

Jonathan Pfefferle, Task 3

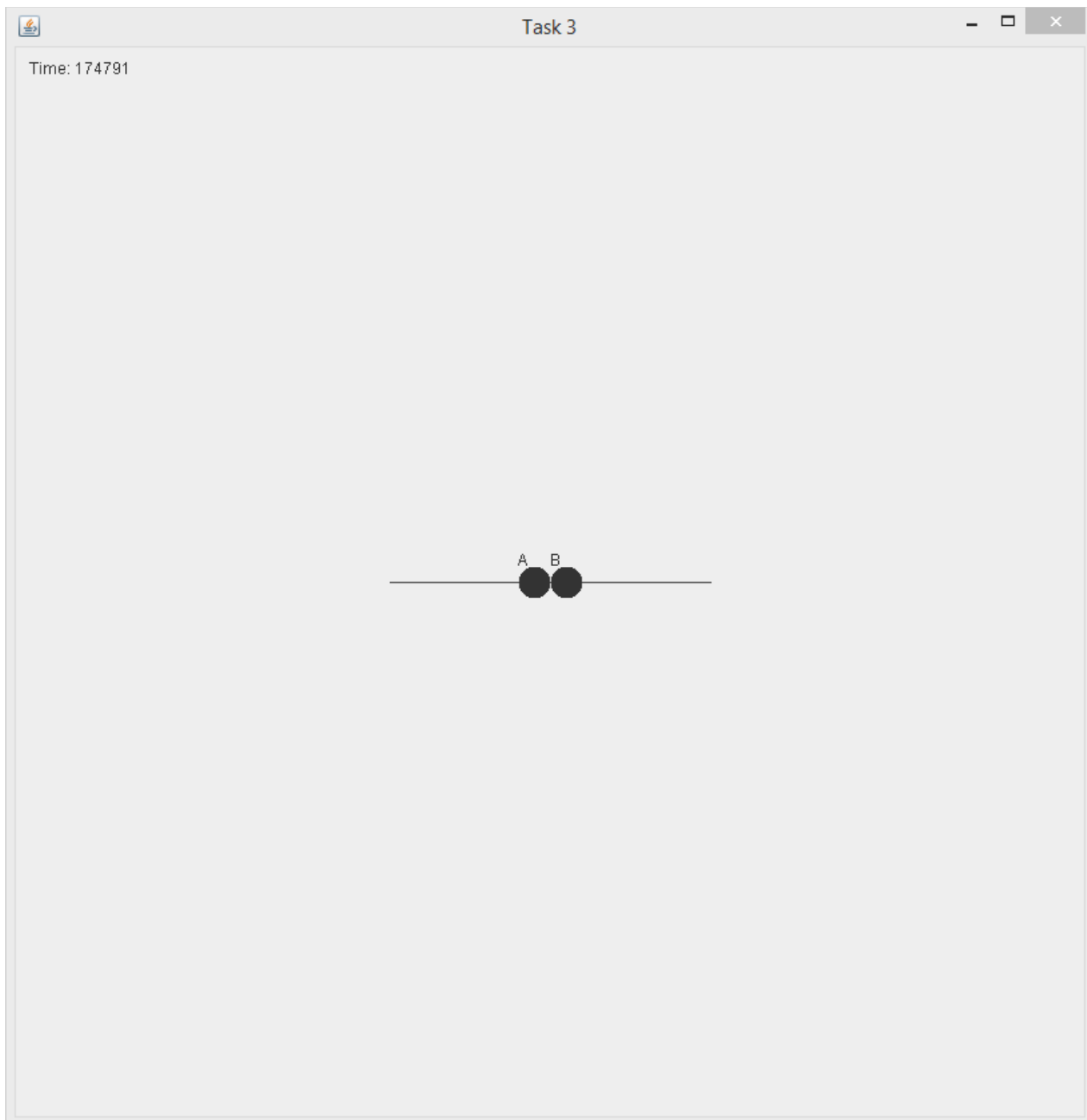
Test 1.A: Colliding Bodies A

Bodies A and B are initially stationary and are pulled toward to each other. The solution is already provided. This is a test of your analyzer only.

Procedures:

Test 1.A was run as given, no changes were made to the code.

Result: The result was a collision at the origin at time index 135000.2, as shown by the following screenshot. Analyzer data dump is on the next page, for clarity.



Test 1.A analyzer data dump.

Body: A

Time: 174791.0

Distance: 135000.2

Velocity:

Min: 5.8910514219983834E-8

Max: 2.2815948370361717E-7

Avg: 7.664457079305429E-8

Std: 2.6405682825364865E-8

Acceleration:

Min: 3.6924667988545616E-21

Max: 1.4726538211107254E-8

Avg: 1.1966205006730266E-14

Std: 1.1461529528956586E-11

Body: B

Time: 174791.0

Distance: 135000.2

Velocity:

Min: 5.8910514219983834E-8

Max: 2.2815948370361717E-7

Avg: 7.664457079305429E-8

Std: 2.6405682825364865E-8

Acceleration:

Min: 3.6924667988545616E-21

Max: 1.4726538211107254E-8

Avg: 1.1966205006730266E-14

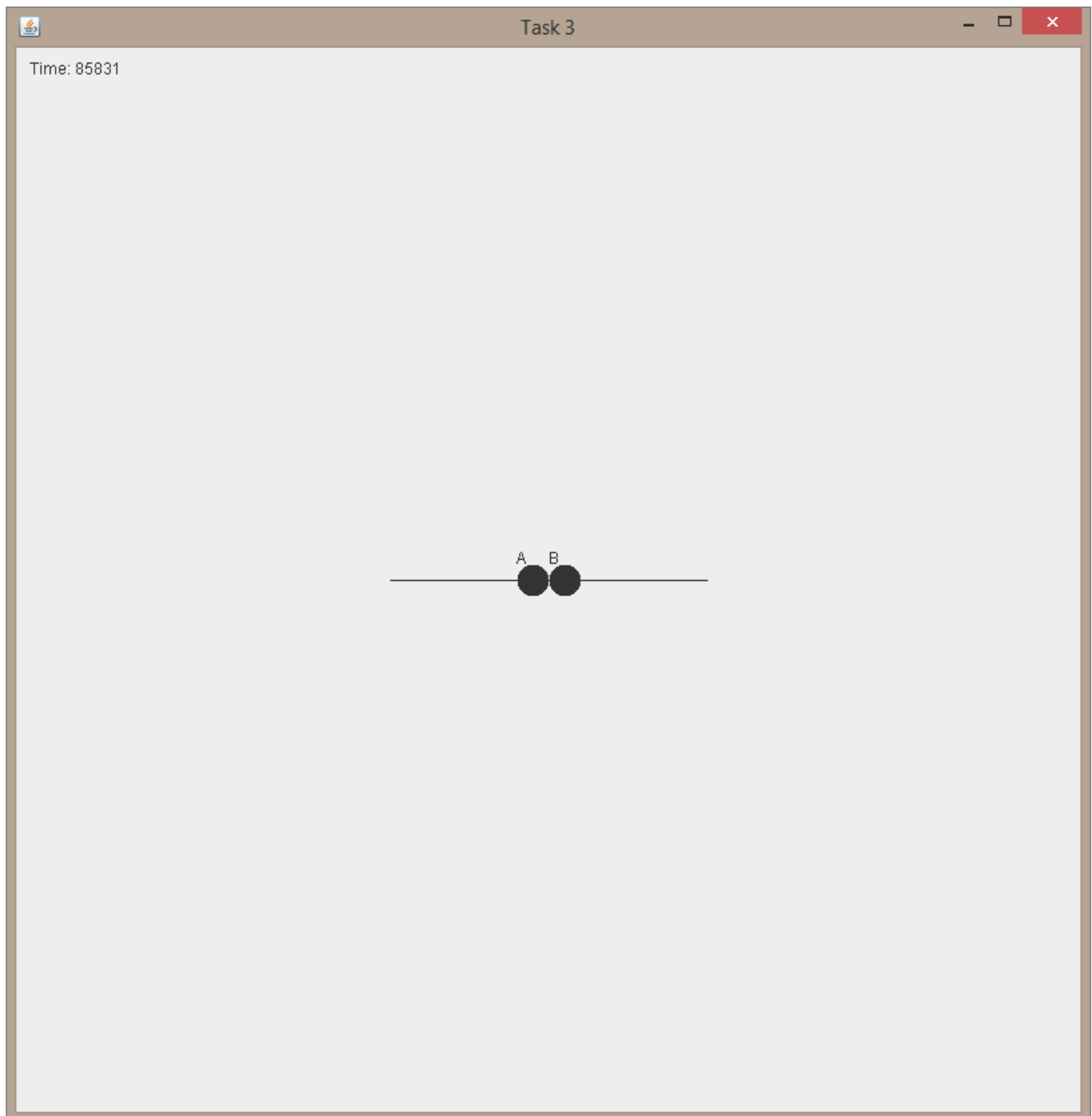
Std: 1.1461529528956586E-11

Test 1.B: Colliding Bodies B

Repeat 1.A, but they are initially moving toward each other. Choose a reasonable speed.

Procedures: Two bodies were set up as per test 1.A, but they were given an initial velocity of one unit per second towards the origin. This speed was picked because it seemed reasonable at the time, and gave a pleasing simulation visual.

Results: The result was a collision of the two bodies at the origin at time index 85831.7, as demonstrated by the below screenshot. Analyzer data dump is on the next page.



Test 1.B Analyzer data dump

Body: A

Time: 85831.7

Distance: 135000.2

Velocity:

Min: 2.774666177562345E-7

Max: 0.10000011781812645

Avg: 1.7657779375424052E-6

Std: 1.3842610063860992E-4

Acceleration:

Min: 1.3173672680690928E-23

Max: 0.025000014727993403

Avg: 4.136776459098131E-8

Std: 2.7766289251645176E-5

Body: B

Time: 85831.7

Distance: 135000.2

Velocity:

Min: 2.774666177562345E-7

Max: 0.10000011781812645

Avg: 1.7657779375424052E-6

Std: 1.3842610063860992E-4

Acceleration:

Min: 1.3173672680690928E-23

Max: 0.025000014727993403

Avg: 4.136776459098131E-8

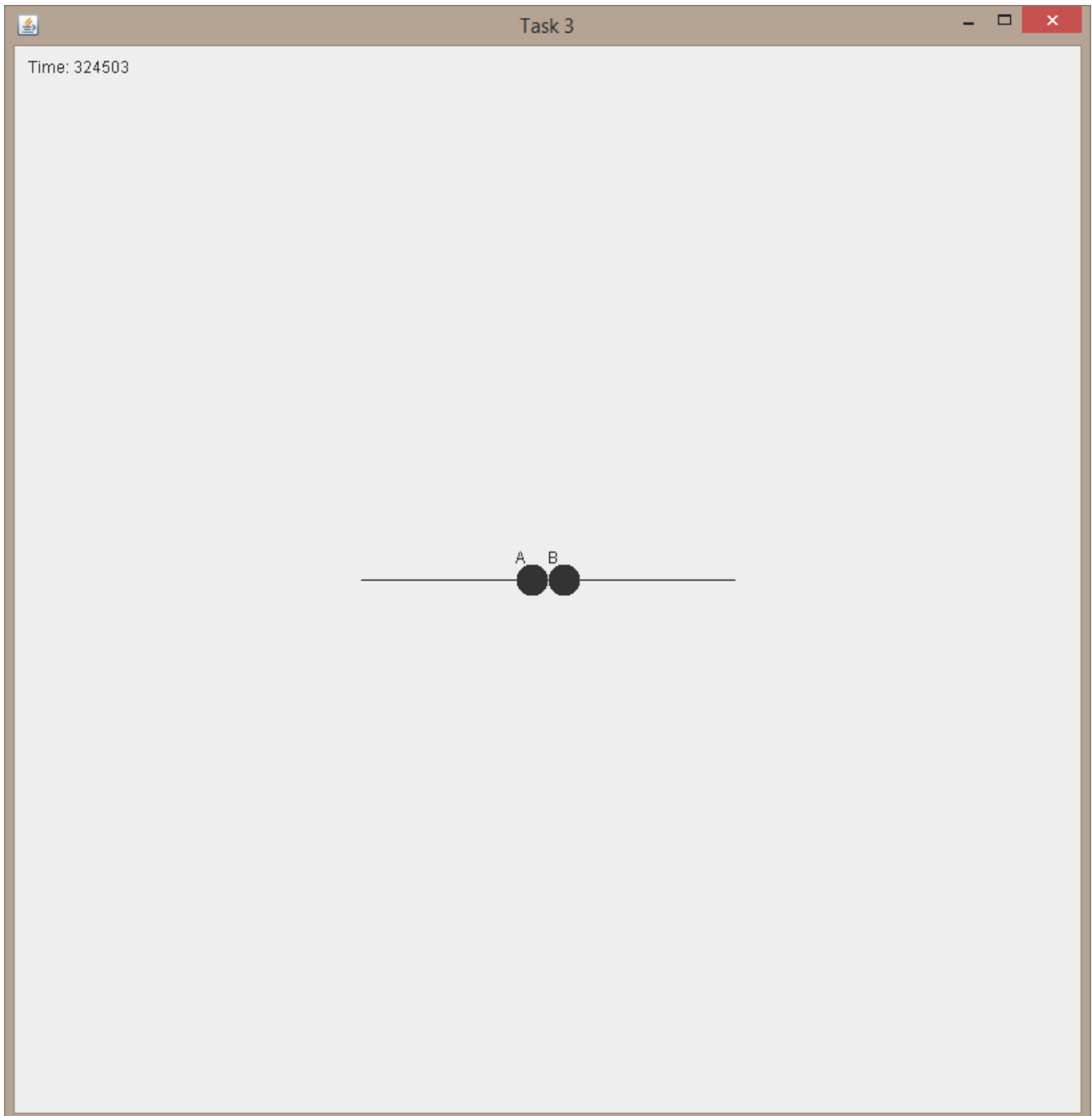
Std: 2.7766289251645176E-5

Test 1.C: Colliding Bodies C

Repeat 1.A, but they are initially moving away from each other. Choose a reasonable speed.

Procedure: Bodies were set up as per Test 1.A, but they were each given an initial velocity of 0.5 units away from the origin. This value was picked because it seemed reasonable. Even something as small as 1 unit resulted in the bodies still moving away from each other as late as time index 350,000 which did not look right.

Results: The result was a collision at the origin at time index 184435.0, as shown by the following screenshot. Analyzer dump is provided on the next page for clarity.



Test 1.C Analyzer Data Dump

Body: A

Time: 324503.9

Distance: 184435.0

Velocity:

Min: 1.2493073486944547E-14

Max: 0.04999988217605278

Avg: 2.2502638813044098E-7

Std: 3.559761666430649E-5

Acceleration:

Min: 7.878569374825392E-21

Max: 0.012499985263275448

Avg: 5.4708991800505865E-9

Std: 7.14004516982605E-6

Body: B

Time: 324503.9

Distance: 184435.0

Velocity:

Min: 1.2493073486944547E-14

Max: 0.04999988217605278

Avg: 2.2502638813044098E-7

Std: 3.559761666430649E-5

Acceleration:

Min: 7.878569374825392E-21

Max: 0.012499985263275448

Avg: 5.4708991800505865E-9

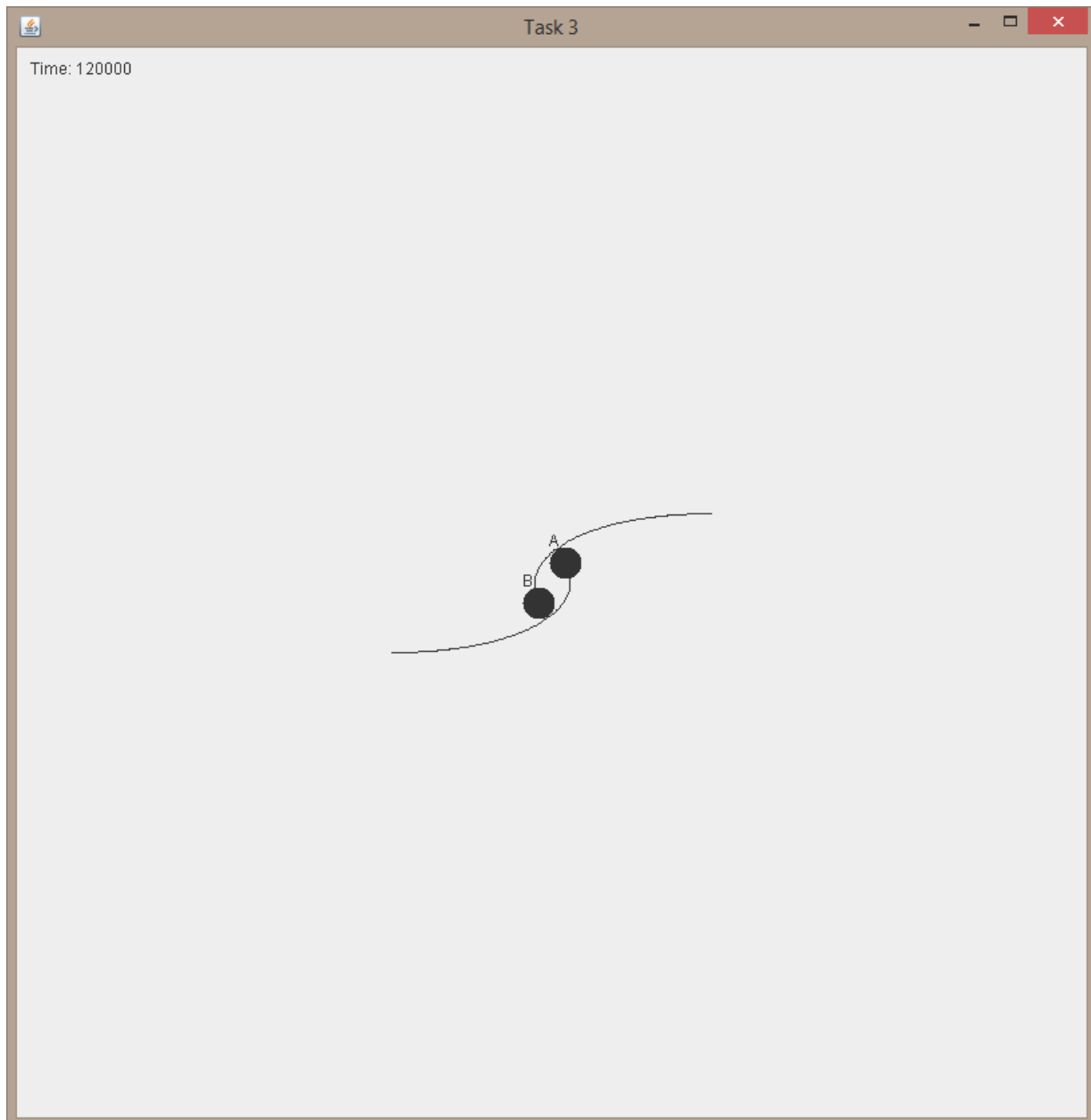
Std: 7.14004516982605E-6

Test 2.A: Passing Bodies A

Repeat 1.B, but they are on opposite parallel paths. How far apart (y) do they need to be to avoid an initial collision?

Procedure: Bodies were set up as per test 1.B, but the bodies were displaced 130,000 units along the y axis. This value was picked as experiments showed it would produce a very close approach with no actual contact. I split the displacement between both bodies (+/- 65000 each) to keep the visualization centered on the origin. As there would be no collision to terminate the simulation, I set the runToTime to 120,000 time units.

Results: The result was a close-approach and near-miss of the two bodies around time-index 100,000, as shown by the below screen shot. Analyzer data dump is on the next page as always.



Test 2.A analyzer dump:

Body: A

Time: 119999.9

Distance: 210611.4

Velocity:

Min: 2.1931735627025817E-7

Max: 0.10000009101350638

Avg: 1.3111939066458488E-6

Std: 1.1707360476186057E-4

Acceleration:

Min: 9.15911279929495E-25

Max: 0.02500001138105241

Avg: 2.958889054428063E-8

Std: 2.3482871070020377E-5

Body: B

Time: 119999.9

Distance: 210611.4

Velocity:

Min: 2.1931735627025817E-7

Max: 0.10000009101350638

Avg: 1.3111939066458488E-6

Std: 1.1707360476186057E-4

Acceleration:

Min: 9.15911279929495E-25

Max: 0.02500001138105241

Avg: 2.958889054428063E-8

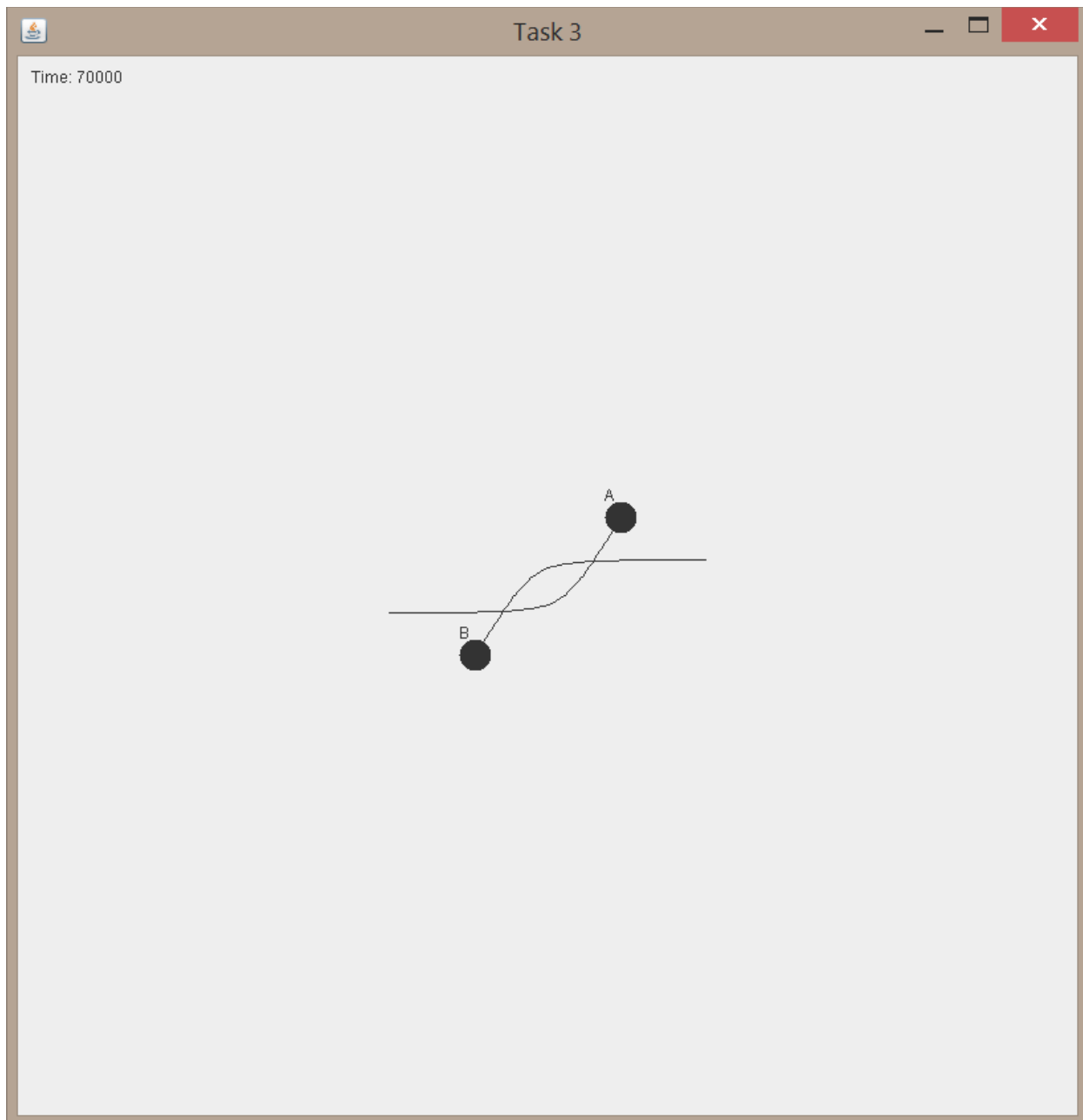
Std: 2.3482871070020377E-5

Test 2.B: Passing Bodies B

Repeat 1.B, but they are on opposite parallel paths. How fast do they need to be to avoid an initial collision? Use the same speed for both.

Procedure: The bodies were setup as per Test 1.B, but they were given a displacement on the y axis of 50,000 units from each other. This value was picked because, as per test 2.A, it will *not* cause the bodies to avoid a collision if they both start from zero speed. The bodies were then given a velocity of 3.2 unit towards the center.

Results: The two bodies made a close approach around time index 50,000, but did not collide, as shown by the below screen shot. Analyzer dump is on the next page.



Test 2.B Analyzer dump

Body: A

Time: 70000.0

Distance: 260158.7

Velocity:

Min: 4.798508551149428E-7

Max: 0.3200001130753668

Avg: 6.555797256665447E-6

Std: 4.90498225341296E-4

Acceleration:

Min: 7.09293047502089E-23

Max: 0.08000001413893183

Avg: 1.623161157150298E-7

Std: 9.838807994804406E-5

Body: B

Time: 70000.0

Distance: 260158.7

Velocity:

Min: 4.798508551149428E-7

Max: 0.3200001130753668

Avg: 6.555797256665447E-6

Std: 4.90498225341296E-4

Acceleration:

Min: 7.09293047502089E-23

Max: 0.08000001413893183

Avg: 1.623161157150298E-7

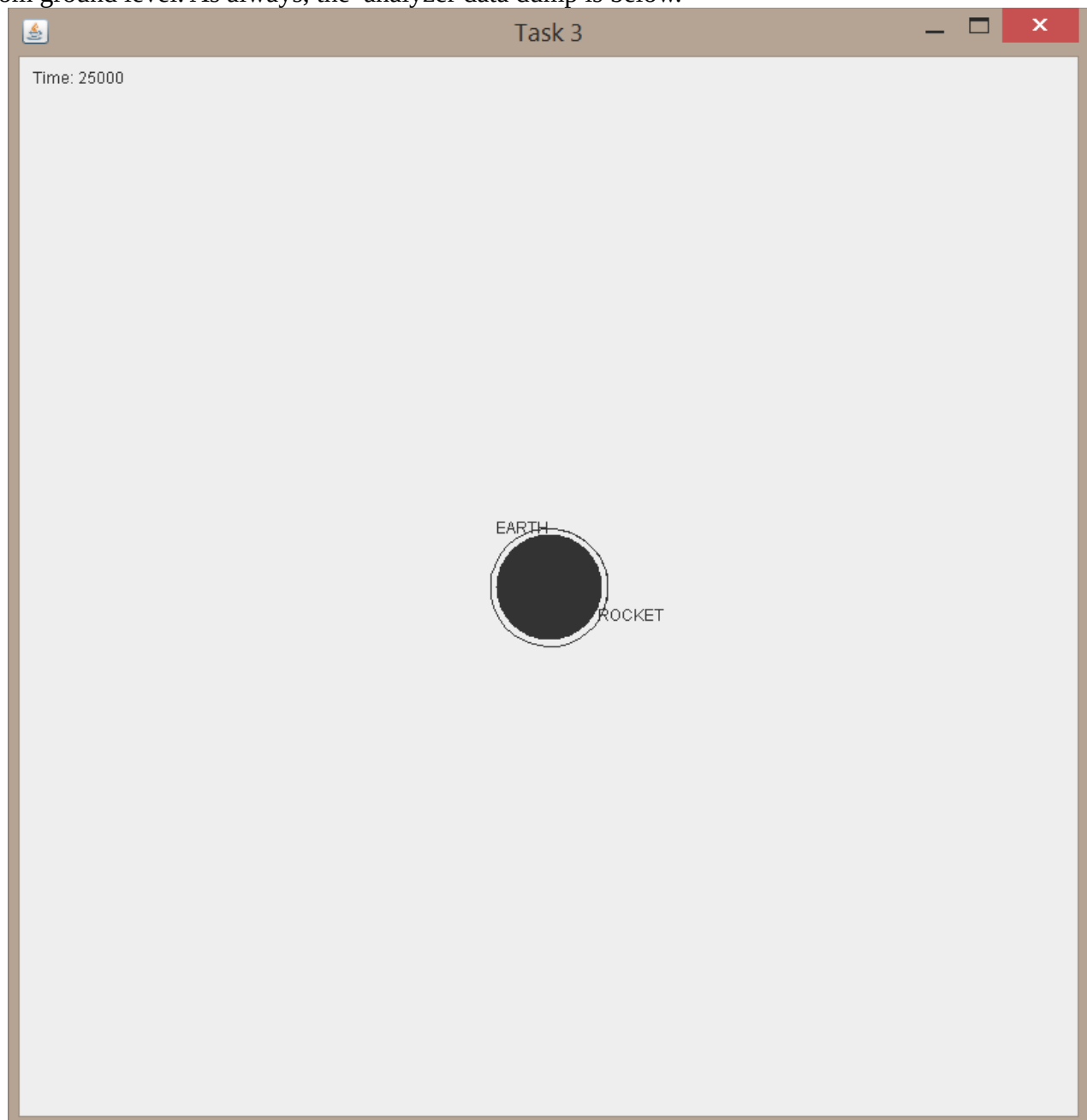
Std: 9.838807994804406E-5

Test 3.A: Launch to Orbit A

The rocket is launched on a tangent to Earth. How fast does the rocket need to go to reach a reasonable orbit without using thrusters? What is the issue in the results?

Procedure: The given setup for Test 3.A was used, but the rocket was given an initial velocity of 19 units along the positive x axis.

Results: The rocket achieved a nice circular orbit, as shown by the below screenshot. However, this doesn't really approximate a true rocket launch, as the rocket's simply "Godzilla'd"—to borrow a bit of terminology from Dr. Tappan—into the correct height and speed, instead of simulating a full launch from ground level. As always, the analyzer data dump is below.



Task 3.A Analyzer data dump.

Body: EARTH

Time: 25000.0

Distance: .6

Velocity:

Min: 6.014798695046579E-17

Max: 1.298178782609765E-10

Avg: 3.0242863001163574E-11

Std: 2.2187184358807026E-11

Acceleration:

Min: 2.5060762586456865E-22

Max: 1.622723476675035E-11

Avg: 9.219191555154073E-17

Std: 3.339458182031475E-14

Body: ROCKET

Time: 25000.0

Distance: 470208.3

Velocity:

Min: 7.468017297781742E-6

Max: 1.9000000021926073

Avg: 9.86270239071795E-5

Std: 0.004872693536593374

Acceleration:

Min: 1.2877481079834828E-16

Max: 0.47500000028339484

Avg: 2.698511888002026E-6

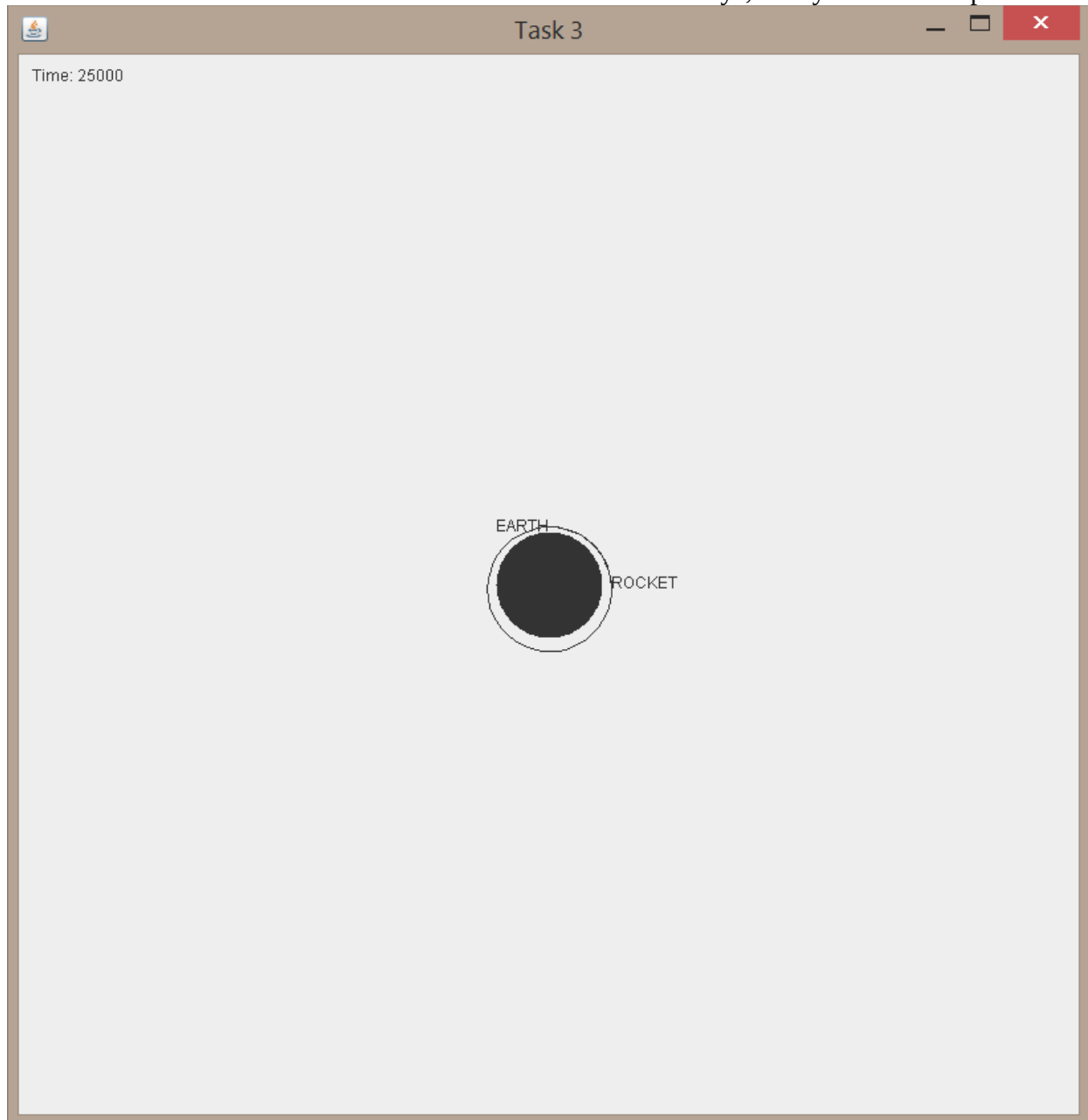
Std: 9.775187582556526E-4

Test 3.B: Launch to Orbit B

Repeat 3.A, but thrusters are allowed

Procedure: The bodies were set up as per Test 3.A, but the rocket was given an initial velocity of 10 along the positive x axis. This speed was chosen because—on its own—it will not allow the rocket to complete an orbit, but it will keep the rocket from plowing into the earth long enough for engine burns to accelerate the rocket into orbit. Burns were then scheduled every quarter-time step between time-indices .25 and 1.75.

Result: The rocket was inserted into an orbit that, while less pretty and circular than in test 3.A, was achieved in a more realistic manner. See screenshot below. As always, Analyzer data dump is below.



Test 3.B Analyzer data dump.

Body: EARTH

Time: 25000.0

Distance: .6

Velocity:

Min: 1.1534634128152195E-16

Max: 1.298178783309816E-10

Avg: 3.0021789079601996E-11

Std: 2.158521913116032E-11

Acceleration:

Min: 4.498802201400264E-22

Max: 1.6227234717746767E-11

Avg: 9.219210082444598E-17

Std: 3.339458168695143E-14

Body: ROCKET

Time: 25000.0

Distance: 460356.8

Velocity:

Min: 7.3213043967687366E-6

Max: 1.0000000072461779

Avg: 8.900628951505426E-5

Std: 0.0027721023188621253

Acceleration:

Min: 1.7528416459727975E-16

Max: 0.2499999997683941

Avg: 1.3969545747611433E-6

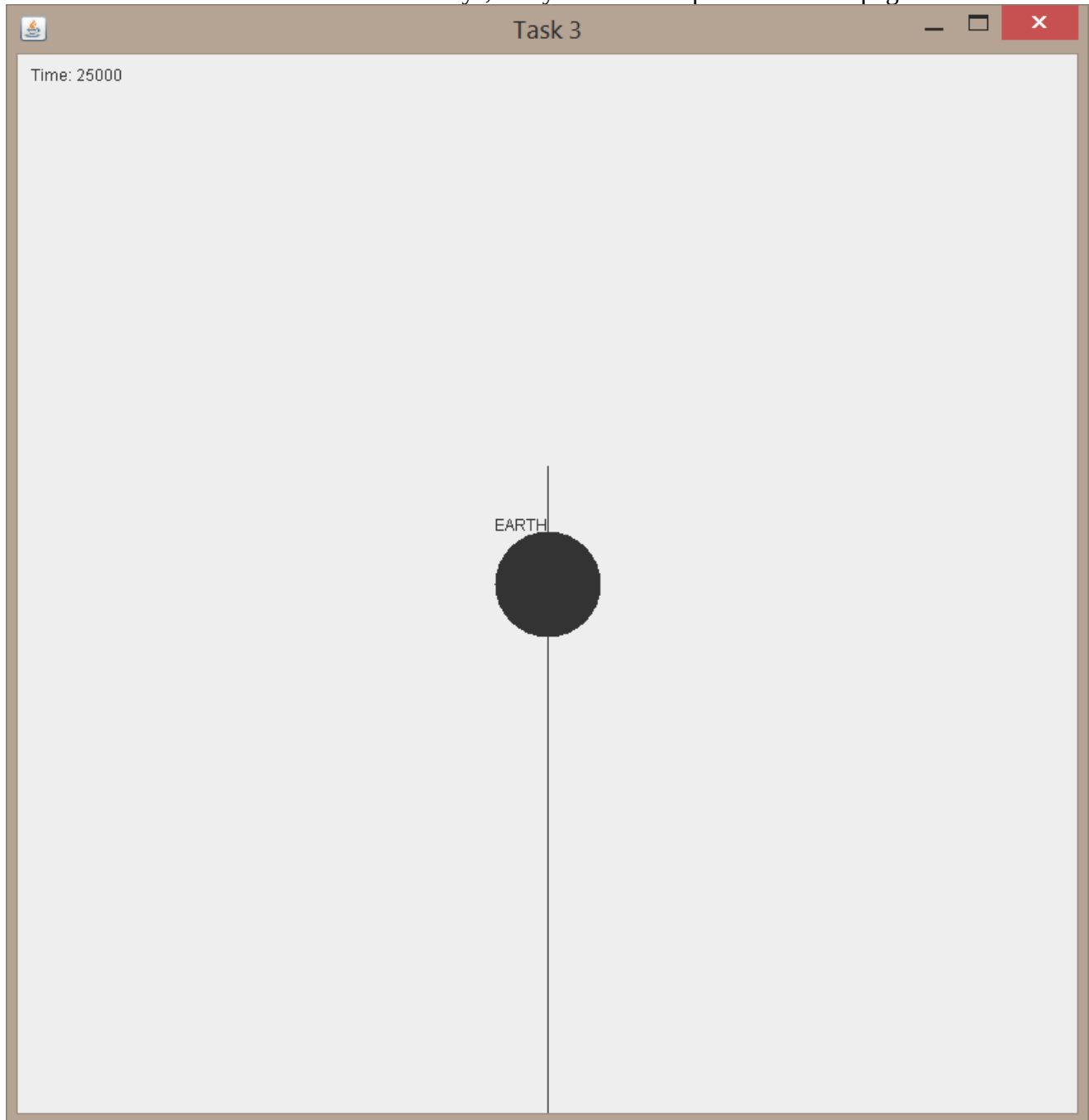
Std: 5.136484927228092E-4

Test 3.C: Launch to Orbit C

Repeat 3.A but straight away from Earth, what happens?

Procedure: The bodies were setup as per Test 3.A, but instead of assigning a velocity along the positive X axis, the rocket was assigned a velocity of equal magnitude along the positive Y axis.

Result: The rocket launched up for a small distance, then fell back to earth. Then, because collisions were turned off, it fell *through* the earth and got spat out the other side at an unreasonably high speed, as detailed in the screenshot below. As always, analyzer data dump is on the next page.



Test 3.C analyzer data dump.

Body: EARTH

Time: 25000.0

Distance: 13.8

Velocity:

Min: 2.220241874750335E-11

Max: 1.0747681058536218E-9

Avg: 2.7968274548183915E-10

Std: 3.661913342932719E-10

Acceleration:

Min: 8.205967334422214E-28

Max: 1.622835567912645E-11

Avg: 9.22985116169632E-17

Std: 3.3397249390105846E-14

Body: ROCKET

Time: 25000.0

Distance: 13452014.4

Velocity:

Min: 4.178654214070793E-11

Max: 1.8998701866075862

Avg: 3.385438019432607E-4

Std: 0.004881939966856969

Acceleration:

Min: 1.052242117485573E-15

Max: 0.4749837716444745

Avg: 2.698419653872982E-6

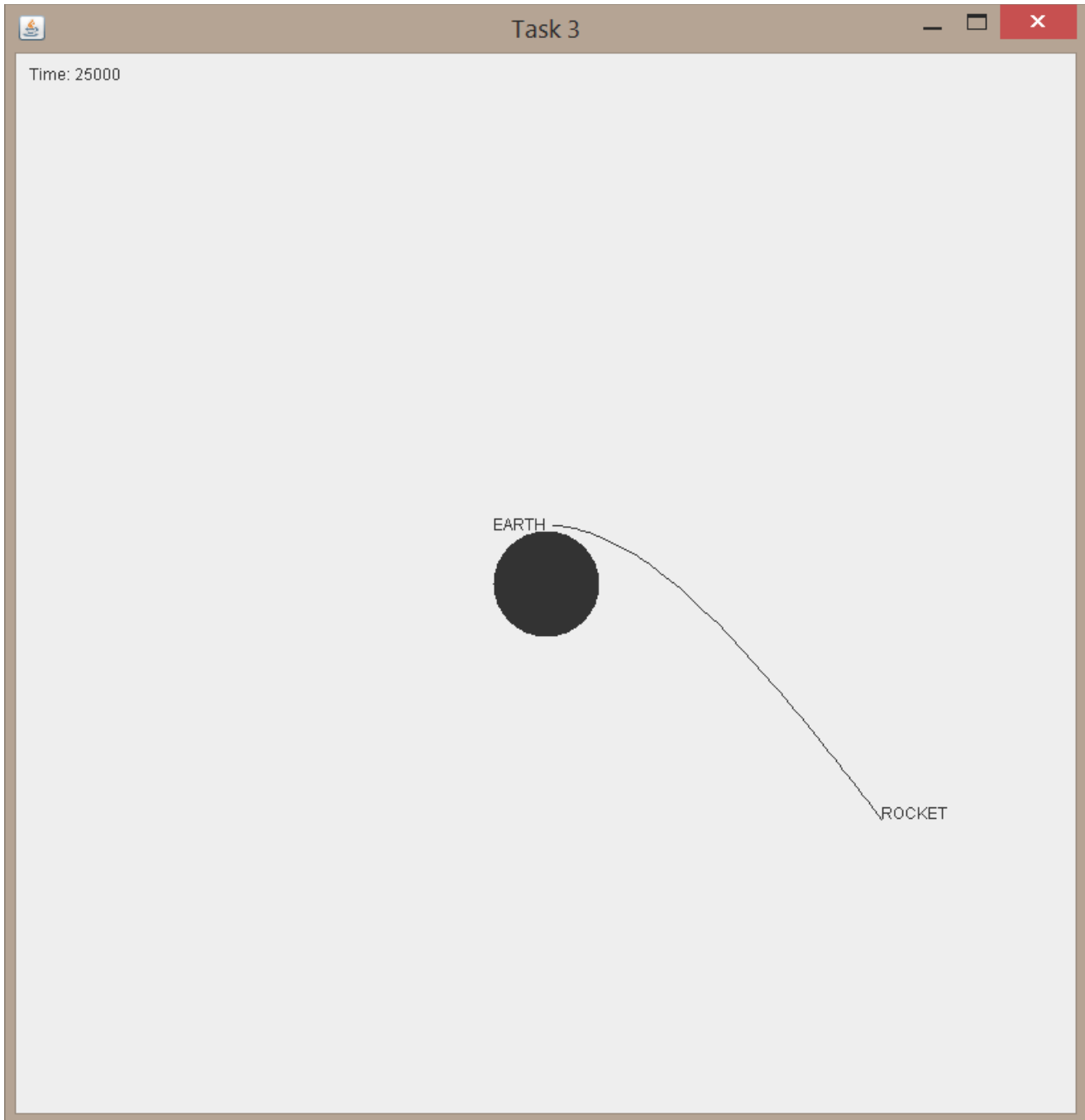
Std: 9.774853604222755E-4

Test 4: Leave Orbit

The rocket is already in orbit around Earth. How fast does the rocket need to go to break orbit? Set the initial velocity; do not use thrusters.

Procedure: The bodies were setup as per Test 3.A, but the rocket was given an initial velocity of 28 units along the positive X axis.

Result: The rocket left orbit as depicted in the screenshot below. As always, the analyzer data dump is on the next page.



Test 4 analyzer data dump

Body: EARTH

Time: 25000.0

Distance: .5

Velocity:

Min: 9.051523658583E-12

Max: 1.2981787814751999E-10

Avg: 2.3323773580898946E-11

Std: 1.5424949352200888E-11

Acceleration:

Min: 1.351417686631858E-22

Max: 1.622723484616993E-11

Avg: 9.219665317987815E-17

Std: 3.339458202215838E-14

Body: ROCKET

Time: 25000.0

Distance: 432174.6

Velocity:

Min: 5.2390033606893735E-6

Max: 2.799999999704953

Avg: 1.358434571762315E-4

Std: 0.007180934823510769

Acceleration:

Min: 1.0383584454504852E-16

Max: 0.7000000006380263

Avg: 3.976754391825181E-6

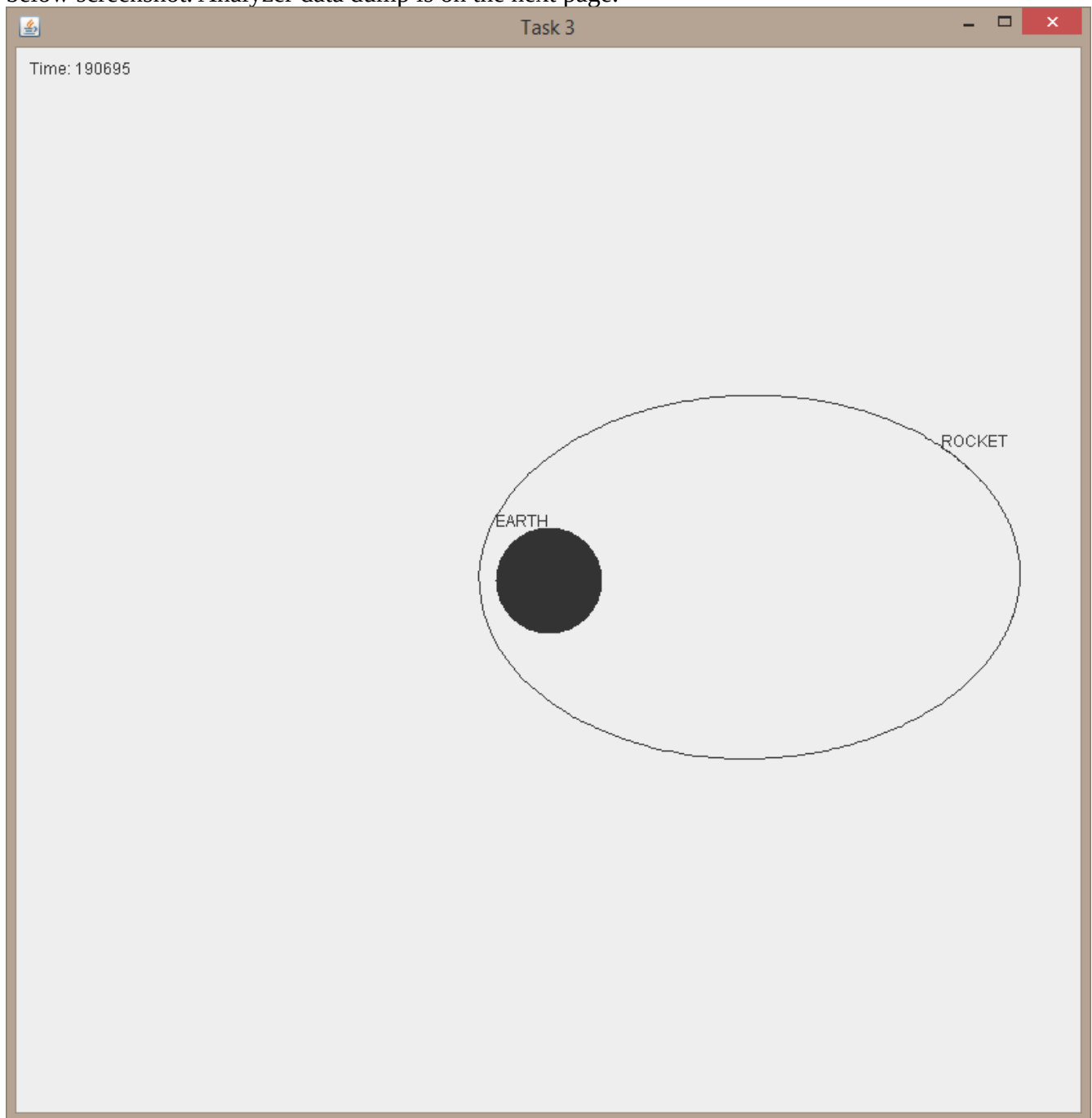
Std: 0.0014405539601297377

Test 5.A: Enter Orbit

Set the rocket up to enter a reasonable orbit around Earth.

Procedure: The given setup was used, but the rocket was given an initial velocity of -3 units along the x axis and 3 units along the y axis.

Results: The rocket was captured into an eccentric but complete orbit around the planet, as seen in the below screenshot. Analyzer data dump is on the next page.



Test 5.A Analyzer data dump.

Body: EARTH

Time: 700000.0

Distance: 5.4

Velocity:

Min: 8.268061338096435E-20

Max: 4.156904225715437E-12

Avg: 4.597225120340877E-13

Std: 6.90077907154872E-13

Acceleration:

Min: 1.3800336726011667E-30

Max: 2.8874901903901904E-13

Avg: 5.858732499789836E-20

Std: 1.1229821181935367E-16

Body: ROCKET

Time: 700000.0

Distance: 5291440.6

Velocity:

Min: 4.844745731331548E-8

Max: 0.4242652572082897

Avg: 1.2226960352990476E-6

Std: 2.0566579302929688E-4

Acceleration:

Min: 4.192595319362459E-26

Max: 0.10606616574224723

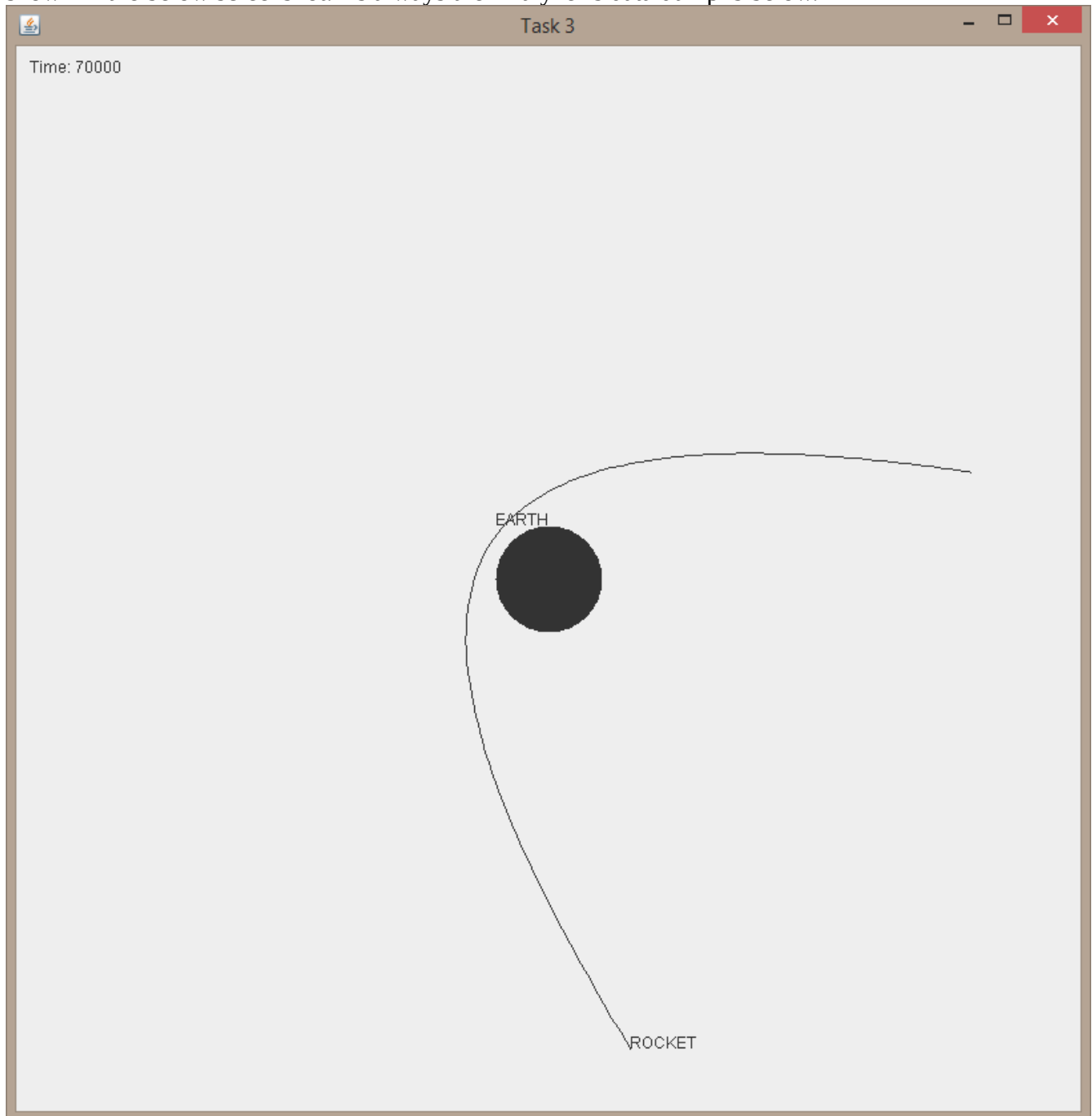
Avg: 2.1520278567606323E-8

Std: 4.125050452510635E-5

Test 5.B: Miss Orbit

Repeat 5.A, but with an initial speed too high to be reasonably captured. (The rocket may assume a comet-like orbit eventually, but do not simulate that far.)

Procedure: The setup was the same as in 5.A, but the rocket was given an initial velocity of -10 along the x-axis and 1.5 along the y-axis. This resulted in a very-close approach followed by escape, as shown in the below screenshot. As always the Analyzer's data dump is below.



Test 5.B Analyzer data dump.

Body: EARTH

Time: 70000.0

Distance: .9

Velocity:

Min: 1.1584791427750982E-12

Max: 7.026369249530509E-12

Avg: 3.4154716722021116E-12

Std: 1.6534093616908043E-12

Acceleration:

Min: 2.5514712574110168E-27

Max: 2.887480168965174E-13

Avg: 5.858981726969099E-19

Std: 3.5511672318725857E-16

Body: ROCKET

Time: 70000.0

Distance: 993910.8

Velocity:

Min: 1.3903754384236642E-6

Max: 1.0111895539587397

Avg: 2.1772224391999313E-5

Std: 0.0015499558221308417

Acceleration:

Min: 2.7539863224711277E-22

Max: 0.25279712185337605

Avg: 5.129129953748795E-7

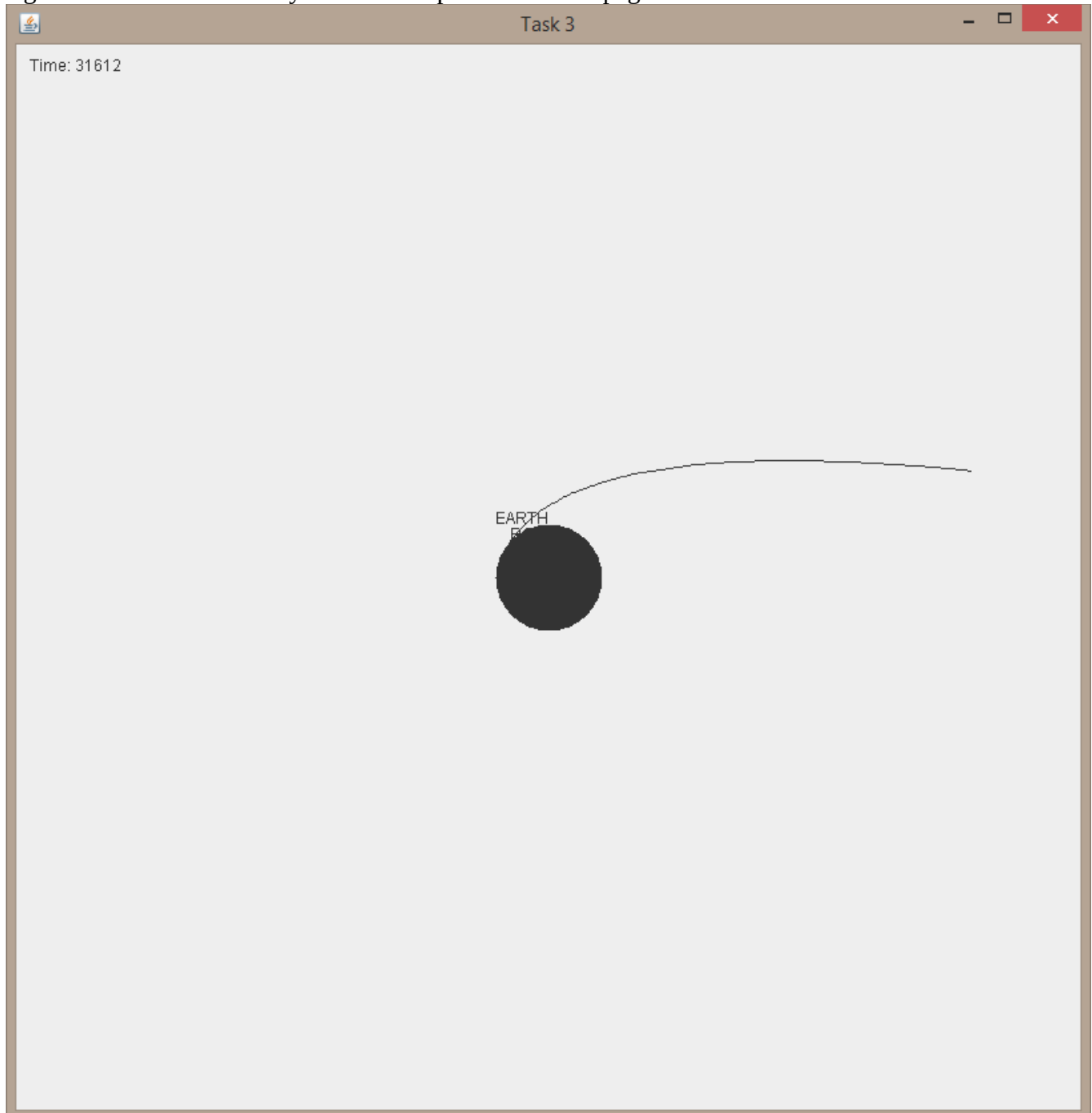
Std: 3.1090273799852557E-4

Test 6.A: Bad Day in Dinosaur City A

Assume *Earth is full of dinosaurs and a meteor is coming. Set up and execute a glancing (tangential) blow.*

Procedure: The simulation is set-up as per test 5.B, but the rocket (or rock, in this case) is given an initial velocity of -10 along the x-axis and 1 along the y-axis.

Results: A tangential impact was recorded at time index 31612, as shown by the screenshot below. Our simulation doesn't account for post-collision events, but it's reasonable to assume there would be a significant event. The analyzer data dump is on the next page.



Test 6.A Analyzer data dump.

Body: EARTH

Time: 31612.7

Distance: .2

Velocity:

Min: 1.158501746226873E-12

Max: 7.784130684970761E-12

Avg: 2.480282084792073E-12

Std: 1.5168969376185673E-12

Acceleration:

Min: 4.9341031631567315E-24

Max: 2.887479999107048E-13

Avg: 1.2973356192566506E-18

Std: 5.284323001295515E-16

Body: ROCK

Time: 31612.7

Distance: 456656.2

Velocity:

Min: 6.874791896451609E-6

Max: 1.0049897362959228

Avg: 4.4278153083345905E-5

Std: 0.002292072415338797

Acceleration:

Min: 6.6938842910849835E-22

Max: 0.2512471623084379

Avg: 1.1287816646066387E-6

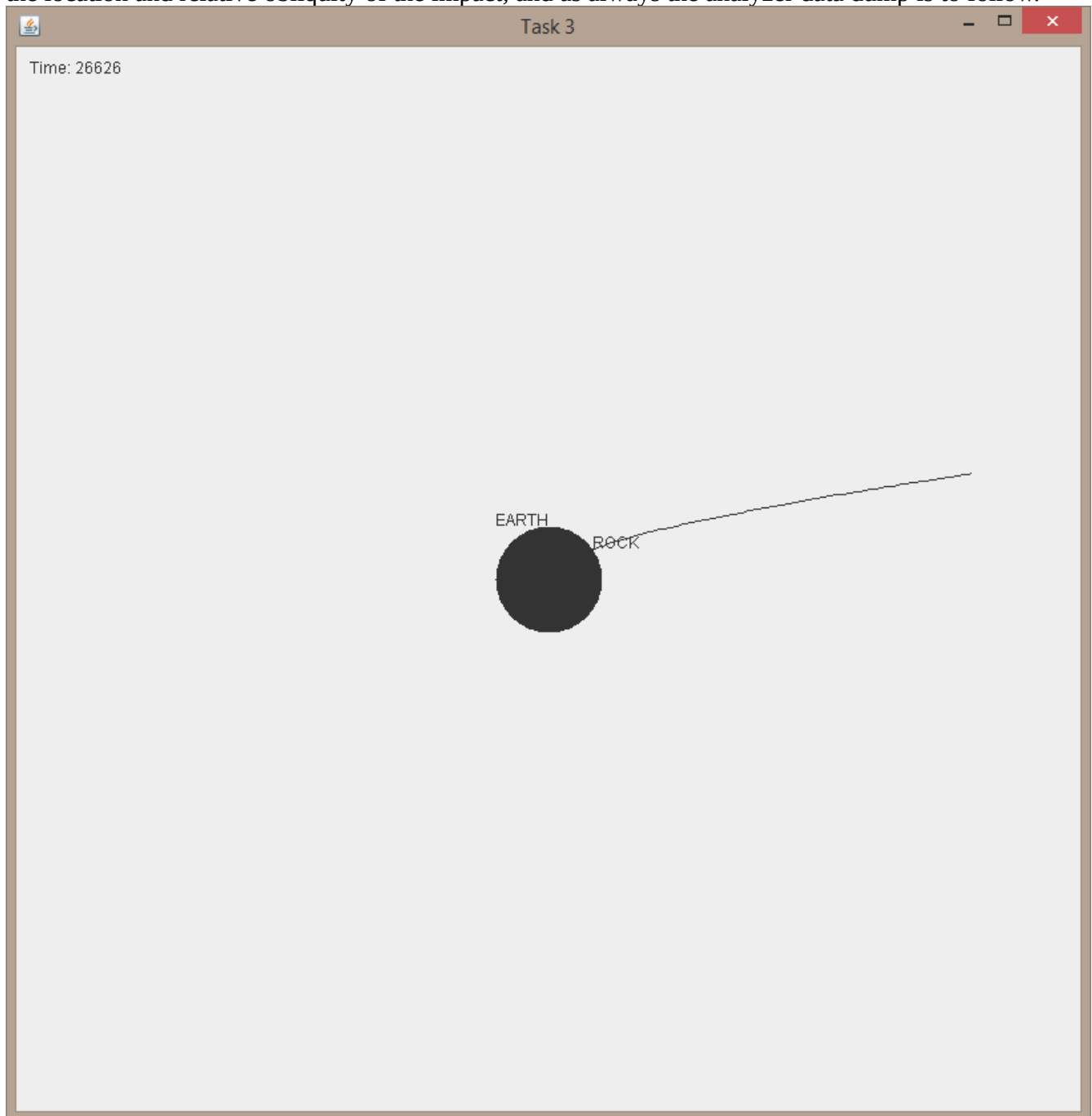
Std: 4.5980304996880503E-4

Test 6.B: Bad Day in Dinosaur City B

Repeat 6.A, but use a direct hit (i.e., perpendicular to Earth.)

Procedure: The simulation is set-up as per Test 6.A, but the rock's initial velocity is changed to -10 along the x-axis and -1.5 along the y-axis to ensure a square hit.

Results: The rock impacted earth at time-index 26626 in what we can only assume was a major emotional event for many denizens of dinosaur city (dinozens, if you will.) A screenshot below shows the location and relative obliquity of the impact, and as always the analyzer data dump is to follow.



Test 6.B Analyzer data dump

Body: EARTH

Time: 26626.1

Distance: .1

Velocity:

Min: 1.1586125760151638E-12

Max: 6.8193083830557264E-12

Avg: 2.188982386543865E-12

Std: 1.137180903092237E-12

Acceleration:

Min: 5.2465771842394825E-24

Max: 2.8874791498199376E-13

Avg: 1.5403011302908085E-18

Std: 5.7579280783946235E-16

Body: ROCK

Time: 26626.1

Distance: 366069.6

Velocity:

Min: 7.578886346951287E-6

Max: 1.0111897201756366

Avg: 5.180667586954646E-5

Std: 0.0025128421092343255

Acceleration:

Min: 5.675030255083636E-22

Max: 0.2527971426302867

Avg: 1.3484511880850532E-6

Std: 5.041036836184285E-4

Test 7: Apollo Program

Recreate a one-way moon mission:

Test 7 was not attempted, as I am not a grad student.