

Simplify each and state the excluded values.

$$1) \frac{m-7}{8m^2-56m}$$

$$2) \frac{m^2+m-12}{m^2-m-6}$$

Simplify each expression. Leave all answers in simplest factored form.

$$3) \frac{x^2-5x+4}{3-3x} \cdot \frac{2x^2+12x}{2x^2-8x}$$

$$4) \frac{10r^3+10r^2}{r+1} \cdot \frac{3r^2-27r}{10r^3-90r^2}$$

$$5) \frac{n^2-13n+40}{7n-35} \div \frac{n^2-16n+64}{n^2-64}$$

$$6) -\frac{4ab}{21c} \div \frac{22a^2}{14c^2}$$

$$7) \frac{\frac{3-v}{v-8}}{\frac{v-3}{v^2-16v+64}}$$

$$8) \frac{\frac{3}{x+1}}{\frac{5}{x-1}}$$

$$9) \frac{5}{3y} + \frac{6}{2xy^2}$$

$$10) \frac{2}{x-5} - \frac{6}{x+6}$$

$$11) \frac{8}{m^2-25} + \frac{9}{m-5}$$

$$12) \frac{2+\frac{1}{x}}{5-\frac{1}{x}}$$

For questions 13-14, write your answers as sentences.

13. You would like to take a special trip in a few years, and you need to save money. You deposit \$325 in an account that pays 6% interest compounded quarterly. How much money will you have after 9 years?

14. A family would like to place \$5000 in an account for 15 years to save for their child's college education. The family has two options. They can invest in an account which pays 4% interest compounded monthly or an account which pays 3.5% compounded daily. Which is the best option and how much more money would the family earn in total by choosing the best option?

Evaluate the logarithm.

15. $\log_6 36$

16. $\log_3 1$

17. $\log_4 32$

18. Rewrite $\log_9 81 = 2$ as an exponential equation. 19. Rewrite $7^3 = 343$ in log form.

Expand each expression.

20. $\log_4 15y^5$

21. $\log_6 \frac{7}{y^3}$

22. $\log_5 9y^3 \sqrt{x}$

Condense each expression.

23. $\log_6 12 - \log_6 y$

24. $3 \log_7 4x + \log_7 3y$

25. $\frac{1}{2} \log x - 2 \log z + \log y$

Solve.

26. $81^{-n-3} < 3^{2n+5}$

27. $16^{-x} = \left(\frac{1}{64}\right)^{x+1}$

28. $36^{5-2x} > \frac{1}{216}$

29. $\log_3 (y-10) = 5$

30. $\log_8 (2x+4) = \log_8 (x^2-11)$

31. $\log_3 (5x+1) = \log_3 (3x+7)$

32. $\log_{16} x = \frac{5}{4}$

33. $\log_x 27 = \frac{3}{2}$

34. $\log_6 x = 7$

35. $\log_2 32 = x + 3$

36. $\log_5 (x-3) - \log_5 8 = 2$

37. $\log_3 x + \log_3 3x = 5$

For 38-41, choose the correct answer.

38. A formula used to compute the current value of a savings account is $A = P(1+r)^n$, where A is the current value; P is the amount deposited; r is the rate of interest for 1 compounding period, expressed as a decimal; and n is the number of compounding periods. Which of the following is closest to the value of a savings account after 5 years if \$10,000 is deposited at 4% annual interest compounded yearly?

- F. \$10,400
- G. \$12,167
- H. \$42,000
- J. \$52,000
- K. \$53,782

40. If $3^x = 54$, then which of the following must be true?

- A. $1 < x < 2$
- B. $2 < x < 3$
- C. $3 < x < 4$
- D. $4 < x < 5$
- E. $5 < x$

39. What is the value of $\log_2 8$?

- A. 3
- B. 4
- C. 6
- D. 10
- E. 16

41. What is the real value of x in the equation $\log_2 24 - \log_2 3 = \log_5 x$?

- F. 3
- G. 21
- H. 72
- J. 125
- K. 243