Student's Manual for Programming Methodology with C++

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Contents

I	I Algorithms			
1	Tim	ne Complexity Analysis	6	
2	Finding the Maximum Subarray Sum		7	
	2.1	Cubic Brute Force Algorithm	7	
	2.2	Quadratic Brute Force Algorithm	8	
	2.3	Divide and Conquer	8	
	2.4	Kadane's Algorithm: A Linear, Incremental Solution	9	
3	Various Ways of Sorting			
	3.1	Quick Sort	10	
	3.2	Merge Sort	11	
	3.3	Insertion Sort	12	
	3.4	Stooge Sort	12	
	3.5	Heap Sort	13	
II	C-	C++		
1	Vari	Variables and Class		
	1.1	The Basics	15	
		1.1.1 Commenting	15	
		1.1.2 Types and Variables	15	
	1.2	j++;	15	
2	Functions		16	
	2.1	Function Definition	16	
	2.2	Procedural Abstraction	16	
	2.3	Argument Passing Mechanism	16	
	2.4	Inline Functions	16	
	2.5	Recursive Functions	16	

3	iostream Headers 17					
	3.1 Keyboard Input and Screen Output	. 17				
	3.2 File In/Output	. 17				
	3.3 Header Files	. 17				
4	Arrays and Pointers 1					
	4.1 Array	. 18				
	4.2 Pointer	. 18				
	4.3 j++¿	. 18				
	4.4 i++¿	. 18				
5	Object-Orientated Programming 19					
	5.1 j++¿	. 19				
	5.2 j++¿	. 19				
	5.3 j++¿	. 19				
	5.4 i++¿	. 19				
6	Defining Classes with OOP					
	6.1 j++¿	. 20				
	6.2 j++¿	. 20				
	6.3 j++¿	. 20				
	6.4 i++¿	. 20				
7	Member Functions					
	7.1 $_{i}++_{i}$. 21				
	7.2 j++¿	. 21				
	7.3 $_{i}++_{\dot{c}}$. 21				
	7.4 $_{i}++_{\dot{c}}$. 21				
8	Namespace and STL 22					
	8.1 j++¿	. 22				
	8.2 j++¿	. 22				
	8.3 j++¿	. 22				
	8.4 j++¿	. 22				
9	Constructors and Destructors 23					
	9.1 j++¿	. 23				
	9.2 _i ++ _¿					
	9.3 _i ++ _i					
	9.4 i++¿	. 23				
10	Public or Private, Friend Declarations 2					
	10.1 j++¿	. 24				
	10.2 ;++;	. 24				

	ن++ز 2.01		24
	10.4 ;++;		24
11	Copy Cons	structors	25
			25
	11.2 ;++;		25
	11.3 ;++;		25
	11.4 ;++;		25
12	Operator C	Overloading and the Rule of Three	26
	12.1 ;++;		26
	12.2 ;++;		26
	12.3 ;++;		26
	12.4 ;++;		26
13	Protected a	and Private Derivations	27
	13.1 ;++;		27
	13.2 ;++;		27
	13.3 ;++;		27
	13.4 ;++;		27
14	Virtual Fur	nctions	28
	14.1 ;++;		28
	14.2 ;++;		28
	14.3 ;++;		28
	14.4 ;++;		28
15	Pure Virtua	al Functions	29
	15.1 ;++;		29
	15.2 ;++;		29
	15.3 ;++;		29
	15.4 ;++;		29
16	Reusing Co	opy Control Members	30
	_	••	30
			30
			30
			30

Part I Algorithms

Time Complexity Analysis

- 1. The running time of an algorithm is relevent to the amount of input. Therefore the running time is a function of the amount of input: T(n)
- 2. Definitions of Time Complexity: with a positive constant *c*,
 - 1) Big-O: $T(n) \ge c \times f_O(n) \Rightarrow T(n) = O(f_O(n))$ Best-case scenarios can be described via Big-O functions.
 - 2) Big-Omega: $T(n) \le c \times f_{\Omega}(n) \Rightarrow T(n) = \Omega\left(f_{\Omega}(n)\right)$ Worst-case scenarios can be described via Big-Omega functions.
 - 3) Big-Theta: $T(n) \ge c \times f(n)$ and $T(n) \le c' \times f(n) \Leftrightarrow T(n) = O(f(n)) = \Omega(f(n)) \Rightarrow T(n) = \Theta(f(n))$ Best- and Worst-case scenarios are the same in Big-Theta functions.
 - 4) Small-O: $T(n) = O(f_o(n)) \neq \Theta(f_o(n)) \Rightarrow T(n) = o(f_o(n))$

Constants are ignored, and only the highest degree of the polynomial's monomials are relevant to Time Complexity Analysis.

- 3. Running Time Calculations
 - 1) Summations for Loops: One loop sequence of running time f(i) is equivalent to:

$$T(n) = \sum_{i=1}^{n} f(i)$$

Two loop sequences of running time f(i, j) is equivalent to:

$$T(n) = \sum_{j=1}^{n} \sum_{i=1}^{n} f(i, j)$$

- 2) Selective Controls: Worst-case scenario, $T(n) = \max(T_1(n), T_2(n), \cdots)$. Best-case = minimum.
- 3) Recursion: T(n) = f(T(n')) (점화식)

Finding the Maximum Subarray Sum

The objective of this challenge is to find the maximum value of the sum of elements in a subarray of a given array. If all integers are negative, said maximum value is the sum of a subarray equivalent to the 'empty set', which is zero.

2.1 Cubic Brute Force Algorithm

```
int max_sum1(int* arr, int arrsize) {
    int maxSum = 0;
    for (int i = 0; i < arrsize; i++) {
        for (int j = i; j < arrsize; j++) {
            int thisSum = 0;
            for (int k = i; k <= j; k++) thisSum += arr[k];
            if (maxSum < thisSum) maxSum = thisSum;
        }
} return maxSum;
}</pre>
```

This algorithm utilises three loops and a function of constant time in the innermost loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} \sum_{j=i}^{n} \sum_{k=i}^{j} 1 = O(n^3)$$

Obviously this method is quite wasteful in both memory and timekeeping. The following two algorithms are substantial progessions from this algorithm:

2.2 Quadratic Brute Force Algorithm

```
int max_sum2(int* arr, int arrsize) {
    int maxSum = 0;
    for (int i = 0; i < arrsize; i++) {
        int iSum = 0;
        for (int j = i; j < arrsize; j++) {
            iSum += arr[j];
            if (maxSum < iSum) maxSum = iSum;
        }
    } return maxSum;
}</pre>
```

This algorithm utilises two loops and a function of constant time in the innermost loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} \sum_{j=i}^{n} 1 = O(n^2)$$

2.3 Divide and Conquer

```
int max_sum3(int* arr, int left, int right) {
        if (left >= right) return arr[left];
31
        else { int hereMax = 0;
32
            int leftSum = max_sum3(arr, left, ((left + right) / 2) - 1);
            int rightSum = max_sum3(arr, ((left + right) / 2) + 1, right);
34
            if (leftSum >= rightSum) hereMax = leftSum;
35
            else hereMax = rightSum;
36
            int leftMax = arr[(left + right) / 2], leftTemp = 0;
            int rightMax = arr[(left + right) / 2], rightTemp = 0;
            for (int i = (left + right) / 2; i >= left; i--) {
                leftTemp += arr[i];
                if (leftMax < leftTemp) leftMax = leftTemp;</pre>
41
            } for (int i = (left + right) / 2; i <= right; i++) {</pre>
                rightTemp += arr[i];
                 if (rightMax < rightTemp) rightMax = rightTemp;</pre>
44
            } int midSum = leftMax + rightMax - arr[(left + right) / 2];
45
            if (hereMax < midSum) hereMax = midSum;</pre>
            return hereMax;
47
        }
   }
```

This algorithm utilises a divisive recursion and selection controls of constant time within each recursion. Therefore, the time complexity analysis goes:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^kT\left(\frac{n}{2^k}\right) + nk, \ \therefore T(n) = 2^{\log_2 n}T(1) + n\log_2 n = n\log_2 n + \varepsilon n = O(n\log n)$$

While these two algorithms are quite effective compared to Cubic Brute Force, this last algorithm manages to provide the fastest solution possible:

2.4 Kadane's Algorithm: A Linear, Incremental Solution

```
int max_sum4(int* arr, int arrsize) {
    int maxSum = arr[0], thisSum = 0;
    for (int i = 0; i < arrsize; i++) {
        thisSum += arr[i];
        if (thisSum > maxSum) maxSum = thisSum;
        else if (thisSum < 0) thisSum = 0;
    } return maxSum;
}</pre>
```

This algorithm utilises one loop and a function of constant time in the loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} 1 = O(n)$$

Since, essentially, the challenge requires a system to read each data at least once, the O(n) function above is obviously the best solution.

Various Ways of Sorting

The objective of this callenge is sorting given algebraic (in this case, double) elements of an aray in incrasing order. Some elements may be of equal value.

3.1 Quick Sort

```
void quicksort(double *arr, int begin, int end) {
        double pivot = arr[begin];
        int i = begin, j = end;
        while (i <= j) {
            while (arr[i] < pivot) i++;</pre>
            while (arr[j] > pivot) j--;
            if (i <= j) {
                 swap(arr[i], arr[j]);
                 i++; j--;
13
        } if (begin < j) quicksort(arr, begin, j);</pre>
14
        if (end > i) quicksort(arr, i, end);
15
   }
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
        double *quick_arr = new double[2500];
        for (int i = 0; i < 2500; i++) quick_arr[i] = input_array[i];</pre>
        quicksort(quick_arr, 0, 2499);
        if (check(quick_arr)) cout << "Quicksort Validated" << endl;</pre>
120
        return 0;
121
   }
```

Quick Sort is a recursive algorithm that does the following:

- 1. Choose a "pivot" element: Line 6
- 2. Swap elements that are larger than the pivot with elements that are smaller but on the righthand side of the chosen element: Lines 8:14
- Continue until all elements are sorted, then recursively proceed with the left and right subarrays of the pivot: Lines 15, 16

Using two half-recursions results in the following time complexity analysis:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^k T\left(\frac{n}{2^k}\right) + kn = O(n\log n)$$

3.2 Merge Sort

```
void mergesort(double * arr, int begin, int end) {
        if (begin < end) {
            int centre = begin + (end - begin) / 2;
20
            mergesort(arr, begin, centre);
21
            mergesort(arr, centre + 1, end);
22
            int n1 = centre - begin + 1;
23
            int n2 = end - centre;
            double* L = new double[n1 + 1];
            double* R = new double[n2 + 1];
26
            for (int i = 0; i <= n1 - 1; i++) L[i] = arr[begin + i];
27
            for (int j = 0; j \le n2 - 1; j++) R[j] = arr[centre + j + 1];
28
            L[n1] = (double)INT_MAX;
            R[n2] = (double)INT_MAX;
            int a = 0, b = 0;
31
            for (int k = begin; k \le end; k++) {
32
                 if (L[a] <= R[b]) arr[k] = L[a++];
33
                 else arr[k] = R[b++];
            }
        }
    }
37
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
88
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
        double *merge_arr = new double[2500];
        for (int i = 0; i < 2500; i++) merge_arr[i] = input_array[i];</pre>
        mergesort(merge_arr, 0, 2499);
        if (check(merge_arr)) cout << "Mergesort Validated" << endl;</pre>
        return 0;
120
    }
121
```

Merge Sort is also a recursive algorithm dependent on two half-recursions. Time complexity analysis goes:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^k T\left(\frac{n}{2^k}\right) + kn = O(n\log n)$$

3.3 Insertion Sort

```
void insertionsort(double* arr, int size) {
        for (int i = 1; i <= size - 1; i++) {
            double key = arr[i];
            int j = i - 1;
49
            while (j \ge 0 \&\& arr[j] > key) {
                 arr[j + 1] = arr[j];
51
                 j--;
            } arr[j + 1] = key;
        }
    }
55
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
        double *insertion_arr = new double[2500];
101
        for (int i = 0; i < 2500; i++) insertion_arr[i] = input_array[i];</pre>
102
        insertionsort(insertion_arr, 2500);
        if (check(insertion_arr)) cout << "Insertionsort Validated" << endl;</pre>
        return 0;
120
    }
121
```

Insertion Sort is a double-loop algorithm, therefore time complexity analysis is as follows:

$$T(n) = \sum_{i=1}^{n} \sum_{j=1}^{i} \epsilon = O(n^2)$$

3.4 Stooge Sort

```
void stoogesort(double* arr, int begin, int end) {
       if (begin >= end) return;
       else if (end - begin == 1) {
59
           if (arr[begin] > arr[end]) swap(arr[begin], arr[end]);
       } else {
61
           int d = (end - begin + 1) / 3;
           stoogesort(arr, begin, end - d);
           stoogesort(arr, begin + d, end);
           stoogesort(arr, begin, end - d);
       }
   }
   int main(int argc, char *argv[]) {
       double *input_array = new double[2500];
       for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
```

```
double *stooge_arr = new double[2500];
for (int i = 0; i < 2500; i++) stooge_arr[i] = input_array[i];
stoogesort(stooge_arr, 0, 2499);
if (check(stooge_arr)) cout << "Stoogesort Validated" << endl;
return 0;
}</pre>
```

Stooge Sort is a recursive algorithm of three subarrays. The time complexity is:

$$T(n) = 3T\left(\frac{3}{2}n\right) + 1, \therefore T(n) \approx O\left(n^{2.7}\right)$$

3.5 Heap Sort

```
void heapsort(double *arr, int n, int i) {
        int largest = i;
        int 1 = 2 * i + 1;
        int r = 2 * i + 2;
        if (1 < n && arr[1] > arr[largest]) largest = 1;
        if (r < n && arr[r] > arr[largest]) largest = r;
        if (largest != i) {
75
             swap(arr[i], arr[largest]);
            heapsort(arr, n, largest);
        }
78
    }
79
    int main(int argc, char *argv[]) {
87
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
        double *heap_arr = new double[2500];
        for (int i = 0; i < 2500; i++) heap_arr[i] = input_array[i];</pre>
        for (int i = 1249; i >= 0; i--)
113
            heapsort(heap_arr, 2500, i);
114
        for (int i = 2499; i >= 0; i--) {
115
             swap(heap_arr[0], heap_arr[i]);
116
            heapsort(heap_arr, i, 0);
117
        } if (check(heap_arr)) cout << "Heapsort Validated" << endl;</pre>
118
        return 0;
120
    }
121
```

Heap sort is a loop-and-recursive algorithm of time complexy analysis

$$T(n) = O(n \log n)$$

Part II

C++

Variables and Class

1.1 The Basics

```
#include <iostream>

int main(void) {

std::cout << "Hello World!";

return 0;
}</pre>
```

C++ is an extension of C.

1.1.1 Commenting

Single-line comments use two forward slashes: // Comment 1 Multi-line comments use a forward slash and a star at each end to denote beginning and end: /* Comment 2 */

1.1.2 Types and Variables

- 1. Primitive, built-in types:
 - 1) void is used to determine functions and variables of no return value.
 - 2) bool, char, int, float, double and et cetra are used to return certain values.
 - 3) unsigned is used to prepend targets that are always of positive value.
- 2. Enumerations: enum is used to define groups of integer constants.

1.2 ;++;

Functions

- 2.1 Function Definition
- 2.2 Procedural Abstraction
- 2.3 Argument Passing Mechanism
- 2.4 Inline Functions
- 2.5 Recursive Functions

iostream Headers

3.1 Keyboard Input and Screen Output

3.2 File In/Output

3.3 Header Files

- 1. Header File: A file that allows the reusage of certain portions of source code. Header files are included to a source code via *##include*, which inserts the header file code at that specific location.
- 2. Headers are used for declaring functions, classes, et cetra, and since a header file can be used multiple times by multiple source codes, defining variables and classes must not happen in a header file.
- 3. Include Guards: Since a single header file can be included multiple times throughout a compiling process and cause compilation errors, prevention methods are supported by the compilers. This "guard from inclusion"s are called **Include guards**:

```
#ifndef _IOSHEADER_H_ // Check if header is yet undefined
#define _IOSHEADER_H_ // If checked, define header

#include <iostream>

class classy {
public:
    void std::cout << "Hello World!" << std::endl;
};

#endif // End selection control</pre>
```

Arrays and Pointers

4.1 Array

1. Sequential container of objects of a single data type with fixed size: int array[3] = {5, 3, 2};

4.2 Pointer

- 1. A pointer is a variable that holds the address of an object, enabling indirect access: int *m = new int[4];
- 2. Adding an integer n to a pointer variable returns the address of an element displaced by n from the original element.

Object-Orientated Programming

- 5.1 ;++;
- 5.2 ;++;
- 5.3 ;++;
- 5.4 ;++;

Defining Classes with OOP

- 5++; 1.6
- 6.2 ;++;
- 6.3 ;++;
- 5++; 4.6

Member Functions

- 7.1 ;++;
- 7.2 ;++;
- 7.3 ;++;
- 7.4 ;++;

Namespace and STL

- 3.1 ;++;
- 8.2 ;++;
- 3++; 8.8
- 8.4 ;++;

Constructors and Destructors

- 9.1 ;++;
- ن++ز 9.2
- 9.3 ;++;
- 9.4 ;++;

Public or Private, Friend Declarations

- ن++; 1.01
- ن++ز 10.2
- 10.3 ;++;
- 10.4 ;++;

Copy Constructors

- ن++ز 11.1
- ن++ز 11.2
- 11.3 ;++;
- 11.4 ;++;

Operator Overloading and the Rule of Three

- 12.1 ;++;
- 12.2 ;++;
- 12.3 ;++¿
- 12.4 ;++;

Protected and Private Derivations

- 13.1 ;++;
- 13.2 ;++;
- 13.3 ;++;
- 13.4 ;++;

Virtual Functions

- 14.1 ;++;
- 14.2 ;++;
- 14.3 ;++;
- 14.4 ;++;

Pure Virtual Functions

- 15.1 ;++;
- ن++ز 15.2
- 15.3 ;++;
- 15.4 ;++;

Reusing Copy Control Members

- 16.1 ;++;
- 16.2 ;++;
- 16.3 ;++;
- 16.4 ;++;