

Workshop proposal: Applied Category Theory

January 20, 2017

1 Organizers

1. John Baez (math)
2. Bob Coecke (physics and linguistics)
3. Brendan Fong (dynamical systems)
4. Aleks Kissinger, main contact (computer science)
5. Joshua Tan, main contact (computer science)

2 Scientific case

2.1 Scientific background

Category theory was developed in the 1940s to translate ideas from one field of mathematics, e.g. topology, to another field of mathematics, e.g. algebra. More recently, category theory has become an unexpectedly useful and economical tool for modeling a range of different disciplines, including programming language theory [?], quantum mechanics [?], systems biology [?], complex networks [?], database theory [?], and dynamical systems [?].

A category consists of a collection of objects together with a collection of maps between those objects, satisfying certain rules. Topologists and geometers use category theory to describe the passage from one mathematical structure to another, while pure category theorists study categories as their own mathematical structures. In computer science and physics, many categorical constructions (e.g. topoi, or Stone duality, or compact closed categories) are used to give a formal semantics of domain-specific phenomena (e.g. recursive types [?], or automata [?], or quantum protocols [?]).¹ In the applied category theory community, a long-articulated vision understands categories as mathematical workspaces for all sciences, similar to how they are used in topology and geometry [?, ?]. While it is too early to say whether this vision will bear fruit,

¹The categorical semantics is often preferable to set- or type-theoretic semantics in some way: for example, compact closed categories have an elegant graphical language in terms of string diagrams.

we do believe that category theory has the potential to bridge *specific* different fields, and moreover that developments in such fields (e.g. automata) can be transferred successfully into other fields (e.g. systems biology) *through* category theory.

Most extant applications of category theory outside of pure mathematics have used categories to model some phenomena, in the tradition of formal semantics. The most recent workshop on applied category theory was held at Dagstuhl, Germany, in 2015, where “the over-arching research theme was to develop categorical methods as a unified approach to the modeling of complex systems, and category theory as a paradigm for mathematical modeling and applied science” [?]. But one of the observations made at Dagstuhl, was that “a weakness of semantics/CT is that the definitions play a key role. Having the right definitions makes the theorems trivial, which is the opposite of hard subjects where they have combinatorial proofs of theorems (and simple definitions). [...] In general, the audience agrees that people sees category theorists only as reconstructing the things they knew already, and that is a disadvantage, because we do not give them a good reason to care enough” [?].

In this workshop, we wish to articulate a natural response: instead of treating the reconstruction as a weakness, we should treat categorification as a natural consequence of transferring and integrating knowledge across disciplines, in the sense of a mathematical workspace. We believe... this is the future? ... this approach has been underrepresented? ... this topic has been largely unexplored? ... the difference is largely psychological, like the difference between classical and modern geometry? ... cited in early examples, like Baez’s ‘rosetta stone’ [?]? ... is the language just convenient for manipulation, or are there real *theorems* that go between fields?

2.2 Specific challenges and outcomes

This workshop will bring together both theorists and practitioners from a wide variety of disciplines to work on new applications of category theory in (1) dynamical systems and networks, (2) systems biology, and (3) cognition and AI, with a special focus on developing a community of early-stage researchers in applied category theory, and on fostering focused dialogue between researchers working on different applications. It will consist of a 5-day workshop week, an attached 3-day tutorial weekend immediately before, and a 3-month online seminar for PhD students called the “Kan Extension Lab”.

Some of the specific challenges and outcomes we wish to address include:

1. Computability: BRENDAN
2. Communication: how do we communicate with other fields? From Dagstuhl: “Learning to talk with different communities is an import an point in the quest of finding open problems in other areas where CT can make a contribution. Coinduction in theorem provers is still an open problem and though the communication issue with the theorem proving community is

not such a big issue one still does not see enough cross-fertilization. Peter mentions that communication problems are also present in quantum computation though there one already sees contributions.”

3. Pedagogy: one of the open problems discussed at Dagstuhl was the perceived and actual difficulty of category theory. Despite the flexibility and expressiveness of categorical tools in mathematics and computer science, the perceived difficulty of category theory has hindered wider acceptance of the formalism in other areas of interest. Different approaches were suggested, including focusing on automated theorem proving. We plan on addressing this problem over the tutorial weekend, and through the organization of the “Kan Extension Lab”.

Other challenges, specific to each application area, include ??? (dynamical systems), ??? (dynamical systems), ??? (systems biology), and ??? (cognition and AI).

Our workshop will be considered a success if it results in joint research between researchers specializing in different applications (e.g. physics and biology, or economics and AI) or in research that carries over techniques from one application domain of category theory to another, and if the workshop introduces new researchers into the field.

2.3 Connection to the Dutch research community

ALEKS: in the Dutch applied category theory community... this would be Bart + Aleks at Nijmegen, plus Martha Lewis, plus some others.

3 Program

3.1 Workshop week

The workshop highlights three particular applications of category theory: (1) to dynamical systems and networks, (2) to systems biology, and (3) to cognition and AI. While there will be a short introductory lecture for each application domain, the afternoons will intermix all three applications by focusing on common techniques (Monday and Wednesday), computational tools (Tuesday), and common problems and goals (Thursday afternoon) across all three. On Thursday morning, there will be a half-day Highlights session of 8-minute talks.

Each working day will include one keynote lecture during the morning that sets the stage for the day, followed by a “lightning round” of four 15-minute talks that delve into specific aspects of content in the keynote lecture. For example, on Tuesday, there will be a survey lecture by Jason Morton on computational category theory, followed by talks on ???, ???, and ???. These will be followed by four additional 15-minute talks in the early afternoon, which will present active areas of research in these topics. Each morning and afternoon will be closed by a problem session or an extended coffee break.

Overview:

Time	Monday	Tuesday	Wednesday	Thursday	Friday
9:00 - 9:30	Arrival			Highlights forum	
9:30 - 10:00	Welcome	Sys. Bio.	Cogn. + AI		talk?
10:00 - 10:30	Dyn. Sys.	(Krivine)	(Coecke)		
10:30 - 11:00	(Baez)	<i>break</i>	<i>break</i>		<i>break</i>
11:00 - 11:30	2 talks	2 talks	2 talks		2 talks
11:30 - 12:30	Discussion	Discussion	Discussion		Discussion
12:30 - 2:00	Lunch	Lunch	Lunch	Lunch	Lunch
2:00 - 3:00	Sheaves (Abramsky)	Computation (Vicary)	Monoidal (?)	Problem Session	Talk?
3:00 - 3:45	<i>break</i>	<i>break</i>	Discussion		Discussion
3:45 - 4:45	Discussion	Discussion	Boat trip and dinner		Closing
4:45 - 5:30	Wine and cheese				

3.2 Tutorial weekend

Immediately prior to the workshop, we will organize a 3-day weekend of tutorials targeted at graduate students and postdocs, though we envision more senior researchers who wish to broaden their horizons will also be interested in attending.

Two keynote lectures at the tutorials will be given by *???, ???, and ???*.

To supplement the tutorial weekend, we will host an online “Kan Extension Lab” for graduate students prior to the workshop, whose participants will present the results of their work in the lab either at the tutorial weekend or at the workshop itself. The output of the Extension Lab will be published in a special issue of *???*.

4 Participants

The estimated number of participants is 55. At the time of writing of this proposal, the planned workshop already has ?? confirmed participants with affiliations in the Netherlands, the UK, the US, and [...].

Confirmed participants for tutorial weekend: ??.

Junior/senior ratio: ??.

1. Samson Abramsky (Oxford), prof, computer science
2. John Baez (UC Riverside), prof, math

3. Bob Coecke (Oxford), prof, computer science
4. Brendan Fong (MIT), postdoc, computer science
5. Joshua Tan (Oxford), PhD, computer science
6. ... [copy over from spreadsheet when complete.]

5 Factsheet

A separate factsheet has been attached to this application.

6 Budget

A separate budget has been attached to this application.