Spring 2019: Advanced Topics in Numerical Analysis: High Performance Computing Assignment 6

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I. 0. FINAL PROJECT

| Project: Implementing FFT | | | | | |
|---------------------------|--|-------------|--|--|--|
| Week | Work | Who | | | |
| 04/15-04/21 | Literature research on FFT and its algorithms | Yongyan Rao | | | |
| 04/22-04/28 | Further literature research, implemented a sequential version of | Yongyan Rao | | | |
| | FFT, checked the correctness by comparing with GSL library | | | | |
| | | Yongyan Rao | | | |
| | Ran tests on the implementations, and worked on report | Yongyan Rao | | | |
| 05/13-05/19 | | Yongyan Rao | | | |

II. 1. MPI-PARALLEL TWO-DIMENSIONAL JACOBI SMOOTHER

A. Blocking version weak scaling study

The following study was conducted with the following parameters, lN = 100, number of iterations 10.

| Number of process(es) | 1 | 4 | 16 | 64 | 256 |
|-----------------------|----------|----------|----------|----------|----------|
| Time (second) | 0.000687 | 0.000895 | 0.099191 | 0.064470 | 3.127207 |

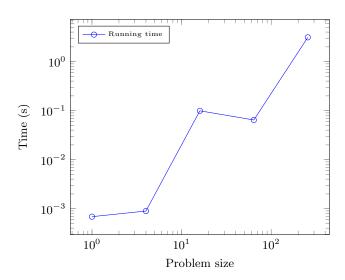


FIG. 1: Weak scaling test

A program is weakly scalable, if when the number of processes/threads increases x times, the program completes an x times larger problem within the same amount of time. Therefore, from the plot above, we can conclude that the Jacobi solver is not weakly scalable.

B. Blocking version strong scaling study

The following study was conducted with the following parameters, $N = \sqrt{10240000} = 3200$, number of iterations

| Number of process(es) | 1 | 4 | 16 | 64 | 256 |
|-----------------------|----------|-------------|-------------|-------------|-------------|
| Time (second) | 0.673925 | 0.171769 | 0.085054 | 0.117849 | 3.683604 |
| Speedup | 1 | 3.923437873 | 7.923495662 | 5.718546615 | 0.182952619 |

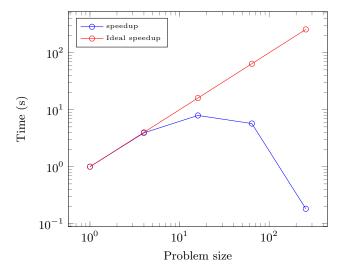


FIG. 2: Strong scaling test

A program is strongly scalable, if when the number of processes/threads increases x times, the program completes a same-size problem x faster, which means the speedup of the program is proportional to the number of processes/threads. Therefore, from the plot above, we can conclude that the Jacobi solver is not strongly scalable. Actually the linearity relation only holds up to four (4) processes.

C. Non-blocking version comparison

The same experiments were conducted using the non-blocking implementation.

| Number of process(es) | 1 | 4 | 16 | 64 | 256 |
|----------------------------|----------|----------|----------|----------|----------|
| 0 (| 0.000687 | | | | |
| Non-blocking time (second) | 0.000673 | 0.000764 | 0.020252 | 0.042427 | 0.717789 |
| | | | | | |
| Number of process(es) | 1 | 4 | 16 | 64 | 256 |
| | 0.673925 | | | | |
| Non-blocking time (second) | 0.624653 | 0.160637 | 0.066820 | 0.057231 | 0.705940 |

From the comparison above, we can conclude that the non-blocking version of the program always has better performance than the blocking version. The advance is more significant when the problem size is large.

III. 2. PARALLEL SAMPLE SORT

With setups, --nodes=8 and --ntasks-per-node=8, i.e., totally 64 processes, the running time versus the number of random numbers generated in a process is presented as below.

| N | 10^{4} | 10^{5} | 10^{6} |
|---------------|----------|----------|----------|
| Time (second) | 0.802799 | 0.851473 | 1.159685 |