

 平衡二叉树的插入

 在二叉排序树中插入新结点后,如何保持平衡?
 查找路径上的所有结点都有可能受到影响

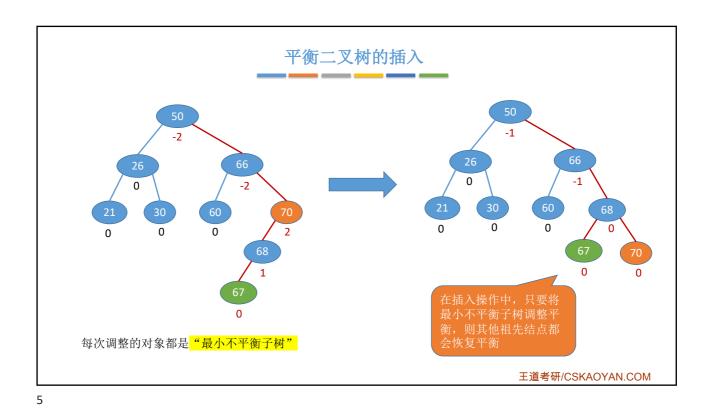
 50
 从插入点往回找到第一个不平衡结点,调整以该结点为根的子树。

 21
 30
 60
 70

 0
 0
 0
 2

 每次调整的对象都是"最小不平衡子树"

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 调整最小不平衡子树A

 IL
 ○
 在A的左孩子的左子树中插入导致不平衡

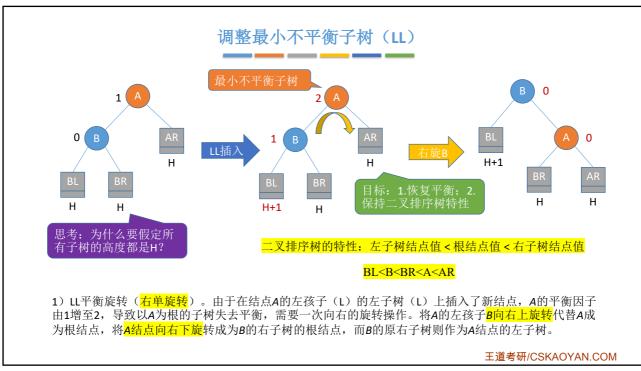
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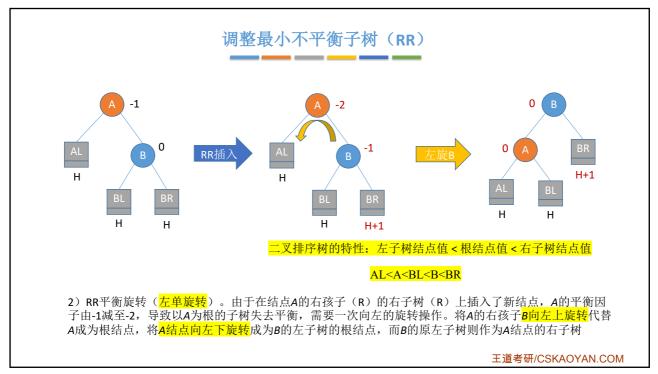
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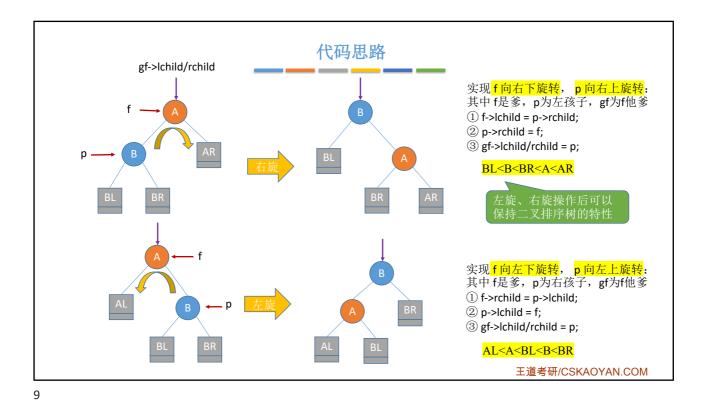
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 在A的右孩子的左子树中插入导致不平衡

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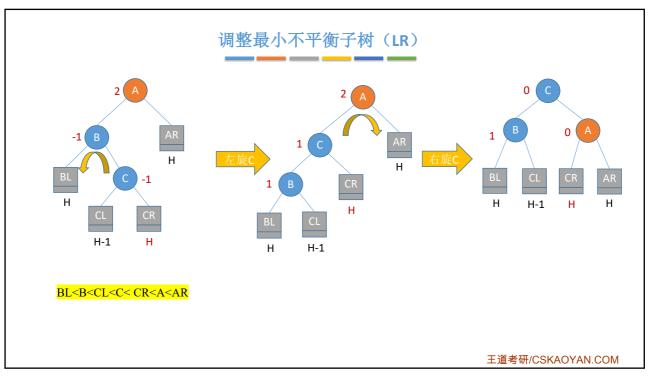


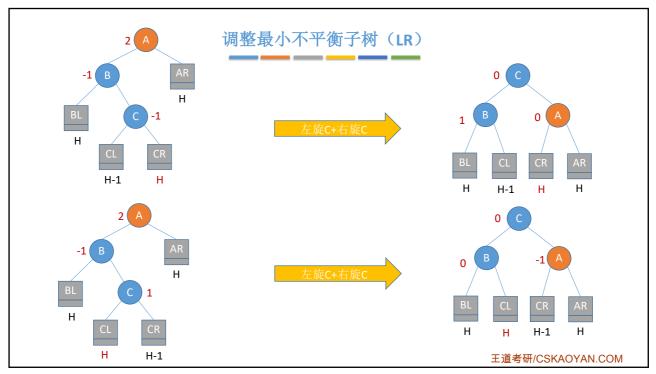


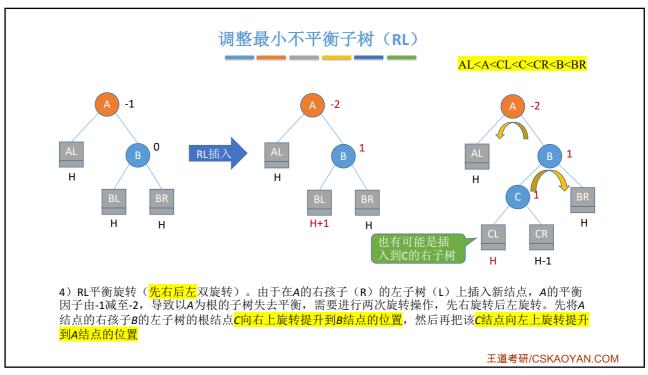


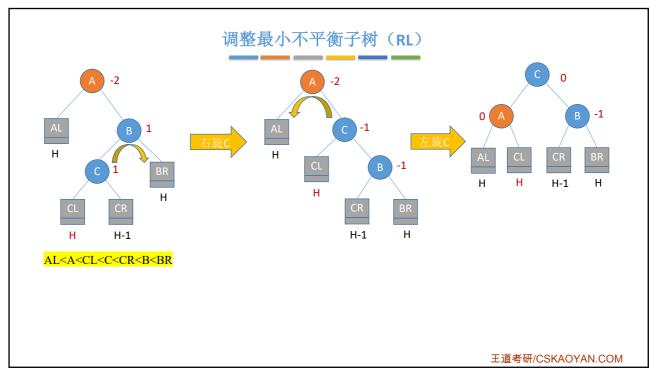
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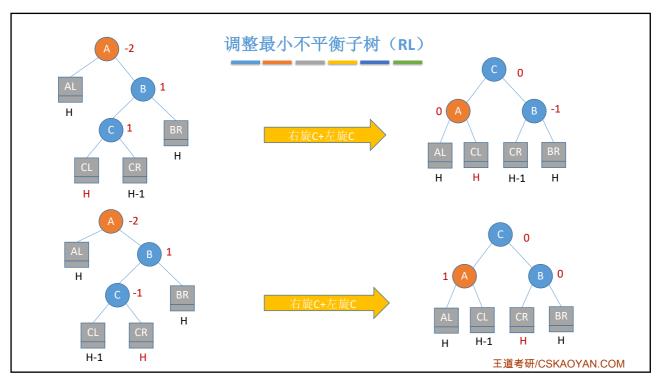
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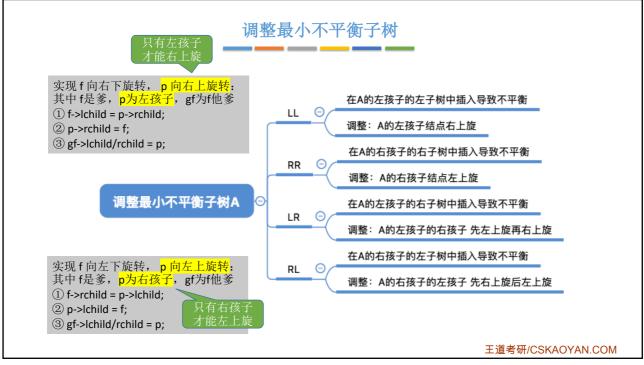


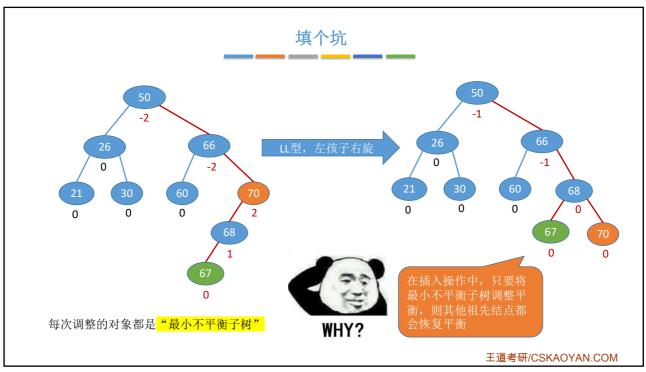


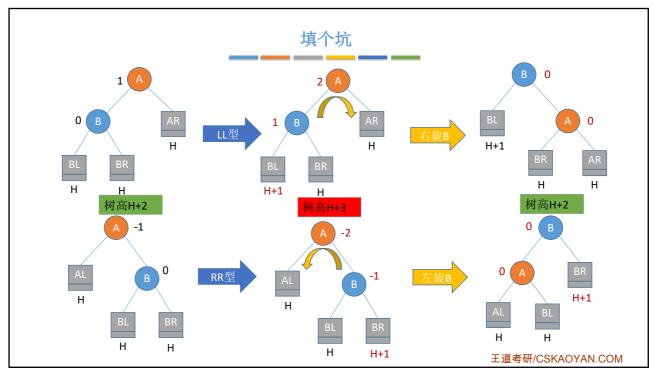






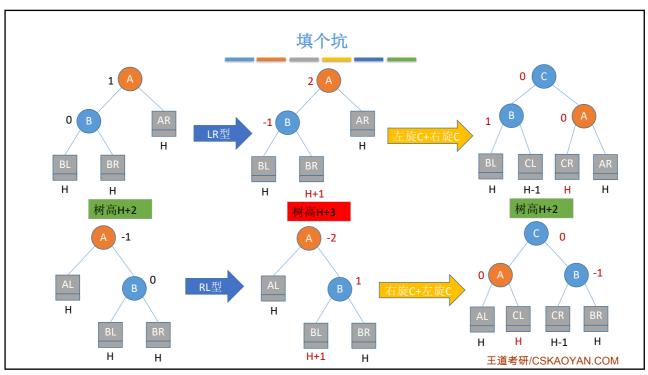


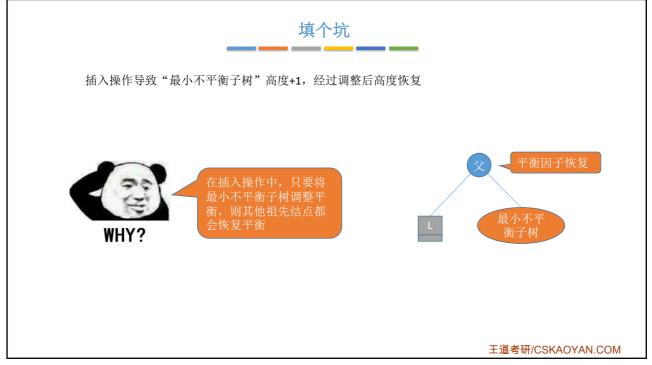


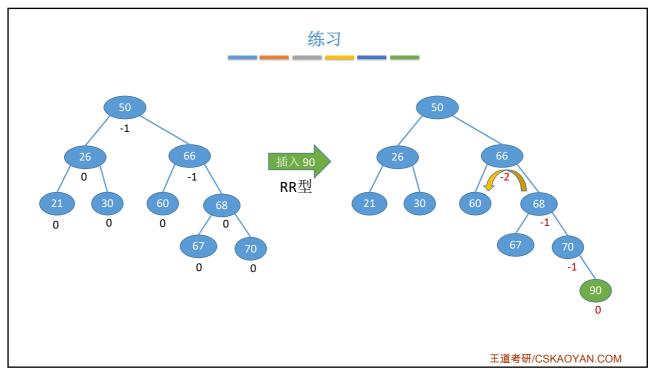


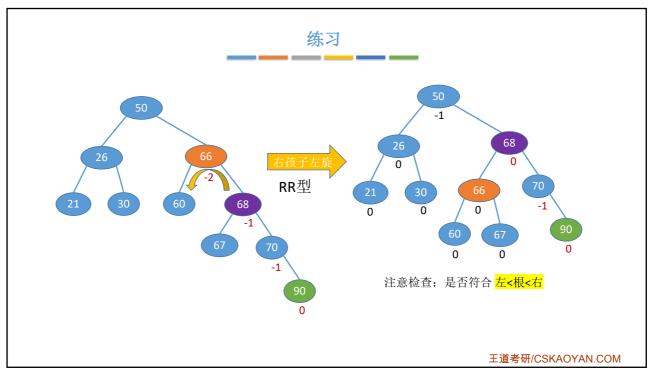
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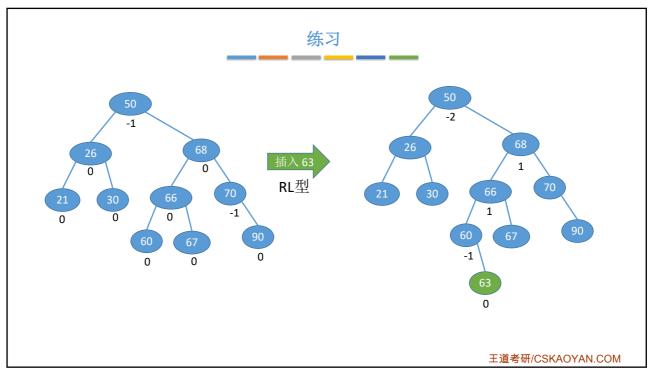
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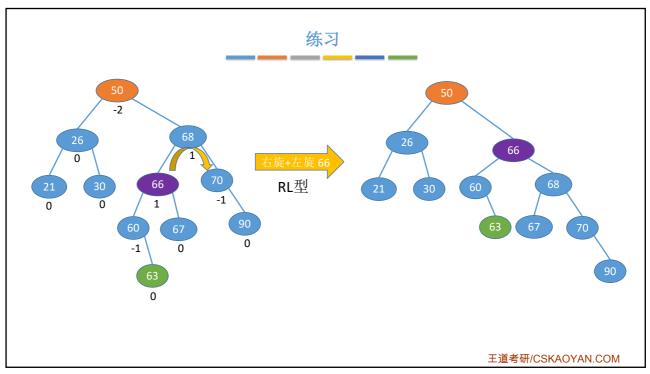


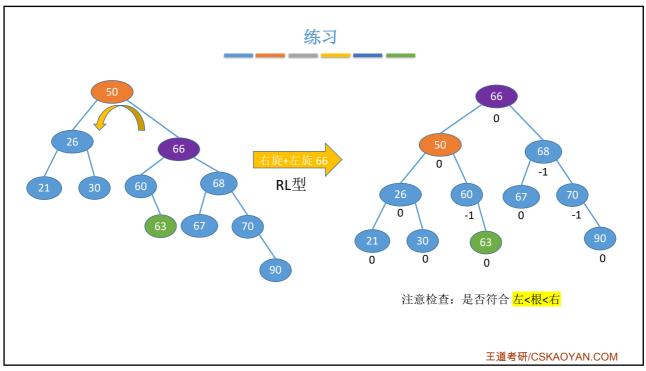


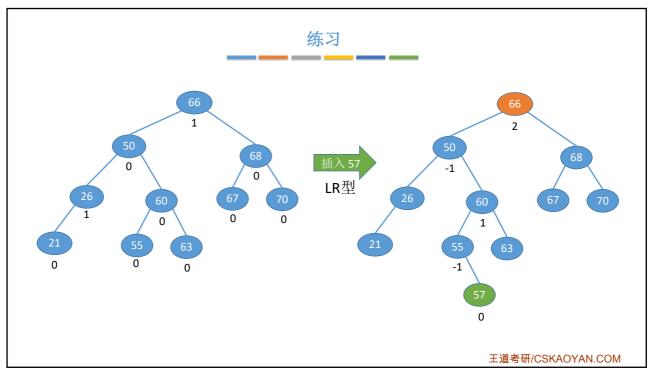


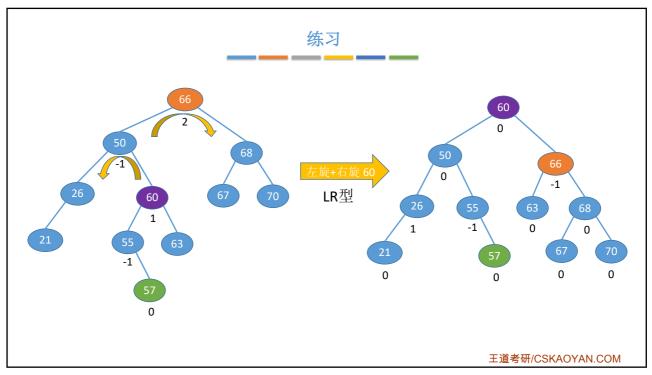












查找效率分析

若树高为h,则最坏情况下,查找一个关键字最多需要对比 h 次,即查找操作的时间复杂度不可能超过 O(h)

平衡二叉树——树上任一结点的左子树和右子树的高度之差不超过1。

假设以 n_h 表示深度为h的平衡树中含有的最少结点数。

则有 $n_0 = 0$, $n_1 = 1$, $n_2 = 2$,并且有 $n_h = n_{h-1} + n_{h-2} + 1$

可以证明含有n个结点的平衡二叉树的最大深度为 $O(\log_2 n)$,<mark>平衡二叉树</mark>的<mark>平均查找长度为 $O(\log_2 n)$ </mark>

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