## Programming Methodology with C++

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## **Contents**

# Part I Algorithms

## Time Complexity Analysis

- 1. The running time of an algorithm is relevent to the amount of input. Therefore the running time is a function of the amount of input: T(n)
- 2. Definitions of Time Complexity: with a positive constant *c*,
  - 1) Big-O:  $T(n) \ge c \times f_O(n) \Rightarrow T(n) = O(f_O(n))$  Best-case scenarios can be described via Big-O functions.
  - 2) Big-Omega:  $T(n) \le c \times f_{\Omega}(n) \Rightarrow T(n) = \Omega\left(f_{\Omega}(n)\right)$  Worst-case scenarios can be described via Big-Omega functions.
  - 3) Big-Theta:  $T(n) \ge c \times f(n)$  and  $T(n) \le c' \times f(n) \Leftrightarrow T(n) = O(f(n)) = \Omega(f(n)) \Rightarrow T(n) = \Theta(f(n))$  Best- and Worst-case scenarios are the same in Big-Theta functions.
  - 4) Small-O:  $T(n) = O(f_o(n)) \neq \Theta(f_o(n)) \Rightarrow T(n) = o(f_o(n))$

Constants are ignored, and only the highest degree of the polynomial's monomials are relevant to Time Complexity Analysis.

- 3. Running Time Calculations
  - 1) Summations for Loops: One loop sequence of running time f(i) is equivalent to:

$$T(n) = \sum_{i=1}^{n} f(i)$$

Two loop sequences of running time f(i, j) is equivalent to:

$$T(n) = \sum_{j=1}^{n} \sum_{i=1}^{n} f(i, j)$$

- 2) Selective Controls: Worst-case scenario,  $T(n) = \max(T_1(n), T_2(n), \cdots)$ . Best-case = minimum.
- 3) Recursion: T(n) = f(T(n')) (점화식)

## Finding the Maximum Subarray Sum

The objective of this challenge is to find the maximum value of the sum of elements in a subarray of a given array. If all integers are negative, said maximum value is the sum of a subarray equivalent to the 'empty set', which is zero.

#### 2.1 Cubic Brute Force Algorithm

```
int max_sum1(int* arr, int arrsize) {
   int maxSum = 0;
   for (int i = 0; i < arrsize; i++) {
      for (int j = i; j < arrsize; j++) {
        int thisSum = 0;
      for (int k = i; k <= j; k++) thisSum += arr[k];
      if (maxSum < thisSum) maxSum = thisSum;
    }
} return maxSum;
}</pre>
```

This algorithm utilises three loops and a function of constant time in the innermost loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} \sum_{j=i}^{n} \sum_{k=i}^{j} 1 = O(n^3)$$

Obviously this method is quite wasteful in both memory and timekeeping. The following two algorithms are substantial progessions from this algorithm:

#### 2.2 Quadratic Brute Force Algorithm

```
int max_sum2(int* arr, int arrsize) {
    int maxSum = 0;
    for (int i = 0; i < arrsize; i++) {
        int iSum = 0;
        for (int j = i; j < arrsize; j++) {
            iSum += arr[j];
            if (maxSum < iSum) maxSum = iSum;
        }
    } return maxSum;
}</pre>
```

This algorithm utilises two loops and a function of constant time in the innermost loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} \sum_{j=i}^{n} 1 = O(n^2)$$

#### 2.3 Divide and Conquer

```
int max_sum3(int* arr, int left, int right) {
        if (left >= right) return arr[left];
31
        else { int hereMax = 0;
32
            int leftSum = max_sum3(arr, left, ((left + right) / 2) - 1);
            int rightSum = max_sum3(arr, ((left + right) / 2) + 1, right);
34
            if (leftSum >= rightSum) hereMax = leftSum;
            else hereMax = rightSum;
36
            int leftMax = arr[(left + right) / 2], leftTemp = 0;
            int rightMax = arr[(left + right) / 2], rightTemp = 0;
            for (int i = (left + right) / 2; i >= left; i--) {
                leftTemp += arr[i];
                if (leftMax < leftTemp) leftMax = leftTemp;</pre>
41
            } for (int i = (left + right) / 2; i <= right; i++) {</pre>
                rightTemp += arr[i];
                 if (rightMax < rightTemp) rightMax = rightTemp;</pre>
44
            } int midSum = leftMax + rightMax - arr[(left + right) / 2];
45
            if (hereMax < midSum) hereMax = midSum;</pre>
            return hereMax;
47
        }
   }
```

This algorithm utilises a divisive recursion and selection controls of constant time within each recursion. Therefore, the time complexity analysis goes:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^kT\left(\frac{n}{2^k}\right) + nk, \quad \therefore T(n) = 2^{\log_2 n}T(1) + n\log_2 n = n\log_2 n + \varepsilon n = O(n\log n)$$

While these two algorithms are quite effective compared to Cubic Brute Force, this last algorithm manages to provide the fastest solution possible:

#### 2.4 Kadane's Algorithm: A Linear, Incremental Solution

```
int max_sum4(int* arr, int arrsize) {
    int maxSum = arr[0], thisSum = 0;
    for (int i = 0; i < arrsize; i++) {
        thisSum += arr[i];
        if (thisSum > maxSum) maxSum = thisSum;
        else if (thisSum < 0) thisSum = 0;
    } return maxSum;
}</pre>
```

This algorithm utilises one loop and a function of constant time in the loop. Therefore, the time complexity analysis goes:

$$T(n) = \sum_{i=1}^{n} 1 = O(n)$$

Since, essentially, the challenge requires a system to read each data at least once, the O(n) function above is obviously the best solution.

## Various Ways of Sorting

The objective of this challenge is sorting given algebraic (in this case, double) elements of an aray in incrasing order. Some elements may be of equal value.

#### 3.1 Quick Sort

```
void quicksort(double *arr, int begin, int end) {
        double pivot = arr[begin];
        int i = begin, j = end;
        while (i <= j) {
            while (arr[i] < pivot) i++;</pre>
            while (arr[j] > pivot) j--;
            if (i <= j) {
                 swap(arr[i], arr[j]);
                 i++; j--;
12
13
        } if (begin < j) quicksort(arr, begin, j);</pre>
14
        if (end > i) quicksort(arr, i, end);
15
   }
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
        double *quick_arr = new double[2500];
        for (int i = 0; i < 2500; i++) quick_arr[i] = input_array[i];</pre>
        quicksort(quick_arr, 0, 2499);
        if (check(quick_arr)) cout << "Quicksort Validated" << endl;</pre>
120
        return 0;
121
   }
```

Quick Sort is a recursive algorithm that does the following:

- 1. Choose a "pivot" element: Line 6
- 2. Swap elements that are larger than the pivot with elements that are smaller but on the righthand side of the chosen element: Lines 8:14
- 3. Continue until all elements are sorted, then recursively proceed with the left and right subarrays of the pivot: Lines 15, 16

Using two half-recursions results in the following time complexity analysis:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^k T\left(\frac{n}{2^k}\right) + kn = O(n\log n)$$

#### 3.2 Merge Sort

```
void mergesort(double * arr, int begin, int end) {
        if (begin < end) {
            int centre = begin + (end - begin) / 2;
20
            mergesort(arr, begin, centre);
21
            mergesort(arr, centre + 1, end);
22
            int n1 = centre - begin + 1;
23
            int n2 = end - centre;
            double* L = new double[n1 + 1];
            double* R = new double[n2 + 1];
26
            for (int i = 0; i <= n1 - 1; i++) L[i] = arr[begin + i];
27
            for (int j = 0; j <= n2 - 1; j++) R[j] = arr[centre + j + 1];
28
            L[n1] = (double)INT_MAX;
            R[n2] = (double)INT_MAX;
            int a = 0, b = 0;
31
            for (int k = begin; k \le end; k++) {
32
                 if (L[a] <= R[b]) arr[k] = L[a++];
33
                 else arr[k] = R[b++];
            }
        }
    }
37
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
88
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
        double *merge_arr = new double[2500];
        for (int i = 0; i < 2500; i++) merge_arr[i] = input_array[i];</pre>
        mergesort(merge_arr, 0, 2499);
        if (check(merge_arr)) cout << "Mergesort Validated" << endl;</pre>
        return 0;
120
    }
121
```

Merge Sort is also a recursive algorithm dependent on two half-recursions. Time complexity analysis goes:

$$T(n) = 2T\left(\frac{n}{2}\right) + n = 2^k T\left(\frac{n}{2^k}\right) + kn = O(n\log n)$$

#### 3.3 Insertion Sort

```
void insertionsort(double* arr, int size) {
        for (int i = 1; i <= size - 1; i++) {
            double key = arr[i];
            int j = i - 1;
49
            while (j \ge 0 \&\& arr[j] > key) {
                 arr[j + 1] = arr[j];
51
                 j--;
            } arr[j + 1] = key;
        }
    }
55
    int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);
        double *insertion_arr = new double[2500];
101
        for (int i = 0; i < 2500; i++) insertion_arr[i] = input_array[i];</pre>
102
        insertionsort(insertion_arr, 2500);
        if (check(insertion_arr)) cout << "Insertionsort Validated" << endl;</pre>
        return 0;
120
    }
121
```

Insertion Sort is a double-loop algorithm, therefore time complexity analysis is as follows:

$$T(n) = \sum_{i=1}^{n} \sum_{j=1}^{i} \epsilon = O(n^2)$$

#### 3.4 Stooge Sort

```
void stoogesort(double* arr, int begin, int end) {
    if (begin >= end) return;
    else if (end - begin == 1) {
        if (arr[begin] > arr[end]) swap(arr[begin], arr[end]);
} else {
        int d = (end - begin + 1) / 3;
        stoogesort(arr, begin, end - d);
        stoogesort(arr, begin + d, end);
        stoogesort(arr, begin, end - d);
}

int main(int argc, char *argv[]) {
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
```

```
double *stooge_arr = new double[2500];
for (int i = 0; i < 2500; i++) stooge_arr[i] = input_array[i];
stoogesort(stooge_arr, 0, 2499);
if (check(stooge_arr)) cout << "Stoogesort Validated" << endl;
return 0;
}</pre>
```

Stooge Sort is a recursive algorithm of three subarrays. The time complexity is:

$$T(n) = 3T\left(\frac{3}{2}n\right) + 1, \therefore T(n) \approx O\left(n^{2.7}\right)$$

#### 3.5 Heap Sort

```
void heapsort(double *arr, int n, int i) {
        int largest = i;
        int 1 = 2 * i + 1;
        int r = 2 * i + 2;
        if (1 < n && arr[1] > arr[largest]) largest = 1;
        if (r < n && arr[r] > arr[largest]) largest = r;
        if (largest != i) {
75
             swap(arr[i], arr[largest]);
             heapsort(arr, n, largest);
        }
78
    }
79
    int main(int argc, char *argv[]) {
87
        double *input_array = new double[2500];
        for (int i = 0; i < 2500; i++) input_array[i] = double(rand() % 2500);</pre>
        double *heap_arr = new double[2500];
        for (int i = 0; i < 2500; i++) heap_arr[i] = input_array[i];</pre>
        for (int i = 1249; i >= 0; i--)
113
             heapsort(heap_arr, 2500, i);
114
        for (int i = 2499; i >= 0; i--) {
115
             swap(heap_arr[0], heap_arr[i]);
116
             heapsort(heap_arr, i, 0);
117
        } if (check(heap_arr)) cout << "Heapsort Validated" << endl;</pre>
118
        return 0;
120
    }
121
```

Heap sort is a loop-and-recursive algorithm of time complexy analysis

$$T(n) = O(n \log n)$$

## Minimum Search on Rotated Array

The objective of this challenge is to find the smallest element in an array that was rotated at a random index after being sorted. Duplicate elements are not allowed for this challenge.

#### 4.1 Solution

```
int Searcher(int* a, int 1, int r) {
       int m = 1 + (r - 1) / 2; // Prevents overflow
       if (1 == r) return a[1];
       else if (a[1] < a[r]) return a[1];
        else if (a[m] < a[r]) {
            if (a[m-1] \le a[m]) return Searcher(a, 1, m - 1);
            else return a[m];
       } else return Searcher(a, m + 1, r);
10
   }
   int main(int argc, char *argv[]) {
        int n; std::cin >> n;
35
       int* input_array = new int[n];
36
       for (int i = 0; i < n; ++i) input_array[i] = int(rand() % n);</pre>
37
        sort(input_array, 0, n - 1); // See Previous Chapter
38
        std::cout << Searcher(input_array, 0, n - 1);</pre>
       return 0;
42
43
   }
```

By using a binary-search method with three nodes, the code above is successful in finding and returning the smallest element. This algorithm uses recursive functions, and shows the time complexity of the following:

$$T(n) = 2T\left(\frac{n}{2}\right) + \alpha = 4T\left(\frac{n}{4}\right) + 3\alpha = \dots = 2^k T\left(\frac{n}{2^k}\right) + \frac{k(k+1)}{2}\alpha, \quad \therefore T(n) = O(\log n)$$

## Finding the k-th Smallest Number

The objective of this challenge is to find the k-th smallest number in an unsorted array. Some elements may be of equal value.

#### 5.1 Sort-and-Find

This solution sorts the unsorted array and returning the value at index k. As seen before, time complexity analysis indicates that this approach requires more than  $O(n \log n)$  amount of time. Since the sorting algorithm has already been presented before, it will not be features again.

#### 5.2 Quick Select

This solution is modeled after the Quicksort algorithm. Unlike Quicksort, this algorithm only focuses on one side of the partition, and therefore its expected running time is  $T(n) = \Theta(n)$ .

```
int quickselect(int* a, int k, int l, int r) {
       if (1 == r) return a[1];
       int x = a[r], i = 1;
       for (int j = 1; j < r; ++j) {
           if (a[j] \le a[r]) \{
                std::swap(a[i], a[j]);
           }
10
       } std::swap(a[i], a[r]);
11
       if (k == i - l + 1) return a[i];
       else if (k < i - l + 1) return quickselect(a, k, l, i - 1);
       else return quickselect(a, k - i + l - 1, i + 1, r);
14
15
   int main(int argc, char *argv[]) {
       int n; std::cin >> n;
18
       int* input_array = new int[n];
```

```
for (int i = 0; i < n; ++i) input_array[i] = int(rand() % n);
int k; std::cin >> k;
std::cout << quickselect(input_array, k, 0, n - 1);
return 0;
}</pre>
```

## Finding the Closest Pair of Dots

The objective of this challenge is to find the distance between the two closest dots on a two-dimensional plane. No two dots occupy the same coordinate.

- 6.1 Naive Solution
- 6.2 Application of the Merge Sort Algorithm

## **Rod Cutting Algorithm**

The objective of this challenge is to determine how to cut an imaginary rod to receive the maximum revenue. Revenue per rod length and initial rod lengths are given. Note that, if the price for the initial rod length is high enough, the optimal solution may require no cutting at all.

#### 7.1 Brute Force

```
int brute(int* price, int n) {
        if (n <= 0) return 0;
       int q = INT_MIN;
       for (int i = 0; i < n; ++i) {
            q = std::max(q, price[i] + brute(price, n - i - 1));
        } return q;
   }
10
   int main(int argc, char *argv[]) {
       int n; std::cin >> n;
36
       int* pricing = new int[n + 1];
37
       pricing[0] = 0;
38
       for (int i = 0; i < n; ++i) pricing[i + 1] = pricing[i] + rand() % n;</pre>
       std::cout << brute(pricing, n + 1);</pre>
       return 0;
   }
```

Since there are n-1 places to either cut or leave, there are  $2^{n-1}$  ways in total to cut a rod of n inches. Therefore a brute force algorithm such as the one presented solves all possible outcomes and finds the maximum value. Time Complexity Analysis shows an exponential time function.

#### 7.2 Dynamic Programming: Top-Down Approach

```
int topdown(int* price, int n, int* memo) {
       if (memo[n] >= 0) return memo[n];
13
       int q = INT_MIN;
       if (n == 0) q = 0;
15
       else {
16
           for (int i = 1; i <= n; ++i) {
17
                q = std::max(q, price[i] + topdown(price, n - i, memo));
           }
       memo[n] = q;
       return q;
21
    }
22
    int main(int argc, char *argv[]) {
35
        int n; std::cin >> n;
        int* pricing = new int[n + 1];
37
        pricing[0] = 0;
        for (int i = 0; i < n; ++i) pricing[i + 1] = pricing[i] + rand() % n;</pre>
39
        std::cout << " ";
        int* arr = new int[n + 1];
        for (int i = 0; i \le n; ++i) {
43
            arr[i] = INT_MIN;
44
        } std::cout << topdown(pricing, n, arr);</pre>
45
        return 0;
    }
```

The most critical reason for the brute force algorithm's exponentailly long time conplexity is that brute force repeats sonving what is essentially the same set of divisions. For example, when processing the cutting of a 9 inch rod, brute force algorithm processes the same 2, 3, and 4-inch dsivision as 6 different methods  $(2, 3, 4), (3, 2, 4), \cdots$ . This can be solved by recording results of previous iterations of the recursion, or the **memoisation** of previous data. With the top-down method presented above, the new array int\* arr is a storage array for the previously processed results.

#### 7.3 Dynamic Programming: Bottom-Up Approach

```
int bottomup(int* price, int n) {
    int val[n + 1];
    val[0] = 0;
    for (int i = 1; i <= n; ++i) {
        int q = INT_MIN;
        for (int j = 0; j < i; ++j) {
            q = std::max(q, price[j] + val[i - j - 1]);
        } val[i] = q;</pre>
```

```
32     } return val[n];
33     }

35     int main(int argc, char *argv[]) {
36         int n; std::cin >> n;
37         int* pricing = new int[n + 1];
38         pricing[0] = 0;
39         for (int i = 0; i < n; ++i) pricing[i + 1] = pricing[i] + rand() % n;
40         std::cout << bottomup(pricing, n + 1);
48         return 0;
49     }</pre>
```

Unusual circumstances can lead to failures in top-down algorithms where not all possible outcomes are tested. The bottom-up approach above often shows strength in constant factors and overall stability, and can be mathematically proven in its ability to always process all subproblems, although such proof will not be provided in this manual.

Both Top-Down and Bottom-Up approaches show a time complexity of  $T(n) = \Theta(n^2)$ .

## **Assembly-Line Scheduling Algorithm**

The objective of this challenge is to move from entry to exit point via stations along two assembly lines. Each station has a fixed time of processing, and from a station one can move to the next station along the line OR the next station on the other assembly line. Elements can be of equal value.

#### 8.1 Brute Force

With n stations on each assembly line, there are  $2^n$  possible ways to choose stations. Therefore the brute force algorithm takes  $\Omega(2^n)$  of time complexity to be completely processed, making it infeasible.

#### 8.2 The Fastest Way

```
#include <iostream>
   #include <ctime>
   int main(int argc, char *argv[]) {
       int n; std::cin >> n;
       srand((unsigned int)time(NULL));
       int* a1 = new int[n]; int* a2 = new int[n];
       int* t1 = new int[n]; int* t2 = new int[n];
       for (int i = 0; i < n; i++) {
           a1[i] = rand() % n; a2[i] = rand() % n;
10
           t1[i] = rand() % n; t2[i] = rand() % n;
11
       } int e1 = rand() % n, e2 = rand() % n;
12
       int x1 = rand() % n, x2 = rand() % n;
       int way1 = e1 + a1[0];
       int way2 = e2 + a2[0];
15
       for (int i = 1; i < n; i++) {
16
           int temp = way1;
17
           way1 = a1[i] + (way1 < way2 + t2[i - 1]) ? way1 : way2 + t2[i - 1];
18
           way2 = a2[i] + (way2 < temp + t1[i - 1]) ? way2 : temp + t1[i - 1];
```

```
20  } std::cout << (way1 + x1 < way2 + x2) ? way1 + x1 : way2 + x2;
21  return 0;
22 }</pre>
```

With a simple loop algorithm and a minimum-evaluating process every iteration, this process shows a time complexity of:

$$T(n) = \Theta(n)$$

## Matrix-Chain Multiplication Algorithm

The objective of this challenge is to calculate the minimum amount of scalar multiplications a group of matrices needs to return the complete and correct matrix product. Consider three matrices  $\mathbf{A}[10][100], \mathbf{B}[100][5]$ , and  $\mathbf{C}[5][50]$ . There are two ways to multiply these matrices:

- 1.  $(\mathbf{A} \times \mathbf{B}) \times \mathbf{C}$ :  $\mathbf{A} \times \mathbf{B}$  requires  $10 \times 100 \times 5 = 5000$  scalar multiplications.  $\mathbf{AB} \times \mathbf{C}$  requires  $10 \times 5 \times 50 = 2500$ . Therefore the total amount of scalar multiplications is 5000 + 2500 = 7500.
- 2.  $\mathbf{A} \times (\mathbf{B} \times \mathbf{C})$ :  $\mathbf{B} \times \mathbf{C}$  requires  $100 \times 5 \times 50 = 25000$  scalar multiplications.  $\mathbf{A} \times \mathbf{BC}$  requires  $10 \times 100 \times 50 = 50000$ . Therefore the total amount of scalar multiplications is 25000 + 50000 = 75000.

Given a chain of n matrices and an integer array of n+1 elements where each matrix  $\mathbf{A_i}$  shows the dimesion of  $(p_{i-1}, p_i)$ , the following solutions are algorithms that minimise scalar multiplication amounts.

#### 9.1 Optimal Solution

```
int main() {
       int n; std::cin >> n;
       int* p = new int[n + 1]; int** m = new int*[n];
       for (int i = 0; i < n; ++i) std::cin >> p[i] >> p[i + 1];
       for (int i = 0; i < n; ++i) {
            m[i] = new int[n]; if (i != 0) m[i][i] = 0;
       } for (int 1 = 2; 1 \le n; ++1) {
10
            for (int i = 1; i \le n + 1 - 1; ++i) {
11
                int j = i + 1 - 1;
12
                m[i][j] = INT_MAX;
13
                for (int k = i; k < j; ++k) {
                    int q = m[i][k] + m[k + 1][j] + p[i - 1] * p[k] * p[j];
15
                    if (q < m[i][j]) m[i][j] = q;
16
                }
17
18
       } std::cout << m[1][n];</pre>
19
       delete[] p;
```

```
21     return 0;
22  }
```

Matrix chain multiplication has  $T(n) = \Theta\left(n^2\right)$  subproblems, each featuring no more than n-1 choices. Therefore the time complexity of this algorithm is:

$$T(n) = \Theta\left(n^3\right)$$

Part II

C++

## Variables and Class

#### 1.1 The Basics

```
#include <iostream>

int main(int argc, char *argv[]) {
    std::cout << "Hello World!" << std::endl;

return 0;
}</pre>
```

C++ is the younger, more powerful and versatile form of what C was meant to be. C++ utilises features such as object-orientated programming not supported by C.

#### 1.1.1 Commenting

Single-line comments use two forward slashes: // Comment 1
Multi-line comments use a forward slash and a star at each end to denote beginning and end: /\* Comment 2
\*/

#### 1.1.2 Types and Variables

- 1. Primitive, built-in types:
  - 1) void is used to determine functions and variables of no return value.
  - 2) bool, char, int, float, double and et cetra are used to return certain values.
  - 3) unsigned is prepended to targets that are always of positive value.
- 2. Enumerations: enum is used to define groups of integer constants.

```
5 enum list { a1 = 1, a2 = 2, a3 = 3, a4 };
```

- 3. Variable Scopes: Varaibles are defined only up to the level of their own declaration.
  - 1) Global Variables: Variables that are declared outside functions and classes. Global variables can be defined as static to make its scope local to one file.
  - 2) Local Variables: Variables that are declared within a function, class, or otherwise enclosed snippets of code. Variables can only be used and memoized within that specific snippet. However, these variables can also be defined as static to retain its value from previous uses and bypass re-initialisation.
- 4. Constant Qualifier: Variables preceded by the keyword const is fixed and cannot be altered by the program.

```
const int a = 3; // a cannot be altered.
```

#### 1.2 Basic Expressions and Statements

- 1. Basic Expressions: Expressions are combinations of iterated variables and operators that portray a new value or meaning.
  - 1) Arithmetic Expressions: Like most other programming languages, C++ features arithmetic operators +, -, \*, /, % which each perform additions, subtractions, multiplications, truncating divisions and modular calculations.

```
std::cout << 5 + 3 << " " << 5 - 3 << " " << 5 * 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " << 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5 / 3 << " < 5
```

2) Relational Expressions: Like most other programming languages, C++ features relational operators ==, !=, <, >, <=, >= which each mean equality, inequality, less-than, greater-than, less-than-or-equal and greater-than-or-equal.

```
std::cout << (5 == 3) << (5 != 3) << (5 < 3) << (5 >= 3) << (5 <= 3) << (5 >= 3) << std::endl; // Result: 010101
```

- 2. Basic Statements: Statements are combinations of expressions and snippets of code that portray the actions to be taken by the program itself.
  - 1) Conditional Statements: Like most other programming languages, C++ features selective execution of code with keywords if...else and switch if...else are used in extensive description of the determining creteria, while switch is used for multiple possible outcomes of the same integer, character, or otherwise relatively simple value.

```
if (1 >= 0 && true) std::cout << "True" << std::endl;
else std::cout << "False" << std::endl; // Result: True
switch(a) { // Recall that const int a = 3 in line 6
case 1: std::cout << "a is " << 1 << std::endl; break;
case 3: std::cout << "a is " << 3 << std::endl; break;
default: std::cout << "a is something else" << std::endl;
} // Result: a is 3</pre>
```

2) Ternary Conditional Operator: The only operator of the C++ language to feature three operands, conditional operator expr1 ? expr2 : expr3 evaluates the boolean value of expr1, and if it is true executes expr2, else expr3.

```
std::cout << 5 << (5 < 3 ? " is greater than " : " is less than ") << 3 << std::endl; // Result: 5 is less than 3
```

3) Iterative Statements: Like most other programming languages, C++ features iterative execution of code with keywords for and while.

```
for (int i = 0; i < 10; ++i) std::cout << i << " "; // Print all digits.

std::cout << std::endl; // Print a new line

int sum = 0, i = 0;

while (i < 10) { // i is processed from 0 to 9

sum += i; // Add all digits to sum

++i; // Increment i by 1
} std::cout << sum << std::endl; // Print the sum of all digits; Result: 45</pre>
```

3. Memory Management: Keywords new and delete each process the allocation and deallocation of memory in C++.

```
int* arr = new int[10]; // Allocate ten consecutive integer variables

delete[] arr; // Deallocate consecutive variables by appending [] to delete
```

## **Functions**

#### 2.1 Function Definition

A function definition consists of four major parts:

- 1. Function Type: The type of value that the function returns. If a function returns an integer value (as shown in Figure 2.1), then the function type is int. Function that do not return a value (as shown is Figure 2.2) are type-defined as void.
- 2. Function Name: The name used to call the process that is the function.
- 3. Function Parameters: The arguments a function requires in order to return corresponding values. Parameters are declared with data types and variable names that are used to indicate said parameters within the function.
- 4. Function Process: The executed process when the function is called. If the function is not a void function, the process ends by returning a value that is correspondent to the type of the function.
- 2.2 Procedural Abstraction
- 2.3 Argument Passing Mechanism
- 2.4 Inline Functions
- 2.5 Recursive Functions

## iostream Headers

#### 3.1 Keyboard Input and Screen Output

#### 3.2 File In/Output

#### 3.3 Header Files

- 1. Header File: A file that allows the reusage of certain portions of source code. Header files are included to a source code via *#include*, which inserts the header file code at that specific location.
- 2. Headers are used for declaring functions, classes, et cetra, and since a header file can be used multiple times by multiple source codes, defining variables and classes must not happen in a header file.
- 3. Include Guards: Since a single header file can be included multiple times throughout a compiling process and cause compilation errors, prevention methods are supported by the compilers. This "guard from inclusion"s are called **Include guards**:

```
#ifndef _IOSHEADER_H_ // Check if header is yet undefined
#define _IOSHEADER_H_ // If checked, define header

#include <iostream>
class classy {
public:
    void std::cout << "Hello World!" << std::endl;
};

#endif // End selection control</pre>
```

## **Arrays and Pointers**

#### 4.1 Array

1. Sequential container of objects of a single data type with fixed size: int array[3] = {5, 3, 2};

#### 4.2 Pointer

- 1. A pointer is a variable that holds the address of an object, enabling indirect access: int \*m = new int[4];
- 2. Adding an integer n to a pointer variable returns the address of an element displaced by n from the original element.

## **Object-Orientated Programming**

- 5.1 ;++;
- 5.2 ;++;
- 5.3 ;++;
- 5.4 ;++;

## **Defining Classes with OOP**

- 5++; 1.6
- 6.2 ;++;
- 6.3 ;++;
- 6.4 ;++;

## **Member Functions**

- 7.1 ;++;
- 7.2 ;++;
- 7.3 ;++;
- 7.4 ;++;

## Namespace and STL

- 3.1 ;++;
- 8.2 ;++;
- 5++; 8.8
- 8.4 ;++;

## **Constructors and Destructors**

- 9.1 ;++;
- ن++ز 9.2
- 9.3 ;++;
- 9.4 ;++;

## Public or Private, Friend Declarations

```
10.1 ;++;
```

ن++ز 10.2

10.3 ;++;

10.4 ;++;

## **Copy Constructors**

- 11.1 ;++;
- ن++ز 11.2
- 11.3 ;++;
- 11.4 ;++;

# Operator Overloading and the Rule of Three

```
12.1 ;++;
```

### **Protected and Private Derivations**

```
13.1 ;++;
```

### **Virtual Functions**

```
14.1 ;++;
```

## **Pure Virtual Functions**

```
15.1 ;++;
```

# **Reusing Copy Control Members**

```
16.1 ;++;
```

- 17.1 ;++;
- 17.2 ;++;
- 17.3 ;++;

- 18.1 ;++;
- 18.2 ;++;
- 18.3 ;++;

- 19.1 ;++;
- 19.2 ;++;
- 19.3 ;++;

20.1 ;++;

20.2 ;++;

ن++ز 20.3

- 21.1 ;++;
- 21.2 ;++;
- 21.3 ;++;

- ن++ز 22.1
- 22.2 ;++;
- 22.3 ;++;

- 23.1 ;++;
- 23.2 ;++;
- 23.3 ;++;

- 24.1 ;++;
- 24.2 ;++;
- 24.3 ;++;