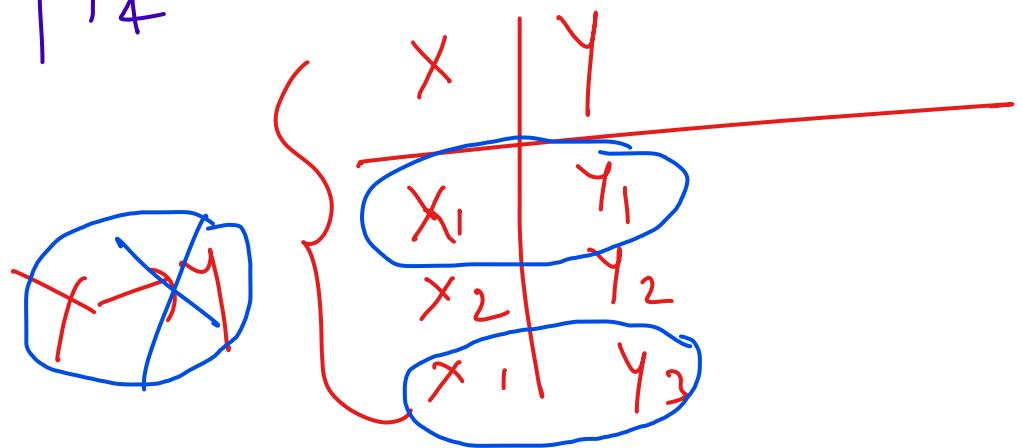


if  $t_1(x_i) = t_2(x)$   
 then  
 $t_1(y) = t_2(y)$

$$x \rightarrow y$$

$$x \rightarrow y$$



Armstrong Rule :-

| R | : (Reflexive Rule)

if  $x \sqsupseteq y$  then

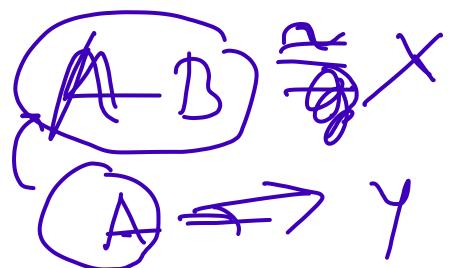
$$\cancel{A \sqsupseteq B \rightarrow C}$$

$$x \rightarrow y$$

$$\left\{ \begin{array}{l} A \sqsupseteq B \rightarrow A \sqsubseteq \\ A \sqsupseteq B \rightarrow B \sqsubseteq \end{array} \right.$$

$$\cancel{A \sqsupseteq B}$$

$$\frac{\cancel{X \supseteq Y} \quad X \rightarrow Y}{X \rightarrow Y ?}$$



$$X \supseteq Y \quad | \quad X \rightarrow Y \quad | \quad \begin{matrix} X = \{A, B, C\} \\ Y = \{B, C\} \end{matrix}$$

Augmentation Rule ( $\vdash R_2$ )

$$X \rightarrow Y \quad \models \quad X z \rightarrow Y z$$

Transitive Rule ( $\vdash R_3$ )

$$\{X \rightarrow Y, Y \rightarrow Z\} \models X \rightarrow Z$$

Decomposition ( $\vdash R_4$ )

$$\{X \rightarrow YZ\} \models \{X \rightarrow Y, X \rightarrow Z\}$$

union or additive ( $\vdash R_5$ )

$$\{X \rightarrow Y, X \rightarrow Z\} \models \{X \rightarrow YZ\}$$

"Pseudo Transitive Rule (TR<sub>6</sub>)

$$\{x \rightarrow y, w \bar{y} \rightarrow z\} \vdash \{w x \rightarrow z\}$$

Closure of attributes

$$R = \{A, B, C, D, E, F\}$$

$$FD = \left\{ \frac{AB \rightarrow C}{CF \rightarrow B}, BC \rightarrow AD, D \rightarrow E \right\}$$

Closure of attributes

$$X\{A\}^+ = \{A\} P.K$$

$$X\{AB\}^+ = \{A, B\} P.K$$

$$\{A, F\}^+ = \{A, F\} P.K$$

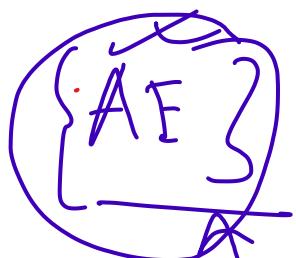
$$\overline{\{A, B, F\}}^+ = \{A, B, C, D, E, F\} P.K$$

$$\begin{array}{c} \bar{A} \bar{B} \bar{F} \Rightarrow B.K \\ \downarrow \quad \downarrow \quad \downarrow \\ \text{prime attribute} \end{array}$$

$R = \{A, B, C, D, E, F\}$

$FD = \{A \rightarrow C, C \rightarrow D, D \rightarrow B, E \rightarrow F\}$

Find out P.K ?



$$\{AE\}^+ = \{A, C, D, B, E, F\} \text{ PK}$$

Candidate Key -

### Full Functional Dependency

$FD = \{X \rightarrow Y, XZ \rightarrow Y, AB \rightarrow C\}$

Q1 Is C is FFD on AB?

Q2 Is Y is FFD on XZ?

Ans:-

Yes

$$AB \rightarrow C \rightarrow C$$

$$X \left[ \begin{array}{l} A \rightarrow C \\ B \rightarrow C \end{array} \right] \not\models | \text{false}$$

Q2 No

$XZ \rightarrow Y$  is Grand

$$\begin{array}{c} X \rightarrow Y \\ Z \rightarrow Y \end{array}$$

So ~~this~~ Y NOT FFD on XZ.

Trivial FD  $\Rightarrow$

$X \cdot Y$

$X \cdot Y \rightarrow X$   
 $X \cdot Y \rightarrow Y$

trivial.

~~Transitive~~ FD

$$X \rightarrow Y, Y \rightarrow Z \vdash X \rightarrow Z$$

Normalization:-

① Insertion anomalies

② Update anomalies  $CSE \xrightarrow{E \rightarrow L_1}$   
New  $\downarrow$

③ Deletion anomalies  $L_2$

<u>EMP</u>	E-name	Dept-id	Department	Dept-loc
1	A	D <sub>1</sub>	CSE	K <sub>1</sub> L <sub>2</sub>
Null	Null	D <sub>2</sub>	ECE	L <sub>2</sub>
2	B	D <sub>1</sub>	CSE	L <sub>2</sub> K <sub>1</sub>
3	C	D <sub>1</sub>	CSE	L <sub>1</sub>

$\rightarrow 4$   
Delete

D

$D_3$

IT

L3

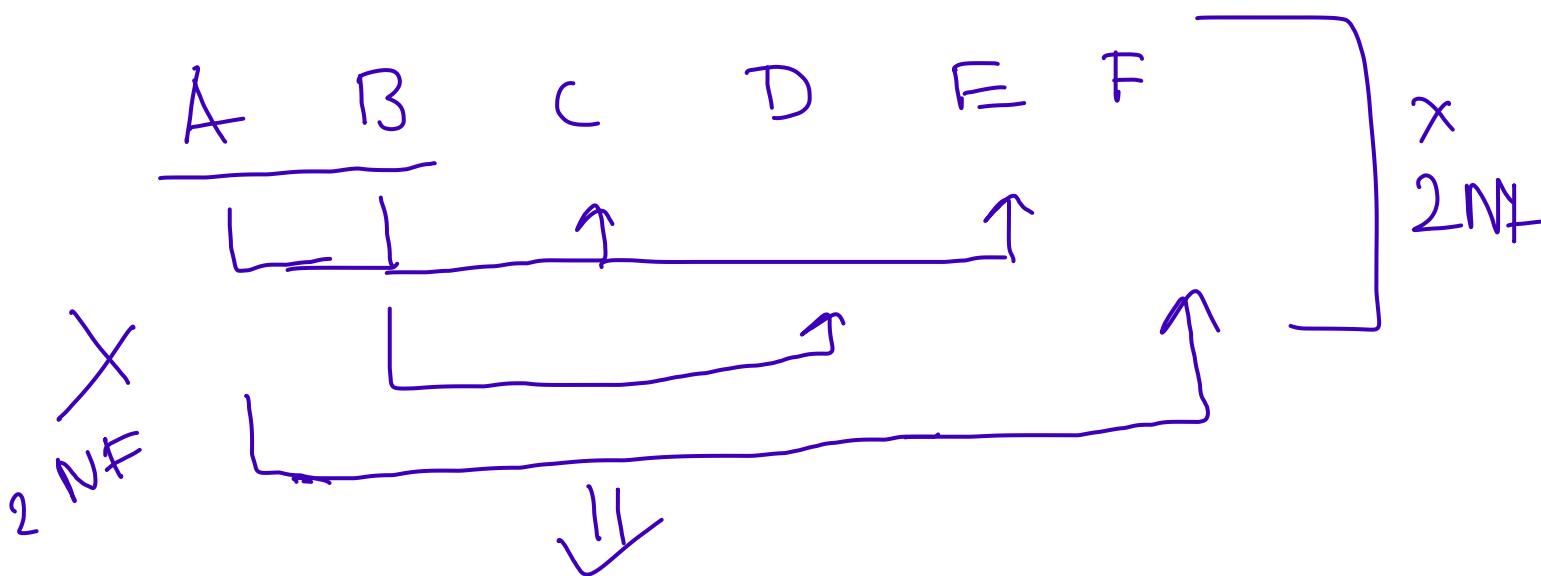
2NF

$AB \rightarrow C, B \rightarrow F, A \rightarrow F, AB \nrightarrow E$

$P.K \Rightarrow \{A, B\}^+ = \{A, B, C, D, F, E\}$

Prime attribute -

Non-prime  $\rightarrow C, D, E, F$

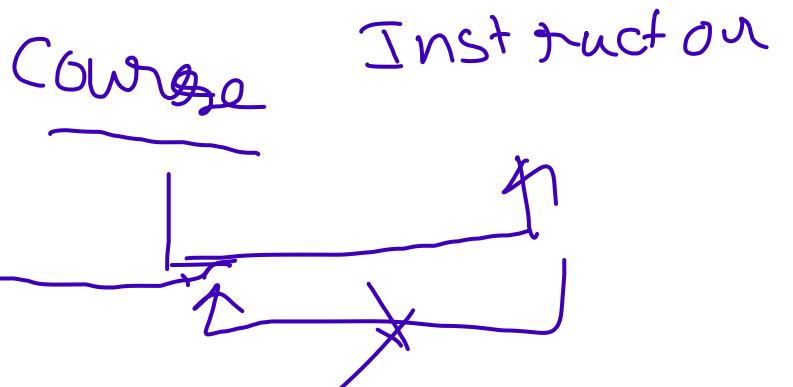
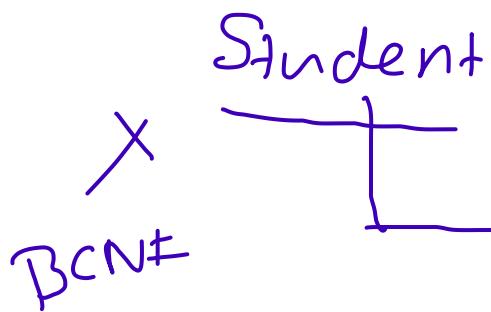


R1	A   B   C   E
	↓   ↓   ↓

R2	B   D
	↓

R3	A   F
	↓

~~(NFC BC NF)~~



P. K  $\Rightarrow$  Student, Course

