

Every time we are stuck all possible subsets we've to try then just think of DP

Post Title

Burst Balloon to maximize coins

→ MCM → Subarray taken at a time & Partitioning it
→ Burst Balloon → Subsequence (Pick any from) Partition also

We have been given N balloons, each with a number of coins associated with it. On bursting a balloon i, the number of coins gained is equal to $A[i-1] \cdot A[i] \cdot A[i+1]$. Also, balloons i-1 and i+1 now become adjacent. Find the maximum possible profit earned after bursting all the balloons.

Assume an extra 1 at each boundary.

Examples:

Input : 5, 10

Output : 60

Explanation - First Burst 5, Coins = $1 \cdot 5 \cdot 10$

Then burst 10, Coins += $1 \cdot 10 \cdot 1$

Total = 60

Input : 1, 2, 3, 4, 5

Output : 110

A recursive solution is discussed here. We can solve this problem using dynamic programming. First, consider a sub-array from indices Left to Right (inclusive).

If we assume the balloon at index Last to be the last balloon to be burst in this sub-array, we would say the coins gained to be $A[\text{left}-1] \cdot A[\text{last}] \cdot A[\text{right}+1]$. $dp[\text{coins}] = \text{current} + \text{last}$

Also, the total Coin Gained would be this value, plus $dp[\text{left}][\text{last}-1] + dp[\text{last}+1][\text{right}]$, where $dp[i][j]$ means maximum coin gained for sub-array with indices i, j.

Therefore, for each value of Left and Right, we need find and choose a value of Last with maximum coin gained, and update the dp array.

Our Answer is the value at $dp[1][N]$.

C++

Java

Python3

C#

Javascript

```
// Java program to illustrate
// Burst balloon problem
import java.util.Arrays;

class GFG{

public static int getMax(int[] A, int N)
{

    // Add Bordering Balloons
    int[] B = new int[N + 2];
    B[0] = B[N + 1] = 1;

    for(int i = 1; i <= N; i++)
```

See in
video for
Approach
in
Tabulation


```
B[i] = A[i - 1];
```

```
// Declaring DP array
```

```
int[][] dp = new int[N + 2][N + 2];
```

```
for(int length = 1;
```

```
length < N + 1; length++)
```

```
{
```

```
for(int left = 1;
```

```
length < N - length + 2; left++)
```

```
{
```

```
int right = left + length - 1;
```

```
// For a sub-array from indices
```

```
// left, right. This innermost
```

```
// loop finds the last balloon burst
```

```
for(int last = left;
```

```
last < right + 1; last++)
```

```
{
```

```
dp[left][right] = Math.max(
```

```
dp[left][right],
```

Left subarray
K (last)

```
dp[left][last - 1] +
```

```
B[left - 1] * B[last] *
```

```
B[right + 1] +
```

```
dp[last + 1][right]);
```

Right subarray
K (last)

```
}
```

```
}
```

```
}
```

```
return dp[1][N];
```

```
}
```

```
// Driver code
```

```
public static void main(String args[])
```

```
{
```

```
int[] A = { 1, 2, 3, 4, 5 };
```

```
// Size of the array
```

```
int N = A.length;
```

```
// Calling function
```

```
System.out.println(getMax(A, N));
```

```
}
```

```
}
```

```
// This code is contributed by dadi madhav
```

Output:

110

So all
understood
now
↓
with string
yt & code
here

→ last is like index 'k'
last balloon to be
burst, which
partition
into sub-array.
e.g.,

1 [5 1 3 8] 1
left ← length → right

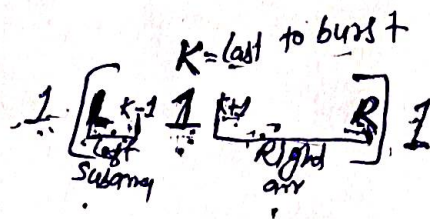
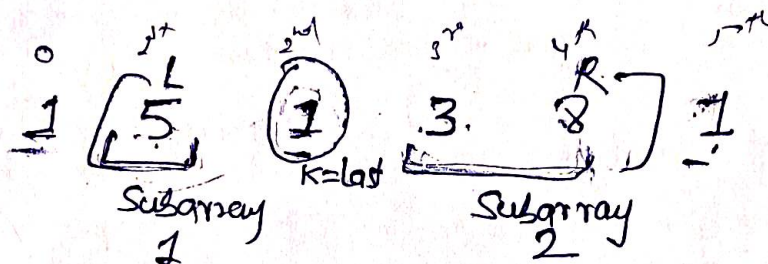
last (let's be last)
↓
last
↓
last
↓
last
↓
last

last can be
one of any from this
1 to 1 or left to right range

Partition DP only like MCM

[5 1 3 8]

How to make approach to bring this question to solve by getting subproblem.



$$DP[L][k-1] + \underbrace{1 \times 1 = 1}_{\text{burst}} \Rightarrow \text{Array}(\text{last}=k) * \text{array}(\text{left}-1) \\ DP[k+1][R] * \text{array}(\text{Right}+1)$$

$$\Rightarrow \text{Max} = \{ \underline{DP[L][k-1]} + \underline{DP[k+1][R]} + \text{arr}(k) * \text{arr}(\text{left}-1) * \text{arr}(\text{Right}+1) \}$$