Student's Manual for Programming Methodology with C++

Paul Kim

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Part I Algorithms

Time Complexity Analysis

- 1. The running time of an algorithm is relevent to the amount of input. Therefore the running time is a function of the amount of input: T(n)
- 2. Definitions of Time Complexity: with a positive constant *c*,
 - 1) Big-O: $T(n) \ge c \times f_O(n) \Rightarrow T(n) = O(f_O(n))$ Best-case scenarios can be described via Big-O functions.
 - 2) Big-Omega: $T(n) \le c \times f_{\Omega}(n) \Rightarrow T(n) = \Omega\left(f_{\Omega}(n)\right)$ Worst-case scenarios can be described via Big-Omega functions.
 - 3) Big-Theta: $T(n) \ge c \times f(n)$ and $T(n) \le c' \times f(n) \Leftrightarrow T(n) = O(f(n)) = \Omega(f(n)) \Rightarrow T(n) = \Theta(f(n))$ Best- and Worst-case scenarios are the same in Big-Theta functions.
 - 4) Small-O: $T(n) = O(f_o(n)) \neq \Theta(f_o(n)) \Rightarrow T(n) = o(f_o(n))$

Constants are ignored, and only the highest degree of the polynomial's monomials are relevant to Time Complexity Analysis.

- 3. Running Time Calculations
 - 1) Summations for Loops: One loop sequence of running time f(i) is equivalent to:

$$T(n) = \sum_{i=1}^{n} f(i)$$

Two loop sequences of running time f(i, j) is equivalent to:

$$T(n) = \sum_{j=1}^{n} \sum_{i=1}^{n} f(i, j)$$

- 2) Selective Controls: Worst-case scenario, $T(n) = \max(T_1(n), T_2(n), \cdots)$. Best-case = minimum.
- 3) Recursion: T(n) = f(T(n')) (점화식)

Finding the Maximum Subarray Sum

The objective of this challenge is to find the maximum value of the sum of elements in a subarray of a given array. If all integers are negative, said maximum value is the sum of a subarray equivalent to the 'empty set', which is zero.

2.1 Cubic Brute Force Algorithm

```
int max_sum1(int* arr, int arrsize) {
    int maxSum = 0;
    for (int i = 0; i < arrsize; i++) {
        for (int j = i; j < arrsize; j++) {
            int thisSum = 0;
            for (int k = i; k <= j; k++) thisSum += arr[k];
            if (maxSum < thisSum) maxSum = thisSum;
        }
} return maxSum;
}</pre>
```

This algorithm utilises three loops and a function of constant time in the innermost loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} \sum_{j=i}^{n} \sum_{k=i}^{j} 1 = O(n^3)$$

Obviously this method is quite wasteful in both memory and timekeeping. The following two algorithms are substantial progessions from this algorithm:

2.2 Quadratic Brute Force Algorithm

```
int max_sum2(int* arr, int arrsize) {
    int maxSum = 0;
    for (int i = 0; i < arrsize; i++) {
        int iSum = 0;
        for (int j = i; j < arrsize; j++) {
            iSum += arr[j];
            if (maxSum < iSum) maxSum = iSum;
        }
    } return maxSum;
}</pre>
```

This algorithm utilises two loops and a function of constant time in the innermost loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} \sum_{j=i}^{n} 1 = O(n^2)$$

2.3 Divide and Conquer

```
int max_sum3(int* arr, int left, int right) {
        if (left >= right) return arr[left];
31
        else { int hereMax = 0;
32
            int leftSum = max_sum3(arr, left, ((left + right) / 2) - 1);
            int rightSum = max_sum3(arr, ((left + right) / 2) + 1, right);
34
            if (leftSum >= rightSum) hereMax = leftSum;
35
            else hereMax = rightSum;
36
            int leftMax = arr[(left + right) / 2], leftTemp = 0;
            int rightMax = arr[(left + right) / 2], rightTemp = 0;
            for (int i = (left + right) / 2; i >= left; i--) {
                leftTemp += arr[i];
                if (leftMax < leftTemp) leftMax = leftTemp;</pre>
41
            } for (int i = (left + right) / 2; i <= right; i++) {</pre>
                rightTemp += arr[i];
                 if (rightMax < rightTemp) rightMax = rightTemp;</pre>
44
            } int midSum = leftMax + rightMax - arr[(left + right) / 2];
45
            if (hereMax < midSum) hereMax = midSum;</pre>
            return hereMax;
47
        }
   }
```

This algorithm utilises a divisive recursion and selection controls of constant time within each recursion. Therefore, the time complexity analysis goes:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^kT\left(\frac{n}{2^k}\right) + nk, \ \therefore T(n) = 2^{\log_2 n}T(1) + n\log_2 n = n\log_2 n + \varepsilon n = O(n\log n)$$

While these two algorithms are quite effective compared to Cubic Brute Force, this last algorithm manages to provide the fastest solution possible:

2.4 Kadane's Algorithm: A Linear, Incremental Solution

```
int max_sum4(int* arr, int arrsize) {
    int maxSum = arr[0], thisSum = 0;
    for (int i = 0; i < arrsize; i++) {
        thisSum += arr[i];
        if (thisSum > maxSum) maxSum = thisSum;
        else if (thisSum < 0) thisSum = 0;
    } return maxSum;
}</pre>
```

This algorithm utilises one loop and a function of constant time in the loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} 1 = O(n)$$

Since, essentially, the challenge requires a system to read each data at least once, the O(n) function above is obviously the best solution.

Various Ways of Sorting

The objective of this callenge is sorting given algebraic (in this case, double) elements of an aray in incrasing order. Some elements may be of equal value.

3.1 Quick Sort

```
double pivot = arr[begin];
        int i = begin, j = end;
        while (i <= j) {
            while (arr[i] < pivot) i++;</pre>
            while (arr[j] > pivot) j--;
            if (i <= j) {
10
                 swap(arr[i], arr[j]);
                 i++; j--;
        } if (begin < j) quicksort(arr, begin, j);</pre>
        if (end > i) quicksort(arr, i, end);
15
    }
16
17
    int main(int argc, char *argv[]) {
87
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
        double *quick_arr = new double[2500];
        for (int i = 0; i < 2500; i++) quick_arr[i] = input_array[i];</pre>
        quicksort(quick_arr, 0, 2499);
        if (check(quick_arr)) cout << "Quicksort Validated" << endl;</pre>
120
        return 0;
121
   }
```

Quick Sort is a recursive algorithm that does the following:

- 1. Choose a "pivot" element: Line 6
- 2. Swap elements that are larger than the pivot with elements that are smaller but on the righthand side of the chosen element: Lines 8:14
- 3. Continue until all elements are sorted, then recursively proceed with the left and right subarrays of the pivot: Lines 15, 16

Using two half-recursions results in the following time complexity analysis:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^k T\left(\frac{n}{2^k}\right) + kn = O(n\log n)$$

3.2 Merge Sort

```
if (begin < end) {
            int centre = begin + (end - begin) / 2;
            mergesort(arr, begin, centre);
21
            mergesort(arr, centre + 1, end);
22
            int n1 = centre - begin + 1;
23
            int n2 = end - centre;
24
            double* L = new double[n1 + 1];
            double* R = new double[n2 + 1];
            for (int i = 0; i <= n1 - 1; i++) L[i] = arr[begin + i];
            for (int j = 0; j \le n2 - 1; j++) R[j] = arr[centre + j + 1];
            L[n1] = (double)INT_MAX;
29
            R[n2] = (double)INT_MAX;
            int a = 0, b = 0;
            for (int k = begin; k \le end; k++) {
32
                 if (L[a] <= R[b]) arr[k] = L[a++];
33
                 else arr[k] = R[b++];
34
            }
35
        }
    }
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
        double *merge_arr = new double[2500];
        for (int i = 0; i < 2500; i++) merge_arr[i] = input_array[i];</pre>
        mergesort(merge_arr, 0, 2499);
        if (check(merge_arr)) cout << "Mergesort Validated" << endl;</pre>
        return 0;
120
    }
121
```

Merge Sort is also a recursive algorithm that depends on two half-recursions, so the time complexity analysis goes:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^kT\left(\frac{n}{2^k}\right) + kn = O(n\log n)$$

3.3 Insertion Sort

```
void insertionsort(double* arr, int size) {
        for (int i = 1; i <= size - 1; i++) {
            double key = arr[i];
            int j = i - 1;
49
            while (j \ge 0 \&\& arr[j] > key) {
                 arr[j + 1] = arr[j];
51
                 j--;
            } arr[j + 1] = key;
        }
    }
55
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
        double *insertion_arr = new double[2500];
101
        for (int i = 0; i < 2500; i++) insertion_arr[i] = input_array[i];</pre>
102
        insertionsort(insertion_arr, 2500);
        if (check(insertion_arr)) cout << "Insertionsort Validated" << endl;</pre>
        return 0;
120
    }
121
```

Insertion Sort is a double-loop algorithm, therefore time complexity analysis is as follows:

$$T(n) = \sum_{i=1}^{n} \sum_{j=1}^{i} \epsilon = O(n^2)$$

3.4 Stooge Sort

```
void stoogesort(double* arr, int begin, int end) {
       if (begin >= end) return;
       else if (end - begin == 1) {
59
           if (arr[begin] > arr[end]) swap(arr[begin], arr[end]);
       } else {
61
           int d = (end - begin + 1) / 3;
           stoogesort(arr, begin, end - d);
           stoogesort(arr, begin + d, end);
           stoogesort(arr, begin, end - d);
       }
   }
   int main(int argc, char *argv[]) {
       double *input_array = new double[2500];
       for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
```

```
double *stooge_arr = new double[2500];
for (int i = 0; i < 2500; i++) stooge_arr[i] = input_array[i];
stoogesort(stooge_arr, 0, 2499);
if (check(stooge_arr)) cout << "Stoogesort Validated" << endl;
return 0;
}</pre>
```

Stooge Sort is a recursive algorithm of three subarrays. The time complexity is:

$$T(n) = 3T\left(\frac{3}{2}n\right) + 1, \therefore T(n) \approx O\left(n^{2.7}\right)$$

3.5 Heap Sort

```
void heapsort(double *arr, int n, int i) {
        int largest = i;
        int 1 = 2 * i + 1;
        int r = 2 * i + 2;
        if (1 < n && arr[1] > arr[largest]) largest = 1;
        if (r < n && arr[r] > arr[largest]) largest = r;
        if (largest != i) {
75
             swap(arr[i], arr[largest]);
            heapsort(arr, n, largest);
        }
78
    }
79
    int main(int argc, char *argv[]) {
87
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
        double *heap_arr = new double[2500];
        for (int i = 0; i < 2500; i++) heap_arr[i] = input_array[i];</pre>
        for (int i = 1249; i >= 0; i--)
113
            heapsort(heap_arr, 2500, i);
114
        for (int i = 2499; i >= 0; i--) {
115
             swap(heap_arr[0], heap_arr[i]);
116
            heapsort(heap_arr, i, 0);
117
        } if (check(heap_arr)) cout << "Heapsort Validated" << endl;</pre>
118
        return 0;
120
    }
121
```

Heap sort is a loop-and-recursive algorithm of time complexy analysis

$$T(n) = O(n \log n)$$

Part II

C++

Variables and Class

- 1.1 ;++;
- 1.2 ;++;
- 1.3 ;++;
- 1.4 ;++;

Functions

- 2.1 ;++;
- 2.2 ;++;
- 2.3 ;++;
- 2.4 ;++;

iostream Headers

- 3.1 ;++;
- 3.2 ;++;
- 3.3 ;++;
- 3.4 ;++;

Arrays and Pointers

- 4.1 ;++;
- 4.2 ;++;
- 4.3 ;++;
- 4.4 ;++;

Object-Orientated Programming

- 5.1 ;++;
- 5.2 ;++;
- 5.3 ;++;
- 5.4 ;++;

Defining Classes with OOP

- 5++; 6.1
- 6.2 ;++;
- 6.3 ;++;
- 5++; 6.4

Member Functions

- 7.1 ;++;
- 7.2 ;++;
- 7.3 ;++;
- 7.4 ;++;

Namespace and STL

- 3.1 ;++;
- 8.2 ;++;
- 3++; 8.8
- 8.4 ;++;

Constructors and Destructors

- 9.1 ;++;
- ن++ز 9.2
- 9.3 ;++;
- 9.4 ;++;

Public or Private, Friend Declarations

- ن++ز 1.01
- ن++ز 10.2
- 10.3 ;++;
- 10.4 ;++;

Copy Constructors

- ن++ز 11.1
- ن++ز 11.2
- 11.3 ;++;
- 11.4 ;++;

Operator Overloading and the Rule of Three

- 12.1 ;++;
- 12.2 ;++;
- 12.3 ;++¿
- 12.4 ;++;

Protected and Private Derivations

- 13.1 ;++;
- 13.2 ;++;
- 13.3 ;++;
- 13.4 ;++;

Virtual Functions

- 14.1 ;++;
- 14.2 ;++;
- 14.3 ;++;
- 14.4 ;++;

Pure Virtual Functions

- 15.1 ;++;
- ن++ز 15.2
- 15.3 ;++;
- 15.4 ;++;

Reusing Copy Control Members

- 16.1 ;++;
- 16.2 ;++;
- 16.3 ;++;
- 16.4 ;++;