

September 21, 2020

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Definition :-

When an equation involves one or more derivatives w.r.t a particular variable. Then that variable is called an independent variable. A variable is called dependent variable if a derivative of that variable occurs. Then equation.

$$\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} = 0$$

has ~~one~~ dependent variable  $V$  and two independent variables  $x$  and  $y$ .

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Definition

:- An equation involving one dependent variable and its derivative w.r.t one or more independent variables, is called a "Differential equation". e.g;

$$i) \frac{d^2}{dx^2} y + 2 \frac{d}{dx} y + y = 0$$

$$ii) \frac{\partial^2}{\partial x^2} u + \frac{\partial^2}{\partial y^2} u + \frac{\partial^2}{\partial z^2} u = 0$$

There are two types of Differential equations:

- i) Ordinary Differential equations
- ii) Partial Differential equations.

### i) Ordinary Differential equations ③

A differential equation which involves the derivatives of the dependent variable w.r.t a single independent variable is known as "Ordinary Differential equation". eg;

$$i) \frac{d}{dx} y + 2y = \cos x$$

$$ii) \frac{d^3}{dx^3} y + xy \cdot \left( \frac{d}{dx} y \right)^2 = 0$$

$$iii) \left( \frac{d^2}{dx^2} y \right)^4 + x \cdot \frac{d}{dx} y - 4xy = 0$$

are ordinary differential equations.

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ii) Partial Differential equation. (4)

A differential equation which contains two or more independent variables and partial derivative w.r.t. them is called a Partial Differential equation. eg;

$$i) \quad x \cdot \frac{\partial z}{\partial x} + y \cdot \frac{\partial z}{\partial y} = nz$$

$$ii) \quad \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} + \frac{\partial^2 V}{\partial z^2} = 0.$$

$$iii) \quad \frac{\partial^3 V}{\partial t^3} = K \cdot \left( \frac{\partial^2 V}{\partial x^2} \right)^2.$$

are the partial differential equations.

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## Order of a Differential equation <sup>(5)</sup>

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The order of a differential equation is the order of the highest ordered derivative that occurs in the equation. e.g.;

$$\frac{dy}{dx} + 2x = 0 \quad \text{has order } 1.$$

and

$$\frac{d^2}{dx^2}y + 2\left(\frac{d}{dx}y\right)^3 + y = 0$$

has order 2.



## Degree of a Differential equation <sup>(6)</sup>

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The degree of a differential equation is defined to be the exponent of the highest order derivative

e.g;

$$i) \left( \frac{d}{dx} y \right)^1 = \cos x$$

$$ii) \left( \frac{d^2}{dx^2} y \right)^1 + 4y = 0$$

$$iii) \left( \frac{d^2}{dx^2} y \right)^1 + 7 \left( \frac{d}{dx} y \right)^3 - 8y = 0.$$

$$iv) \left( \frac{d^3}{dx^3} y \right)^2 - 2 \left( \frac{d}{dx} y \right)^4 + y = 0.$$

has degrees 1, 1, 1, 2.

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