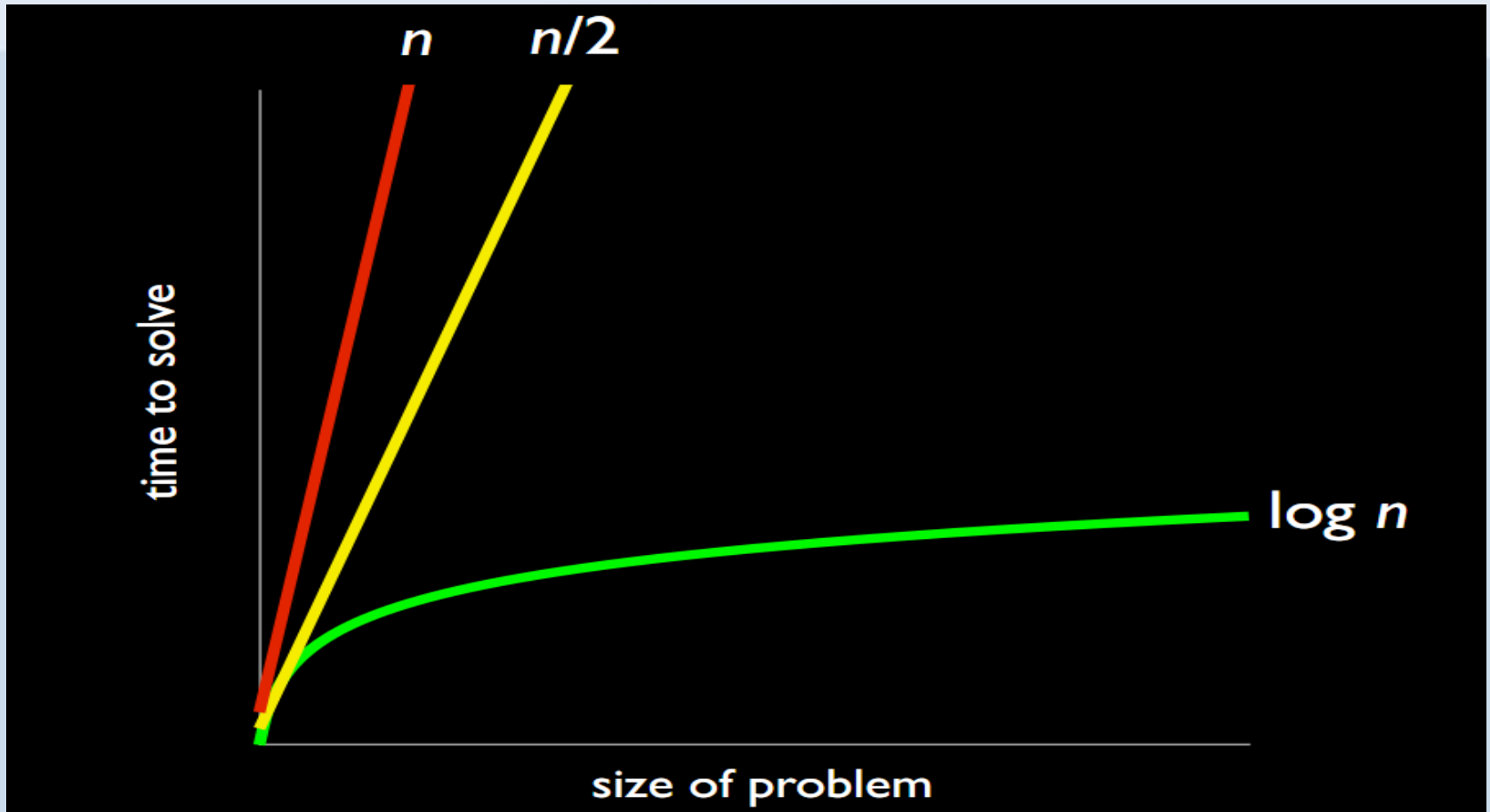
If I count everybody in this class individually - **Linear**

$O(n/2)$



If I count the class in pairs

$O(\log n)$ 



If I count the class using the Week 1 algorithm - **Binary**

Search Algorithms



- ❖ Write the algorithm to perform a **linear search** on an array.

Linear Search Algorithm

Input: An array **A** storing **N** items, element to be searched for - **searchKey**

Output: **i**, position of the searched for element in the array

Linear Search Algorithm



```
for  $i = 0, i < n$  do  
    if  $A[i] = \text{searchKey}$   
        return  $i$   
return  $-1$ 
```


Search Algorithms



- ❖ Write the algorithm to perform a **binary search** on an array.

Binary Search Algorithm

1. Determine middle element of subarray
2. If searchKey is the middle element return its index
3. Else if searchKey is in the left subarray
 - Highest index is the index of the middle element – 1
4. Else if searchKey is in the right subarray
 - Lowest index is the index of the middle element + 1

Binary Search Algorithm

Input: An array **A**, element to be searched for – **searchKey**, lowest index of array – **low**, highest index of array – **high**.

Output: **i**, position of the searched for element in the array

Binary Search Algorithm



Middle = (low + high)/2

If searchKey = A[middle]

return middle

Else if searchKey < A[middle]

high = middle - 1

Else if searchKey > A[middle]

low = middle + 1

What is wrong with this algorithm?

Binary Search Algorithm



While low \leq high

Middle = (low + high)/2

If searchKey = A[middle]

return middle

Else if searchKey < A[middle]

high = middle - 1

Else if searchKey > A[middle]

low = middle + 1

Binary Search Algorithm



Alter your algorithm to find this card in a pack of playing cards.

Order of suits are:

- ❖ Hearts
- ❖ Diamonds
- ❖ Clubs
- ❖ Spades



Thank You !

